<table>
<thead>
<tr>
<th>Field</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Title</td>
<td>SOME COMMENTS ON THE DEVELOPMENT OF THE THEORY OF PROTON TRANSFER IN SOLUTION</td>
</tr>
<tr>
<td>Author(s)</td>
<td>CHRISTOV, S. G.</td>
</tr>
<tr>
<td>Citation</td>
<td>JOURNAL OF THE RESEARCH INSTITUTE FOR CATALYSIS HOKKAIDO UNIVERSITY, 24(1), 27-43</td>
</tr>
<tr>
<td>Issue Date</td>
<td>1976-09</td>
</tr>
<tr>
<td>Doc URL</td>
<td><a href="http://hdl.handle.net/2115/25005">http://hdl.handle.net/2115/25005</a></td>
</tr>
<tr>
<td>Type</td>
<td>bulletin (article)</td>
</tr>
<tr>
<td>File Information</td>
<td>24(1)_P27-43.pdf</td>
</tr>
</tbody>
</table>

Hokkaido University Collection of Scholarly and Academic Papers : HUSCAP
Some Comments on the Development of the Theory of Proton Transfer in Solution

By

S. G. Christov*)

(Received January 14, 1976)

Abstract

The bond stretching model and the solvation barrier model for proton transfer in solution and their relations to the author's work are considered. The essential results of that work are shown to be quite independent of any assumption about the relative role of the bond-stretching and the solvent reorganization in the proton transfer. Some misinterpretations of the above treatment are discussed.

In a recent paper of Dogonadze and Kuznetsov, two different approaches to the calculation of the probability of proton transfer in polar media have been compared. The first one, originating from the work of Horiuti and Polanyi, takes into account only for the stretching of the chemical bond A—H+ of a molecule AH+ in a solution due to the chemical excitation of the vibrational states in the course of reaction. The other approach, used by Dogonadze et al., considers the primary role of the solvent polarization which changes during the proton transfer process, according to an idea suggested first by Libbi and developed further by Marcus, Hush, Levich and Dogonadze for electron transfer processes. A similar comparison between the two approaches is also made in a paper of Kristalik, Tsinisky and Titova. Surprisingly, in both papers, as well as in some earlier papers of the same authors, my work is quoted as a treatment of proton transfer reactions in which the role of the solvent is "entirely ignored" as in the bond-stretching model of Horiuti-Polanyi used by other authors. This statement is, however, completely incorrect, which is easily seen if one reads more carefully my papers.

The choice of a model to describe a physical process depends largely on the purpose of investigation. The model may be adequate to reality in some respect and not adequate in another respect. Thus, in 1935 Horiuti...
S. G. Christov

and Polanyi described the proton transfer reaction $AH^+ + B \rightarrow A + H^+ B$ in terms of a potential barrier obtained by the intersection of two curves representing the electronic energies of the bond to be broken $(A-H^+)$ and the bond to be formed $(H^+-B)$ as functions of the corresponding internuclear distances. This barrier model leads to a relationship between classical activation energy $E_a$ and reaction heat $Q$ of the form

$$E_a = E_0^a + \beta Q, \quad E_a - Q = E_0^a - \alpha Q$$

(1)

where $\beta$, and $\alpha = 1 - \beta$, are the “transfer coefficients” assumed to be constants. These relations permit to derive the Brønstedt equations for acid-base catalysis which relate the rate constants to the dissociation constants of the acid and the base. In a similar way one can obtain, as pointed out by Frumkin$^{14}$) the Tafel equation in electrode kinetics. It is easily seen that these conclusions follow from the geometric properties of the potential barrier and not from the assumption that the barrier represents the electronic energy of the system $A-H-B$. This model explains also the influence of the nature of the metal on the hydrogen evolution reaction. The theory of Horiuti-Polanyi$^2$) is consistent in the framework of the classical model assumed. However, this model is not adequate since the calculations show that at the actual internuclear distances the quantum-mechanical tunneling of the proton plays a dominant role$^*$. This suggests that the solvent effects are important in proton transfer processes.

Dogonadze et al.$^{3,4}$) have used a harmonic oscillator model$^{6,8}$ to describe the dynamical role of the solvent in proton transfer reactions. The general approach is based on a separation of variables using either a harmonic approximation for the proton vibration or a double adiabatic approximation, which means to include the proton energy into the electronic energy to obtain an effective potential for the motions of solvent molecules. This procedure implies that a solvent fluctuation is necessary to make possible the proton transfer by a tunneling process from the initial ground state to the final ground state of vibration. Thus, no any change of the $A-H$ bond-length takes place, so that the activation energy is entirely determined by the solvent reorganization. In the framework of this model a consistent quantum-mechanical theory is used to calculate the proton transfer probability, which is essentially based on the assumption that the Franck-Condon approximation is valid (i.e. the proton transfer occurs at fixed positions of the solvent molecules). A more careful examina-

$^*$ The possibility of proton tunneling was first assumed by Polanyi$^{15}$) who stimulated the calculations of Bawn and Ogden$^{16}$). Similar calculations have been performed by Bell$^{17}$, Christov$^{11,18}$, Conway$^{19}$, Dogonadze et al.$^4$)
Some Comments on the Development of the Theory of Proton Transfer in Solution

tion of this assumption seems to be necessary\(^*\). In any case, the model of DOGONADZE et al. is convenient to describe, at least qualitatively, the role of the solvent in proton transfer processes. This model is, however, incomplete as far as the translation-rotation motions of solvent molecules are disregarded\(^5\). It implies, moreover, that the solvent fluctuation takes place at a fixed distance between reactants. A justification of this adiabatic approximation is desirable. The model may be also not adequate, because it neglects completely the stretching of the A-H bond in all proton-transfer reactions\(^**\).

