



Title	The system $\text{NaFe}^{3+}\text{Si}_2\text{O}_6\text{-CaFe}^{2+}\text{Si}_2\text{O}_6$ at low oxygen fugacity
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THE SYSTEM  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ - $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$   
AT LOW OXYGEN FUGACITY

by

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(with 1 table and 8 text-figures)

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*Abstract*

The  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$ -rich part of the system  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ - $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  was determined at the temperature range of  $1100^\circ\text{C}$ - $1250^\circ\text{C}$  and at oxygen fugacities of  $10^{-9}$ ,  $10^{-10}$ , and  $10^{-11}$  atm. It was found that a high temperature form of hedenbergite has not  $\beta$ -wollastonite structure, but bustamite structure in the temperature range of  $1100^\circ\text{C}$ - $1175^\circ\text{C}$ . Three  $\text{Fe}^{2+}$ -bearing silicate phases were also confirmed by X-ray diffraction patterns and optical properties: Fe-bustamite<sub>ss</sub>,  $\beta$ -Fe-wollastonite<sub>ss</sub>, and  $\alpha$ -Fe-wollastonite<sub>ss</sub> (ss: solid solution). These three phases are solid solutions between  $\text{CaSiO}_3$  and  $\text{FeSiO}_3$  at low oxygen fugacity;  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$  enters into the liquid when the crystalline phases coexist with liquid. The following phase assemblages were encountered with increasing temperature: Fe-bustamite<sub>ss</sub> + iron oxide + liquid,  $\beta$ -Fe-wollastonite<sub>ss</sub> + Fe-bustamite<sub>ss</sub> + iron oxide + liquid,  $\beta$ -Fe-wollastonite<sub>ss</sub> + iron oxide + liquid,  $\beta$ -Fe-wollastonite<sub>ss</sub> +  $\alpha$ -Fe-wollastonite<sub>ss</sub> + iron oxide + liquid, and  $\alpha$ -Fe-wollastonite<sub>ss</sub> + iron oxide + liquid. The assemblages are essentially the same throughout the range of oxygen fugacity investigated, except that magnetite converts to wüstite at low oxygen fugacity. Application of the system to the natural pyroxene is also given.

Introduction

From experimental study of the system acmite-diopside and the natural pyroxene from alkalic rocks, Yagi (1966) suggested that there are continuous solid solutions in the system acmite-diopside-hedenbergite. Later Ohashi (1967) confirmed the presence of a complete series of solid solutions in the system acmite-hedenbergite at subsolidus temperature, and Nolan (1969) showed that continuous solid solutions exist in the subsolidus region of the system diopside-hedenbergite-acmite. However, investigations of the high temperature region in the system acmite-hedenbergite has not yet been accomplished.

Bowen et al. (1933), investigating the system  $\text{CaO-FeO-SiO}_2$ , demonstrated that  $\beta$ -wollastonite forms a solid solution with ferrosilite, which enters into  $\beta$ -wollastonite up to 70 mole percent at high temperature with the substitution

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of  $\text{Fe}^{2+}$  for Ca. Recently, many studies on the system  $\text{CaO-FeO-SiO}_2$  were carried out and the problems related to the structure of high temperature forms of hedenbergite are presented (Peacor and Prewitt, 1963; Prewitt and Peacor, 1964; Rutstein, 1971; Rutstein and White, 1971; Matsueda, 1973).

From his experimental study Rutstein (1971) claimed that  $\text{Fe}^{2+}$  cannot substitute for Ca more than about 10 atomic percent in the  $\beta$ -wollastonite structure, and that specimens containing more than 10 percent  $\text{Fe}^{2+}$  have bustamite structure. Matsueda (1973), from his study of natural specimens as well as experimental work on the system  $\beta$ -wollastonite-ferrosilite, concluded that the structure of iron wollastonite is different from that of  $\beta$ -wollastonite.

In the present study the phase diagram of the system acmite-hedenbergite is determined at the temperature range of  $1100^\circ\text{C} - 1250^\circ\text{C}$  and at the oxygen fugacity ( $f_{\text{O}_2}$ ) of  $10^{-9} - 10^{-11}$  atm and the structural problem of  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  is also discussed.

## Experimental Methods

The ordinary quenching method was employed for the investigation of the phase diagram.

Homogeneous glasses were prepared by melting pure chemicals in a  $\text{Pt}_{90}\text{Rh}_{10}$  crucible previously saturated with iron. Pure quartz,  $\text{Fe}_2\text{O}_3$ ,  $\text{CaCO}_3$  and pure  $\text{Na}_2\text{Si}_2\text{O}_5$  were used as sources. These homogeneous glasses were used as starting materials for quenching experiments. Starting materials were held in  $\text{Pt}_{60}\text{Rh}_{40}$  envelopes in order to minimize the loss of iron and suspended in a vertical quenching furnace. A  $\text{Pt-Pt}_{87}\text{Rh}_{13}$  thermocouple used to measure the temperature was calibrated at the standard melting points of Au ( $1062.6^\circ\text{C}$ ) and diopside ( $1391.5^\circ\text{C}$ ).

The atmosphere in the furnace was controlled by running mixtures of  $\text{CO}_2$  and  $\text{H}_2$  gas at definite ratios. Calibration for oxygen fugacity was made by examining the stability field of hematite, magnetite, and wüstite.

X-ray diffraction patterns of the crystalline phases were obtained with  $\text{CuK}\alpha$  radiation at 35 KV and 20 mA at room temperature. Reflections of (210) and (102) of  $\beta$ -wollastonite, and (204) and (204) of bustamite were obtained at a scanning speed of 1/4 degree per minute, with silicon as an external standard.

## Experimental Results and Discussions

### *Crystalline phases*

In the present experiment three different silicate phases were recognized.

