Nonequilibrium steady-state response of a nematic liquid crystal under simple shear flow and electric fields

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The effect of a dc electric field on the response of a nematic liquid crystal under shear flow has been investigated by measuring the shear stress response to an ac electric field used as a probe. It was found that both the first- and second-order responses do not vanish at high frequencies, but have constant nonzero values. The experimental results are in good agreement with calculations based on the Ericksen-Leslie theory. The role of the Parodi relation (which is derived from the Onsager reciprocal relation) in the stress response is discussed.

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I. INTRODUCTION

Nematic liquid crystals (NLCs) can be easily taken to nonequilibrium states by applying external forces, so they have been widely used to investigate various types of nonequilibrium phenomena. Here, we confine ourselves to a nonequilibrium steady state (NESS), in which there are still many fascinating phenomena. NESSs are an interesting subject for study in general, because some theoretical results are similar to ones for the equilibrium state (ES). For example, in some cases the fluctuation-dissipation theorem (FDT) in the ES can be modified to hold in an NESS [1–6]. It should also be noted that the linear response to an external force and the correlation function of fluctuations can be defined in an NESS as well as in the ES. In an NESS of an NLC, brought about by a steady shear flow, Patriansyah et al. [7] calculated the correlation function and the response function of the director orientation on the basis of a hydrodynamic theory of NLCs, called the Ericksen-Leslie (EL) theory, and derived a modified FDT, assuming that the director is independent of position, that is, the monodomain case. In this system nonconservative forces are induced by the rotational flow, which violate the Parodi relation (which is derived from the Onsager reciprocal relation) in the stress response is discussed.

II. THEORETICAL CALCULATION BASED ON EL THEORY

NLCs are composed of rodlike molecules with the long axes aligned statistically parallel to each other. The average orientation of molecules is represented by a unit vector $\mathbf{n}$ which is called the director. Ericksen and Leslie have formulated a continuum theory for the velocity $\mathbf{v}$ and the director $\mathbf{n}$ of NLCs [9–14]. Hereafter, we assume a monodomain (i.e., the director is independent of position) and a simple shear flow. Under these assumptions, the EL equations can be simplified and we need only the following equations for our purpose. The angular momentum balance gives

$$\mathbf{n} \times \mathbf{h} = \gamma_1 \mathbf{n} \times \mathbf{N} + \gamma_2 \mathbf{n} \times \mathbf{A} \mathbf{n}, \quad (1)$$

where $\mathbf{h}$ is the molecular field, $\mathbf{N}$ is the rate of change of the director with respect to the background fluid, and $\mathbf{A} = 1/2(\nabla_{\perp} \mathbf{v}_{\parallel} + \nabla_{\parallel} \mathbf{v}_{\perp})$ is the symmetric part of the velocity gradient. The parameters $\gamma_1$ and $\gamma_2$ are the rotational and irrotational viscosity coefficients. The components of the molecular field $\mathbf{h}$ are given by

$$h_\alpha = -\frac{\partial f}{\partial n_\alpha}, \quad (2)$$

where $f$ is the free energy density. When subjected to an electric field, the free energy density can be written as

$$f = -\frac{1}{2}\varepsilon_0 \varepsilon_\perp E^2 - \frac{1}{2}\varepsilon_0 \Delta \varepsilon (\mathbf{n} \cdot \mathbf{E})^2, \quad (3)$$

where $\varepsilon_0$ is the dielectric constant in a vacuum, and $\Delta \varepsilon$ is the dielectric anisotropy defined as $\Delta \varepsilon = \varepsilon_{\parallel} - \varepsilon_{\perp}$ with $\varepsilon_{\parallel}$ and $\varepsilon_{\perp}$ being the dielectric constants parallel and perpendicular to the director, respectively ($\Delta \varepsilon = 11.5$ for 5CB [15]). The rate of change of the director is defined as

$$N_\alpha = \frac{dn_\alpha}{dt} - W_{\alpha \beta} n_\beta, \quad (4)$$

where $W_{\alpha \beta} = 1/2(\nabla_{\perp} \mathbf{v}_{\parallel} - \nabla_{\parallel} \mathbf{v}_{\perp})$ is the antisymmetric part of the velocity gradient. The constitutive equation for the viscous stress tensor is