On the basis of the above assumptions the theory of DOGONADZE et al.\(^3,4\) provides a detailed picture of the molecular mechanism of charge transfer in solution and, in particular, of proton transfer at electrodes. The consequences of this theory agree qualitatively with the experimental facts concerning both the influence of the cathode nature on the proton discharge and the so called barrierless and activationless hydrogen evolution reactions\(^9\). However, the isotope effects are explained only by a change of the preexponential factor \(K\) in the Arrhenius equation

\[
v = Ke^{-Ea/kT},
\]

since the activation energy \(E_a\) is assumed to depend entirely on the solvent properties. This conclusion is not in accordance with the observation that in many proton transfer reactions\(^21\), including proton discharge\(^32\), the isotope substitution affects both \(K\) and \(E_a\)\(^21\). Furthermore, the theory of DOGONADZE et al.\(^3,4\) is not able at present to justify a fundamental equation of chemical kinetics—the Tafel relation

\[
\eta = a + b \ln i
\]

which is shown to be valid for the hydrogen evolution in a wide range of overvoltage \(\eta (\sim 1\text{ V and more})\) and several orders of magnitudes with respect to the current density \(i\).

Thirty years ago (1945–1948), my first work on the theory of metal ion discharge\(^22\; a\) was stimulated by Gurney\(^23\) who was the first to introduce the concepts of quantum mechanics in electrochemistry. The potential barrier is assumed to be a result of the intersection of two curves which describe the interactions of the ion with the polar solvent and the metal.

\(^*\) See footnote on p. 41.

\(^**\) Calculations with two dimensional models for the gas phase reaction AH+B→A+HB, where A and B are heavy particles (or atomic groups), show\(^20\) that the most probable configuration A–H–B at which the H-atom transfer occurs, involves a considerable stretching of the A–H bond. This might be the situation in the case of proton transfer in solution too.
S. G. Christov

lattice, respectively. This model implies a slow motion of the ion and an
adiabatic adjustment of the motions of the solvent molecules and the elec-
tron cloud in the metal. Subsequently\textsuperscript{22b), a similar picture was used to
describe the proton discharge: “We can represent the energy barrier for
the proton transfer by a potential curve in the metal-electrolyte boundary
region, obtained by combination of two separate curves representing the
potential energy of the proton in hydrated and adsorbed state, respectively.
The first curve will have a deep well because of the large hydration energy
of the proton, due to the considerable Coulomb forces acting between it
and the electric dipoles of the water molecules, which are related to the
small radius of the proton. The potential curve for adsorbtion has the
same form as that for adhesion of metal ions to the lattice of the same or
an other metal” (Ref. (22 b), pp. 67-68). Clearly, this is not the Horiuti-
Polanyi bond-stretching model in which the interaction of the proton
with the solvent is completely ignored but, in contrary, this is a model
which neglects entirely the bonding between the proton and the water
molecule. This is certainly an oversimplification of the real situation,
which is, however, allowed for the purpose of the investigation considered.

The problem was to derive the relationship between current density
and electrode potential taking into account for the possibility of nuclear
tunneling. For the purpose it is necessary to solve the Schrödinger
equation

\[ \frac{\hbar^2}{2\mu} \Delta \phi + (E - V(x)) \phi = 0 \]  \hspace{1cm} (4)

in order to calculate the transition probability through and over the po-
tential barrier \( V(x) \). The solutions \( \phi(x) \) depend only on the shape of the
barrier and not on the nature of the potential energy involved. Using an
arbitrary (one-dimensional) barrier model a current expression of the form

\[ i = \mathcal{I}_t(Q, T) K^{1/2} e^{-E_a(Q)/kT} \]  \hspace{1cm} (5)

has been derived\textsuperscript{22), where the classical activation energy \( E_a \) is expressed
as a function of reaction heat \( Q = Q_r + \eta \), or overvoltage \( \eta \), by

\[ E_a = E_t - \alpha \varepsilon \eta . \]  \hspace{1cm} (6)

In (5) \( \mathcal{I}_t(Q, T) \) is the tunneling correction to the classical Tafel equation

\[ i^t = K^{1/2} e^{-E_a(Q)/kT} = i^{0} e^{-\alpha \varepsilon \eta /kT}. \]

This correction depends on the geometrical properties of the barrier, the
mass of the ion, the temperature and is generally a function of reaction
Some Comments on the Development of the Theory of Proton Transfer in Solution

heat $Q$ (or overvoltage $\eta$). Therefore, in the general case, expression (5) does not represent the TAFEL equation (3). The conditions at which $x, (\eta, T)$ may be independent of $\eta$ have been also discussed in that time\textsuperscript{20}.

