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Abstract

We investigate how an amoeba mechanically moves its own center of gravity using the model organism Physarum plasmodium. Time-dependent velocity fields of protoplasmic streaming over the whole plasmodia were measured with a particle image velocimetry program developed for this work. Combining these data with measurements of the simultaneous movements of the plasmodia revealed a simple physical mechanism of locomotion. The shuttle streaming of the protoplasm was not truly symmetric due to the peristalsis-like movements of the plasmodium. This asymmetry meant that the transport capacity of the stream was not equal in both directions, and a net forward displacement of the center of gravity resulted. The generality of this as a mechanism for amoeboid locomotion is discussed.

condensed running title: Locomotive mechanism of an amoeba

keywords: amoeboid movement, cellular rhythm, migration, visualization, soft matter

1 Introduction

Amoebae form temporary structures for movement called pseudopods. These deformed regions of the cell subsequently disassemble, and the cell continues to form new pseudopods while disassembling the old ones. Thus, amoeboid movement is based on a continuous deformation of cell shape induced by the motive force of the protoplasmic flow, which is driven by osmotic and mechanical pressures. Because the motive force drives the flow of protoplasm and deformation of cell, amoeboid movement can be characterized by the spatiotemporal variation of flow and deformation[1].

Amoeboid movement is associated with drastic changes in cell shape. So studies naturally focus on what mechanical forces are involved and how they are coordinated to move the mass of the cell. In other words, the problem is to determine how the locally generated forces are organized in order to move the entire cell body.
The local force generation originates from contractile proteins like actin and myosin. The stresses generated by active contraction of actomyosin and osmotic pressures generated by depolymerizing actomyosin are possible sources of force generation. In *Amoeba proteus*, one of the most widely used model organisms for study on amoeboid movement, it was reported that posterior regions of amoeba actively contracted by consumption of ATP and pushed protoplasmic sol forward[2, 3, 4, 5, 6]. On the contrary, a totally different theory was also proposed: naked protoplasmic sol without any cell membrane showed the ability to move; posterior parts were pulled forward by anterior regions where transitions of protoplasm from sol to gel occur[2, 6].

The above two theories seem contradictory, and each theory is supported by experimental results. However, it is possible that both mechanisms are involved simultaneously in amoeboid motility. The relative importance of the two mechanisms may vary with internal and external conditions. Understanding the forces involved in amoeboid locomotion is one of the classical problems of cell biology and continues to be an active area of research. At the present time, it is very loosely accepted that high pressure generated in the posterior region pushes protoplasm forward[7, 8, 9].

In addition to the cytological experiments discussed above, techniques of molecular biology have been used to understand actin-myosin dynamics and their role in pseudopod extension and retraction. Visualizing the spatio-temporal variations of actin protein and associated molecules gives dynamic images of cell movement. Based on these experiments, various mechanisms for pseudopod formation were proposed. Nonetheless it is still an open question as to how a whole cell can move. It is difficult to coordinate measurements of the extension/retraction of pseudopodia with spatial measurements of mass transport throughout the entire cell body with sufficient resolution.

Here we consider the global problem of amoeboid movement: how do amoebae organize these locally generated forces to move their center of gravity? In this paper, we combine experimental measurement for mass transport and a theoretical explanation for the observed phenomena in order to identify the key processes involved in the displacement of the mass of the cell.

The model organism used here is the plasmodia of the true slime mold *Physarum polycephalum*, a common model organism for studying cell motility. The *P. polycephalum* plasmodium is a giant protoplasmic aggregate that shows a wide variety of cell behaviors. Its rhythmic contractions and the resulting streaming of protoplasm have been well studied from a cytological point of view [10, 11, 12, 13]. Recently, researchers have detected patterns of locally self-sustained rhythmic contraction associated with the cell’s behavior [14, 15, 16, 17, 18, 19, 20, 21, 20], implying that the streaming pattern is organized as a single system throughout the cell.

Pattern formation of the rhythmic contractions is involved in the coordination of local contractile activity and has been considered from two viewpoints: first, the theory of so-called coupled oscillator systems [22, 24, 25, 26, 23, 27, 28]; and second, the theory of complex viscoelastic matter [29, 30, 31, 32, 33]. To unify these two views, it is essential to clarify how the movement of the plasmodium is generated by the spatiotemporal pattern of contraction and streaming. Towards this goal, in this paper we make spatio-temporal measurements of the streaming velocity and the body deformation and relate this to the movement of the center of mass of the organism.
To relate the local transport to the displacement of the center of mass, it is necessary to know the flow velocity at all regions of cell to sufficient accuracy. For this purpose, we develop a new technique for measuring the velocity field of protoplasmic streaming through the entire body with a quasi two-dimensional extent using particle image velocimetry. Although this technique was developed for *Physarum*, it has the potential to be applied to other model systems of amoeboid movement.

When plasmodia are smaller than about 100–200 µm, no regular rhythmicity of protoplasmic streaming and no contraction is observed. These tiny plasmodia can move, but the speed of movement is very small. When the size reaches 200–300 µm, regular rhythmic contraction and streaming appear and the locomotion speed is much faster than that of the smaller plasmodia. The shape of the body becomes tadpole-like as shown in Fig. 1 (a). Thus, there is a critical size for the organism to exhibit fast locomotion and organized rhythmic activity. In our experiments, we studied organisms in the tadpole shape that exhibit the fast locomotion.

Based on these experiments, we present a physical mechanism for amoeboid movement, focusing on displacement of center of mass, in *Physarum*. The mechanism is proposed for *Physarum* but it may be applicable to other model systems such as *Amoeba proteus* etc., and we discuss the generality of the mechanism.

2 Organism and methods

2.1 Preparation of plasmodia for observation of protoplasmic streaming and deformation of cell shape

Plasmodia of *P. polycephalum* were grown on oat flakes for a few days in troughs (35 x 25 cm²) under dim light. Tiny portions (less than 1 mm³) were cut from the front tips of the plasmodia and placed on a plain agar plate. After waiting for several hours until the plasmodial pieces were moving around and had tubular shapes, portions of their tips were again removed, placed on another agar plate, and cover glasses were placed over them. After standing overnight, the fragments displayed amoeboid movement. Different samples had different forms, but only those with a tadpole-like shape were used, as this seemed to be the simplest structure permitting reasonable migration rates.

