Design of Taper Structure for Highly Efficient Coupling Between 1-D Photonic Crystal Coupled Resonator Optical Waveguide and Straight Waveguide

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Abstract—This paper presents a design method of a taper structure for highly efficient coupling between 1-D photonic crystal coupled resonator optical waveguides (1-D PC-CROWs) and input straight waveguides. We propose a new taper structure where not only air hole radius but also waveguide width are varied linearly in order to adjust the dispersion curves shift. By using the proposed tapered structure, we can connect each waveguide with high transmission over wide bandwidth. Our numerical simulation results show that a transmission of 98% around 1550 nm wavelength in a 6.6 μm long taper can be obtained with a 42 nm bandwidth.

Index Terms—Coupled resonator optical waveguide (CROW), finite-element method (FEM), photonic crystal.

I. INTRODUCTION

COUPLED RESONATOR OPTICAL WAVEGUIDES (CROWs) are highly attractive for integrated delay lines, nonlinear effects enhancement [1], and dispersion compensators [2]. Especially, optical delay lines have emerged as key components for future optical networks and information processing systems. There is a wide range of applications of optical delay lines, such as optical packet switches [3], [4], optical buffers [5], optical regenerators [6], wavelength converters [7], and optical delay-line filters [8]. CROWs are attractive for these applications because of their specific small group velocity and zero group velocity dispersion (GVD) at the transmission miniband [9]–[19]. CROWs can be classified in several categories in terms of the resonance structures such as, CROWs relying on ring resonators [18], Fabry-Perot cavities, and photonic crystal (PC) microcavities [12], [13], [15], [16], [20]. Among configurations relying on one- to three-dimensional PC cavities, 1-D PC-CROWs based on photonic wires are the most attractive in terms of simplicity, while keeping the advantages of PCs such as compactness and integrability [21], [22]. One of the drawbacks of 1-D PC-CROWs is its intrinsic propagation losses due to diffraction. This strongly limits their usefulness in various applications [23]. However, recently we have shown a loss reduction mechanism for the 1-D PC-CROWs and low-loss 1-D PC-CROWs structure for the first time to the best of our knowledge [24], therefore the low-diffraction-loss 1-D PC-CROWs can be a good candidate for developing various ultra compact optical circuits. When we construct optical devices based on PC-CROWs, it is necessary to efficiently couple the light into CROWs from regular waveguides with low reflection over wide wavelength range. Zain et al. proposed a taper structure to achieve high efficiency coupling between straight waveguides and single defect high-Q nanocavity [25]. However, the proposed taper can connect each waveguide only at a resonance wavelength. In this paper, we present a design method of a taper structure for highly efficient and broad band connection between 1-D PC-CROWs and input straight waveguides.

The remainder of this paper is structured as follows. In Section II, we first describe a model of 1-D PC-CROWs and the need of a taper structure by considering the transmission characteristic of directly coupled CROWs and straight waveguides. Next, we show a design method of a taper structure, where the tapering is achieved by a linear variation in the air-hole radius. This strongly limits their usefulness in various applications [23]. However, recently we have shown a loss reduction mechanism for the 1-D PC-CROWs and low-loss 1-D PC-CROWs structure for the first time to the best of our knowledge [24], therefore the low-diffraction-loss 1-D PC-CROWs can be a good candidate for developing various ultra compact optical circuits. When we construct optical devices based on PC-CROWs, it is necessary to efficiently couple the light into CROWs from regular waveguides with low reflection over wide wavelength range. Zain et al. proposed a taper structure to achieve high efficiency coupling between straight waveguides and single defect high-Q nanocavity [25]. However, the proposed taper can connect each waveguide only at a resonance wavelength. In this paper, we present a design method of a taper structure for highly efficient and broad band connection between 1-D PC-CROWs and input straight waveguides.

Fig. 1. Top view of 1-D PC-CROW directly connected to input straight waveguide (type 1).

Fig. 2. Transmission characteristics for a type-1 tapered structure.

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II. DESIGN METHOD OF TAPER STRUCTURES

A. Direct Connection Between CROWs and Straight Waveguides

We consider a 1-D PC-CROW structure which is connected with straight waveguide as shown in Fig. 1. We set structural parameters of CROWs as follows. The lattice constant $a$ of 1-D PCs is 300 nm, the waveguide width $w$ is $1.2a = 360$ nm, and the air hole radius $r_1$ is $0.3a = 90$ nm. We set the defect after every fourth air hole to make resonance structure, the cavity distance is set as $b = 2.5a = 750$ nm, and the intercavity distance $\Lambda$ is $5.5a = 1650$ nm in the present case. We use silicon, with the refractive index of 3.48, as the core material and air as the cladding material. We assume that there is no variation in the $y$-direction. To reduce the diffraction losses, we set the radius of the air hole “adjacent” to the cavity as $r_2 = 0.2a = 60$ nm for minimizing the reflection at the cavity edge [24]. The tangential wavenumber components of the leaky guided modes which couple to cladding modes can be decreased, resulting in the reduction of propagation losses due to diffraction. The propagation losses of this 1-D PC-CROW is $\sim 0.2$ dB/mm [24]. Note that, the scattering loss in $y$-direction is not considered in this case, therefore the propagation losses of a real 1-D PC-CROW may be larger.

