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QUANTITATIVE EXPLANATION OF FRAGMENTATION OF THE SKELETAL BONDS IN MASS SPECTRA OF AMINO ACID ESTERS^{*})

By

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Abstract

Mass spectra of ethyl esters of twelve amino acids have been investigated, in order to confirm the usefulness of the MO method to study the fragmentation of their skeletal bonds. The result has been shown successful to predict the base peaks of each ester without ambiguity and their fractions to the total peaks semiquantitatively.

Since the constants characteristic to each functional group have been found transferable to different compounds, applicability of this method to more complex compounds has been shown promising, even though its theoretical basis is not established yet.

Introduction

It has been shown that the molecular orbital (MO) theory for mass spectra, in spite of its semi-empirical nature, can explain quantitatively the skeletal fragmentation in mass spectra of such compounds as normal¹⁾ and cyclic alkanes,²⁾ ketones,³⁾ amines,⁴⁾ ethers,⁵⁾ and esters.⁶⁾ Thereby, knowledge of the constants characteristic to each functional group is required. If they are given, relative abundance of each mass-spectral fragments composed of n carbon numbers (C_n) has been predicted quantitatively.

It will be a next step for confirming the usefulness of the theory to investigate the transferability of the characteristic constants to any other compound. If it be shown successful, the theory will be promising to be used widely to investigate mass spectra, even though its theoretical basis is not established yet. Amino acid esters are suitable compounds from this viewpoint, because they include several functional groups in their structure, and

^{*}) The XIV report on the molecular orbital theory for mass spectra (XIII: YAMAMOTO, ITOH and HIROTA, *Nippon Kagaku Zasshi*, **89**, in press (1968)).

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TABLE I. Amino Acid Esters

Glycine ester	$ \begin{array}{cccc} & 6 & 5 & 4 & 3 \\ & \text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & 2 & & & 1 \\ & \text{NH}_2 & & \text{O} & \end{array} $
Alanine ester	$ \begin{array}{cccc} & 7 & 6 & 5 & 4 & 3 \\ & \text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & 2 & & & 1 \\ & \text{NH}_2 & & \text{O} & \end{array} $
α -amino butyric acid ester	$ \begin{array}{cccc} & 8 & 7 & 6 & 5 & 4 & 3 \\ & \text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & 2 & & & 1 \\ & \text{NH}_2 & & \text{O} & \end{array} $
β -Amino butyric acid ester	$ \begin{array}{cccc} & 8 & 7 & 6 & 5 & 4 & 3 \\ & \text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & 2 & & & 1 \\ & \text{NH}_2 & & \text{O} & \end{array} $
γ -Amino butyric acid ester	$ \begin{array}{cccc} & 8 & 7 & 6 & 5 & 4 & 3 \\ & \text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & 2 & & & & 1 \\ & \text{NH}_2 & & & \text{O} & \end{array} $
Norleucine ester	$ \begin{array}{cccc} & 10 & 9 & 8 & 7 & 6 & 5 & 4 & 3 \\ & \text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & & & & 2 & & & 1 \\ & & & & \text{NH}_2 & & \text{O} & \end{array} $
Leucine ester	$ \begin{array}{cccc} & 9 & 8 & 7 & 6 & 5 & 4 & 3 \\ & \text{C} & \diagdown & \text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & & \text{C} & \diagup & 2 & & & 1 \\ & & & & \text{NH}_2 & & \text{O} & \end{array} $
Isoleucine ester	$ \begin{array}{cccc} & 9 & 8 & 7 & 6 & 5 & 4 & 3 \\ & \text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & 10 & & 2 & & & 1 \\ & \text{C} & \text{NH}_2 & & \text{O} & \end{array} $
Aspartic acid ester	$ \begin{array}{cccc} & 12 & 11 & 10 & 9 & 8 & 7 & 6 & 5 & 4 \\ & \text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & & & & & 3 & & 2 & & & 1 \\ & & & & \text{O} & & \text{NH}_2 & & \text{O} & \end{array} $
Lysine ester	$ \begin{array}{cccc} & 11 & 10 & 9 & 8 & 7 & 6 & 5 & 4 \\ & \text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & & & & & 2 & & & 1 \\ & \text{NH}_2 & & & & \text{NH}_2 & & \text{O} & \end{array} $
Serine ester	$ \begin{array}{cccc} & 7 & 6 & 5 & 4 & 3 \\ & \text{CH}_2 & -\text{CH} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & 8 & & 2 & & & 1 \\ & \text{OH} & & \text{NH}_2 & & \text{O} & \end{array} $
Phenylalanine ester	$ \begin{array}{cccc} & 8 & 7 & 6 & 5 & 4 & 3 \\ & \text{C}_6\text{H}_5 & -\text{C} & -\text{C} & -\text{C} & -\text{O} & -\text{C} & -\text{C} \\ & & & 2 & & & 1 \\ & & & \text{NH}_2 & & \text{O} & \end{array} $

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most of the characteristic constants have already been determined. Besides, they are interesting from the standpoint of analyzing amino acids.