Each sample was pressed downward and squeezed by the weight of its cover glass, and was sufficiently transparent for the protoplasm to be observed with a microscope (type VH5000; Keyence Co., Tokyo, Japan). The protoplasm was full of intracellular vesicles, and the thickness of the organisms remained relatively constant during amoeboid motion. The streaming vesicles were markers yielding information on flow velocity. Microscopic images were taken with a charge-coupled device (CCD) camera and recorded as a digital video (DV) movie.
2.2 Measurement of velocity field of protoplasmic streaming by particle image velocimetry

The DV format movies of plasmodia were transferred from the DV camera to computer files, and then read with analyzing programs. The velocity fields inside the plasmodia were measured by a method called particle image velocimetry ([34]). In this approach, movies of fluids containing small marker particles are numerically analyzed to determine the velocity fields by tracking the movement of each particle, assuming the velocity of the marker particle to be equal to that of the fluid around it.

As the plasmodia already contained the vesicles in our case and they could not be removed, we used them as marker particles. Here we briefly describe the process of particle recognition and velocity field measurement. Appendix A gives more complete and precise description.

The original video is in full color. But the color is not strong enough to be useful in the subsequent analysis. So we are working with the converted gray scale images like in Fig. 1 (a). In this example, the vesicles appear as dark spots.

As we mainly interested in the moving particles, we want to eliminate immovable particles and enhance the images of moving particles. This is accomplished by subtracting the image accumulated over a long period (about 17 seconds) from the present image. A sample of the image enhanced in this way is shown in Fig. 1 (b). In this image, the darker spots represent moving particles, the lighter spots represent the free space previously occupied by particles in the accumulated image. To recognize the moving particle, the pixels darker than a threshold are defined to be occupied by particles and one connected group of occupied pixels (indicated by white polygons in Fig. 1 (b)) is defined as one particle.

Next we track the movements of recognized particles. This amounts to identifying a particle in one frame with a particle in the next frame. This task is not always possible for every particle. Especially, in our case, the particles themselves are not stable. The vesicles changed shape and aggregated to form larger particles that may subsequently split again.

To avoid the complexity and to minimize the possible errors in this situation, we take the simplest approach to this task. We only identify two particles in consecutive two frames if and only if two particles overlap each other exclusively: a particle in the present frame overlaps not multiple particles but only one particle in the next frame and vice versa. Some sample trajectories connecting the center of gravity of identified particles are shown in Fig. 1 (c). The longest trajectory near the center lasts over 1 second.

We calculate velocity of each particle from these trajectories. To exclude the possible erroneous identifications, we calculate velocity only for trajectories of more than 4 frame length. Thus we can assign velocity to some particles as shown in Fig. 1 (d).

As seen in this figure, the number of particles successfully assigned velocities seems too little at one moment. But if we collect velocity data over a few seconds, we get enough data to interpolate the entire space. In Fig. 2 (a), the velocity data of last 3 seconds are depicted. We assign some pixels the velocity averaged over time according to the method described in Appendix A. In this stage, the velocity is not defined on every pixel.

Then the velocity is averaged over space by the method in Appendix A. If the initial
data of velocities of clusters is dense enough, the velocity is assigned on every pixel as depicted in Fig. 2 (b).

As a check, we compare the trajectories of the vesicles and the trajectories of virtual fluid particles obtained by integrating the velocity field measured above. The integration is calculated numerically using Runge-Kutta method. The values of the vector field for pixels are assigned to the centers of the pixels. The values of the vector field at the other points are bilinearly interpolated from these values at lattice points.

Depicted in Fig. 2 (c) is the superposition of the positive part of the enhanced image discussed above. A moving vesicle appears as a elongated spot indicating its direction of movement. In Fig. 2 (d), we draw integrated orbits on (c). They agree very well considering the size of one pixel.

Since the resulted velocity field is obtained by averaging over some tens of individual data, theoretically the error of the mean is only a few percent even if the error of the individual data is some tens percent. In this case, the error should be measured by the time and space resolutions which are about 6 seconds and 5 µm. As the typical period of shuttle flow in plasmodia is about 100 seconds, this time resolution is good enough to investigate the various phenomena related to shuttle flows. But the typical width of channels in our plasmodia is 10 to 30 µm. So, for example, to get the velocity profile across the channel or to get the total flux through a section of the channel is beyond the precision of our data.

### 2.3 Determination of cell shape and position of center of mass, and introduction of anterior-posterior coordinate system for plasmodia

The cell shape is detected by outlining the edge of plasmodium. The center of gravity of a plasmodium is calculated by assuming the existence of unit point mass at the center of each pixel occupied by the plasmodium.

To measure and describe the movement of plasmodia, we need an appropriate time-independent coordinate system. Our coordinate system consists of one longitude curve coinciding roughly with the center line of shuttle flow and/or the trail of the plasmodium (called anterior posterior axis or AP axis), and a set of straight lines perpendicular to the longitude curve (called latitude lines; see Appendix B for more precise definitions).

To construct this coordinate system we only need the edge curve outlining the plasmodium, and the position of the anterior and posterior ends of this edge. As explained in Appendix B, we can calculate the anterior and the posterior positions from two edge curves that are an appropriate time apart.

Our coordinate system for a sample plasmodium is shown in Fig. 3. The same sample was used for most of the following figures. This coordinate system is calculated from the four edge curves 140 seconds apart, which are depicted in Fig. 3. We define the length of the longitude curve measured from point P as the longitude coordinate value. All points on the same latitude line have the same longitude coordinate value. The latitude coordinate value can be defined as the length of the latitude line from the longitude curve with the appropriate sign to distinguish the two sides. However, we do not need the
The width of a plasmodium is defined as the area occupied by the plasmodium between two adjacent latitude lines equally spaced on the longitude line divided by the space between two adjacent latitude lines. In our sample case, the spacing is 6.5 \( \mu m \). This amounts to measuring the width in the direction perpendicular to the longitude line.