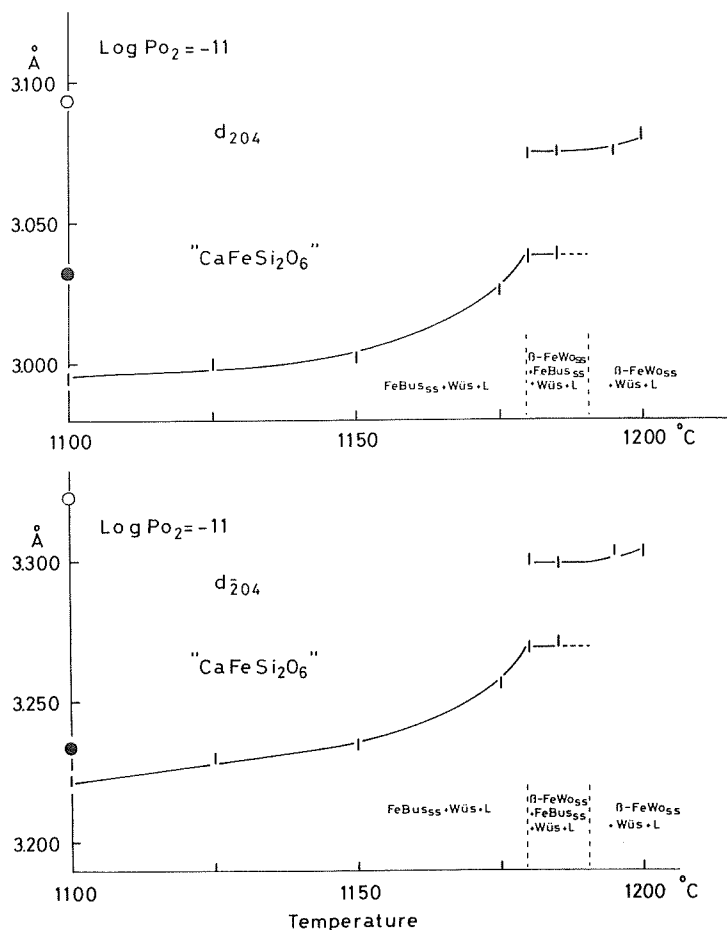


Fig. 1 Changes of d-spacings of  $\beta$ -Fe-wollastonite<sub>SS</sub> and Fe-bustamite<sub>SS</sub> crystallized from the composition of  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  at  $10^{-11}$  atm  $f_{\text{O}_2}$ . The open circles represent  $d_{210}$  and  $d_{102}$  of  $\beta$ -wollastonite and the solid circles  $d_{204}$  and  $d_{204}$  of bustamite. The following abbreviations will be used throughout all figures and tables. Fe-Bus = Fe-bustamite,  $\beta$ -Fe-Wo =  $\beta$ -Fe-wollastonite,  $\alpha$ -Fe-Wo =  $\alpha$ -Fe-wollastonite, Wüs = wüstite, Mt = magnetite.

From the X-ray diffraction patterns and optical data, it is suggested that these three crystalline phases correspond to bustamine<sub>SS</sub>,  $\beta$ -wollastonite<sub>SS</sub>, and  $\alpha$ -wollastonite<sub>SS</sub>. As all of these phases incorporate  $\text{Fe}^{2+}$ , henceforth these phases will be described as Fe-bustamite<sub>SS</sub>,  $\beta$ -Fe-wollastonite<sub>SS</sub>, and  $\alpha$ -Fe-wollastonite<sub>SS</sub>, respectively. The  $\beta$ -wollastonite<sub>SS</sub> and the  $\alpha$ -wollastonite<sub>SS</sub> represent wollastonite<sub>SS</sub> and pseudowollastonite<sub>SS</sub>, respectively, as defined by Bowen et al. (1933).

X-ray diffraction patterns of bustamite and  $\beta$ -wollastonite are similar, but

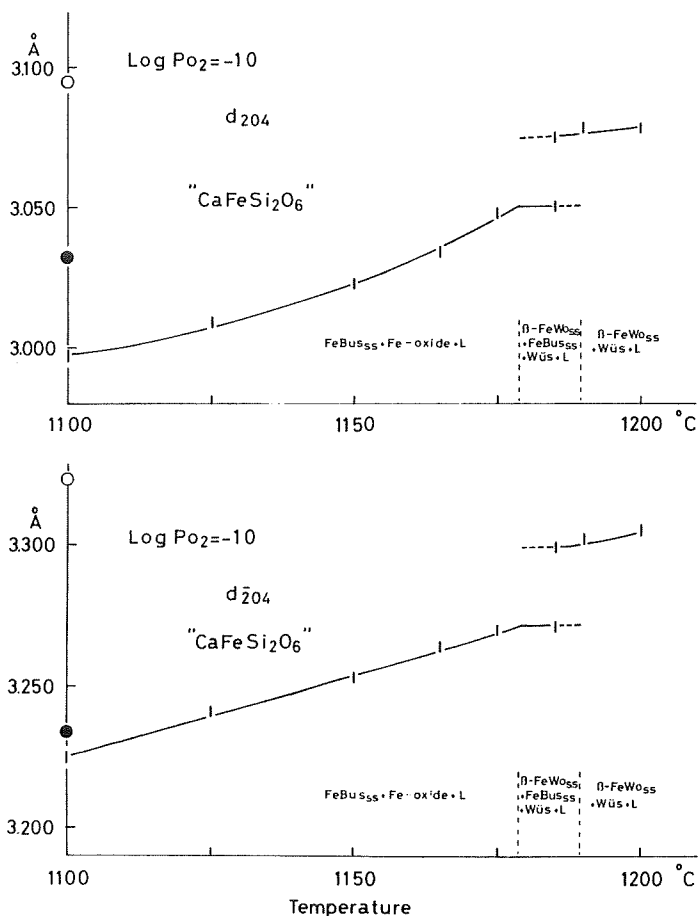


Fig. 2 Change of d-spacings of  $\beta$ -Fe-wollastonite<sub>SS</sub> and Fe-bustamite<sub>SS</sub> crystallized from the composition of  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  at  $10^{-10}$  atm  $f_{\text{O}_2}$ . The open circles represent  $d_{210}$  and  $d_{102}$  of  $\beta$ -wollastonite and the solid circles  $d_{204}$  and  $\bar{d}_{204}$  of bustamite. Abbreviations are same as in Fig. 1.

the peaks of bustamite are located at  $1-1.5^\circ$  higher angle side in  $2\theta$  compared to  $\beta$ -wollastonite. The diffraction peaks, however, shift to the bustamite side due to  $\text{Fe}^{2+}$  substitution for Ca in the  $\beta$ -wollastonite structure and it may become difficult to determine whether the structure of the phases present belongs to  $\beta$ -wollastonite or to bustamite when  $\beta$ -wollastonite<sub>SS</sub> contains considerable amounts of  $\text{Fe}^{2+}$ .

The crystalline material of composition  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  was prepared at  $f_{\text{O}_2}$  of  $10^{-11}$  and  $10^{-10}$  atm to examine whether these two phases are mutually distinguishable or not. Figs. 1 and 2 show the changes of d-spacings of (204) as a function of temperature. Only one peak corresponding to that of bustamite

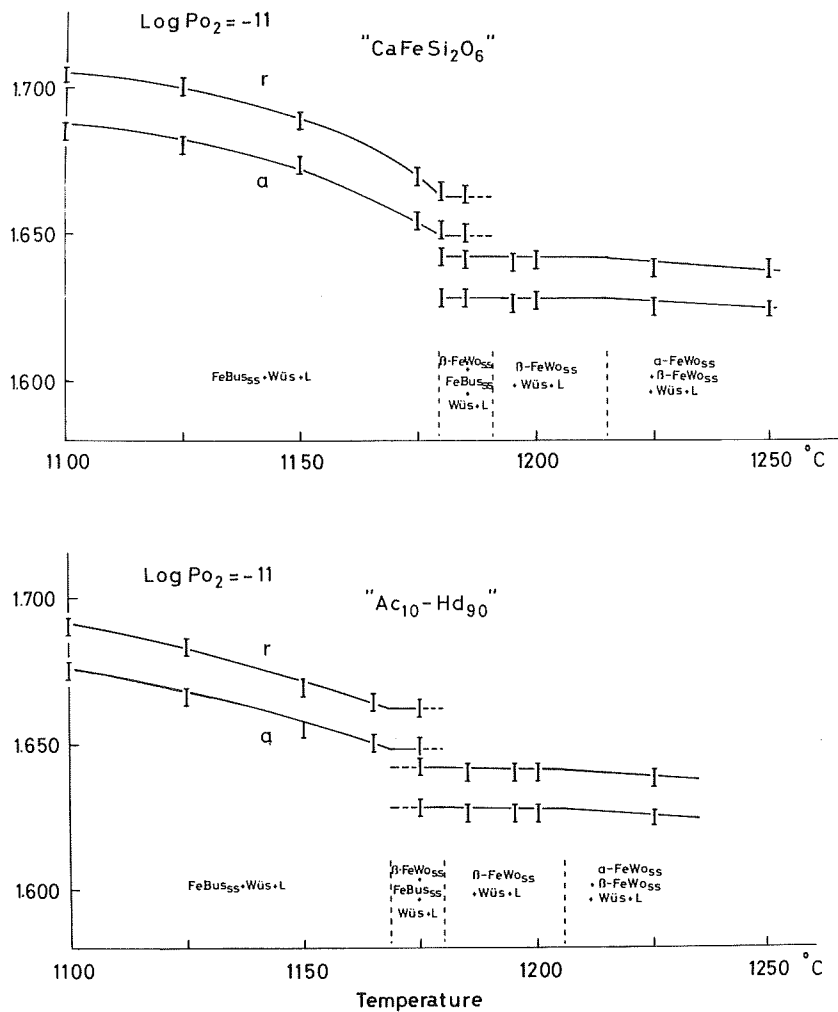


Fig. 3 Change of refractive indices of  $\beta$ -Fe-wollastonite<sub>SS</sub> and Fe-bustamite<sub>SS</sub> crystallized from the compositions of  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  and  $\text{Ac}_{10}\text{Hd}_{90}$  at  $10^{-11}$  atm  $f_{\text{O}_2}$ . Abbreviations are same as in Fig. 1.

was observed and the d-spacing increases with increasing temperature between  $1100^\circ\text{C}$  and  $1175^\circ\text{C}$ . The peak of (204) splits at  $1180$  and  $1185^\circ\text{C}$ , giving two different d-spacings. One is similar to the d-spacing of  $\beta$ -wollastonite and the other to that of bustamite. However, at higher temperatures again only one peak was observed, which gave a d-spacing similar to that of  $\beta$ -wollastonite (Figs. 1 and 2).

Optical methods are also useful to identify the silicate phases encountered. Two silicate phases A and B were observed in the run charges of the

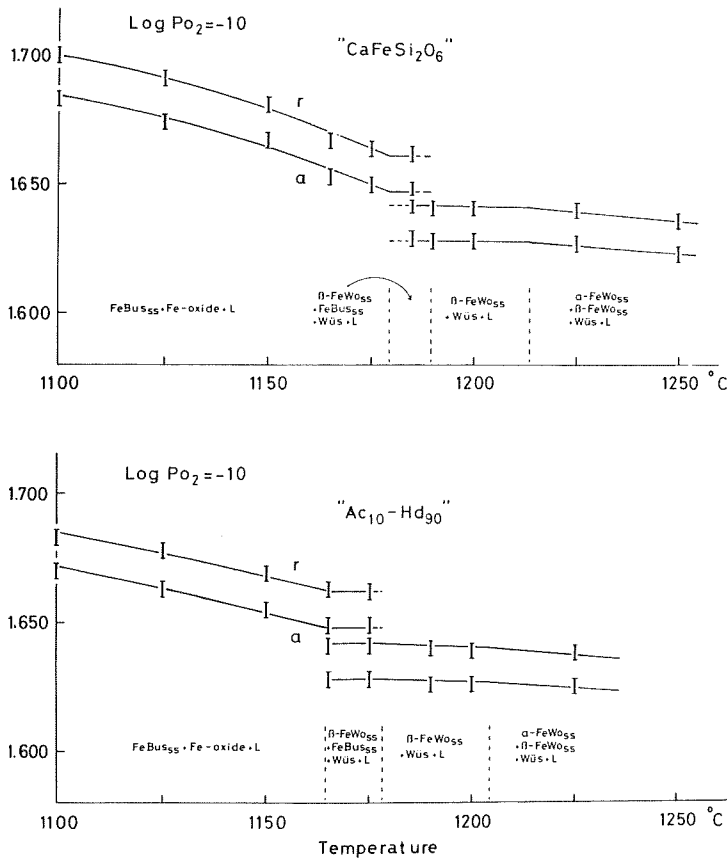


Fig. 4 Change of refractive indices of  $\beta$ -Fe-wollastonite<sub>SS</sub> and Fe-bustamite<sub>SS</sub> crystallized from the compositions of  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  and  $\text{Ac}_{10}\text{Hd}_{90}$  at  $10^{-10}$  atm  $f_{\text{O}_2}$ . Abbreviations are same as in Fig. 1.

composition of  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  at  $1180^\circ\text{C}$  and  $1185^\circ\text{C}$  and also that of  $\text{Ac}_{10}\text{Hd}_{90}$  at  $1175^\circ\text{C}$ . These two phases show different refractive indices as follows: A-phase  $\alpha = 1.628 \pm 0.003$ ,  $\gamma = 1.642 \pm 0.003$ ; B-phase  $\alpha = 1.647 \pm 0.003$ ,  $\gamma = 1.662 \pm 0.003$ . The A-phase was not encountered below these temperatures and the B-phase disappears above these temperatures. Comparing with the X-ray data it is evident that the A-phase corresponds to the  $\beta$ -wollastonite structure and the B-phase to the bustamite structure. The changes of refractive indices as a function of temperature are given in Figs. 3, 4, and 5. If the  $\beta$ -wollastonite<sub>SS</sub> changes in composition while maintaining its structure, the d-spacing and the refractive indices should change continuously. However, as seen in Figs. 1, 2, 3, 4, and 5, the changes of these values are discontinuous, indicating that there should be some change in the structural state. The observations mentioned above lead to the following conclusion: the phase with

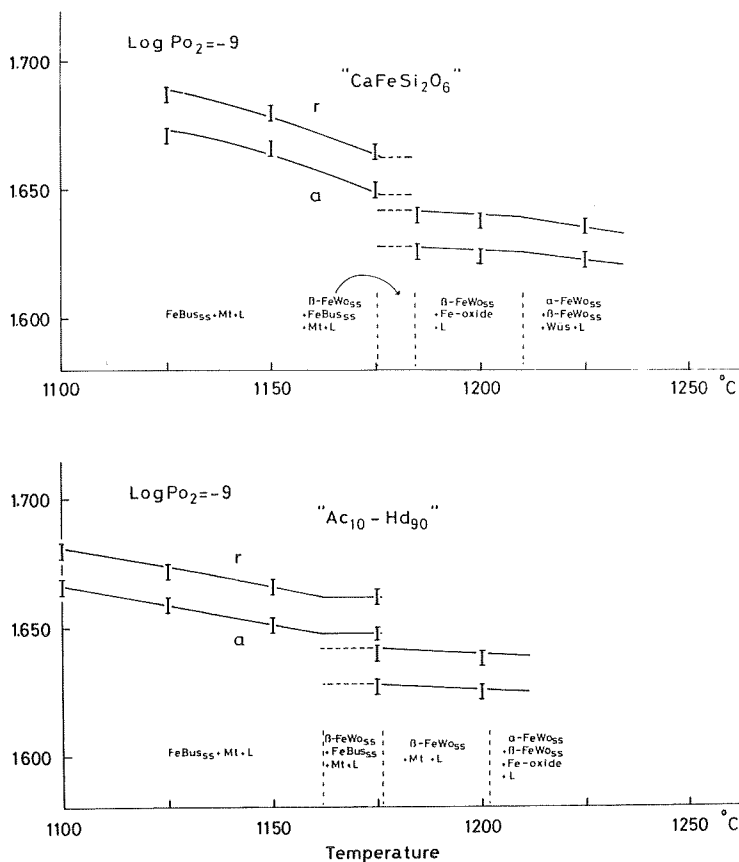


Fig. 5 Change of refractive indices of  $\alpha$ -Fe-wollastonite<sub>SS</sub> and Fe-bustamite<sub>SS</sub> crystallized from the compositions of  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  and  $\text{Ac}_{10}\text{Hd}_{90}$  at  $10^{-9}$  atm  $f_{\text{O}_2}$ . Abbreviations are same as in Fig. 1.

low refractive indices and larger d-spacing has  $\beta$ -wollastonite structure, whereas the phase with high refractive indices and smaller d-spacing is presumed to have bustamite structure.

Rutstein (1971) found that bustamite with composition between  $(\text{Ca}_{0.9}\text{Fe}_{0.1})\text{SiO}_3$  and  $(\text{Ca}_{0.8}\text{Fe}_{0.2})\text{SiO}_3$  shows a split in the peaks of X-ray diffraction patterns, indicating the presence of two phases. He also distinguished these two phases by infrared spectral analyses and concluded that these two phases correspond to the structures of  $\beta$ -wollastonite and bustamite, although their optical properties were not given. Matsueda (1973) found the natural mineral to have different structure from  $\beta$ -wollastonite and called the structure of this mineral "iron wollastonite structure" which corresponds to the bustamite investigated by Rutstein. Since in the present study the presence of



$\beta$ -wollastonite structure including  $\text{Fe}^{2+}$  is recognized in addition to  $\alpha$ -wollastonite and bustamite structures, it is not proper to use the term "iron wollastonite" for the mineral which has a bustamite structure.

In the present investigation, therefore, the three phases mentioned above are called  $\alpha$ -Fe-wollastonite<sub>SS</sub>,  $\beta$ -Fe-wollastonite<sub>SS</sub> and Fe-bustamite<sub>SS</sub>, because X-ray diffraction patterns are shifted from the pure compounds, indicating that  $\text{Fe}^{2+}$  is incorporated in the structures. Since there is some confusion concerning the structural states of these phases according to different workers, the nomenclature is compared in Table 1.

Table 1 The structural states of  $\alpha$ -Fe-wollastonite,  $\beta$ -Fe-wollastonite, and Fe-bustamite by different workers.

Phase present in this study	Structural states	
	Rutstein (1971)	Matsueda (1973)
$\alpha$ -Fe-wollastonite	—	—
$\beta$ -Fe-wollastonite	$\beta$ -wollastonite	$\beta$ -wollastonite
Fe-bustamite	bustamite	iron wollastonite

Under the microscope the Fe-bustamite<sub>SS</sub> forms nearly equant plates at lower temperatures and slender plates or prisms at higher temperatures, both being about 0.04 – 0.01 mm in length. The  $\beta$ -Fe-wollastonite<sub>SS</sub> forms slender plates or prisms, about 0.04 – 0.01 mm in length. Both of them are pale green and non-pleochroic. The  $\alpha$ -Fe-wollastonite<sub>SS</sub> forms equant plates or squares, about 0.02 – 0.04 mm in size. Pleochorism is distinct as follows:  $X'$  = colorless,  $Z'$  = pale green. The  $\alpha$ -wollastonite<sub>SS</sub> is distinguished from the other phases by its high birefringence. In addition to the silicate phases very small amounts of oxide minerals, magnetite and wüstite, are present throughout all runs.

### Phase diagrams

Results of quenching experiments for the oxygen fugacities  $10^{-11}$ ,  $10^{-10}$ ,  $10^{-9}$  atm are listed in appendices 1, 2, and 3 with refractive indices of the silicate minerals, and the phase diagrams for each of the isobaric sections are shown in Figs. 6, 7, and 8. The transition boundary of wüstite and magnetite is calculated from the data of Darken and Gurry (1945) to locate it at  $1143^\circ\text{C}$  at  $10^{-10}$  atm and  $1270^\circ\text{C}$  at  $10^{-9}$  atm.

At  $10^{-11}$  atm  $f_{\text{O}_2}$ , the following assemblages were encountered with falling temperature:  $\alpha$ -Fe-wollastonite<sub>SS</sub> + wüstite + liquid,  $\alpha$ -Fe-wollastonite<sub>SS</sub> +  $\beta$ -Fe-wollastonite<sub>SS</sub> + wüstite + liquid,  $\beta$ -Fe-wollastonite + wüstite + liquid,  $\beta$ -Fe-wollastonite<sub>SS</sub> + Fe-bustamite<sub>SS</sub> + wüstite + liquid, and Fe-bustamite<sub>SS</sub> +

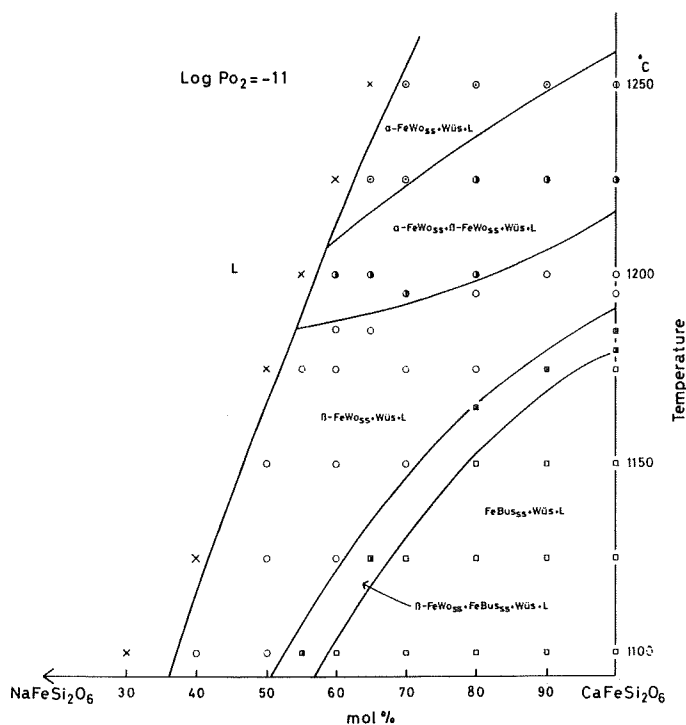


Fig. 6 Phase diagram of the system  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ - $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  at  $10^{-11}$  atm  $f_{\text{O}_2}$ . Abbreviations are given in Fig. 1.

wüstite + liquid. In the sections with  $f_{\text{O}_2}$  of  $10^{-10}$  and  $10^{-9}$ , the same assemblages were confirmed, except that wüstite converts to magnetite at lower temperatures.

In each section it is observed that the upper stability of each phase assemblage increases with increasing  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  and also that the stability field of each assemblage increases with decreasing  $f_{\text{O}_2}$ . On the other hand, the liquid field extends towards  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  with increasing  $f_{\text{O}_2}$ .

Since the present system is a join of a five-component system,  $\text{Na}_2\text{O}$ - $\text{CaO}$ - $\text{FeO}$ - $\text{SiO}_2$ , the iso-fugacity T-X section is not binary, but pseudo-binary. When the composition is projected from the oxygen apex onto the  $\text{Fe-SiO}_2$  line, magnetite and wüstite are compositionally coincident, so that the system is treated as a four-component system in the analysis of phase assemblages (see Lindsley et al., 1968). Therefore, a five-phase assemblage is univariant and a four-phase assemblage is divariant. In the  $10^{-11}$  atm section two divariant assemblages are present,  $\beta$ -Fe-wollastonite<sub>SS</sub> + Fe-bustamite<sub>SS</sub> + wüstite + liquid and  $\alpha$ -Fe-wollastonite<sub>SS</sub> +  $\beta$ -Fe-wollastonite<sub>SS</sub> + wüstite + liquid. In the  $10^{-10}$  atm and  $10^{-9}$  atm sections, the magnetite-wüstite inversion curve appears and

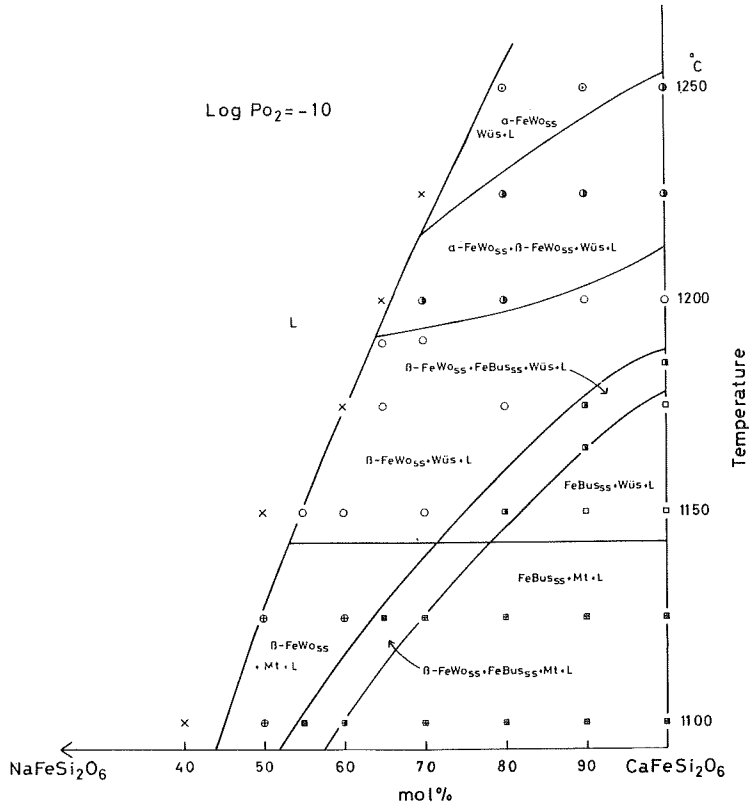


Fig. 7 Phase diagram of the system  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ - $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  at  $10^{-10}$  atm  $f_{\text{O}_2}$ . Abbreviations are given in Fig. 1.

crosses the divariant assemblage fields mentioned above, resulting in the presence of univariant assemblages:  $\beta$ -Fe-wollastonite<sub>SS</sub> + Fe-bustamite<sub>SS</sub> + wüstite + magnetite + liquid ( $10^{-10}$ ) and  $\alpha$ -Fe-wollastonite<sub>SS</sub> +  $\beta$ -Fe-wollastonite<sub>SS</sub> + wüstite + magnetite + liquid. Therefore, the univariant curve indicating these two assemblages has a positive slope in the T- $f_{\text{O}_2}$  projection and must lie on the magnetite-wüstite inversion plane which is independent of the composition in the T-X- $f_{\text{O}_2}$  space. These two univariant curves meet together at an invariant point where  $\alpha$ -Fe-wollastonite<sub>SS</sub>,  $\beta$ -Fe-wollastonite<sub>SS</sub>, Fe-bustamite<sub>SS</sub>, magnetite, and wüstite coexist with liquid.

When  $\text{Fe}^{3+}$  is not present at low  $f_{\text{O}_2}$ , say  $10^{-11}$ , sodium can not enter into the crystalline phases in the form of  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ , but all of this molecule is contained in the liquid. However, when magnetite is present, indicating the existence of  $\text{Fe}^{3+}$ , it is possible that some of the  $\text{Fe}^{3+}$ , in the form of  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ , can be incorporated in the silicate phases and the remainder is contained in the liquid. The amount of  $\text{Fe}^{3+}$  in the silicate phases may increase

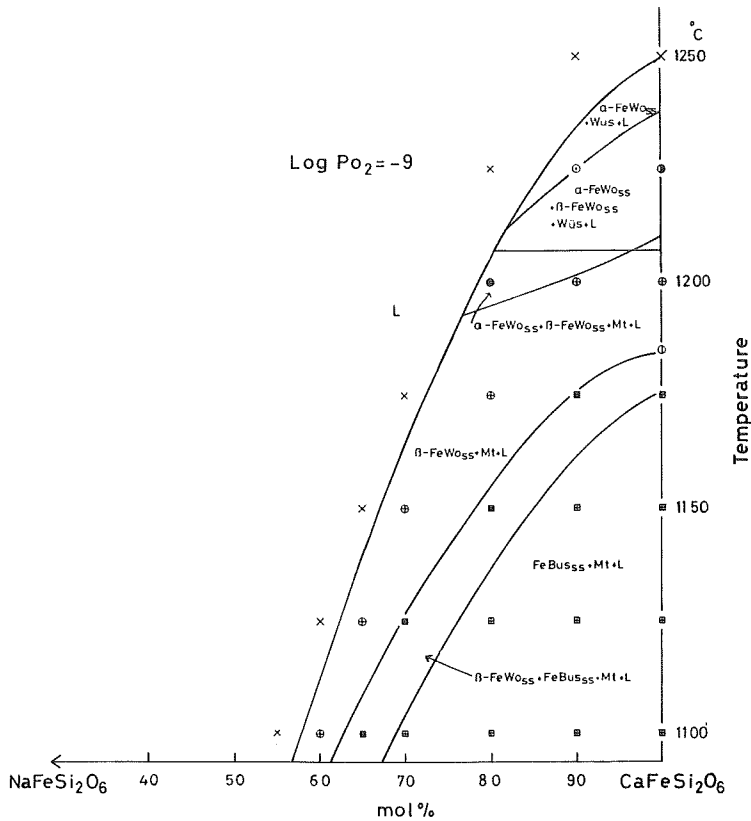


Fig. 8 Phase diagram of the system  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ - $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  at  $10^{-9}$  atm  $f_{\text{O}_2}$ . Abbreviations are given in fig. 1.

with decreasing amount of liquid and finally a complete series of solid solutions between  $\text{NaFe}^{3+}\text{Si}_2\text{O}_6$  and  $\text{CaFe}^{2+}\text{Si}_2\text{O}_6$  is formed at subsolidus temperatures as demonstrated by Ohashi (1976).

#### *Application to natural pyroxene*

The present experimental evidence supports the former conclusion of Yagi (1966) that at low  $f_{\text{O}_2}$  the pyroxene trend proceeds from diopsidic towards hedenbergitic and at high  $f_{\text{O}_2}$  from diopsidic through soda augite to aegirine. Recently Ewart et al. (1976) called attention to the fact that acmite-enrichment occurs only after extreme Fe-enrichment and not only  $f_{\text{O}_2}$  but activity of alumina in liquid plays an important role in determining the courses mentioned above. The presence of the acmite molecule in pyroxene also depends upon the concentration of calcium in the liquid. From their experimental studies Onuma and Yagi (1975) and Yoshikawa and Onuma (1975) suggested that at high  $f_{\text{O}_2}$

when enough calcium and aluminum are present  $\text{Fe}^{3+}$  enters into pyroxene in the form of  $\text{CaFe}^{3+}\text{AlSiO}_6$  and sodium forms nepheline, also that pyroxene proceeds towards acmite only when  $\text{Na} > \text{Fe}^{3+} + \text{Al}$ , as pointed out by Huckenholz (1973) in his study of natural pyroxene.

The above statement leads to the following conclusion: When  $f_{\text{O}_2}$  is higher than the magnetite-wüstite transition curve, pyroxene becomes acmitic in the case of  $\text{Na} > \text{Fe}^{3+} + \text{Al}$ , or fassaitic in the case of  $\text{Na} < \text{Fe}^{3+} + \text{Al}$ ; when  $f_{\text{O}_2}$  is lower than the magnetite-wüstite curve, it becomes hedenbergitic in either case.

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Appendix I Results of quenching experiments for the system  $\text{NaFe}^{+3}\text{Si}_2\text{O}_6 - \text{CaFe}^{+2}\text{Si}_2\text{O}_6$  at  $10^{-11}$  atm  $f_{\text{O}_2}$  and refractive indices of the pyroxenoids.

Composition (mol %)		Temp. ( $^{\circ}\text{C}$ )	Phases	Refractive indices ( $\pm 0.003$ )		
Ac	Hd			$\alpha$	$\gamma$	
0	100	1100	Fe-bus+wüs+gl	1.685	1.705	Fe-bus
		1125	Fe-bus+wüs+gl	1.680	1.700	Fe-bus
		1150	Fe-bus+wüs+gl	1.673	1.688	Fe-bus
		1175	Fe-bus+wüs+gl	1.654	1.669	Fe-bus
		1180	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.651	1.664	Fe-bus
				1.628	1.642	$\beta$ -Fe-wo
		1185	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.650	1.663	Fe-bus
				1.628	1.641	$\beta$ -Fe-wo
		1195	$\beta$ -Fe-wo+wüs+gl	1.626	1.640	$\beta$ -Fe-wo
		1200	$\beta$ -Fe-wo+wüs+gl	1.627	1.641	$\beta$ -Fe-wo
		1225	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.625	1.638	$\beta$ -Fe-wo
				1.609	1.652	$\alpha$ -Fe-wo
		1250	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.624	1.638	$\beta$ -Fe-wo
1.609	1.653			$\alpha$ -Fe-wo		
10	90	1100	Fe-bus+wüs+gl	1.675	1.691	Fe-bus
		1125	Fe-bus+wüs+gl	1.666	1.683	Fe-bus
		1150	Fe-bus+wüs+gl	1.655	1.669	Fe-bus
		1165	Fe-bus+wüs+gl	1.650	1.664	Fe-bus
		1175	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.649	1.662	Fe-bus
				1.628	1.642	$\beta$ -Fe-wo
		1185	$\beta$ -Fe-wo+wüs+gl	1.626	1.640	$\beta$ -Fe-wo
		1195	$\beta$ -Fe-wo+wüs+gl	1.626	1.640	$\beta$ -Fe-wo
		1200	$\beta$ -Fe-wo+wüs+gl	1.626	1.640	$\beta$ -Fe-wo
		1225	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.624	1.638	$\beta$ -Fe-wo
1.609	1.653			$\alpha$ -Fe-wo		
1250	$\alpha$ -Fe-wo+wüs+gl	1.609	1.654	$\alpha$ -Fe-wo		
20	80	1100	Fe-bus+wüs+gl	1.658	1.674	Fe-bus
		1125	Fe-bus+wüs+gl	1.655	1.669	Fe-bus
		1150	Fe-bus+wüs+gl	1.649	1.663	Fe-bus
		1165	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.647	1.662	Fe-bus
				1.628	1.642	$\beta$ -Fe-wo
		1175	$\beta$ -Fe-wo+wüs+gl	1.626	1.640	$\beta$ -Fe-wo
		1195	$\beta$ -Fe-wo+wüs+gl	1.625	1.639	$\beta$ -Fe-wo
		1200	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.622	1.636	$\beta$ -Fe-wo
				1.610	1.653	$\alpha$ -Fe-wo
		1225	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.623	1.636	$\beta$ -Fe-wo
1.609	1.653			$\alpha$ -Fe-wo		
1250	$\alpha$ -Fe-wo+wüs+gl	1.609	1.653	$\alpha$ -Fe-wo		

## Appendix 1 (continued)

Composition (mol %)		Temp. (°C)	Phases	Refractive indices (±0.003)		
Ac	Hd			$\alpha$	$\gamma$	
30	70	1100	Fe-bus+wüs+gl	1.655	1.668	Fe-bus
		1125	Fe-bus+wüs+gl	1.652	1.665	Fe-bus
		1150	$\beta$ -Fe-wo+wüs+gl	1.626	1.639	$\beta$ -Fe-wo
		1175	$\beta$ -Fe-wo+wüs+gl	1.622	1.634	$\beta$ -Fe-wo
		1195	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.622	1.636	$\beta$ -Fe-wo
				1.609	1.654	$\alpha$ -Fe-wo
		1225	$\alpha$ -Fe-wo+wüs+gl	1.609	1.653	$\alpha$ -Fe-wo
		1250	$\alpha$ -Fe-wo+wüs+gl	1.609	1.652	$\alpha$ -Fe-wo
35	65	1125	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.648	1.662	Fe-bus
				1.628	1.642	$\beta$ -Fe-wo
		1185	$\beta$ -Fe-wo+wüs+gl	1.625	1.639	$\beta$ -Fe-wo
		1200	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.623	1.636	$\beta$ -Fe-wo
				1.609	1.653	$\alpha$ -Fe-wo
		1225	$\alpha$ -Fe-wo+wüs+gl	1.610	1.653	$\alpha$ -Fe-wo
	1250	gl				
40	60	1100	Fe-bus+wüs+gl	1.652	1.666	Fe-bus
		1125	$\beta$ +Fe-wo+wüs+gl	1.626	1.640	$\beta$ -Fe-wo
		1150	$\beta$ -Fe-wo+wüs+gl	1.624	1.638	$\beta$ -Fe-wo
		1175	$\beta$ -Fe-wo+wüs+gl	1.624	1.637	$\beta$ -Fe-wo
		1185	$\beta$ -Fe-wo+wüs+gl	1.624	1.638	$\beta$ -Fe-wo
		1200	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.621	1.635	$\beta$ -Fe-wo
				1.610	1.653	$\alpha$ -Fe-wo
			1225	gl		
45	55	1100	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.649	1.663	Fe-bus
				1.627	1.641	$\beta$ -Fe-wo
		1175	$\beta$ -Fe-wo+wüs+gl	1.624	1.636	$\beta$ -Fe-wo
		1200	gl			
50	50	1100	$\beta$ -Fe-wo+wüs+gl	1.627	1.640	$\beta$ -Fe-wo
		1125	$\beta$ -Fe-wo+wüs+gl	1.625	1.638	$\beta$ -Fe-wo
		1150	$\beta$ -Fe-wo+wüs+gl	1.623	1.634	$\beta$ -Fe-wo
		1175	gl			
60	40	1100	$\beta$ -Fe-wo+wüs+gl	1.623	1.636	$\beta$ -Fe-wo
		1125	gl			
70	30	1100	gl			

Abbreviations are given in Fig. 1.



Appendix 2 Results of quenching experiments for the system  $\text{NaFe}^{+3}\text{Si}_2\text{O}_6 - \text{CaFe}^{+2}\text{Si}_2\text{O}_6$  at  $10^{-10}$  atm  $f_{\text{O}_2}$  and refractive indices of the pyroxenoids.

Composition (mol %)		Temp. ( $^{\circ}\text{C}$ )	Phases	Refractive indices ( $\pm 0.003$ )		
Ac	Hd			$\alpha$	$\gamma$	
0	100	1100	Fe-bus+mt+gl	1.683	1.700	Fe-bus
		1125	Fe-bus+mt+gl	1.674	1.691	Fe-bus
		1150	Fe-bus+wüs+gl	1.667	1.681	Fe-bus
		1165	Fe-bus+wüs+gl	1.653	1.667	Fe-bus
		1175	Fe-bus+wüs+gl	1.650	1.664	Fe-bus
		1185	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.648	1.663	Fe-bus
				1.629	1.642	$\beta$ -Fe-wo
		1190	$\beta$ -Fe-wo+wüs+gl	1.628	1.641	$\beta$ -Fe-wo
		1200	$\beta$ -Fe-wo+wüs+gl	1.628	1.641	$\beta$ -Fe-wo
		1225	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.627	1.640	$\beta$ -Fe-wo
				1.609	1.653	$\alpha$ -Fe-wo
		1250	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.623	1.636	$\beta$ -Fe-wo
1.609	1.652			$\alpha$ -Fe-wo		
10	90	1100	Fe-bus+mt+gl	1.670	1.683	Fe-bus
		1125	Fe-bus+mt+gl	1.663	1.678	Fe-bus
		1150	Fe-bus+wüs+gl	1.655	1.669	Fe-bus
		1165	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.649	1.663	Fe-bus
				1.628	1.641	$\beta$ -Fe-wo
		1175	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.649	1.662	Fe-bus
				1.628	1.641	$\beta$ -Fe-wo
		1185	$\beta$ -Fe-wo+wüs+gl	1.626	1.640	$\beta$ -Fe-wo
		1200	$\beta$ -Fe-wo+wüs+gl	1.626	1.639	$\beta$ -Fe-wo
		1225	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.625	1.638	$\beta$ -Fe-wo
1.609	1.653			$\alpha$ -Fe-wo		
1250	$\alpha$ -Fe-wo+wüs+gl	1.609	1.652	$\alpha$ -Fe-wo		
20	80	1100	Fe-bus+mt+gl	1.655	1.669	Fe-bus
		1125	Fe-bus+mt+gl	1.651	1.665	Fe-bus
		1150	$\beta$ -Fe-wo+Fe-bus+wüs+gl	1.648	1.662	Fe-bus
				1.629	1.642	$\beta$ -Fe-wo
		1200	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.621	1.638	$\beta$ -Fe-wo
				1.609	1.654	$\alpha$ -Fe-wo
		1225	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.623	1.636	$\beta$ -Fe-wo
1250	$\alpha$ -Fe-wo+wüs+gl	1.609	1.653	$\alpha$ -Fe-wo		
30	70	1100	Fe-bus+mt+gl	1.654	1.658	Fe-bus
		1125	Fe-bus+mt+gl	1.650	1.664	Fe-bus
		1150	$\beta$ -Fe-wo+wüs+gl	1.626	1.640	$\beta$ -Fe-wo
		1190	$\beta$ -Fe-wo+wüs+gl	1.622	1.636	$\beta$ -Fe-wo