$$\sigma_{\alpha \beta}^{(\text{visc})} = \alpha_4 A_{\alpha \beta} + \alpha_1 n_\alpha n_\beta A_{\mu \mu} + \alpha_5 n_\alpha n_\mu A_{\mu \beta} + \alpha_6 n_\beta n_\alpha A_{\mu \mu} + \alpha_2 n_\alpha N_\beta + \alpha_3 n_\beta N_\alpha, \quad (5)$$

where $\alpha_i$ ($i = 1, \ldots, 6$) are Leslie coefficients, in terms of which $\gamma_1$ and $\gamma_2$ are expressed as $\gamma_1 = \alpha_3 - \alpha_2$ and...
\( \gamma_2 = \alpha_6 - \alpha_5 \). For 5CB these coefficients have been determined \([16]\): \( \alpha_1 = -0.00767 \text{ Pa s}, \alpha_2 = -0.08171 \text{ Pa s}, \alpha_3 = -0.00433 \text{ Pa s}, \alpha_4 = 0.06642 \text{ Pa s}, \alpha_5 = 0.06725 \text{ Pa s}, \alpha_6 = -0.01879 \text{ Pa s at 25 }^\circ \text{C}. \) These values are used in numerical calculations later. Note that, here, an NLC is treated as an incompressible fluid.

In reality, the monodomain and simple shear flow assumptions may not be exactly satisfied for various reasons. For example, in our experiment no surface treatment for aligning molecules is made so that the director and flow are spatially disturbed at least near the surfaces. Note that our model also does not accommodate defects (e.g., disclinations). Furthermore, larger deformations from the flow-aligning state are reported to take place \([17]\). For simplicity, however, we adopt the assumptions shown in Fig. 1(a), where \( \mathbf{n}(t) = (\cos \theta, 0, \sin \theta) \) and \( \mathbf{v} = \gamma \alpha x \mathbf{x} \) with \( \gamma \) and \( \alpha \) being the shear rate and the unit vector along the \( x \) axis, respectively.

Here, we calculate the stress change due to a small ac electric field, that is, in the nonperturbed state, the flow alignment angle \( \theta_0 \) (as shown in Fig. 1) in the steady state is given as \([18]\)

\[
\theta_0 = \cos^{-1} \sqrt{\frac{(\varepsilon_0 \Delta \varepsilon E_0^2)^2 - \gamma_1 \gamma_2 \gamma_2 + \gamma_2^2 \gamma^2}{2[(\varepsilon_0 \Delta \varepsilon E_0^2)^2 + \gamma_2^2 \gamma^2]}}.
\]

In the special case of \( E_0 = 0 \), \( \theta_0 \) reduces to

\[
\theta_0 = \frac{1}{2} \cos^{-1} \left( -\frac{\gamma_2}{\gamma_1} \right).
\]

The angle \( \theta_0 \) monotonically increases with increasing electric field, as shown in Fig. 2 where the values of the viscosities and the dielectric anisotropy for 5CB at 25 \(^\circ\)C, corresponding to the experimental conditions, are used. Expanding \( \theta \) up to the second order with respect to \( \Delta E \), we obtain the following expression for \( \Delta \theta \):

\[
\Delta \theta(t) = \Delta \theta_{2,0} + \text{Re}[\Delta \theta_{1,1} e^{i\omega t}] + \text{Re}[\Delta \theta_{2,2} e^{2i\omega t}],
\]

with

\[
\Delta \theta_{1,1}(\omega) = -\frac{\varepsilon_0 \Delta \varepsilon E_0 \Delta \varepsilon \sin 2\theta_0}{i \omega \tau + 1} \gamma_1,
\]

\[
\Delta \theta_{2,2}(\omega) = \frac{(1/2)|\Delta \theta_{1,1}|^2(\gamma_2 \gamma_2 \cos 2\theta_0 - \varepsilon_0 \Delta \varepsilon E_0 \sin 2\theta_0) + \Delta \theta_{1,1} \varepsilon_0 \Delta \varepsilon E_0 \Delta \varepsilon E_0 \cos 2\theta_0 + \varepsilon_0 \Delta \varepsilon \Delta \varepsilon^2 \sin 2\theta_0}{2i \omega \tau + 1} \gamma_1,
\]

and

\[
\Delta \theta_{2,0} = \Delta \theta_{2,2}(0),
\]

where the first subscript of \( \Delta \theta \) indicates the order with respect to \( \Delta E \) and the second one the harmonic order. The relaxation time \( \tau \) is defined by

\[
\tau = -\frac{\gamma_1}{\gamma_2 \gamma_2 \sin 2\theta_0 + \varepsilon_0 \Delta \varepsilon E_0 \cos 2\theta_0}.
\]