### 3 Results

#### 3.1 Propagation of changes in streaming direction from posterior to anterior end

Fig. 4 shows a sequence of velocity fields of protoplasmic streaming in two-dimensional space (the white arrows) and rates of width changes measured perpendicularly to AP axis (the gray arrows). The width of the tail end began to become thinner although the anterior parts became thicker (see the figure at 290 sec). This thinning motion propagated forward (306 sec and 322 sec). At 338 sec, the tail began to thicken though the anterior parts still showed thinning, and the thickening propagated forward again (354, 370 sec). The width changes always propagated from the posterior end to the anterior end.

Changes in the direction of protoplasmic streaming also propagated from the tail to the front similar to the propagation of width changes. The forward flow was observed only in the rear region at 290 sec, and then became clear at the middle region at 306 sec. At 322 sec., the forward flow was observed only in the anterior region. At 338 sec, backward flow appeared in the tail region and propagated forward at 354 and 370 sec. Accompanying the propagation of the width changes, the changes of streaming direction also propagated from the posterior to anterior end. Figure 4 shows a typical sequence of a sample, but these propagation patterns were always observed with almost no exceptions in a few tens of fast migrating samples.

We concluded that flows in both directions and the deformation of both contraction and relaxation, all begin at the posterior end of the plasmodium, and then propagate towards the anterior. These flows are established the cooperative contraction and relaxation of actomyosin systems distributed throughout the plasmodium. The contraction and relaxation of these systems appear as shrinkage or expansion of width of the plasmodium.

In order to capture the spatio-temporal patterns of the propagation of these changes, a spatio-temporal plot was depicted by reducing two dimensional space to one dimensional space along AP axis in Fig. 5. The maximum streaming velocity over a latitude line is assigned at the corresponding position on the AP axis. Gray scale in Fig. 5 indicates this velocity. Brighter levels correspond to the forward direction and darker levels correspond to the backward directions. Closed and open circles indicate zero velocity points which are the points where the streaming direction reverses. The set of zero velocity points comprise almost straight lines in Fig. 5. Each straight line defines a velocity with which the vector field is moving from the posterior to the anterior part of the plasmodium. We will call this type of velocity field a shifting velocity field or SVF and call this velocity the shifting velocity.

Consider this vector field in relation to locomotive mechanism of plasmodia.
center of gravity moves forward by the forward streaming flow and backward by the backward flow. So the center of gravity of the plasmodium is oscillating with the shuttle streaming. Consider the ratio of the displacement by the forward flow to the displacement by the backward flow. In a migrating cell, the ratio should be larger than one. The problem is to determine origin of this imbalance.

Let us consider the movement of a virtual particle in the plasmodium as shown in Figure 6, assuming the type of space-time structure of vector field such as we observed in the plasmodia. The hatched band on the left-hand side is the forward flow region, and the band on the right-hand side is the backward flow region. A virtual fluid particle starting from point A is carried to point B by the forward flow, and then reaches point C via the backward flow. We will call the distances $l_F$ and $l_B$ the forward and backward migration distances respectively. The migration distance reflects the transportation capability of each flow. If there is no other constraint in the system, the longer migration distance means the longer displacement of the center of gravity.

The forward migration distance $l_F$ is always greater than the backward one $l_B$ when the shifting velocity of the flow is forward, namely $l_B < l_F$. If this asymmetry in migration distance is a major source which eventually moves the plasmodium forward, the ratio of migration distance $l_F/l_B$ should correspond to the ratio of the displacement by the forward flow to the backward flow in amoeboid movement. In the next subsection, we check this relationship experimentally.

### 3.2 Examination of relationship between migration distance ratio and displacement of center of gravity

First, we calculate the migration distances in Fig. 6. For simplicity, assume that the flow velocity is constant in one band of Fig. 6. We can estimate the migration distance from the shifting velocity of the flow $u > 0$, the constant velocity of the flow $v$ and duration of the flow in one direction $T$. The length of each forward or backward flow region is given by $L = uT$. This region is moving with velocity $u$ in positive direction. In accordance with the experimental results, we assume $|v| < u$. Then a virtual fluid particle is in the flow region for time duration of $t$ given by the following formula:

$$t = \frac{L}{u - v}.$$  

The migration distance of the virtual fluid particle for this flow is given by the following:

$$l = vt = \left| \frac{Lv}{u - v} \right| = \left| \frac{uvT}{u - v} \right|. \quad (1)$$

This formula holds for the forward flow when $v > 0$ and for the backward flow when $v < 0$.

For the actual data in Fig. 5, the shifting velocity $u$ was calculated as the average of inclinations of the two sides of the flow band and $T$ was measured at the center of the figure. For $v$, we first find the maximum velocity vector for each forward and backward flow band in Fig. 5. As these values can be anomalous, we took $v$ the average velocity.
over ten pixels around the position of that maximum in the original velocity field at the
time of that maximum.

Next we calculated the ratio of the forward displacement to the backward displace-
ment of the center of gravity. Figure 7 shows the orbit of the center of gravity projected
onto the line connecting the initial and the last positions of the center of gravity plotted
against time. The extrema are marked by small squares. The forward displacement \(D_F\)
from one local minimum to the next local maximum is due to the forward flow, and the
backward displacement \(D_B\) from a maximum to the next minimum is due to the backward
flow.

The displacement ratios \(D_F/D_B\) in six samples of freely migrating plasmodia are
plotted against the migration distance ratio, \(l_F/l_B\), in Fig. 8. The sizes of the samples
ranged from 200 \(\mu\)m to 500 \(\mu\)m. Although some points deviate considerably from the di-
agonal, the agreement is good in the sense that the center of the distributed data points
is close to the theoretical diagonal line in spite of the crude approximation. This implies
that the asymmetry of migration distance ratio is the major source of asymmetric dis-
placement of the center of gravity. Furthermore, the above plot can detect the anomalous
data points as explained below. We conclude that SVF is the main cause of directional
migration of center of gravity.

3.3 Abrupt formation of streaming channel in relation to devi-
ation in ratio

Many factors might contribute to the deviation in Fig. 8. We now present a case in which
we can identify a cause of the large deviations in Fig. 8. This is related to the structure
of the shuttle flow near the anterior ends of plasmodia.

As seen in Fig. 5, the strong shuttle flow abruptly disappears about 100 \(\mu\)m short
of the anterior end in the time from 0 to 260 sec, as indicated by the white dashed line.
Judging only from this figure, the flow seems to contradict the law of continuity in fluid
dynamics. But actually, at this point of disappearance, the strong flow plunges into a
gel-rich region and slowly fan out.