The problem has been treated again more extensively in a later period (1958–1963), using different one-dimensional models for the potential barrier (such as the asymmetric ECKART and parabolic potentials\textsuperscript{11a,18}). In this way it has been possible to estimate the tunneling correction $\alpha = \exp \left( -\frac{2}{T} \right)$ by both numerical and analytical calculations. The quantum-mechanical justification of the TAFEL equation (3) is given for the first time in 1958, when considering a large amount of tunneling ($x \approx 300$) through an ECKART barrier\textsuperscript{11a}). A general treatment of the problem in a closed analytical form, including any possible tunneling degree, has been done using an asymmetric parabolic barrier\textsuperscript{24a}). This allows to determine the conditions of validity of TAFEL equation and to derive expressions for the TAFEL slopes $b = d\eta / d\ln i$. Formulas for the classical transfer coefficients $\beta_e$ and $\alpha_e$ have also been obtained\textsuperscript{11,24a}). For an arbitrary potential barrier $V(x)$

$$
\beta_e = \frac{1}{2} \left( 1 + \frac{r^2 Q}{4E_0^2} \right), \quad \alpha_e = 1 - \beta_e, \quad Q = \epsilon (\varphi - \varphi_0),
$$

where $E_0$ is the barrier height at the electrode potential $\varphi = \varphi_0$ ($Q = 0$) and $r \leq 1$ (for a parabolic barrier $r = 1$).

The temperature dependence of the current as well as the kinetic isotope effects have been also investigated by means of the same simple barrier models\textsuperscript{18a, b}). A characteristic temperature was introduced\textsuperscript{11a)} as a very useful criterion for determining the role of nuclear tunneling. The simple expression\textsuperscript{25}

$$
T_k = \frac{h \nu^*}{\pi k}, \quad \nu^* = \frac{1}{2\pi} \sqrt{\frac{f^*}{\mu^*}},
$$

was derived for any simple continuous barrier, where $\nu^*$ is the frequency of an imaginary vibration with a force constant $f^*$ equal to the absolute value of curvature just at the barrier top, $\mu^*$ being the effective mass transferred. In the temperature range $T > T_k / 2$ the tunneling correction can be estimated by the formula\textsuperscript{18a, 25 c}

$$
\alpha = \frac{(\pi/2) (T_k / T)}{\sin [(\pi/2) (T_k / T)]} - \frac{1/2 (T_k / T)}{1 - 1/2 (T_k / T)}
$$

$$\times \exp \left[ \frac{T_k}{T} - 2 \right] \delta_0 (E_e - Q) \right].
$$

The second term may be neglected for $T > 2/3 T_k$. At $T = T_k$, by defini-
tion\textsuperscript{11 a,25 a)}, the probability for tunneling is just equal to the probability for hopping over the barrier. For $T>2T_k$, $\zeta \approx 1$, \textit{i.e.} the nuclear motion practically obeys the laws of classical mechanics. For $T<T_k/2$ tunneling largely prevails and quantum mechanics is absolutely necessary to describe the reaction course.

Evidently, the general results from these investigations are independent of the assumptions concerning the nature of interactions determining the barrier potential. No any statement is made anywhere in my work that the potential energy should be necessarily related to the bond stretching as in the Horiuti-Polanyi model\textsuperscript{*}). In contrary, it is claimed quite definitely that "the potential energy conditioned by the interactions of ion with all the surrounding particles in the metal and the solution passes through a maximum determining the height of the energy barrier for this process" (Ref. (18c), p. 724). It is only the \textit{existence} of the barrier a necessary condition for the derivation of the current-potential relationship (5) and for several other general conclusions concerning the temperature dependence of the current, the Bröndstedt relations, the isotope effects \textit{etc.}\textsuperscript{11,22,24,26} The restriction to a one-dimensional potential barrier is not essential for the purposes of a \textit{qualitative} description which incorporates the nuclear tunnel effect in the theory of proton transfer processes. It is, however, in general, not adequate to the real situation, where the potential energy is a function of all nuclear coordinates of the system, including reactants and solvent molecules. Therefore, a more complete description of reaction requires a multi-dimensional treatment using a potential energy surface $V(x_1, x_2, \cdots)$ instead of a potential curve $V(x)$.