Next, we calculate the shear stress response. The shear stress \( \sigma_{yz} \) in the present case can be also expanded with respect to \( \Delta E \):

\[
\sigma(t) = \sigma_0 + \Delta \sigma_{2,0} + \text{Re}[\Delta \sigma_{1,1}(\omega) e^{i\omega t}] + \text{Re}[\Delta \sigma_{2,2}(\omega) e^{2i\omega t}],
\]

FIG. 1. (Color online) (a) A simple shear flow is applied along the \( x \) axis with a velocity gradient parallel to the \( z \) axis. An electric field is applied along the \( z \) direction. (b) We define \( \theta \) to be the angle between the director and the \( x \) axis when the electric field is applied.
where \( \sigma_0 \) is the shear stress with no ac electric field. It should be noted that the \( \omega \) response \( \Delta \sigma_{1,1} (\omega) \) appears under dc electric fields, as can be seen from Eq. (9); this response vanishes for \( E_0 = 0 \). The stress is independent of the polarity of the electric field as NLCs are nonpolar and, therefore, the stress response depends on \( E(\omega)^2 = E_0^2 + 2E_0 \Delta E \cos \omega t + \Delta E^2/2 [1 + \cos (2\omega t)] \) as shown in Eq. (6), clearly indicating that the \( \omega \) response \( \Delta \sigma_{1,1} (\omega) \) should emerge under dc electric fields in addition to the \( 2\omega \) response \( \Delta \sigma_{2,2} (\omega) \).

From Eqs. (5), (7a), and (9)–(12), the unperturbed shear stress \( \sigma_0 \) and the responses \( \Delta \sigma_{1,1} (\omega) \), \( \Delta \sigma_{2,0} \), and \( \Delta \sigma_{2,2} (\omega) \) are obtained:

\[
\sigma_0 = \dot{\gamma} \left[ a_1 \sin^2 \theta_0 \cos^2 \theta_0 + \frac{1}{2} (a_4 + (a_5 - a_2) \sin^2 \theta_0 + (a_3 + a_6) \cos^2 \theta_0) \right] \sin 2\theta_0, \tag{14}
\]

\[
\Delta \sigma_{1,1} (\omega) = \dot{\gamma} \left[ a_1 \cos 2\theta_0 - \frac{1}{2} (a_2 + a_3) + i \omega (a_3 \cos^2 \theta_0 - a_2 \sin^2 \theta_0) \right] \Delta \theta_{1,1} (\omega), \tag{15}
\]

\[
\Delta \sigma_{2,2} (\omega) = \frac{\dot{\gamma}}{2} \left[ \alpha_1 \cos 4\theta_0 - 2(a_2 + a_3) \sin 2\theta_0 + 2i \omega (a_3 \cos^2 \theta_0 - a_2 \sin^2 \theta_0) \right] \Delta \theta_{2,2} (\omega)
+ \frac{\dot{\gamma}}{2} \left[ a_1 \cos 4\theta_0 - (a_2 + a_3) \cos 2\theta_0 - i \omega (a_2 + a_3) \sin 2\theta_0 \right] \Delta \theta_{1,1} (\omega)^2, \tag{16}
\]

\[
\Delta \sigma_{2,0} = \Delta \sigma_{2,2} (0). \tag{17}
\]

When we compare the above theoretical result with experimental one, the parallel-plate geometry of the rheometer which is used in our experiment should be considered. For this geometry, the apparent shear stress is given by [8]

\[
\Delta \sigma^{(R)} (\omega) = \frac{4}{\gamma_R} \int_0^{\gamma_R} \Delta \sigma (\omega, \gamma) \gamma^2 d\gamma, \tag{18}
\]

where \( \gamma_R \) is the shear rate at the edge of the rotating disks. The numerically calculated results are presented in Sec. IV.