One of shortcomings of presenting the movements of plasmodia by the velocity fields
is that the slow flow tends to be ignored. To investigate the slow flow near the anterior
end, we utilized the superposed image of positive part of the enhanced images used in
Fig. 2 (c).

We depicted in Fig. 9 the superposed enhanced image and velocity field near the
anterior end. A semi-(or quarter)spokewise pattern formed by the elongated black spots
were visible at 40 seconds and 325 seconds and less obviously at 225 seconds. Those images
were captured at the height of the forward flows. The channel of shuttle streaming ended
at the center of the spokewise pattern. There was no definite channel in the spokewise
pattern. This kind of flow structure seemed ubiquitous. In larger plasmodia, the same
structures were found also at the posterior end.

This flow structure is relevant to the above deviation of ratio because the position of
this flow structure did not gradually move forward. It stayed at the same position for a
few periods of shuttle streaming, then abruptly a new channel of considerable length was
formed and the spokewise pattern appeared at the end of this new channel as shown in
Fig. 9. When the flow pattern changed in this way, the above deviation in the ratio was observed. We will show this by checking flow data and the corresponding ratio data.

The process of the formation of the new channel is shown in Fig. 9 at 225, 285 and 325 seconds. From 40 to 225 seconds, the position of the end of the channel stayed at the almost same position (the lower white dashed line). But at 325 seconds, it appeared at a position about 50 µm closer to the anterior end than the previous position (the upper white dashed line). A new channel appeared between these two positions during the forward flow at 325 seconds. This new channel can already be recognized during the backward flow at 285 seconds.

This same process was also apparent in Fig. 5. The slanted black and white columns corresponding to shuttle streaming expand 50 µm to the anterior end at 300 seconds.

The corresponding ratio data is shown in Fig. 10. This is one of the six experiments from Fig. 8. The attached numbers are the temporal order of the data points. Each data point was calculated from three consecutive extrema from the projected center of gravity curve shown in Fig. 7. Data point 0 was calculated from the first, second, and third extrema of the center of gravity curve, data point 1 was calculated from the second, third, and fourth extrema, and so on.

The deviations of data points 4 and 5 were the largest in Fig. 10. This means that the anomaly causing these deviations occurred between the sixth and seventh extrema of the projected center of gravity curve shown in Fig. 7, and that it arose in the time period from 290 to 340 seconds. The anomaly consisted of the fact that the displacement ratio was too large. This means that the center of gravity moved forward anomalously fast during the forward flow corresponding to the white column at 300 seconds in Fig. 5.

So, the deviation in ratio was observed at the white column at 300 seconds in Fig. 5, exactly when a new channel was formed (or opened). Because of the new expanded channel, the transportation capability of the forward flow was also expanded larger than before. The large movement of the center of gravity resulted from this fact.

When the channel was formed, the total area of the plasmodium suddenly enlarged as shown by the lower time course in Fig. 7. Normally in forward displacement, the total area decreased meaning that the plasmodium contracted. However, in the anomaly the total area did not decrease, but rather it remained constant. The increased area gradually decreased during each contraction. We consider the variations in total area in the discussion.

### 3.4 Variation of channel width in relation to wave propagation of changes in flow direction

There are two frames of reference for describing the fluid motion: Lagrangian and Eulerian. In the Lagrangian representation, the fluid motion is described by the motion of the fluid particles. In the Eulerian representation, the fluid motion is described by the velocities of the fluid at spatially fixed points. In the above experiment and analysis, we used both reference frames. The raw experimental data are Lagrangian because we measured the positions of vesicles. From these data, we construct velocity fields in the Eulerian frame. We did this because these velocity fields are easier to display, and the Lagrangian representation can be recovered by integrating the Eulerian velocity field to
obtain the orbits of fluid particles. In the argument of SVF we returned to Lagrangian representation, but this simplified the presentation.

Switching between the two frames is not always trivial. The kind of flow described in the argument of SVF in the Lagrangian frame is difficult to describe in the Eulerian frame. This is because in such a flow the channel width is not constant in time. Now we explain this and then check the data to show that the channel was really wider during the forward flow than during the backward flow.

Assume that protoplasm is flowing through a channel of a plasmodium according to the velocity profile in Figure 6. Furthermore, assume that the diameter of the channel is constant in time and space. Consider a cross section of the channel at position B. During each of forward and backward flow, the amount of protoplasm flowing through the cross section is given by \((\text{migration distance}) \times (\text{area of the cross section})\). Let \(F_F\) be the total amount of protoplasm flowing through this cross section during the forward flow and \(F_B\) be that during the backward flow. We have \(F_F > F_B\) both from the migration length argument and from the fact that the plasmodium is moving forward.

On the other hand, the amount of protoplasm flowing through the cross section is also given by \((\text{duration of flow}) \times (\text{absolute value of velocity of fluid}) \times (\text{area of the cross section})\). According to the velocity profile in Figure 6, the duration and absolute value of velocity of flows are almost the same for the forward and backward flows. So the constant radius channels cannot accommodate the flows described in Figure 6. The channel radius must be wider during the forward flow than during the backward flow. Now we confirm this fact from the experimental data.

Figure 11 shows the relationship of the velocity field (gray pattern) and the width variation (circles) in the same sample as Fig. 5. Brighter gray scale indicates high speed of flow and it gives no information on flow direction. The flow direction is indicated by the trajectories of virtual fluid particles, drawn by the black lines. Black and white circles indicate the lower and upper extrema, respectively, of width variation, which mean the rate of width change is zero. For instance, the thickening process begins at the time indicated by black circles, and thinning begins at white circles. The most relevant result here is that the extrema of width variations almost always occurred a little after the reversal (expressed by the black regions) of the flow direction.