The way for a generalization of the theory in this direction has been discussed in details already in Ref. (26). The first step is to relate the reaction to the classical motion of a configuration point along the line of minimum energy on the potential surface as made in the transition state theory. The second step is to include a factor $\zeta$, which takes into account for the non-classical behaviour of nuclei for motion along the reaction path. Assuming this motion to be entirely separable from the other motions (vibrations and rotations) we can calculate the tunneling correction in the usual way to obtain an equation of the form (5). This is the reason for

\textsuperscript{*}) This model has been used sometimes\textsuperscript{11 a,18 b,24} for qualitative discussions emphasizing, however, its shortcomings rather than its advantages. Thus, it is claimed that "in the presence of pure electrostatic interactions one can put some objections towards this model" (Ref. (24 a), p. 847).
some comments on the development of the theory of proton transfer in solution

the statement: "It is necessary to underline that the relation (7)* and the conclusions derived from there have rather general character. This follows from that, that the one-dimensional barrier can be considered as a profile along the "reaction path" on the surface of the many-dimensional barrier" (Ref. (26), p. 1557). A complete separation of the reaction coordinate is possible, for instance, if one treats the motions of reactants and products (including solvent molecules) as harmonic vibrations. This is just the model used by Dogonadze et al.3 4 in their treatment of electron and proton transfer processes. Therefore, many results of my previous investigations, based on an one-dimensional barrier potential, can be applied to this model, without any restrictions concerning the tunneling degree**).

The main shortcomings of the oscillator model, as mentioned above, is the neglect of the translation-rotation motions of reactants and solvent molecules. In particular, inclusion of the relative translation of reactants would lead to a curvilinear reaction coordinate as in gas phase reactions. This coordinate is dynamically non-separable except in reactants (products) region and transition state, i.e. the saddle on the potential surface. This restricts the applicability of one-dimensional calculations for quantitative estimates of tunneling corrections to relatively high temperatures, at which tunneling occurs mainly in an area around the saddle-point, i.e. near the top of the barrier along the reaction coordinate. Thus, in the region of moderate tunneling ($T> T_s/2$) a corrected transition state theory expression for the rate constant

$$v = \dot{\mathcal{X}}_{ae} \frac{kT}{h} \frac{Z_{ae}^+}{Z} e^{-E_s/kT}$$

(10)

applies, where $\dot{\mathcal{X}}_{ae}$ is given by the first term in (9), $Z_{ae}^+$ is the partition function of the "activated complex" (transition state) and $Z$ is the full partition function of reactants, both including the surrounding solvent molecules. This is just the expression discussed in my papers Ref. 11 b) and (26). Introducing (6), (7) and (9) into (10) gives a current-voltage relation of the type (5). The resulting expression is more general than (5) as far as all degrees of freedom of the over-all system (reactants + solvent) are included into the multi-dimensional potential surface, however, it is restricted to the temperature range $T> T_s/2$, while equation (5) applies for all temperatures.

*) It corresponds to Eq. (5) of the present paper.

**) This has been recently done using the harmonic oscillator model for the solvent in the framework of a complete theory of electron-transfer processes37. A similar treatment is possible to a large extent for proton-transfer processes37 b).
S. G. Christov

An important consequence from (10) is that the TAFEL equation is always valid in the range of moderate tunneling \( T > T_d / 2 \) where the second term in (9) only slightly depends on reaction heat \( Q \) (i.e. on electrode potential \( \eta \)) provided the classical transfer coefficient (7) is nearly constant, which requires that \( \tau Q / 4 E_c \ll 1 \). This justifies the conclusions derived earlier \(^{18b,34}\) by means of an one-dimensional treatment of ion (proton) transfer processes.

A more general treatment of these processes has been proposed on the basis of a new formulation of chemical kinetics \(^{28}\), which leads to an equation of the form

\[
\nu = \mathcal{Z} \frac{kT}{h} \frac{Z^*}{Z} e^{-E_u/kT}
\]

where \( Z^* \) is a partition function of reactants in which the motion along the reaction coordinate is excluded and \( \mathcal{Z} \) is a suitably defined quantum correction factor. The derivation of (11) is based on an exact quantum-mechanical expression in which the notion of an “activated complex” is avoided, i.e. no use is made of the hypothesis that the transition state represents a stationary state configuration being in thermal equilibrium with reactants. A formal generalization of activated complex theory in which \( \mathcal{Z}_{ac} \) in (10) represents an exact quantum correction was more recently proposed \(^{28b}\). A comparison between the classical limits of (10) and (11) then shows, that if \( \mathcal{Z}_{ac} = 1 \) equation (10) corresponds to the extreme case of a very slow motion along the reaction coordinate and when \( \mathcal{Z} = 1 \) expression (11) refers to the other extreme case of a very fast motion along the classical reaction path. These general formulations of the reaction rate theory allow a reconsideration of all previous investigations of ion transfer processes*. In this way, as already shown in Ref. (12), a justification of many earlier results on the basis of an exact quantum-mechanical theory becomes possible.

The above inspection shows that the essential results of my work on the theory of ion-transfer processes are not related with the bond-stretching model of Horiuti-Polanyi\(^{29}\) nor with the recent solvation barrier model of Dogonadze et al.\(^{3,4}\). For the purposes of my investigations no a priori assumptions have been made about the part played by the bond-stretching or the solvent reorganization, because, in principle, both are included in

---

*) This was first presented at the Electrochemistry meeting in Moscow, April, 1971 as well as at the 22nd Meeting of the International Society of Electrochemistry, Dubrovnik, Yugoslavia, September 1971, followed by the International School of Quantum Electrochemistry, Ohrid, Yugoslavia, September, 1971. See Ref. (12).
Some Comments on the Development of the Theory of Proton Transfer in Solution

the potential barrier.

Therefore, there is a large misinterpretation of the results of my work as presented in the papers of Dogonadze et al.\textsuperscript{12} and Kristalik et al.\textsuperscript{9} This can be immediately seen just in my papers referred to by those authors. Thus, for example, it is stated: "It is obvious that the absolute values of the barrier parameters, calculated on the basis of special one-dimensional models, cannot be of great importance, if we have not sufficient reasons to believe that no changes in the electronic configurations of the unreacting atoms or no considerable departure from the equilibrium polarization of the solvent occur during the proton transition. In the last case a multi-dimensional interpretation of the results of such calculations, as discussed above, is necessary. Especially, then it is not permissible to take the reduced mass of the system equal to the proton mass, so that the effective (one-dimensional) barrier width will depend on the choice of this magnitude \((\mu^* \neq m_H)\)" (Ref. (11 b), p. 182). This statement concerns a semi-empirical approach for estimating the parameters of an effective one-dimensional barrier using experimental data for isotope effects which has been used independently by Bell\textsuperscript{29} and myself\textsuperscript{18}. The results of such calculations are usually interpreted\textsuperscript{29,30} by means of the bond-stretching model as parameters of the actual barrier for the proton transfer. The above interpretation in terms of a many-dimensional barrier, including motions of reactants and solvent molecules, has been first proposed by myself in Ref. (26). According to this interpretation "using experimental values for the kinetic parameters one can estimate the barrier height \(E_t\) and the product \(l/\mu\), i.e. determine \(\mathcal{K}_t\), without knowledge of the effective mass \(\mu\). If we assume \(\mu = m_H\) we can calculate the width \(2l\) of a parabolic barrier which approximates the top region of the effective one-dimensional barrier for the proton discharge. The one-proton approximation is, however, not a necessary condition for estimating the role of the tunnel effect in the above manner" (Ref. (26), p. 1558). Repeatedly, it is stated: "Assuming that proton-transfer processes occur in the region of moderate tunneling we can estimate the tunneling corrections using Eqs. (5) and (6) on the basis of experimental data for the kinetic parameters \(E'_a\), \(K'\) and \(S\). Thus, the characteristic temperature \(T_k\) can be calculated by means of Eq. (3) without knowlege of the potential energy surface. Inversely, we may estimate the dimensions of the effective one-dimensional barrier, which is equivalent to the real many-dimensional barrier. Such calculations have been made independently for several catalytic acid-base reactions\textsuperscript{14,15} and for the electrolytic hydrogen evolution\textsuperscript{3,5}. In this way, as expected, values
for $\mathcal{E}$, between 1 and 7 have been found thereby confirming the rule of a moderate role of tunneling in proton-transfer processes in solution" (Ref. (12), p. 70).

I believe, it is not necessary to give more references to show that the general approach in my work is based on the idea that, \textit{a priori}, bond-stretching and solvent reorganization play equally important roles in the kinetics of proton transfer processes. Consequently, the statements of Dogonadze et al.\textsuperscript{1)} that I treat the proton-transfer only \textquotedblleft as the process of movement of the system on two-dimensional potential energy surface\textquotedblright and \textquotedblleft this approach ignores entirely the rearrangement of the solvent molecules in the course of the reaction\textquotedblright are quite misleading.

Actually, the two-dimensional considerations in Ref. (11 b) concern only the simple gas phase reactions of the type $\text{AH} + \text{B} \rightarrow \text{A} + \text{HB}$, where A and B are heavy atoms or atomic groups, for the purpose of comparing with the results of the usual one-dimensional treatment of the reaction coordinate. The comparison shows that this treatment overestimates the tunneling corrections not to much if the reaction proceeds in the region of moderate tunneling ($T > T_k/2$) or somewhat in the region of large tunneling ($T \leq T_k/2$) as is usually the case at room temperatures. The same conclusions are recently drawn in an undoubted way on the basis of exact two-dimensional calculations$^{28 b})$. These conclusions agree with the results of the above semiempirical approach of estimating tunneling corrections for proton transfer in solutions$^{18,29}$, which actually imply, as discussed above, a multi-dimensional potential surface including all motions of reactants and solvent molecules$^{11 b,30}$. At $T \geq T_k/2$ the most probable reaction path crosses the saddle point of the surface very near to the classical reaction coordinate$^{20}$, which allows an approximate estimation of the tunneling correction using the energy profile along that coordinate. In particular, in the temperature range $T > 2/3 T_k$, the first term of formula (9) represents a quite good approximation, provided $T_k$ is calculated by (8) with the corresponding value of the effective mass $\mu^\text{eff}$. Taking $\mu^\text{eff}$ to be equal to the proton mass ($\mu^\text{eff} = m_H$) leads to lower values of the tunneling corrections$^{11 b,20}$. These conclusions are valid not only for two-dimensional but also for arbitrary many-dimensional potential surfaces$^\text{*}$. This is the basis of the explanation of the isotope effects in hydrogen

\textsuperscript{*} Wigner$^{31}$ has shown that for a $n+1$ dimensional energy surface the tunneling correction is given to a first approximation by $\mathcal{E} = 1 + h\nu^\text{eff}/24 kT$. This result may be obtained by a series expansion of the first term in (9) if only the first two terms of the series are considered.
Some Comments on the Development of the Theory of Proton Transfer in Solution

evolution I proposed in Ref. (12). There, the above formula (9) for the tunneling correction was used, which implies a parabolic approximation of the potential along the reaction coordinate in the vicinity of the saddle point of the many-dimensional potential surface (See Fig. 1 in Ref. (12)). Although, quantitatively, this formula is sufficiently accurate only for $T > 2/3 T_k$, it is quite suitable for qualitative purposes also for $T \geq T_k$. It follows from it that “the tunneling factor $\mathcal{E}$, will generally decrease with the increase of (the electrode potential) $\varphi$.” If $T > 2/3 T_k$ the second term in (7 a) may be neglected so that Eq. (3) is obtained, which is now independent of $Q(\varphi)$. It results that the electrolytic separation factor according to (6) should decrease with the increase of electrode potential, when $T < 2/3 T_k$ and it remains constant when $T > 2/3 T_k$. These predictions seem to be the unique explanation of the experimentally observed strong potential dependence of the $H/T$ separation factor in acid solutions and its potential independence in basic solutions. In the first case, because of the attraction of the $H_2O^+$ ion by the cathode the transfer distance of the proton is certainly smaller than in the second case, when a proton from the neutral $H_2O$ molecule is discharged. Hence, the effective barrier width for the proton transfer in acid solutions will be smaller than in basic solutions, so that it is likely that if in the first case the reaction occurs at $T \approx T_k/2$ it may proceed in the second case in the region $T > 2/3 T_k$” (Ref. (12), p. 71).

Krishtalik et al. have misinterpreted the above explanation when claiming that in it the “proton coordinate” is concerned. Actually, in Ref. (12) $T_k$ is defined by the above Eq. (8) for a many-dimensional energy surface and at $T \geq T_k/2$ the formula (9) for $\mathcal{E}$ refers to tunneling along the reaction coordinate in the saddle-region. It is not the proton, but a configuration point with an effective mass $\mu^*$ which tunnels through the barrier along that coordinate. Both the motions of the proton and the solvent molecules, which are not separable in the saddle-region, are included in this description of the tunneling process (although practically the quantum behaviour of the system is determined by the proton motion only). Isotope substitution ($H \rightarrow D$) affects $T_k$ and $\mathcal{E}$ through the corresponding change of the effective mass. Any change of the barrier along the “proton coordinate”, which facilitates tunneling of the proton, will increase the tunneling of the system-point along the reaction coordinate, too. This situation can be described also in terms of the change of an effective

*) Formulas for $T \leq T_k/2$ and $T \geq T_k/2$ are also given in Ref. (12) (Eqs. 7 a, b, c). See also Ref. (24 a).
S. G. Christov

barrier for the proton tunneling, in the sense discussed above. This is
the meaning of the explanation of the isotope effects in electrolytic hydro­
gen evolution proposed in Ref. (12). Evidently, it is not related with the
bond-stretching model at all, as incorrectly claimed by KRISHTALIK et al.9)
Evidence that the parameters of the many-dimensional barrier considered
fit the conditions $T \geq T_k/2$ was also given by stating that “the possibility
of large tunneling ($T < T_k/2$) is to be excluded because it leads to abnormal
high TAFEL slopes (see below). Thus the potential dependence of $\mathcal{E}$,
according to (7a, b) is consistent with the classical (practically constant)
TAFEL slopes in the corresponding region $T \geq T_k/2$” (Ref. (12), footnote
p. 71).

It should be stressed that in this way it is possible to explain the
experimental fact30) that in hydrogen evolution both the apparent activation
energy $E_a$ and the pre-exponential factor $K$ in the empirical ARRHENIUS
equation (2) change due to the isotope substitution. This fact contradicts
the consequences of the model of DOGONADZE et al.3-4), that $E_a$ remains
the same and only $K$ is affected by that substitution.

There are no any difficulty, in principle, to explain the barrierless and
activationless processes, as well as the influence of the nature of metal
cathode on the proton discharge, by means of the concept of a potential
surface including all interactions with the solvent and the metal. The
formulas (7) for the classical transfer coefficients

$$\beta_s = \frac{\partial E_s}{\partial Q}, \quad \alpha_s = 1 - \beta_s,$$

(12)

can be easily derived24a,b) using the parabolic approximation of the barrier
potential along the reaction coordinate near the saddle point. The quantum
transfer coefficients defined by11b,12)

$$\beta = \frac{\partial E_a}{\partial Q}, \quad \alpha = 1 - \beta,$$

(13)

where $E_a$ is the experimental activation energy, can be related to the
classical ones by the equation12,28a)

$$\beta = \beta_s + kT^2 \frac{\partial \ln \mathcal{E}}{\partial T \partial Q}$$

(14)

which follows from (10) or (11). We have $\beta=1$ ($\alpha=0$) for barrierless and
$\beta=0$ ($\alpha=1$) for activationless processes, hence
Some Comments on the Development of the Theory of Proton Transfer in Solution

\[ \beta_e = 1 - kT^2 \frac{\partial \ln \mathcal{Z}}{\partial T \partial Q}, \quad \text{barrierless} \]

\[ \beta_e = kT^2 \frac{\partial \ln \mathcal{Z}}{\partial T \partial Q}, \quad \text{activationless}. \]

These relations are quite general and independent on any hypothesis about the detailed mechanism of the reaction. Eqs. (13) and (14) show that only if the quantum correction \( \mathcal{Z} \) is independent of reaction heat \( Q \) (or electrode potential \( \phi \)), then, \( \beta = \beta_e (\alpha = \alpha_e) \). This is certainly the case when the reaction proceeds in the region of moderate tunneling \( (T > T_k/2) \) where the second term in (9) may be neglected. In the region of large tunneling \( (T < T_k/2) \) however, in general, \( \beta \neq \beta_e (\alpha \neq \alpha_e) \). This is, in particular, the situation when barrierless and activationless processes occur for which according to (15) \( \beta_e < \beta = 1 \) and \( \beta_e > \beta = 0 \), respectively. These general conclusions have been illustrated using simple (one-dimensional) models for the barrier along the reaction coordinate assumed to be separable\(^{11,12}\).

Another definition of the transfer coefficients

\[ \beta_k = -kT \frac{\partial \ln \nu}{\partial Q}, \quad \alpha_k = 1 - \beta_k, \quad (16) \]

closely related to the BRÖNSTEDT equation (TAPEL equation), should be distinguished from (13). We obtain, indeed, from (10) or (11) the relation

\[ \beta_k = \beta_e - kT \left( \frac{\partial \ln \mathcal{Z}}{\partial Q} + \frac{\partial \ln K}{\partial Q} \right), \quad (17) \]

where \( K = \frac{kT^2}{h} \frac{Z^*}{Z} \), which generally differs from (14). As pointed out in Ref. (12), p. 73, only when both the quantum correction \( \mathcal{Z} \) and the partition function ratio \( Z^*/Z \) are independent of reaction heat, we obtain \( \beta_k = \beta = \beta_e \). Therefore, a possibly detectable difference between \( \beta_k \) and \( \beta \) may give us evidence for a large degree of tunneling\(^{13}\) and should be taken into account when interpreting the barrierless and activationless processes too\(^{14,15,16}\). This detailed discussion is obviously overlooked by KRISHTALIK et al.\(^9\)

The general trend of my investigations has been to avoid possibly all unnecessary assumptions which may restrict the validity of the relations derived. Such assumptions are, for instance, that only the bond-stretching or only the solvent reorganization are responsible for the proton transfer. In the general case, the activation process involves approaching of reactants, changes of chemical bonds and rearrangement of solvent molecules. The relative role of each of these processes may vary to a large extent with the variation of reactants and solvent nature. Therefore, a general
theory of reactions in solution should take into account *a priori* in an 
equal way for all degrees of freedom of reactants and solvent\(^{12}\).

The way to the generalization of a theory is not always easy and 
straightforward. Different ways are often followed by different investiga-
tors. In chemical kinetics the solvent effects have been frequently neg-
lected\(^2\) or underestimated when applying transition state theory, account 
being taken usually by approximate estimates of the solvation energy of 
reactants and activated complexes in assuming equilibrium configuration of 
the solvent molecules\(^{33}\). In the first period of my own work\(^{22,24}\) a such 
reversible solvation during the ion transfer has been also implicitly assumed, 
however, without using activated complex theory. The dynamical role of 
the solvent was first taken into account in electron-exchange reactions. For 
the purpose Marcus\(^6\) and Husch\(^7\) used transition state theory in treat-
ing adiabatic processes, while Levich and Dogonadze\(^8\) were concerned 
with a treatment of non-adiabatic reactions on the basis of the quantum-
mechanical perturbation theory. The possibility of a similar consideration 
of proton transfer was first discussed by Kuznetsov\(^{34}\) in terms of the 
(not very clearly defined) notion of a "proton term". Independently, during 
the Faraday Discussion on "The Kinetics of Proton Transfer Processes" 
(1965) Bell\(^{35}\) raised the question of a possible role of non-equilibrium solva-
tion from point of view of the activated complex theory. This discussion\(^*)\) 
stimulated my work\(^{11 b,26}\) in the direction of a generalization of the theory 
to include both solvent-effects and quantum effects (nuclear tunneling) in 
a many-dimensional description of the (adiabatic) proton-transfer reactions. 
In the same time Dogonadze, Kuznetsov and Levich\(^3\) applied the 
harmonic oscillator model for the solvent to the proton discharge, introducing 
the concept of an "electron-proton term" in a well defined way. This 
model is very useful for an application of perturbation theory to describe 
the irreversible solvent polarization in non-adiabatic processes, but it might 
overestimate the role of the solvent in the proton transfer. In the subse-
quent development of the theory by Dogonadze et al.\(^4\) the adiabatic pro-
cesses are also considered by introducing additional criteria for a separation 
of the proton motion from that of solvent molecules in the transition