## Appendix 2 (continued)

Composition (mol %)		Temp. (°C)	Phases	Refractive indices (±0.003)		
Ac	Hd			$\alpha$	$\gamma$	
		1200	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl +gl	1.620	1.634	$\beta$ -Fe-wo
				1.609	1.653	$\alpha$ -Fe-wo
		1225	gl			
35	65	1125	$\beta$ -Fe-wo+Fe-bus+mt+gl	1.648	1.662	Fe-bus
				1.628	1.642	$\beta$ -Fe-wo
		1175	$\beta$ -Fe-wo+wüs+gl	1.624	1.637	$\beta$ -Fe-wo
		1190	$\beta$ -Fe-wo+wüs+gl	1.622	1.636	$\beta$ -Fe-wo
		1200	gl			
40	60	1100	Fe-bus+mt+gl	1.650	1.664	Fe-bus
		1125	$\beta$ -Fe-wo+mt+gl	1.626	1.640	$\beta$ -Fe-wo
		1150	$\beta$ -Fe-wo+wüs+gl	1.623	1.636	$\beta$ -Fe-wo
		1175	gl			
45	55	1100	$\beta$ -Fe-wo+Fe-bus+mt+gl	1.648	1.662	Fe-bus
				1.627	1.642	$\beta$ -Fe-wo
		1150	$\beta$ -Fe-wo+wüs+gl	1.622	1.635	$\beta$ -Fe-wo
50	50	1100	$\beta$ -Fe-wo+mt+gl	1.623	1.635	$\beta$ -Fe-wo
		1125	$\beta$ -Fe-wo+mt+gl	1.622	1.635	$\beta$ -Fe-wo
		1150	gl			
60	40	1100	gl			

Abbreviations are given in Fig. 1.

Appendix 3 Results of quenching experiments for the system  $\text{NaFe}^{+3}\text{Si}_2\text{O}_6 - \text{CaFe}^{+2}\text{Si}_2\text{O}_6$  at  $10^{-9}$  atm  $f_{\text{O}_2}$  and refractive indices of the pyroxenoids.

Composition (mol %)		Temp. (°C)	Phases	Refractive indices ( $\pm 0.003$ )		
Ac	Hd			$\alpha$	$\gamma$	
0	100	1100	Fe-bus+mt+gl			
		1125	Fe-bus+mt+gl	1.671	1.687	Fe-bus
		1150	Fe-bus+mt+gl	1.666	1.680	Fe-bus
		1175	Fe-bus+mt+gl	1.650	1.665	Fe-bus
		1185	$\beta$ -Fe-wo+mt+gl	1.626	1.640	$\beta$ -Fe-wo
		1200	$\beta$ -Fe-wo+mt+gl	1.624	1.638	$\beta$ -Fe-wo
		1225	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+wüs+gl	1.623	1.636	$\beta$ -Fe-wo
			1.608	1.653	$\alpha$ -Fe-wo	
10	90	1100	Fe-bus+mt+gl	1.666	1.680	Fe-bus
		1125	Fe-bus+mt+gl	1.659	1.672	Fe-bus
		1150	Fe+bus+mit+gl	1.651	1.666	Fe-bus
		1175	$\beta$ -Fe-wo+Fe-bus+mt+gl	1.647	1.662	Fe-bus
				1.627	1.641	$\beta$ -Fe-wo
		1200	$\beta$ -Fe-wo+mt+gl	1.625	1.638	$\beta$ -Fe-wo
		1225	$\alpha$ -Fe-wo+wüs+gl	1.609	1.653	$\alpha$ -Fe-wo
		1250	gl			
20	80	1100	Fe-bus+mt+gl	1.655	1.668	Fe-bus
		1125	Fe-bus+mt+gl	1.653	1.666	Fe-bus
		1150	$\beta$ -Fe-wo+Fe-bus+mt+gl	1.647	1.661	Fe-bus
				1.627	1.640	$\beta$ -Fe-wo
		1175	$\beta$ -Fe-wo+mt+gl	1.627	1.640	$\beta$ -Fe-wo
		1200	$\alpha$ -Fe-wo+ $\beta$ -Fe-wo+mt+gl	1.625	1.638	$\beta$ -Fe-wo
				1225	gl	1.609
30	70	1100	Fe-bus+mt+gl	1.650	1.664	Fe-bus
		1125	$\beta$ -Fe-wo+Fe-bus+mt+gl	1.648	1.662	Fe-bus
				1.627	1.641	$\beta$ -Fe-wo
		1150	$\beta$ -Fe-wo+mt+gl	1.628	1.641	$\beta$ -Fe-wo
		1175	gl			
35	65	1100	$\beta$ -Fe-wo+Fe-bus+mt+gl	1.647	1.664	Fe-bus
				1.628	1.642	$\beta$ -Fe-wo
		1125	$\beta$ -Fe-wo+mt+gl	1.625	1.638	$\beta$ -Fe-wo
		1150	gl			
40	60	1100	$\beta$ -Fe-wo+mt+gl	1.623	1.636	$\beta$ -Fe-wo
		1125	gl			
45	55	1100	gl			

Abbreviations are given in Fig. 1.