Fig. 12 shows the time course of the width change (the upper curve) and the maximum flow velocity (the lower curve) at a fixed position (indicated by the black dashed line in Figure 11) on AP coordinate. The forward flows begin before the peaks of the width variation and end before the bottom of the width variation. Similarly, the backward flows start before the bottom of width variation and end before the peak. The vertical lines in Fig. 12 mark the time of flow reversal, and they indicate the relationship between the flow direction and the width variation. This delay means that the average width over the period of forward flow is wider than that of backward flow.
4 Discussion

4.1 Possible mechanisms for how the propagation begins from the tail end

It was found that SVF was a major source of asymmetric net transport in protoplasmic mass. We discuss here how the characteristic propagation of various movements begin from the posterior end. One possible explanation is that the intracellular Ca$^{2+}$ concentration is not the same at tail and front. In fact, in Physarum, some patterns and periodic wave trains of Ca$^{2+}$ are observed[35, 36]. This asymmetry may form the characteristic pattern of propagation from tail to front.

According to the 2-pool model for intracellular Ca$^{2+}$ dynamics, the frequency of the calcium oscillation increases as the basal level of cytoplasmic Ca$^{2+}$ increases[37]. Cytoplasmic calcium varies through calcium entry from extracellular space. When the ratio of surface area to protoplasmic volume is compared every local region of amoeba, it is relatively higher in tail than in front because cell shape of tail region is long and thin. This is a possible cause of high cytoplasmic Ca$^{2+}$ in tail. According to the theory of coupled limit-cycle oscillators, phase wave propagate from high frequency regions[38].

The above argument may be applicable to other cells. In Amoeba proteus, contraction in the posterior region is regarded as a motive force of mass transport and Ca$^{2+}$ is actually high in the posterior region[39, 40, 41, 42]. Although there is no direct evidence of wave propagation of contraction and Ca$^{2+}$, periodicity of contraction is observed[43]. In the above sense, cytological events are common in Amoeba proteus and Physarum. So the locomotive mechanism proposed here may not limited only to Physarum.

On the other hand, another explanation for the characteristic propagation comes from a mathematical model for coupled oscillator systems with a mass conservation law, which was proposed for rhythmic amoeboid movement in Physarum[28]. According to this theory, directional propagation of phase waves can spontaneously appear without any macroscopic asymmetry initially given. The symmetry is broken by small random fluctuations. These ideas from nonlinear dynamics are useful in explaining the symmetry breaking necessary for amoeboid movement.

4.2 Release of pressure accompanying total area variations

As shown in Fig. 7, the total areas of plasmodia were not preserved during the experiments; instead they oscillated, and their extreme values coincided precisely with those of the projected center of gravity curves. In Fig. 7, vertical broken lines are drawn from the local minima of the total area curve. Except for a few cases, those vertical lines are very close to, or simply coincide with the local maxima of the projected center of gravity curves. This very precise correspondence suggests that the variation in area directly reflects the variation of some physical quantity, most likely the pressure.

At a local maximum of the projected center of gravity curve, most regions of the plasmodium are contracting and the anterior part is being pushed forward. This is the state where the inner pressure of the plasmodium is presumably the greatest. At this point, the area is at its local minimum.
We propose two possible reasons for the total area variations. The higher the inner pressure, the rounder the plasmodium becomes to contain it. Then it may sink deeper into flat agar gel. The second explanation is that the volume changes observed are related to morphological changes in the plasmodium. There are many invaginated pits filled with water on surface of plasmodium. The water may be squeezed out of cavity of invagination when the plasmodium contracts. This explanation is supported by the previous observation: the ectoplasm cortex of plasmodial veins become thinner when contracting[44, 45]. In fact, the thickness of endoplasmic cortex varied temporally as as shown in Fig. 4.

The oscillation of the total area is interrupted during the anomaly in the period from 290 to 340 seconds in Fig. 7. It then resumes with a new and larger baseline. Considering that the total area is inversely proportional to the inner pressure, the change of the total area is consistent with the expansion of the channel. Up to 290 seconds the gel-rich region at the anterior end hinders the forward flow and the inner pressure mounts. This reveals itself in the slight decrease of the baseline of the oscillation in total area. At the anomaly, the mounted pressure is released by the forward flow, which propels the center of gravity forward faster than usual. This release of pressure appears as an increase of the baseline of the total area. Subsequently, the total area oscillates around a higher baseline as the inner pressure is lowered by the expansion of the channel.

We have observed similar sets of characteristic data (large displacement ratios, blockages and release of forward flow, and anomalous total area curves) in other experiments and samples. These observations were all consistent with the above mentioned interpretation.

4.3 Formation of flow channel in viscoelastic protoplasm in cell

The technique used in this report allowed us to record spatiotemporal variations of protoplasmic flow in the anterior region of the sheet-like structure. Protoplasmic streaming is not clear in this region, and the flow is relatively slow compared with that in a tube because of sponge-like structure of gel in the anterior sheet-like part. Sol flows slowly through narrow cavities of the sponge. However, we noted some channels in which the protoplasmic flow was much faster; such channels appear suddenly rather than developing gradually and their positions do not vary. Subsequently, one of the channels grows into a tubular structure known as a plasmodial vein. Hence, channels are the precursor of tubes. These observations provide insight into the morphogenesis of veins.

The protoplasm is a complex viscoelastic material with the characteristics of a non-Newtonian fluid. Thixotropy is one such feature, and a gel converts to a flowing sol when the pressure is large enough to break some of the intermolecular structures of the gel. Once flow starts, the viscosity decreases so that the flow becomes easier. This complex process is difficult to understand unless its dynamics are considered in terms of mathematics and physics. In fact, regular shuttle streaming is not observed in organisms <100 µm in diameter. This implies the occurrence of some kind of instability. A mathematical model capturing the essence of the complex cell dynamics will be greatly needed in future work.
4.4 Amoeboid movements based on nonlinear waves and oscillations

The relationship between the present results and previous findings that appear to contradict them [17, 18] must be considered here. In our previous work, we observed that the contraction waves transmit from the anterior to the posterior part of large plasmodia with veins and sheets. At that time, due to technological limitations (that is, analog television cameras and less-powerful personal computers), we used coarse-grained images instead of detailed ones. Under those conditions, we mainly observed changes in the thickness of the sheets. Preliminary observations show that in large plasmodia with veins and sheets, the forward flow in veins enters the sheets near the anterior rim, then bounces off the rim and transforms into backward flow through the sheet. We believe that what we observed in the previous work was this backward flow in the sheet. Further investigation to clarify this point is underway.