At first, we consider a direct connection between ten periods of the CROWs and the straight waveguide (type 1). Fig. 2 shows the transmission characteristic for the TM mode calculated by 2-D finite-element time domain beam propagation method (FETD-BPM) [26], where the magnetic field is polarized along $y$-axis. We can see from this figure that we cannot achieve high transmission over wide bandwidth due to the effect of reflection at the connection interface, even though there are some high transmission peaks. Therefore, we should design a taper structure to connect each waveguides with a high transmission.

B. Tapering Connection Between CROWs and Straight Waveguides

To improve the transmission characteristics, the CROW and the straight waveguide are connected by the taper structure as shown in Fig. 3 (type 2), where $N$ is the number of periods that constructs the taper region, namely, total length of the taper becomes $N\Lambda$. The starting position of the waveguide taper is assumed to be $z = 0$ and the center position of $j$th ($j = 1, 2, 3, 4$) air hole at $i$th ($i = 1, 2, \ldots, N$) fundamental structure is defined as $z = z_{ij}$. To make the gentle variation of the refractive index along the propagation direction, we vary the air hole radius linearly as

$$R_{ij} = R_0 + (1 - R_0)/(NA)$$  \hspace{1cm} (1)

where $R_{ij}$ and $R_0$ are the reduction rate of the air hole radius at $z = z_{ij}$ and $z = 0$, respectively. The air hole radius at $z = z_{ij}$ becomes $r_1 R_{ij}$ (for $j = 2, 3$) or $r_2 R_{ij}$ (for $j = 1, 4$). We can see from (1) that the air hole radius at the tapered waveguide is determined by setting $N$ and $R_0$. We further show how to calculate the air hole radius in the tapered section with $N = 9$ and $R_0 = 0.1$ structure. For example, we consider the ninth ($i = 9$) fundamental structure. The center position of the air hole: $z_{91}$, $z_{92}$, $z_{93}$, and $z_{94}$ are

$$z_{91} = 8\Lambda + \frac{1}{2}b = 45.25a$$
$$z_{92} = z_{91} + a = 46.25a$$
$$z_{93} = z_{92} + a = 47.25a$$
$$z_{94} = z_{93} + a = 48.25a.$$  \hspace{1cm} (2)

By assigning these values to (1), the air hole radius in this segment is determined as follows:

$$r_{91} = r_2 R_{91} = 0.92r_2 = 55 \text{ nm}$$
$$r_{92} = r_1 R_{92} = 0.94r_1 = 85 \text{ nm}$$
$$r_{93} = r_1 R_{93} = 0.96r_1 = 86 \text{ nm}$$
$$r_{94} = r_2 R_{94} = 0.98r_2 = 59 \text{ nm}.$$  \hspace{1cm} (3)

Fig. 4 shows the transmission characteristic for the CROW using a type-2 tapered structure with $N = 9$ and $R_0 = 0.1$. The transmission is limited to the lower frequency range and it is highly oscillating. In addition, we can see from this figure that the transmission at higher frequency range is completely suppressed even if we use taper structure for air hole radius variation.

To understand the transmission suppression at higher frequency range, the dispersion curves for CROWs with different air-hole radius are plotted in Fig. 5(a), where the air hole radii $r_1$ and $r_2$ are changed to $r_1'$ and $r_2'$, respectively, at a fixed waveguide width $w = 1.2a$. The dispersion curve of a straight waveguide is also plotted in Fig. 5(a) in order to make a comparison. We can see from these results that the dispersion
Fig. 5. Dispersion curves of CROWs (a) with different air hole radius and constant waveguide width and (b) with different air hole radius and waveguide widths.