### III. EXPERIMENT

We used the NLC 5CB (4-n-pentyl-4’-cyanobiphenyl; Tokyo Chemical Industry) without any further treatment. Measurements were carried out with a parallel-plate rheometer (Physica MCR300, Anton Paar) at room temperature (25 °C).

![Graph](image)

**FIG. 2.** \( E_0 \) dependence of \( \theta_0 \) calculated from the EL theory. The angle \( \theta_0 \) increases monotonically and tends to saturate when \( E_0 > 200 \text{ V mm}^{-1} \).

5CB exhibits transitions from crystal to nematic phases at 18 °C and from nematic to isotropic phases at 35 °C, so we conducted experiments at 25 °C around the center of the nematic phase. The diameter of the rotating plate and the gap between the two parallel plates are 35 and 0.2 mm, respectively. In the rheometer, the shear rate is defined at the edge of the upper plate and the shear stress at the corresponding shear rate is calculated from the mechanical torque by assuming that the sample is a Newtonian fluid. Figure 1 shows the relation among the flow direction, the velocity gradient, and the electric field, which is applied to the sample by using a synthesizer (Model 1940, NF) and a high-voltage amplifier (Model 4005, NF). The experimental setup is shown in Fig. 3. The shear stress was measured with a vector signal analyzer (HP89410A, Hewlett-Packard) and the first- and second-order harmonics were obtained.

The shear stress response to ac electric field under steady shear flow and electric fields was measured by applying a small ac electric field \( \Delta E \cos (\omega t) \). We obtained the first-order response \( \Delta \sigma_{1,1} (\omega) \) and the second-order response \( \Delta \sigma_{2,2} (\omega) \), which should be proportional to \( \Delta E \) and \( \Delta E^2 \), respectively, for small \( \Delta E \). The dc electric field dependencies of the first- and second-order responses are shown in Fig. 4, where the measurements were done at \( \gamma = 10 \text{ s}^{-1} \) and \( E_0 = 100 \text{ V mm}^{-1} \). Linearity was confirmed to hold at least up to \( \Delta E = 20 \text{ V mm}^{-1} \). All the measurements were performed at \( \Delta E = 14.1 \text{ V mm}^{-1} \) and \( \gamma = 10 \text{ s}^{-1} \).

### IV. RESULTS AND DISCUSSION

First, we discuss the first-order response \( \Delta \sigma_{1,1} (\omega) \) shown in Fig. 5 (lines are experimental results and dots are theoretical predictions). The first-order response appears only when we apply a dc electric field \( E_0 \). When \( E_0 \) is low (\( E_0 = 20 \text{ V mm}^{-1} \)) [see Fig. 5(a)], the experimental stress response resembles Debye-type relaxation. However, as we increase \( E_0 \) to 80 \text{ V mm}^{-1} [see Fig. 5(b)], we can see that the response remains nonzero even at high frequencies, forming what is
referred to as a plateau. The emergence of the plateau is the most remarkable characteristic of the response to ac electric field under dc electric fields. From the EL theory, it is easily seen that the plateau comes from the third term with $i\omega$ in the bracket on the right-hand side of Eq. (15) because

$$\Delta \theta_{1,1}(\omega) \propto \frac{\varepsilon_0 \Delta \varepsilon E_0 \Delta E \sin 2\theta_0}{\gamma_1 \alpha_3 \cos^2 \theta_0 - \alpha_2 \sin^2 \theta_0 \tau},$$

(19)

It should be noted that the director response $\Delta \theta_{1,1}(\omega)$ vanishes at high frequencies, but the stress response $\Delta \sigma_{1,1}(\omega)$ remains nonzero.

At higher values of $E_0$, the height of the plateau is larger than at low frequencies, as shown in Figs. 5(b) (80 V mm$^{-1}$) and 5(c) (160 V mm$^{-1}$). The agreement between the experimental and theoretical results for all $E_0$ shown in Fig. 5 is fairly good. The dependence of plateau height $\Delta \sigma_{1,1}(\infty)$ on $E_0$ is shown in Fig. 6 for the experiment and the theoretical result in Eq. (15). From Fig. 6, we observe that when $E_0 < 40$ V mm$^{-1}$ the plateau is small. As we increase $E_0$ to more than 50 V mm$^{-1}$, the plateau height increases sharply. In the same figure, we also plot the $E_0$ dependencies of $\Delta \sigma_{1,1}$ calculated at zero frequency and experimentally obtained from Fig. 5 at 0.23 rad s$^{-1}$. The agreement between them is good. The low-frequency and high-frequency (plateau)

values exchange at around $E_0 = 90$ V mm$^{-1}$. The imaginary part of the response (Fig. 5) goes to zero at both low and high frequencies, and shows good agreement between theory and experiment. The peak or valley frequency of the imaginary part is seen to increase with increasing dc electric field, though it changes sign from positive to negative at around $E_0 = 90$ V mm$^{-1}$ corresponding to the above-mentioned exchange of the low- and high-frequency values of the response.

Next, let us discuss the second-order response $\Delta \sigma_{2,2}$ (Fig. 7). This response is more complicated than the first-order response since there are contributions from the first-order mode $\Delta \theta_{1,1}$ as well as $\Delta \theta_{2,2}$, as can be seen from Eq. (16). It should be noted that the second-order response appears even without a dc electric field, as shown in Fig. 7(a). The stress response resembles Debye-type relaxation for $E_0 = 0$. However, one may notice that the real part becomes slightly negative at around 10 rad s$^{-1}$. We have previously observed this negative part and shown that it originates from nonconservative forces due to the shear flow [8]. This is a remarkable characteristic of nonequilibrium steady states of systems under shear flow and is observed also in an immiscible polymer blend in which one polymer is dispersed as droplets.
in the other [19]. The nonconservative forces also violate the fluctuation-dissipation relation (FDR). Fatriansyah et al. have theoretically clarified the mechanism of the appearance of the nonconservative forces in NLCs and derived a modified FDR [7]. According to the theory, the nonconservative forces can emerge only when the director is out of the shear plane. In Sec. II, however, we assumed that the director is confined in the shear plane and, therefore, we cannot reproduce the negative part in the present model. The director may tend to be in the shear plane under a dc electric field. Therefore, it is expected that our monodomain model works better as the dc electric field is increased.

From Fig. 7, it is obvious that there is a plateau at every dc electric field except for $E_0 = 0$ [Fig. 7(a)]. As we increase $E_0$, the plateau, which is the characteristic of the system under dc electric fields, appears. The origin of the plateau in the second-order response is the same as that in the first-order response. The plateau comes from the $\omega$ term proportional to $\Delta \theta_{1,2}$ in Eq. (16), which includes a factor $(\alpha_3 \cos^2 \theta_0 - \alpha_2 \sin^2 \theta_0)$. This factor also appears in the $\omega$ term of the first-order response [see Eq. (15)]. Interestingly, this vanishes at $E_0 = 0$ due to the Parodi relation $\alpha_6 - \alpha_5 = \alpha_2 + \alpha_3$, which is easily proved by using Eq. (7b). Note that the second-order response does not vanish for $E_0 = 0$ unlike the first-order response. It is obvious that the factor is in general not zero for $E_0 \neq 0$. When we increase $E_0$ to 80 V mm$^{-1}$, the plateau at high frequencies rises, as shown in Fig. 7(b). The plateau becomes remarkable for $E_0 = 120$ V mm$^{-1}$ [Fig. 7(d)]. The agreement between the experimental and theoretical results is good. The imaginary part of the response also shows good agreement between theory and experiment.

Figure 8 shows the $E_0$ dependence of $\Delta \sigma_{1,2}$ calculated at zero frequency and experimentally obtained from Fig. 7 at 0.23 rad s$^{-1}$. Also in the same figure we show the $E_0$ dependence of the height of the plateau. Good agreement is obtained between the theory and experiment. The $E_0$ dependencies are more complicated than those in the first-order response.

Finally, we show experimental evidence that the plateau observed in the real part of the first-order response should be ascribed to the time derivative of the director, but not to $\Delta \theta_{1,1}$ itself. To do so, we made an optical measurement using crossed
FIG. 6. (Color online) $E_0$ dependence of the first-order response at very low frequency ($0.23 \text{rad s}^{-1}$ for the experiment and exactly zero for the theory), $\text{Re}[\Delta \sigma_{11}(\omega \to 0)]$. Also shown is the dependence of plateau height $\text{Re}[\Delta \sigma_{11}(\omega \to \infty)]$. For dc electric fields higher than around 90 V mm$^{-1}$, $\text{Re}[\Delta \sigma_{11}(\omega \to \infty)]$ becomes larger than $\text{Re}[\Delta \sigma_{11}(\omega \to 0)]$.

When an electric field is applied, the birefringence $n_x(\theta) = n_x(\theta) - n_0(\theta)$, where $n_0$ and $n_x$ are the ordinary and extraordinary refractive indices, respectively, will change and here the observation is assumed to be made perpendicular to the parallel plates as shown in Fig. 3. In NLCs, $n_0$ is independent of the director orientation $\theta$. However, $n_x(\theta)$ is dependent on $\theta$:

$$n_x(\theta) = \frac{n_\parallel n_\perp}{(n_\perp \cos^2 \theta + n_\parallel \sin^2 \theta)^{1/2}} - n_\parallel,$$

where $n_\parallel$ and $n_\perp$ are the refractive indices parallel and perpendicular to the director. On the other hand, the transmitted light intensity of the NLC under crossed polarizers is given by

$$I = I_0 \sin^2(2\alpha) \sin^2 \frac{\pi n_x(\theta) d}{\lambda},$$

where $I_0$ is the incoming light intensity, $\alpha$ is the angle between the polarizer and the $x$ axis, $d$ is the sample thickness, and $\lambda$ is the wavelength of the light in a vacuum. For a small change of $\theta$, $\Delta \theta$, due to the application of an ac electric field, the corresponding change of $I$, $\Delta I$, is obtained from Eqs. (20)

FIG. 7. (Color online) Frequency dispersion of $\Delta \sigma_{22}$ as a function of angular frequency $\omega$. The theoretical curves are obtained from Eq. (16). A plateau appears under dc electric fields as well as in the first-order response.
and (21):

$$\Delta I = I_0 \sin^2(2\alpha) \sin 2 \left[ \frac{\pi n_u(\theta_0)d}{\lambda} \right] \times \frac{n_\perp n_\parallel (n_\perp^2 - 2n_\parallel^2 \cos \theta_0) \sin \theta_0}{2(n_\perp^2 \cos^2 \theta_0 + n_\parallel^2 \sin^2 \theta_0)^{3/2}} \Delta \theta, \quad (22)$$

where $\theta_0$ is the angle without any ac electric field.

In the optical measurement we replaced the upper plate by a glass disk with diameter 40 mm so that we could observe the transmitted light through the sample. As a light source we used a halogen lamp (LS-LHA, Sumita Optical Glass). The light intensity was converted by a photosensor into a voltage and it was amplified (C6386, Hamamatsu Photonics).

The experimental result is shown in Fig. 9 for $E_0 = 200$ V mm$^{-1}$. Note that the vertical axis is adjusted so that the theoretical and experimental results coincide as well as possible, because it is difficult to determine the coefficient in Eq. (22). The agreement between the experiment and theory is good, though the data are scattered to some degree. The relaxation frequency experimentally observed is in good agreement with the one theoretically obtained. There is no plateau in the optical response, in contrast to the stress response, convincing us that the plateau observed in the shear stress response should be ascribed to the time derivative of the director. This plateau is a remarkable feature in the shear stress response brought about by the application of a dc electric field. Furthermore, by performing an optical measurement, the director response is confirmed to vanish at high frequencies, strongly supporting the above-mentioned mechanism for the appearance of the plateau. It was also clarified that the plateau in the second-order response disappears in the absence of a dc electric field, due to the Parodi relation, which is derived from the Onsager reciprocal relation.

V. SUMMARY

We have investigated the NESS response of an NLC to an ac electric field under constant dc electric field and steady shear flow. The first- and second-order shear stress responses were theoretically obtained from the EL theory assuming a monodomain model. It was found theoretically and experimentally that when we apply a dc electric field both responses remain constant and nonzero even at high ac electric field frequencies. That is, there is a plateau, which originates from the time derivative of the director. This plateau is a remarkable feature in the shear stress response brought about by the application of a dc electric field. Furthermore, by performing an optical measurement, the director response is confirmed to vanish at high frequencies, strongly supporting the above-mentioned mechanism for the appearance of the plateau. It was also clarified that the plateau in the second-order response disappears in the absence of a dc electric field, due to the Parodi relation, which is derived from the Onsager reciprocal relation.

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