In large plasmodia with veins and sheets, velocity measurements cannot be made by the present methods due to the lack of transparency and the large velocity of flow. However, now that we can measure the thickness of the veins with precision, we can estimate the velocity fields inside them based on the present mechanism. We hope to soon be in a position to confirm this theory.

In this paper, we have established that the direction of locomotion and the direction of propagation of the contraction phase coincide in small plasmodia. The next question is whether this relationship still holds in other situations, such as tactic responses to stimulation and the locomotion of organisms with more complex shapes. When this question is answered, we might begin to understand how the amoeba organizes the various regions of its protoplasm to achieve behavioral feats such as maze solving. Dynamical aspects of oscillations and waves should be studied at a level of whole body of amoeba in order to clarify mechanics of amoeboid locomotion by integrating molecular events of mechano-chemical interactions.

Appendix A

One DV movie consists of 29.97 frames per second, each of which has 720×480 pixels:

\[ S = \{(x, y) \in \mathbb{Z} : 0 \leq x < 720, 0 \leq y < 480\} \]

where \( S \) is a set of pixels in a frame. Each pixel has an integer value from 0 (brightest) to 255 (darkest). A movie \( g \) is expressed as a mathematical function.

\[ g(x, y, t) \in \mathbb{Z}, 0 \leq g(x, y, t) < 256, 0 \leq t < t_{\text{total}}, (x, y) \in S \]

To enhance the moving vesicles in the images of the movie, we subtract the accumulated image \( G_m(x, y, t) \) from the original image. In the following analysis we set \( m = 500 \) to be about 16.6 seconds.

\[ G_m(x, y, t) = \frac{1}{m} \sum_{k=0}^{\infty} \left( \frac{m-1}{m} \right)^k g(x, y, t - k) \]
\[ g_m(x, y, t) = g(x, y, t) - G_m(x, y, t) \]

We recognize the moving vesicles as the black granules in \( g_m \). As a threshold, we set \( C_t = 256 \times 0.75 \).

\[ C(t) = \{(x, y) \in S : C_t \leq g_m(x, y, t)\} \]

To separate one vesicle from the rest of \( C(t) \), we decompose \( C(t) \) into connected components called clusters \( c(t|i), i = 1, \ldots, N_c(t) \) and \( C(t) = \bigcup_{i=1}^{N_c(t)} c(t|i) \).

A set \( c \subset S \) is connected, when for any pair of points \((x_1, y_1), (x_0, y_0) \in c \) there is a sequence of points \((x_1, y_1), (x_2, y_2), \ldots, (x_k, y_k) = (x_0, y_0)\), all in \( c \), such that \((x_{i+1}, y_{i+1}) \in n(x_i, y_i), i = 1, 2, \ldots, k - 1 \) where \( n(x, y) = \{(x + 1, y), (x - 1, y), (x, y + 1), (x, y - 1)\} \cap S \) is a set of nearest neighbours of \((x, y)\). We can reach \((x_0, y_0)\) from \((x_1, y_1)\) by a route in \( c \).

To track the movements of clusters we have to establish the correspondences between the clusters in two consecutive frames. The cluster \( c(t|i) \) in frame \( t \) corresponds to \( c(t-1|j) \) in frame \( t-1 \), when \( c(t|i) \) overlaps only \( c(t-1|j) \), and \( c(t-1|j) \) overlaps only \( c(t|i) \). We express this correspondence by the function \( l(i, t) = j \).

More precisely, \( l(i, t) = j \) if and only if both sets \( \{j | c(t|i) \cap c(t-1|j) \neq \emptyset\} \) and \( \{i : c(t|i) \cap c(t-1|j) \neq \emptyset\} \) have only one element. Otherwise, it is undefined.

The center of gravity of the \( i \)-th cluster in frame \( t \) is defined as follows:

\[ p(t|i) = \sum_{(x,y) \in c(t|i)} g_m(x, y, t)(x, y). \]

From \( N + 1 \) consecutive corresponding clusters we obtain the velocity per frame of the \( i \)-th cluster in frame \( t \).

\[ v(t|i) = \frac{p(t|i) - p(t - N|l(t - (N - 1), \ldots, l(t - 1, l(t, i)) \ldots))}{N}. \]

We use \( N = 3 \) in the following formulae.

From the velocities of the clusters we construct the velocity field. First, we assign velocities to the points in the clusters with defined velocities. The function \( \theta_0 : S \rightarrow \{0, 1\} \) is 1 at a point where the velocity is thus defined, 0 at other points.

\[ \theta_0(x, y, t) = \begin{cases} 1, & (x, y) \in c(t|i) \text{ for some } i \\ 0, & \text{otherwise} \end{cases} \]

\[ u_0(x, y, t) = \begin{cases} v(t|i), & \theta_0(x, y, t) = 1 \\ 0, & \text{otherwise} \end{cases} \]

Then we smooth the velocity field by geometric series in time. But the velocity is not always defined at the point. We compensate for this effect by modifying the normalization factor \( F_1 \) defined as follows:

\[ F_1(x, y, t) = \sum_{i=-\infty}^{\infty} \left( \frac{w - 1}{w} \right)^{|i|} \theta_0(x, y, t - i). \]
We set $w = 90$. If the zero term $\theta_0 = 1$ are too many in this series, the velocity cannot be defined at that point. We set the threshold $F_t = 0.02 \times w$. $\theta_1$ indicates whether the velocity is thus defined or not:

$$\theta_1(x, y, t) = \begin{cases} 1, & F_t < F_1(x, y, t) \\ 0, & \text{otherwise} \end{cases}$$

$$u_1(x, y, t) = \begin{cases} F_1(x, y, t)^{-1} \sum_{i=-\infty}^{\infty} \left( \frac{w - 1}{w} \right)^{|i|} u_0(x, y, t - i), & \theta_1(x, y, t) = 1 \\ 0, & \theta_1(x, y, t) = 0 \end{cases}$$

Finally, we interpolate the velocity to fill the undefined points. The average velocity in a square $Sq(x, y)$ is assigned to that point. We set $n_x = 4$ and $n_y = 4$ in the following.