III. MINIATURIZATION OF TAPER LENGTH

In this section, we consider the effect of waveguide parameters constructing the taper to design more compact tapered structure. At first, we evaluate the effect of $R_0$. The parameters in previous type-3 structure ($R_0 = 0.1$ and $N = 9$) means that the rate of air hole radius variation ($R_{ij} - R_{(i-1)j}$) is 0.1. Therefore, we can estimate the effect of $R_0$ by changing type-3 taper for $N$ while keeping $R_{ij} - R_{(i-1)j}$ as 0.1. Fig. 8 shows the transmission characteristics for $R_0 = 0.1, 0.2, 0.3,$ and 0.4, where $N$ becomes 9, 8, 7, and 6, respectively. We have to also decide $w_0$ for each structure, which can be easily determined from the dispersion curves in Fig. 5(b) for fixed $R_0$ and follows as 0.82μm, 0.84μm, 0.86μm, and 0.88μm, respectively, for each $R_0$. We can see from Fig. 5 that $R_0 = 0.1$ and 0.2 structures show almost flat top characteristics over 98% transmission. On the other hand, the transmission oscillates as $R_0$ increases further which is due to the reflection at the connection interface. This is because as $N$ decreases, the waveguide structure approaches to type-1 structure. In case of $R_0 = 0.4$, the transmission oscillates between 0.7 and 1.0, therefore if more than 90% transmission is required, we should keep $R_0$ less than 0.3. So far, we have considered the tapered structure for constant ratio of air-hole radius variation (0.1). If this value increases, the total taper length decreases, which suggests the decrement of $N$.

Next, we examine the transmission characteristics for different $N$ while keeping fixed $R_0$. We have evaluated the transmission characteristics for three values of $R_0$, namely 0.1, 0.2, and 0.3 and varied the number of periods $N$ in every case. The transmission characteristics are plotted in Figs. 9(a)–(c) for $R_0 = 0.1, 0.2,$ and 0.3, respectively, with $N$ as a variable. It can be inferred from the results that the transmission changes abruptly in short wavelengths as we decrease the $N$, resulting in narrower bandwidth. This may be due to the mismatch of the dispersion relationship between actual tapered structure and the waveguide structure as shown in Fig. 5. The parameters that construct the taper are determined from the dispersion curves for a model structure, where the waveguide width and the air hole radius are varied at a constant rate along $z$-direction. On the other hand, type-3 taper structure is changed by varying the waveguide width and the air hole radius linearly with a gentle variation in the refractive index, but not with a constant rate. When the rate of air-hole radius variation is small (e.g., $R_{ij} - R_{(i-1)j} = 0.1$), the each sectional taper structure can be approximated by waveguide structure with tailored waveguide width and air hole radius with a constant ratio. However, when the rate of air-hole radius variation becomes large for small $N$, the taper can not be approximated by the model. This results in mismatch of dispersion relationship and the degradation of transmission at the shorter wavelength range. Also, the waveguide width in taper section changes abruptly for small $N$ structure, therefore scattering loss due to abrupt waveguide width variation should be taken into account. However, more than 99.9% transmission was obtained even for $R_0 = 0.2$ and $N = 2$ structure without air holes (straight waveguide). Hence, scattering loss due to abrupt waveguide width variation is negligible which can be ignored. We can see from Fig. 9 that the taper length can be shortened to less than half of previous type-3 structure with almost same wavelength range by choosing $R_0 = 0.2$ and $N = 4$. 

curve is red-shifted as air hole radius decreases. In other words, if we reduce the air hole radius at a constant waveguide width, there is no guided mode at short wavelengths, resulting in the complete suppression of the transmission at short wavelengths as shown in Fig. 4.

In order to adjust the dispersion curve shift due to air hole radius variation, we simultaneously vary the waveguide width and the air hole radius. The dispersion curves for CROWs with different air-hole radius and waveguide width are shown in Fig. 5(b), where the air hole radii $r_1$ and $r_2$ are changed to $r_1'$ and $r_2'$, respectively, and the waveguide width $w$ is changed to $w'$. We can see that the dispersion curve of the CROWs with reduced air hole radius and waveguide width is in the almost same frequency range for the CROWs to be connected with the air hole radii $r_1$ and $r_2$ and the waveguide width $w$. Based on the above analysis, we propose a new tapered structure, type-3, shown in Fig. 6, where the air hole radius and the waveguide width are changed linearly at the same time. The variation in air-hole radius is defined by (1) whereas, the variation in waveguide width is given as

$$w_{i-1} = w_0 + (w - w_0)(i - 1)/N \quad (3)$$

where $w_{i-1}$ and $w_0$ are waveguide width at $z = (i - 1)\Lambda$ and $z = 0$, respectively. Fig. 7 depicts the transmission characteristic for connection between input waveguide and CROWs using type-3 taper structure with $N = 9$, $R_0 = 0.1$, and $w_0 = 0.82\mu m$. By using the tapered structure type 3, the reflection at the connection end can be minimized and the transmission can be improved drastically. More than 98% transmission is achieved for 42 nm bandwidth around 1550 nm wavelength range in the case of $\Lambda = 1.65 \mu m$. The total length of the proposed taper is $\sim 14.8 \mu m$. 

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at a constant rate of air hole radius variation structure.

5%, and 5%.

Because these taper structures are set as 0.2,

value, range. In ,

We note that increment of becomes 0, and structure, on the other hand at lower . We can also see that the bandwidth does not as 0.2 and 4, respectively. As estimated from . In this case,

It is estimated that the value of 5% error,

values in Fig. 10(a). In this

lower for .

Therefore, air hole radius should be controlled within 0.1.

We consider the fabrication tolerances of taper waveguide. At first, we examine the coupling characteristics of CROWs and straight waveguide by using proposed taper waveguide with error in the air hole radius. We assume that all the air hole in a taper section is fabricated with Δ% error from designed parameters. The coupling characteristics can be estimated from dispersion curves, therefore, we show dispersion curves of the 1-D PC-CROWs with various Δ values in Fig. 10(a). In this case, the air hole radius is \( r_1' / r_1 = r_2' / r_2 = 0.8 \times (1 + \Delta) \) and the waveguide width is 0.6μm. It is estimated that the value of Δ needs to be controlled within \(-5% < \Delta < 5\%\) range. In Fig. 10(b), we show transmission characteristics for a type-3 tapered structure with \( \Delta = 0, -5\%, \) and 5%. As we have discussed in previous section, \( R_0, u_0, \) and \( N \) are set as 0.2, 0.84μm, and 4, respectively. We can see that as estimated from dispersion curve, transmission at higher frequency becomes lower for \( \Delta = -5\% \) structure, on the other hand at lower frequency, transmission becomes lower for \( \Delta = 5\% \) structure. Therefore, air hole radius should be controlled within \( \pm 5\% \) error.

Next, we consider the effect of fabrication error in the waveguide width of the taper waveguide. In Fig. 11(a), we show dispersion curves of the 1-D PC-CROWs for \( r_1' / r_1 = r_2' / r_2 = 0.8 \) and \( w' / w = 0.96 \times (1 + \Delta) \). From these results, it is estimated that the waveguide width needs to be controlled within \(-5\% < \Delta < 5\%\) range. Fig. 11(b) shows transmission characteristics of type-3 taper structure for \( \Delta = 0, -5\%, \) and 5%. For these Δ value, \( u_0 \) becomes 0.84μm × (1 + Δ). In this case, we set \( R_0 \) and \( N \) as 0.2 and 4, respectively. As estimated from dispersion curve, transmission at the higher frequency becomes lower for \( \Delta = 5\% \). We can also see that the bandwidth does not change for \( \Delta = -5\% \) structure because these taper structures can support CROW’s mode, however, transmission oscillates due to abrupt waveguide width change (refractive index change) in the taper region. This reflection can be reduced by increasing \( N \). For example, we also plot transmission characteristic for \( N = 8 \) and \( \Delta = -5\% \) in Fig. 11(b). We note that increment of \( N \) means the number of air hole we have to control increases and taper length becomes longer. If we require more than 90% transmission, \( u_0 \) needs to be controlled within \( \pm 5\% \) error, ±20 nm variation. In addition, in a 2-D coupled photonic crystal heterostructure nanocavities, it is known that guiding characteristics are sensitive to waveguide parameters [27], therefore, the
waveguide parameters of our 1-D PC-CROWs will also need to be well controlled.

Through this investigation, we can see that both air-hole size and waveguide width in the taper waveguide need to be fabricated within ±5% error. Regarding the controllability of the air hole diameters, it is known that the fabrication error can be decreased to the order of 20 nm by using a current fabrication technology relying on the inspection of scanning electron microscope (SEM) images. However, Beggs et al. recently proposed a novel measurement technique of the air hole size in photonic crystal slabs and reported that the fabrication error can be reduced to the order of approximately 5 nm [28]. If this technique can be applied to 1-D PC-CROWs, highly efficient coupling will be achieved in the realistically fabricated structure.

V. CONCLUSION

We have presented a design method of a taper structure for highly efficient connection between 1-D PC-CROWs and straight waveguides. We have first examined the transmission characteristic of a directly connected structure between CROWs and straight waveguides (type 1). Then in order to minimize the effect of reflection at the connection interface, we designed a taper where air hole radius is varied linearly (type 2). These tapers can not achieve efficient connection due to reflection and complete transmission suppression at short wavelengths. The cause of this suppression is the shift of the dispersion curves due to variation in air hole radius. To adjust the dispersion curve shift, we simultaneously varied the waveguide width and the air hole radius and proposed a type-3 tapered structure. The proposed type-3 taper can connect CROWs and straight waveguides with transmission of more than 98% in the whole C-band. Through numerical simulations, we find a 14.8 μm taper length which can be further reduced by varying \( R_0 \) and \( N \) to a value of 6.6 μm for a suitable set of \( R_0 \) and \( N \). We have also shown fabrication tolerances of the taper waveguide and found that both the air hole and waveguide width need to be controlled within ±5% fabrication error.

In order to consider the scattering losses in the vertical direction, one has to carry out 3-D simulations, which are currently under consideration.

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