\(^*)\) During this discussion\(^{36}\) I emphasized at many places the role of the solvent 
(reversible and irreversible polarization) in proton transfer processes. Thus, for 
instance, it is stated: "If we assume a barrier width of \(r_0 \approx 0.5-0.8\) A (for an 
orientation of one H-O-bond normal to the electrode surface), which leads to large 
proton tunneling, it is again possible to explain the experimental facts by sup-
posing a significant contribution of non-equilibrium solvation of the transitoin 
state to the activation energy" (Ref. (36), p. 255). See also p. 60, 263, 266.
Some Comments on the Development of the Theory of Proton Transfer in Solution

configuration of the system\(^*\). Account is taken, in principle, also for the bond stretching, however, the primary role is ascribed to the reorganization of the solvent. In my recent work\(^{28}\) the nonadiabatic processes were included in the general formulation of the theory. A detailed treatment of electron transfer reactions from this point of view, in which the restrictions of perturbation theory are avoided, was presented using the harmonic oscillator model for the solvent\(^{27}\). A similar treatment of proton transfer processes is also possible\(^{27b}\). Thus, different ways have been followed by Dogonadze et al.\(^{3,4}\) any myself to a more general theory of charge-transfer in solution.

The famous theory of Horiiuti and Polanyi\(^{2}\) has played and plays also nowadays an important role by stimulating the development of chemical kinetics. The more recent theory of Levich and Dogonadze,\(^{8}\) further developed extensively by Dogonadze et al.\(^{4}\), is certainly an important contribution to the study of charge-transfer processes in solution. To recognize this does not mean at all that this is the unique consistent

\(^*\) The conditions for a separation of the motions of proton and solvent molecules was initially defined by\(^{3}\)

\[
\Delta E = \hbar \nu_p \gg \hbar \nu_s (< kT)
\]

where \(\nu_p\) and \(\nu_s\) are the vibration frequencies of the proton and the solvent molecule, respectively. This implies, that both the electron and proton transfer probabilities are very small (completely non-adiabatic reactions), so that the electron-proton transfer takes place in a very small region of configuration space (including proton and solvent coordinates). If, however, the electron transfer probability is large (electronically adiabatic processes), then, there is a large transition region in configuration space in which the above condition of separability is not applicable.

Subsequently\(^{4}\) an additional condition

\[
\Delta E_{\beta} = \hbar \nu^\beta \gg kT (> \hbar \nu_s)
\]

for the transition region is introduced. Here \(\nu^\beta\) is defined by (8) for a motion along the proton coordinate, so that the above condition is actually identical with \(T \ll T^\beta_{\gamma} (T < T^\beta_{\gamma}/2)\), which means that the proton transfer occurs predominantly by tunneling. If, however,

\[
\Delta E_{\beta} = \hbar \nu^\beta \lesssim kT
\]

\(i.e. T \gtrless T^\beta_{\gamma} (T > T^\beta_{\gamma}/2)\), the proton motion in the transition region is a quasiclassical (or classical) one and cannot be separated from the motions of solvent molecules\(^{27b}\). The Franck-Condon approximation (fixed positions of solvent molecules during the proton transfer) is not applicable in this situation, although \(\hbar \nu_p \gg \hbar \nu_s\) in the initial and final state. The conditions (a) and (b) together justify the double adiabatic approximation used by Dogonadze et al. The idea to include the energy of a fast vibration into the adiabatic potential of the system has been first proposed by Hirschfelder and Wigner\(^{27}\) as an way for a justification of transition state theory. The work of Dogonadze et al. is a successful application of this idea to nonadiabatic processes. This point will be discussed elsewhere\(^{27b}\).
quantum theory of these processes, nor that earlier or other simultaneous investigations in the same field should be overlooked or misinterpreted. Representing an older generation, I believe, it is necessary to quote all what has been done previously by other authors and to compare more carefully the results obtained by different methods. An objective information is needed for the history of the field and for the education of young people starting research in that field. It would be useful for everybody to know that any problem can be treated using different approaches, each of them having some advantages and some shortcomings. Therefore, any attempt to treat the theory of charge transfer from an other point of view could contribute to a more complete understanding of these complicated chemical processes.

References

15) M. POLANYI, Naturwiss., 21, 316 (1933).
Some Comments on the Development of the Theory of Proton Transfer in Solution

34) A. M. KUZNETSOV, *“Osnovnie voprosi sovremennoi teoreticheskoi elektrokimii”* (Fundamental Problems of the Contemporary Theoretical Electrochemistry), Mir, Moskwa, 1965, p. 40.