$$Sq(x, y) = \{(i, j) \in S : |i - x| \leq n_x, |j - y| \leq n_y\}$$

Then the velocity field we use in subsequent analysis is given by the following:

$$u_2(x, y, t) = \begin{cases} u_1(x, y, t), & \theta_1(x, y, t) = 1 \\ F_2(x, y, t)^{-1} \sum_{(x, y) \in Sq(x, y)} \theta_1(x, y, t), & 0 < F_2(x, y, t) \\ \text{undefined}, & \text{otherwise} \end{cases}$$

where

$$F_2(x, y, t) = \sum_{(x, y) \in Sq(x, y)} \theta_1(x, y, t).$$

### Appendix B

To extract the edge of a plasmodium we use the accumulated image defined in Appendix A. We choose the threshold around $E_t = 0.5 \times 256$, but sometimes we need to find the optimum value manually. This depends on the quality of the original movie.

$$G(t) = \{(x, y) \in S : E_t \leq G_m(x, y, t)\}$$

We denote the connected component of $G(t)$ corresponding to our plasmodium by $E(t)$. To construct the coordinate system we take two sets $E(t_1)$ and $E(t_2)$, where $t_1 < t_2$. Then the forward set is defined as follows:

$$F = E(t_2) \cap \overline{E(t_1)},$$

where $\overline{E(t_1)}$ is the complement of $E(t_1)$ with respect to $S$. The connected components of $F$ are denoted by $F_i$, where $F = \cup_i F_i$.

Each component $F_i$ has two kinds of boundaries. One is the boundary of $E(t_2)$,

$$\partial F_i^+ = \{(x, y) \in F_i : n(x, y) \cap \overline{E(t_2)} \neq \emptyset\}.$$

The other is the boundary adjacent to $E(t_1)$,

$$\partial F_i^- = \{(x, y) \in F_i : n(x, y) \cap E(t_1) \neq \emptyset\}.$$
We can express movements of boundaries by analogy with the dipole moment vector of electromagnetism. We assume that a positive charge $1$ is distributed uniformly on the boundary $\partial F_i^+$ and negative charge $-1$ on $\partial F_i^-$. 

Then we define the dipole vector of $F_i$ as follows:

$$p_i = \frac{|F_i|}{|\partial F_i^+|} \sum_{(x,y) \in \partial F_i^+} (x,y) - \frac{|F_i|}{|\partial F_i^-|} \sum_{(x,y) \in \partial F_i^-} (x,y),$$

where we denote the number of elements in set $F$ by $|F|$. The length of the vector $p_i$ is set proportional to the area of $F_i$.

We can similarly define the backward set as follows:

$$B = E(t_1) \cap \overline{E(t_2)}.$$

The connected components of $B$ are as follows: $B = \cup_i B_i$. 

The boundaries of $B_i$ are as follows:

$$\partial B_i^+ = \{(x,y) \in B_i : n(x,y) \cap E(t_2) \neq \emptyset\}$$

and

$$\partial B_i^- = \{(x,y) \in B_i : n(x,y) \cap \overline{E(t_1)} \neq \emptyset\}.$$

The backward dipole vector is as follows:

$$q_i = \frac{|B_i|}{|\partial B_i^+|} \sum_{(x,y) \in \partial B_i^+} (x,y) - \frac{|B_i|}{|\partial B_i^-|} \sum_{(x,y) \in \partial B_i^-} (x,y).$$

The center of gravity of a set $A$ is defined as follows:

$$Cg(A) = \sum_{(x,y) \in A} (x,y).$$

The boundary of a set $A$ is defined as

$$\partial A = \{(x,y) \in A : n(x,y) \cap \overline{A} \neq \emptyset\}.$$

We denote by $D$ the displacement vector of the center of gravity from $E(t_1)$ to $E(t_2)$ where

$$D = Cg(E(t_2)) - Cg(E(t_1)).$$

With respect to this vector $D$, we pick a frontmost forward dipole vector and a rearmost backward dipole vector of more than a defined size. Denoting the inner product of vectors by $(,)$:

$$i_F = \max_{i,T_d \in \{F_i\}} (D, Cg(F_i))$$
\[ i_B = \min_{i,T_{\alpha} < |B_i|} (D, C g(B_i)) \]

The main motivation for defining forward and backward dipole vectors is to pinpoint the heads and tails of plasmodia. The head \( Ph(t) \) is the foremost boundary point with respect to the forward dipole vector \( p_{f_{\alpha}} \).

\[ Ph(t) = \max_{(x,y) \in \partial E(t)} (p_{f_{\alpha}}, (x, y)). \]

Likewise, the tail \( Pt(t) \) is defined as

\[ Pt(t) = \min_{(x,y) \in \partial E(t)} (p_{b_{\alpha}}, (x, y)). \]

Thus, for a pair of sets \( E(t_1) \) and \( E(t_2) \), we obtain four points on the plane \( Pt(t_1), Pt(t_2), Ph(t_1) \) and \( Ph(t_2) \) and for sets \( E(t_1), \ldots, E(t_n) \), we have \( Pt(t_1), \ldots, Pt(t_n) \) and \( Ph(t_1), \ldots, Ph(t_n) \). Assuming \( (D, Pt(t_n)) < (D, Ph(t_1)) \) (if not, just discarding some Ph’s), the sequence of points \( \{Pt(t_1), \ldots, Pt(t_n), Ph(t_1), \ldots, Ph(t_n)\} \) is the first approximation to our longitude curve.

If the segment from \( Pt(t_n) \) to \( Ph(t_1) \) is relatively long as in Fig. 3, we take some extra points on this segment \( P_1, \ldots, P_k \) and shift their position to the center of the plasmodium \( P'_1, \ldots, P'_k \) in a direction perpendicular to this segment. We now have a second approximation \( \{Pt(t_1), \ldots, Pt(t_n), P'_1, \ldots, P'_k, Ph(t_1), \ldots, Ph(t_n)\} \) to our longitude curve.

Finally, to round the corners, the sequence of points is passed through low-pass filter using a two-dimensional fast Fourier transform (FFT).