Mass spectra of ethyl esters of several important amino acids were already measured, and mechanism of their fragmentation was also investigated by BIEMANN *et al.*⁷⁾ In the present paper, ethyl esters of glycine, alanine, α -, β -, γ -amino butyric acid (ABA), norleucine, leucine, isoleucine, asparatic acid, lysine, serine and phenylalanine will be studied. The skeletal structure of these twelve esters are shown in Table I,*⁾ where the numerals attached to each skeletal bond are the bond numbers to be used frequently. Numbering of the C-H and N-H₂ bonds is omitted, because their bond-scission will not be discussed.

Theory

In the first report of this research,¹⁾ it was assumed that the scission-probability of each skeletal bond of the bombarded molecule is given in proportion to the electron density of the highest occupied MO at the bond. This fundamental assumption was modified into a generalized one in a previous report,⁸⁾ where the electron density of the bombarded molecule was substituted for the charged density of the superexcited species produced from the molecule by electron bombardment. The former assumption, therefore, can be regarded as a conventional one to calculate the scission probability of the ions. However, as has been discussed in the previous reports, both results are the same at the present stage of the theory, because the method of calculation remains also the same. This situation is convenient to carry out the prediction of fragmentation of organic compounds, because of simplicity in calculation.

According to this standpoint, mass spectral data will be arranged by collecting the peaks under the same skeletal bond-scission, so that comparison between theory and experiment becomes simplified. This procedure assumes implicitly that the peaks due to hydrogen attachment and detachment can be regarded as much slower secondary processes than those of scission of skeletal bonds. The secondary fragmentations have to be considered to some extent also in the skeletal bond-scission in complex molecules, and of course, these processes have to be included to explain all the mass spectral peaks completely.

The most important point to be noted lies in the second assumption that the C=O and C-N bonds are not rupturable, irrespective of the charge density at these bonds. This assumption was adopted already in the cases of ketones, amines and acids, and could explain the experimental result very well. The

*) Vertical dotted lines at the bonds indicate the most rupturable bonds to be explained by Table V.

success thus obtained may be explained by the possibility that, due to the calculation method of approximation, a larger part of the charge density at C=O and C-N bonds corresponds to that at the lone pair electrons, loss of which does not effect of the stability of the bonds and produces merely molecular ions. However, since this explanation lacks a firm theoretical basis, this assumption will be regarded as a conventional one to explain the experiment, until the time when it is replaced by a more reasonable one, which will be reported in future.

Calculation

Now, the charge density at the HO orbital is calculated by the approximate method of LCBO,⁹⁾ making the CH₃, CH₂, CH and NH₂ group as united atoms. Details of the procedure are not described, in order to avoid duplication with the previous reports.^{3,4)} Instead of it, the procedure will be explained by making α -aminobutyric acid (ABA) ester as an example. The secular equation to determine the eigen-values of the ester is,

$$\begin{vmatrix} \alpha_0 - E & 0 & 0 & 0 & \beta_0 & \beta_0 & 0 & 0 \\ 0 & \alpha_N - E & 0 & 0 & 0 & \beta_N & \beta_N & 0 \\ 0 & 0 & \alpha_t - E & \beta & 0 & 0 & 0 & 0 \\ 0 & 0 & \beta & \alpha - E & \beta & 0 & 0 & 0 \\ \beta_0 & 0 & 0 & \beta & \alpha - E & \beta & 0 & 0 \\ \beta_0 & \beta_N & 0 & 0 & \beta & \alpha - E & \beta & 0 \\ 0 & \beta_N & 0 & 0 & 0 & \beta & \alpha - E & \beta \\ 0 & 0 & 0 & 0 & 0 & 0 & \beta & \alpha_t - E \end{vmatrix} = 0. \quad (1)$$

The constants α , β , α_0 etc. in Eq. (1) denote the coulombic and exchange integrals in the meaning of the present LCBO method. Their definition may

TABLE II. Coulombic and Exchange Integrals

	$C^i - C$	$C^{i+1} - C^i$	C=O	C-NH ₂	C-OH	C ₆ H ₅ -C
$C^i - C$	α	β	β_0	β_N	β_{OH}	β_p
$C^{i+1} - C^i$		α	β_0	β_N	β_{OH}	β_p
C=O			α_0	—	—	—
C-NH ₂				α_N	—	—
C-OH					α_{OH}	—
C-C ₆ H ₅						β_p

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be understood easily by Table II. The remaining α , corresponds to α of the terminal $\text{CH}_2\text{-CH}_3$ or $\text{CH}_3\text{-CH}$ bond, and its value is taken to be $\alpha+2\beta$, according to the unpublished results on normal alkanes.

In Eq. (1), C-O-C bond is taken to be the same as C-C-C bond for the sake of simplicity, considering the successful result when this approximation was adopted to the fragmentation of five methyl esters, $\text{CH}_3\text{COOC}_n\text{H}_{2n+1}$.⁶⁾

In the present research, it is sufficient only if the expansion coefficients of HO energy level, λ_h , can be determined, and it is not the primary aim to evaluate the energy levels, including ionization potentials. Considering the situation, $\alpha_0, \alpha_N, \beta_0$ etc. are substituted by Eq. (2) and λ by $(\alpha-E)/\beta$.

$$\alpha_0 = \alpha + x_0\beta, \quad \alpha_N = \alpha + x_N\beta, \quad \beta_0 = y_0\beta, \quad \beta_N = y_N\beta, \quad (2)$$

Thus, Eq. (1) is transformed into Eq. (3).

$$\begin{vmatrix} \lambda+x_0 & 0 & 0 & 0 & y_0 & y_0 & 0 & 0 \\ 0 & \lambda+x_N & 0 & 0 & 0 & y_N & y_N & 0 \\ 0 & 0 & \lambda+2 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & \lambda & 1 & 0 & 0 & 0 \\ y_0 & 0 & 0 & 1 & \lambda & 1 & 0 & 0 \\ y_0 & y_N & 0 & 0 & 1 & \lambda & 1 & 0 \\ 0 & y_N & 0 & 0 & 0 & 1 & \lambda & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & \lambda+2 \end{vmatrix} = 0. \quad (3)$$

Similarly, $x_{\text{OH}}, x_p, y_{\text{OH}}$ and y_p , which can be defined as above become

TABLE III. Comparison of Experimental and Theoretical Scission Probability of Bonds of Propyl Alcohol and Propyl Benzene

Bond Number	Propyl alcohol			Propyl benzene*)		
	1	2	3	1	2	3
	HO-C-C-C			-C-C-C		
Scission probability						
Exper. %	13	84	3	8	89	3
	(API # 425)			(API # 310)		
Calc. %	20	71	9	10	83	7
Constants used in calculation	$x_1=1, x_2=0, x_3=2$ $y_{12}=1, y_{23}=1$			$x_1=0, x_2=-1, x_3=2$ $y_{12}=0.5, y_{23}=1$		

*) Presence of the peaks ascribable to rupture of benzene ring is neglected in the comparison, though they amount to *ca.* 20% of the total peak height.

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necessary to be known in the cases of serine and phenylalanine, corresponding to the functional groups, C-OH and C-C₆H₅. They are determined from the mass spectra of propylalcohol and propylbenzene, respectively. The calculated bond scission from these constants are compared with those of the observed as shown in Table III, where x_2 , the x constant corresponding to benzyl group, will be denoted by x_B hereafter. Though the agreement is not so good, they are used preliminarily in the present paper.

It is not only simpler to use Eq. (3) in calculation, but also is more practical than to use Eq. (1), because all the constants in Eq. (3) are referred to the coulombic and exchange integrals of the C-C bonds as the standards, making it of no use to know their values in energy unit.

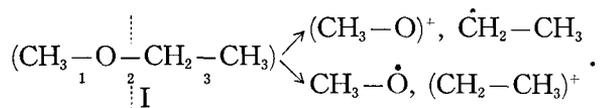
Now, the numerical values of the integrals hitherto used^{3,4)} are as follows :

$$\begin{aligned} \alpha &= -13.75 \text{ V}, & \alpha_0 &= -12.37 \text{ V}, & \alpha_N &= -9.61 \text{ V}, \\ \beta &= -1.80 \text{ V}, & \beta_0 &= -2.63 \text{ V}. \end{aligned} \quad (4)$$

By use of Eq. (2), x_0 , x_N , y_0 and y_N can be obtained from the above values. Similarly, x_{OH} , x_p , x_B , y_{OH} and y_p can be estimated as described above. The results are summarized as follows :

$$\begin{aligned} x_0 &= -0.77, & x_N &= -2.31, & x_{OH} &= 1, & x_p &= 0, & x_B &= -1, \\ y_0 &= 1.46, & y_N &= 0.69, & y_{OH} &= 1, & y_p &= 0.5. \end{aligned}$$

Experimental scission-probability will be determinable by investigating all the mass spectral peaks; *e.g.*, in the case of methyl ethyl ether (I), sum of the peaks ascribable to C₂H₅⁺ and CH₃O⁺ gives the scission-probability of bond 2.



Besides, (CHO)⁺ ion also might be added to the scission of bond 2, because the ion was probably produced by the detachment of 2H from the (CH₃O)⁺ ion by some process.

As described in the theoretical part, the C=O and C-NH₂ bonds are assumed to be unrupturable, irrespective of their electron density, in accordance with the fact that the corresponding peaks are observed very few, though this assumption has not been explained theoretically. Scission probability, therefore, is to be calculated, neglecting the contribution of electron density at these bonds. It has to be admitted that this assumption is to be replaced by more reasonable one, also because of the experimental reason.

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Results and Discussion

In Table IV, calculated energy values of the HO level are shown in λ unit for each ester, and also the squared expansion coefficients, *i. e.*, the

TABLE IV. HO Energy Levels and the Expansion Coefficients over the Bond Orbitals of Amino Acid Esters

Ester	Glycine	Alanine	α -ABA	β -ABA	γ -ABA	Norleucine	
HO energy level λ_h (λ unit)	3.33	2.64	2.66	2.59	2.44	2.66	
1	1.988	10.520	8.131	4.005	1.923	7.508	
2	91.006	75.334	79.393	82.038	92.038	79.954	
3	0.000	0.002	0.001	0.001	0.002	0.004	
4	0.000	0.037	0.025	0.024	0.041	0.027	
Electron density of the HO level ^{a)} %	5	0.042	0.218	0.148	0.134	0.201	0.138
6	7.009	13.646	10.875	4.533	0.287	10.078	
7		0.244	1.363	8.751	1.411	1.837	
8			0.063	0.514	3.098	0.372	
9						0.071	
10						0.010	

Ester	Leucine	Isoleucine	Asparatic acid	Lysine	Serine	Phenyl-alanine	
HO energy level λ_h (λ unit)	2.66	2.66	2.66	2.66	2.82	2.80	
1	7.434	7.083	6.698	7.418	7.984	4.668	
2	80.026	80.568	79.760	79.706	79.572	83.214	
3	0.004	0.003	0.780	0.267	0.001	0.001	
4	0.026	0.024	0.003	0.004	0.024	0.011	
5	0.136	0.127	0.022	0.026	0.144	0.668	
Electron density of the HO level ^{a)} %	6	9.988	9.566	0.118	0.136	10.700	6.588
7	1.897	2.217	9.085	9.965	1.464	5.352	
8	0.425	0.237	2.458	1.880	0.109	0.099	
9	0.032	0.033	1.058	0.414			
10	0.032	0.142	0.014	0.116			
11			0.002	0.069			
12			0.000				

a) Electron density above the dotted line is assumed not to contribute to fragmentation.

electron density in %. In the case of phenylalanine, scission of the benzene ring was ignored, because it cannot be calculated by the present approximation.

Number of the most rupturable bond and the fraction of the peaks thus producible to the total peaks can be derived easily from Table IV. The results are described in the corresponding position in each ether in Table V, where the fraction of the electron density is the one when contribution of C=O and NH₂ are omitted from the total. Experimental base peaks and bond number relating to their ion formation are shown in Table V for each esters

TABLE V. Highest Peaks in Mass Spectra of Amid Acid Esters and their Number of Most Rupturable Bonds^{a)}

Ester	Glycine	Alanine	α -ABA	β -ABA	γ -ABA	Norleucine
1° Observed base peak	30 CNH ₄ ⁺	44 C ₂ NH ₆ ⁺	58 C ₃ NH ₆ ⁺	44 C ₂ NH ₆ ⁺	30 CNH ₄ ⁺	86 C ₅ NH ₁₂ ⁺
2° Its numbers of the ruptured bond	6	6	6	7	8	6
3° Fraction to the i) total peaks % ii) ^{b)}	98 —	81 82	67 <i>ca.</i> 80	67 68	49 —	45 65
Calculated bond number of the base peak	6	6	6	7	8	6
Fraction of the electron density %	99	96	87	63	51	80

Ester	Leucine	Isoleucine	Asparatic acid	Lysine	Serine	Phenylalanine
1° Observed base peak	86 C ₅ NH ₂₂ ⁺	86 C ₅ NH ₁₂ ⁺	116 C ₅ NOH ₁₀ ⁺	84 C ₅ NH ₁₀ ⁺	60 C ₂ NOH ₆ ⁺	120 C ₈ NH ₁₀ ⁺
2° Its numbers of the ruptured bond	6	6	7	7	6	6
3° Fraction to the i) total peaks % ii)	39 55~70	48 68	35 50~60	43 58 ^{d)}	53 59	43 ^{e)} —
Calculated bond number of the base peak	6	6	7	7	6	6
Fraction of the electron density %	80	77	71	79	85	54

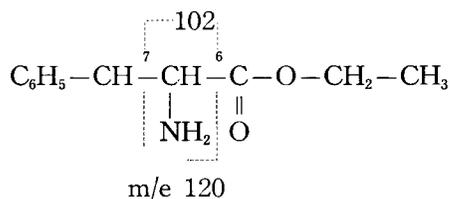
a) Ionizing voltage: 70 e.v.

b) The values when the peaks probably produced successively by fragmentation of the base peak ion are taken into account.

c) If the peaks ascribable to the bond-scission of the benzene ring is eliminated from the total, this % increases up to 47%.

d) The m/e 30 peak was allotted to the secondary ion from the m/e 101 peak primarily produced.

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m/e 120 peak is produced by the scission of bond 6 as expected by the largest electron density in Table IV, but its contribution to the total peaks reaches only 32% in height. Bond 7 of this ester is also rupturable, as indicated by large electron density at this bond, and actually m/e 102 peak appears as the second highest, and total contribution of the scission at bond 7 amounts to 40% in height. Now that such an explanation can be given theoretically, this ester will not become an obstacle in analyzing the ester, but rather offers a support to the theory.

In the above discussion, the most rupturable bond, but not the most producible peak was made the problem in concern. This is inevitable due to the reason that, as widely accepted, when a parent positive ion ruptured into a positive ion and a radical, any general rule on which species becomes charged is not known yet. However, since the base peaks include always more negative group in the case of amino acid esters, their assignments are practically easy, because the fragment containing amino group would become the positive ion. It can be said, therefore, that the base peaks of the amino acid esters are predictable by the present method.

Besides, this result is satisfactory from the viewpoint of the present research to investigate the transferability of the constants characteristic to each functional groups, even though some of them are still of preliminary nature. Investigation in this line has to be carried out also from the reason to consider the scission of C=O bond and rupture of phenyl group. Further, degree of agreement between theory and experiment may increase if better characteristic constants are selected. Especially, substitution of the constants for the C-O bond of ether type for others is desirable, because main cause of quantitative discrepancy in the fraction of the electron density in Table V is ascribable to smaller percentage of theoretical scission probability at the C-O bond. For instance, the m/e 29 peak from asparatic acid ester can be assignable to be C_2H_5^+ ion by comparing the spectrum of ^{15}N labelled ester, indicating the peak to be produced by scission of bond 5 or 11. Contrary to the theoretical expectation, its height reaches half the base peak m/e 116. If the height of this peak is omitted, experimental values at 3° i) and 3° ii) in Table V increase upto 42% and 60~72%, respectively.

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Second, similar substitution is necessary on the characteristic constants of the C=O and C-N bonds, corresponding to the experimental result that they are ruptured, though in small amount. Of course, a more advanced approximation has to be adopted basing on theoretical grounds, in order to answer this requirement.

Further, other amino acid esters having special functional groups, say tyrosine, methionine, proline, *etc.* will be investigated similarly in the cases when their characteristic constants are known. During the procedure, it has to be taken care that this method is applicable only to evaluate the primary scission of the skeletal bonds. Actually, secondary scission may occur immediately after the primary, and some of them occurs so fast that the peaks produced are included in the mass spectra. One of the important example is the m/e 84 peak of lysine ester, as already indicated. It will be a remaining problem in what case such a secondary process has to be considered in the explanation of the peaks in mass spectra.

Conclusion

Though detailed theoretical basis of the MO method was not given, it would be sufficient to conclude that the present theory will be potentially useful as a semi-empirical tool, to study the mass spectra of such complex compounds as amino acids esters, so far as the primary scission of skeletal bonds is concerned.

Acknowledgment

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Remarks added in Proof: Consistency of the parameters peculiar to each functional group, Eq. (4), was shown on various chain compounds in a paper published already (K. HIROTA, Nippon Kagaku Zasshi, **89**, 327 (1968)).

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