References


5 Figure caption

Figure 1: The process of particle recognition and identification. All images are captured from processed movies and at the same frame in the movies. Blowups are smoothed by the texture smoothing mechanism of OpenGL to ease the jaggyness. (a) The original image converted to gray scale. The smallest rectangle indicates the position of blowups in (b)-(d) and Figs. 2 (a)-(b). The middle rectangle indicates the position of blowups in Figs. 2 (c)-(d). The largest rectangle indicates the position of Figs. 9. (b) Blowup of the enhanced image. Darker pixels are now occupied by moving particles and lighter pixels are previously occupied but now free of particles. The white polygons indicate the recognized clusters. The smallest rectangles correspond to one pixels. (c) Trajectories of the center of gravity of the recognized clusters. (d) The velocity of recognized clusters. To avoid the misidentification, the velocity is calculated from last 4 trajectory points. The underneath plasmodium image is blowup of the original image.

Figure 2: The process of vector field measurement and comparison of trajectories of vesicles and the path line obtained from the measured vector field. All images are captured from processed movies. Figures (a) and (b) are at the same frame in the movies as in Figs. 1. Figures (c) and (d) are at the same frame. (a) The cluster velocity data in the last 3 seconds. Older the data, the darker are the arrows. (b) The resultant vector field obtained by averaging the data depicted in figure (a) over time(± 90 frames) and space (±3 pixels). (c) The superposition of positive enhanced image over about 10 seconds. The older is the image, the fainter is the spot. The moving vesicles should appear as elongated dark spots like comets. (d) The path lines obtained by numerically integrated the constructed vector field are drawn on figure (c). A circle is depicted on the path line every 0.5 second.

Figure 3: Coordinate system of the plasmodium in Figs. 4. This plasmodium has come from the right and is completing an upward turn. Edge curves are shown at 10 seconds (thin dotted curve), 150 seconds (thin broken curve), 290 seconds (thin solid curve) and 430 seconds (thick solid curve). The numbers indicate length scale (µm). The curve P to A is the longitude curve. The solid and dotted lines perpendicular to this longitude curve are the latitudinal lines. Arrows are examples of anterior and posterior dipole vectors, which are defined in Appendix B.

Figure 4: A sequence of velocity fields and the rate of width change of the plasmodium moving upwards. The white arrows represent the vector field at the points on the lattice whose size is arbitrarily chosen. The black arrows represent the rate of change of the width of the plasmodium. The width is measured in the direction perpendicular to the longitude line. A pair of black vectors of opposite direction and equal length is drawn on the line perpendicular to the longitude line.

Figure 5: The gray scale plot of the maximum velocity vector of the same plasmodium as in Fig. 4 on the time-AP axis plane. The length of the maximum velocity vector over the latitude line with sign indicating the direction of the flow is plotted. The forward
flows are represented by the lighter shade, and the backward flows are represented by the
darker shade. The solid white circles mark the onset of the forward flow, and the solid
black circles mark the onset of the backward flow. These circles are fitted with white lines
to obtain the shifting velocity of the vector field. The shifting velocities except first two
flows are $12 \pm 1 \mu m/s$. The absolute value of the averaged velocity of the flow over the
channel is $3 \pm 0.5 \mu m/s$.

**Figure 6:** Schematic drawing of the locomotive mechanism of shuttle flow in
plasmodia. The two hatched bands on the time-latitude plane are the shifting vector
fields from Fig. 4. The width of the vector field is $L$, and the duration at the fixed
latitudinal point is $T$. Hence the shifting velocity of the vector field is $u = L/T$. A
fluid particle starting from point A on the latitude curve is carried by the forward flow to
point B, then by the backward flow to point C. The migration distance $l_F$ is the distance
between A and B and $l_B$ is the distance between B and C.

**Figure 7:** Movement of the center of gravity of the plasmodium in Fig. 4. The
inset in the upper left-hand corner is the movement on the original image plane, and a
broken line connects the first and last data points. A small square marks the last data
point. The upper curve is the projection of the two-dimensional data onto the dotted line
of the inset. Small squares mark the extreme points. The bottom curve is the area of
the plasmodium in the movie image. The central solid line of this curve is the average.
The broken lines above and below the center line represent 105% and 95% of the average
value. Vertical broken lines are drawn from the local minimum of this curve to the center
of gravity curve. Note the coincidence between the extrema of the two curves.

**Figure 8:** The ratio of displacement of the center of gravity versus the ratio of the
migration distances of forward and backward flows, $l_F/l_B$. Data from six experiments are
plotted. The shifting velocity of the velocity field $u$, the velocity of the flow $v$ and the
duration of the flow $T$ are obtained from the data in Fig. 5 and the migration distance
is calculated from Eq. 1. Displacement ratios are calculated from every three consecutive
extrema in the projected center of gravity curve. A different symbol is used for each
experiment.

**Figure 9:** Semi-spokewise flow patterns near the anterior end. The white dashed
lines are the latitude lines at the longitude positions indicated by the two white dashed
lines in Fig. 11.

**Figure 10:** The displacement ratio versus the migration distance ratio of the
plasmodium in Fig. 4. Data points are numbered in temporal order. Data point 0 is
calculated from the first, second and the third extrema marked by small squares of the
projected center of gravity curve in Fig. 7, data point 1 is calculated from the second,
third, and fourth extrema, and so on.

**Figure 11:** Joint plot of the absolute value of the velocity field (gray scale),
points of onset of contractions (white circles) and relaxation (black circles), orbits of fluid
particles obtained by numerically integrating the velocity field (black solid curves) and the longitudinal positions of the anterior and posterior ends of the plasmodium (white curves) on the time-longitude plane. The time series of width and velocity of the flow at longitude 120 $\mu m$ (indicated by the black dashed line) is depicted in Fig. 12. Two white dashed lines indicate the corresponding positions of the white dashed lines in Fig. 9.

**Figure 12:** The time series of the width (upper curve) and the maximum flow velocity (lower curve), both at the black dashed line in Figure 11. The length of the maximum velocity vector over the latitude line is plotted with sign indicating the direction of the flow. The positive velocity means the forward flow. The mass center of line segment AB (thus the time average of width in forward flow) is larger than that of BC (the averaged width in backward flow). Due to the delay of the extrema of the width, the width is wider during the forward flow than during the backward flow. Vertical lines indicate the points of reversal of the flow.
Figure 2:
Figure 4:
Figure 5:
Figure 6:
Figure 7:
Figure 8:
Figure 10:
Figure 11:
Figure 12: