



Title	Nanoscale mechanical contacts probed with ultrashort acoustic and thermal waves
Author(s)	Dehoux, Thomas; Wright, Oliver B.; Voti, Roberto Li; Gusev, Vitalyi E.
Citation	Physical Review B, 80(23), 235409 https://doi.org/10.1103/PhysRevB.80.235409
Issue Date	2009-12-15
Doc URL	http://hdl.handle.net/2115/42549
Rights	©2009 The American Physical Society
Type	article
File Information	PRB80-23_235409.pdf



[Instructions for use](#)



Nanoscale mechanical contacts probed with ultrashort acoustic and thermal waves

Thomas Dehoux and Oliver B. Wright*

Division of Applied Physics, Graduate School of Engineering, Hokkaido University, Sapporo 060-8628, Japan

Roberto Li Voti

Dipartimento di Energetica, Sapienza Università di Roma, Via A. Scarpa 16, Roma 00161, Italy

Vitalyi E. Gusev

Laboratoire de Physique de l'Etat Condensé, UMR CNRS 6087, Université du Maine, Le Mans F-72085, France

(Received 5 October 2009; published 8 December 2009)

Using an ultrafast optical technique we measure coherent phonon-pulse reflection from—and heat flow across—a mechanical contact of nanoscale thickness between a thin metal film and a spherical dielectric indenter. Picosecond phonon wave packets at ~ 50 GHz returning from this interface probe the pressure distribution, the contact area, and the indentation profile to subnanometer resolution, revealing the film deformation *in situ*. These measurements and simultaneous thermal-wave imaging at ≥ 1 MHz are consistent with significant enhancement of phonon transport across the near-contact nanogap.

DOI: [10.1103/PhysRevB.80.235409](https://doi.org/10.1103/PhysRevB.80.235409)

PACS number(s): 68.35.Ct, 78.20.Nv, 46.55.+d, 43.35.+d

I. INTRODUCTION

The properties of mechanical contacts between solids depend on how individual asperities mesh on the nanoscale, and a physical understanding is vital in engineering for the study of friction, lubrication, and electrical or heat conduction as well as in biology for the study of cell-membrane adhesion or joints.^{1,2} A generic approach to studying static mechanical contacts that facilitates the separation of elastic and plastic behaviors is the use of microscale or macroscale spherical (Hertz) indenters.^{1,3} This geometry is an apt choice for the lateral imaging of the contact by penetrating wave fields.⁴

The contact area can be imaged by optical interferometry combined with microscopy.⁵ Ultrasonic imaging, applicable also to opaque materials, allows one to map in addition the interfacial stiffness or the contact pressure.^{6,7} However, with a spatial resolution on the order of the ~ 0.1 mm acoustic wavelength at the typical maximum frequencies ~ 30 MHz used, one cannot effectively probe nanoscale deformations. Neither can one accurately study interfaces with nanoscale roughness. Likewise, probing mechanical contacts using modulated thermoreflectance up to the maximum frequencies ~ 3 kHz used is limited in spatial resolution by the ~ 30 μm thermal-diffusion length.⁸ One can image nanoindentation processes in a transmission electron microscope with subnanometer resolution, but this technique is not suited to spatially resolved mapping over the contact area.⁹

In this paper we implement much shorter acoustic and thermal wavelengths to map the deformation in or near a Hertz mechanical contact of nanoscale thickness. We introduce an *in situ* coherent phonon and thermal-profiling technique at frequencies ~ 100 GHz and ≥ 1 MHz, respectively, more than 1000 times higher than previously used in contact mechanics.

II. EXPERIMENTAL SETUP

The setup is shown in Fig. 1(a). The sample is a 110-nm

polycrystalline Cr film sputtered on a (0001) sapphire substrate of thickness 0.8 mm. The sample lies on a rigid holder pierced with a 1.8-mm radius hole for optical access. A sintered silicon-nitride sphere¹⁰ of diameter $D=5.96$ mm is indented into the pristine Cr film using a high-precision displacement stage. The applied load, stable at each setting to $\pm 5\%$ over several hours, is measured with a load cell. To investigate contacts with nanoscale separations, we use highly polished surfaces. The rms roughnesses of the film, indenter and substrate, determined by atomic force microscopy (AFM) with 40-nm step size [see Fig. 1(b)], are $\sigma_f=3$ nm, $\sigma_i=13$ nm, and $\sigma_s=1$ nm, respectively.¹¹ Picosecond longitudinal coherent-phonon pulses are thermoelastically generated at the film-substrate (f - s) interface with linearly polarized optical pump pulses of duration 200 fs, repetition frequency 80 MHz, wavelength 810 nm (optical reflectivity 0.23), and pulse energy $E=0.5$ nJ from a Ti:sapphire mode-locked laser.^{12–14} This light is chopped at 1.1 MHz for thermal-wave excitation and lock-in detection. The reflectivity change $\delta R(t)$ is measured with frequency-doubled circularly polarized probe pulses of wavelength $\lambda_{pb}=405$ nm (reflectivity $R_0=0.29$) and energy 0.06 nJ as a function of the pump-probe time delay t . The coaxial pump

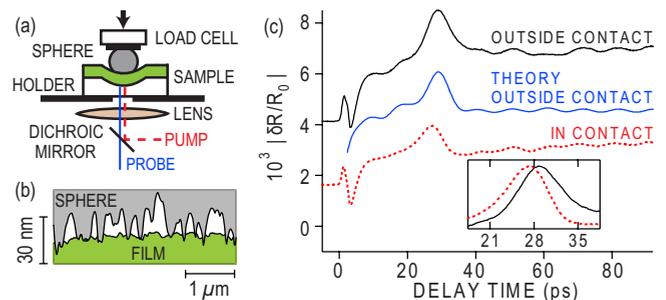


FIG. 1. (Color online) (a) Setup. (b) AFM traces. (c) $|\delta R(t)/R_0|$ at $F=4.2$ N. The theory out of contact is shown displaced. Inset: normalized experimental echoes.

and probe beams are focused at the f - s interface by a laterally scanned $\times 50$ objective lens to spots of radii $w_1=1.9\ \mu\text{m}$ and $w_2=1.1\ \mu\text{m}$ (intensity at $1/e^2$), respectively [effective radius $w=(w_1^2+w_2^2)^{1/2}=2.2\ \mu\text{m}$]. Pertinent physical properties are the longitudinal sound velocity v_n , density ρ_n , Poisson's ratio ν_n , Young's modulus E_n , thermal conductivity κ_n , and heat capacity C_n , with $n=i, f$, and s for the indenter, film and substrate.¹⁵

III. RESULTS FOR THE ACOUSTIC EXPERIMENTS

A. Shape of the acoustic echoes

Figure 1(c) shows the amplitude $|\delta R(t)/R_0|$ (where $\delta R < 0$) for the load $F=4.2\ \text{N}$ in and out of contact.¹⁶ $\delta R \propto E$ was checked up to pump-pulse energy $E=0.5\ \text{nJ}$. For $t < 0$, $|\delta R|$ is lower in contact due to thermal-wave effects, as discussed later. At $t=0$ we observe a peak followed by a dip and then a rise in $|\delta R/R_0|$ at $t=10\text{--}20\ \text{ps}$. This is due to the cumulative effects of a transient-temperature rise¹⁷ $\delta T \sim 500\ \text{K}$ ($dR/dT < 0$) and strain generation.^{12,18}

Initially a hydrostatic compressive stress field is generated in Cr over a depth $z_{ac} \sim 35\ \text{nm}$ determined by the optical skin depth $\sim 30\ \text{nm}$ (Ref. 19) and the electron diffusion depth $\sim 15\ \text{nm}$.¹⁴ The acoustic impedances $Z_n = \rho_n v_n$ of Cr and Al_2O_3 imply a low film-substrate reflection coefficient $r_{fs} = (Z_s - Z_f)/(Z_s + Z_f) = -0.04$, so two unipolar compressive coherent-phonon pulses (of strain amplitude $\sim 10^{-3}$) are launched perpendicular to the f - s interface in both materials.²⁰ In Al_2O_3 these pulses create oscillations in δR (visible after 40 ps) at the Brillouin frequency $2n_s v_s / \lambda_{pb} \approx 100\ \text{GHz}$, with $n_s = 1.76$ the Al_2O_3 refractive index.²⁰⁻²² In Cr a broadband picosecond strain pulse of frequency $0 < f \leq 100\ \text{GHz}$ (Ref. 23) and wavelength $\Lambda \geq 70\ \text{nm}$ is reflected from the film-indenter (f - i) interface with a reflection coefficient r_{fi} (determined later). This pulse is detected at the f - s interface as an echo at $\sim 30\ \text{ps}$. Because of the low value of r_{fs} , only one echo is resolved. Echoes normalized using r_{fi} in and out of contact are shown in Fig. 1(c). When in contact the echo arrives earlier, is reduced in height, and is asymmetrically distorted, although the echo spectrum is not significantly changed. The echo shape depends on the longitudinal strain η that in the near-surface region can be written in the approximate form^{12,14}

$$\eta(z, t) \propto \theta(z - v_f t) \exp[(v_f t - z)/z_{ac}], \quad (1)$$

where θ is the unit step function and z is the depth. We combine this equation with an ultrasonic attenuation that rises quadratically with the frequency for Cr in the GHz range.¹⁴ The resulting $\eta(z, t)$ allows one to derive the expected reflectivity variation that arises through the photoelastic effect.^{12,24} The central curve in Fig. 1(c) shows the predicted $|\delta R(t)/R_0|$ out of contact using the photoelastic constant $p_{12}^s = -0.03$ for Al_2O_3 (Ref. 21) and the fit $p_{12}^f = 0.28 + 0.00i$ for Cr. For the Cr film in this study, ultrasonic attenuation $\beta = 600\ \text{f}^2\ \text{m}^{-1}$ (f in GHz) gives the best fit to the echo with a film thickness $h = 110\ \text{nm}$.^{14,25}

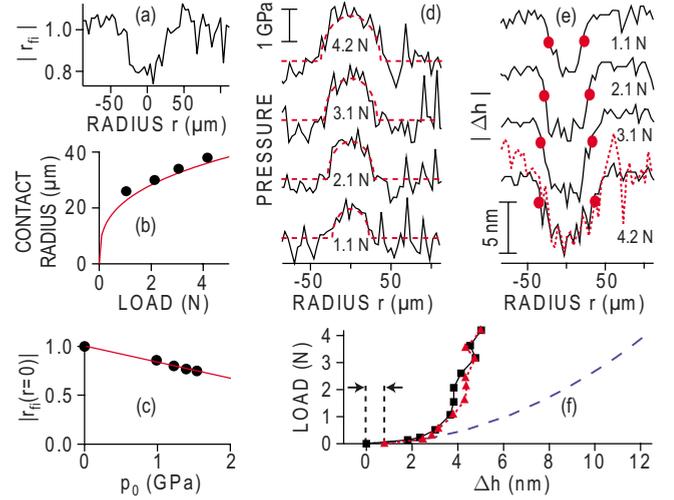


FIG. 2. (Color online) (a) Acoustic reflection coefficient $|r_{fi}|$ vs r at $F=2.1\ \text{N}$. (b) Contact radius from $|r_{fi}|$ (dots) and Hertz theory for Al_2O_3 - Si_3N_4 (line). (c) $|r_{fi}(r=0)|$ against p_0 (dots) with fit (line). (d) Pressure p vs r (solid lines) and Hertz theory (dashed lines). (e) Film indentation Δh . Dots: Hertz contact radii. Dashed line: $-p(r)$ for $F=4.2\ \text{N}$. (f) F vs $|\Delta h|$ at $r=0$ for loading (■) and unloading (▲) compared with theory (dashes). Arrows: permanent deformation.

B. Profiles of the acoustic reflection coefficient

A left-right average of the base of the echo determines the echo height. Setting $r_{fi} = -1$ outside the contact determines the in-contact value. We plot $|r_{fi}|$ vs radial coordinate r in Fig. 2(a) for load $F=2.1\ \text{N}$ in $4\text{-}\mu\text{m}$ steps. The fluctuations, showing some correlation with scans at different F , are caused by surface roughness. Over the contact, $|r_{fi}|$ decreases to 0.8. For a perfect contact, $r_{fi} = r_{fi}^{\text{th}} = (Z_i - Z_f)/(Z_i + Z_f) = -0.17$. Interstitial air gaps, shown in Fig. 1(b), result in a larger $|r_{fi}|$. As F increases, the total asperity (i.e., real contact area) increases, and $|r_{fi}(r=0)|$ decreases. We can empirically fit our data with $|r_{fi}(r=0)| = 1 - (F/110)^{0.4}$, with F in N. To obtain further insight into the local variations within the contact, we must calibrate our results in terms of pressure.

We first estimate the contact radius a from Hertz theory¹ for a sphere indenting a frictionless half space

$$a^3 = 3FD/8E^*, \quad (2)$$

where $E^* = [(1 - \nu_i^2)/E_i + (1 - \nu_s^2)/E_s]^{-1} = 200\ \text{GPa}$ is the effective modulus. We derive a from $|r_{fi}(r)|$ and compare it to theory in Fig. 2(b). The data lie above the predictions, consistent with theories for elastically indented thin films for $E_f/E_s < 1$.²⁶ To apply Hertz theory, the combined surface roughness $\sigma = (\sigma_1^2 + \sigma_2^2)^{1/2} \approx 13\ \text{nm}$ should also be considered. In our case the roughness parameter $\alpha = \sigma D/2a^2 < 0.07 \ll 1$ for $F > 1.1\ \text{N}$, so Hertz theory is valid.¹ We thus use the Hertz pressure

$$p(r) = p_0 [1 - (r/a)^2]^{1/2}, \quad (3)$$

with maximum value $p_0 = 3F/2\pi a^2$, to derive $|r_{fi}(p_0)|$ from the measured $|r_{fi}(F)|$ at $r=0$. We see a linear decrease $|r_{fi}(p_0)| \approx 1 - p_0/p_1$ in Fig. 2(c) with $p_1 = 6.1\ \text{GPa}$. This pro-

vides a calibration to obtain $p(r)=p_1[1-|r_{fi}(r)|]$, showing good agreement with theory in Fig. 2(d). Before discussing these results in detail we first present the results for film indentation.

C. Profiles of the indentation

Uniquely, with picosecond ultrasonics we can directly extract the film indentation $\Delta h=v_f\Delta\tau/2$ from the echo arrival-time variation $\Delta\tau$ during loading.²⁷ $\Delta h(r)$, plotted in Fig. 2(e), varies over regions slightly larger than the contact radii a , as expected. Striking correlation at each load F between the fluctuations in $\Delta h(r)$ and $-p(r)$ [see dashed line in Fig. 2(e)] confirms that these are indeed induced by roughness. Finer scale data at $r=0$ is shown in Fig. 2(f) for a first load-unload cycle in steps of 0.5 N lasting 10 min per point. The overall shape of F vs $|\Delta h|$ is evidently governed by elasticity. The application of linear elasticity theory for a thin Cr film on a rigid substrate indented by a rigid sphere leads to the following equation:²⁸

$$F = \pi D \rho_f v_f^2 \Delta h^2 / 2h. \quad (4)$$

The predicted load-indentation curve is shown by the dashed line in Fig. 2(f). Unsurprisingly, the measured $|\Delta h|$ (<6 nm) is smaller because of the indenter and substrate elasticity. In comparison, the deformation of the substrate-indenter system is much larger: $\delta=2a^2/D > 180$ nm for $F > 1.1$ N.¹

A permanent plastic deformation ~ 1 nm remains after unloading [see arrows in Fig. 2(f)]. However, the Vickers hardness $H \approx 15$ GPa of thin-film Cr,²⁹ the softer material, indicates that the maximum pressure $p_0=1.5$ GPa is not sufficient for bulk-film yielding.¹ This justifies the use of linear elastic theory for the bulk deformation of Cr. In order to understand the origin of the plasticity, one should consider the asperity deformation. For our Gaussian distribution of asperity heights, this is governed by the so-called plasticity index:^{2,30}

$$\psi = (E^*/H)(\sigma/r_a)^{1/2}. \quad (5)$$

Here $\psi \geq 3$, where $r_a \leq 0.3$ μm is the AFM-measured average Si_3N_4 asperity radius; $\psi > 1$ indicates Cr plastic compression by the harder Si_3N_4 . For noninteracting asperities, overall force balance dictates that $S_r H = S_0 p$, where S_r and S_0 are the real and nominal contact areas, respectively.^{2,4} At the maximum load $F=4.2$ N, $S_r/S_0 \approx 0.1$ at $r=0$. Using the measured Si_3N_4 rms roughness $\sigma_i=13$ nm and rms surface slope 0.2 rad, we estimate a corresponding contact clearance $u \sim 15$ nm, with an average asperity contact radius $R_a \sim 60$ nm at a density $N_a \sim 10$ μm^{-2} .³¹ This order of magnitude for u demonstrates that picosecond ultrasonics is exquisitely sensitive to the closing of nanoscale gaps between solids.

D. Interpretation of the results for acoustic reflection coefficient

Precise modeling of $|r_{fi}|$ from contacts is complicated by the broadband strain pulse. At very low frequencies, it is

common to assume the presence of a thin interlayer of thickness l , density ρ , and longitudinal sound velocity v , or a contact stiffness per unit area $K=\rho v^2/l$.^{7,32-35} For plastic deformation of asperities, each of Hertz stiffness $2E^*R_a$,^{1,6} $K=2E^*R_a N_a \leq 0.2$ GPa nm⁻¹. This implies a reduced $|r_{fi}|$ for $f \lesssim K/(2\pi Z_f) = 0.7$ GHz ($\Lambda \gtrsim 10$ μm). However, this results in a negligible change in $|r_{fi}|$, inconsistent with the observed $\sim 25\%$ reduction at $F=4.2$ N. Since wavelengths $\Lambda \gtrsim 70$ nm $\sim R_a$ are present at the f - i interface, this model should be replaced by a theory of acoustic scattering from nanoscale contacts.

To this end, consider the diffraction of a strain pulse, of radial dependence $\eta_1 \propto \exp(-r^2/w_1^2)$ governed by the pump spot of radius w_1 , generated at the f - s interface. The z and t dependences in η_1 are implicit here. This pulse reaches the f - i interface in the near field without lateral spreading since the Cr thickness satisfies the relation $h \ll w_1^2/\Lambda$. Provided $R_a \gtrsim \Lambda/2\pi$, reasonable only at frequencies $f \gtrsim 20$ GHz, each contacting asperity can be approximated to have a reflection coefficient $|r_{fi}^{\text{th}}|=0.17$, assuming negligible mode conversion.³⁶ We define a corresponding normalized top-hat function $T(\mathbf{r}-\mathbf{d}_i)$, where \mathbf{r} and \mathbf{d}_i are, respectively, the in-plane position vector and that of the i th asperity. The reflected field $\eta_2(\mathbf{r})$ at the f - i interface is then

$$\eta_2(\mathbf{r}) = \eta_1(\mathbf{r}) - (1 - |r_{fi}^{\text{th}}|) \sum_i T(\mathbf{r} - \mathbf{d}_i) \eta_1(\mathbf{d}_i). \quad (6)$$

Applying Babinet's principle to the diffraction of this discontinuous source—analogue to a holey cheese—over the propagation length h and positing randomly distributed asperities over the probe spot of radius w_2 , we get the following simple result based on relative areas:

$$|r_{fi}| = 1 - (1 - |r_{fi}^{\text{th}}|) \pi R_a^2 N_a, \quad (7)$$

where $h \ll w_2^2/\Lambda$. Using $\pi R_a^2 N_a = S_r/S_0$, this implies

$$|r_{fi}(r=0)| = 1 - (1 - |r_{fi}^{\text{th}}|) p_0/H. \quad (8)$$

However, even using extrapolation to $f=0$ only leads to an 8% drop in $|r_{fi}|$ at $F=4.2$ N. So this model of acoustic diffraction only partially explains our finding of a $\sim 25\%$ reduction in $|r_{fi}|$ at this load. An additional mechanism for enhanced acoustic transmission or scattering should therefore be sought.

The above model is limited to high frequencies but also in that it ignores the asperity vibrational eigenmodes.^{37,38} Even for frequencies well below their longitudinal resonance $\sim v_i/(2u) \sim 300$ GHz, enhanced transmission and echo distortion can result when the lateral mode structure and the contribution of evanescent waves to r_{fi} are considered. The required numerical analysis of this process is beyond the scope of this paper. It is clear, however, that our experimental approach is apt for probing the physics of acoustic diffraction from and resonance in nanoasperities.

IV. RESULTS FOR THE THERMAL EXPERIMENTS

A. Thermal profiles of the contact

To obtain contact profiles based mainly on thermal waves with diffusion lengths $\mu_n = (2\kappa_n/C_n\omega)^{1/2} \approx 3$ μm , we make

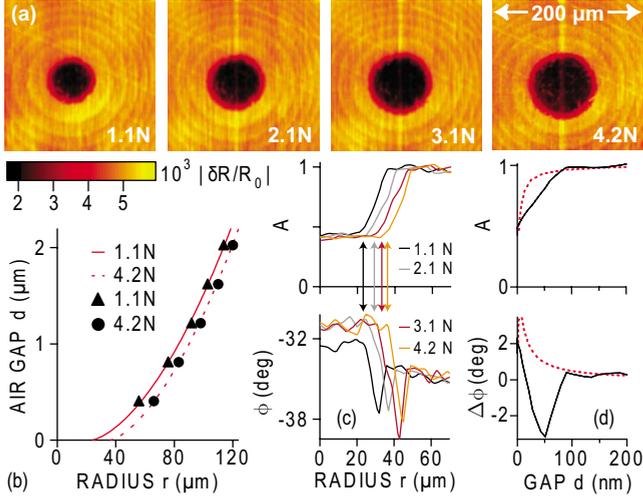


FIG. 3. (Color online) (a) $|\delta R/R_0|$ images of the contact. (b) Measured air gap (▲, ●) and Hertz theory (lines) for two loads. (c) Normalized amplitude and phase for $t = -10$ ps. Arrows: contact radii. (d) Normalized amplitude and phase difference for 1.1 N and 3D thermal-diffusion theory (dashed lines).

radial scans of $|\delta R/R_0|$ at $t = -10$ ps to avoid acoustic effects. The probed temperature variation is $A \sin(\omega t + \phi)$, where $\sin \omega t$ is in phase with the chopping at 1.1 MHz and ϕ is the phase lead recorded by the lock-in amplifier. $|\delta R/R_0| \propto A$ [~ 70 K (Ref. 17)], normalized with respect to its out-of-contact value, and phase lead ϕ are plotted vs r in Fig. 3(c). The contact radius, determined from the initial rise in A or decrease in ϕ [arrows in Fig. 3(c)], agrees with Hertz theory. At larger r , A saturates, whereas ϕ shows a sharp minimum. Both remain constant over the contact area for $F \geq 1.1$ N.

Confirmation of these results in two spatial dimensions is shown for $|\delta R/R_0|$ in Fig. 3(a) for a $200 \times 200 \mu\text{m}^2$ region scanned in $1\text{-}\mu\text{m}$ steps.³⁹ We resolve the circular contact area as well as low-contrast Newton's rings.⁵ These arise from variations in pump-light absorption on residual transmission to the f - i air gap.¹⁹ The derived air gap agrees with Hertz theory [see Fig. 3(b)].

B. Interpretation of the thermal profiles

The three-dimensional (3D) thermal-diffusion equation was solved for a sinusoidal spatially Gaussian heat source (of radius $w = 2.2 \mu\text{m}$) at the f - s interface with an air gap d below a flat and parallel (in practice to $< 1^\circ$) Si_3N_4 surface. The effect of the periodic laser-pulse trains when probing at the chopping frequency was also included using a sum arising from harmonics of the 80 MHz repetition rate.⁴⁰ Harmonics up to order ~ 2000 (corresponding to ~ 160 GHz thermal waves) give a non-negligible contribution here, but only those with frequencies ≤ 1 GHz ($\mu_n \geq h$) probe the f - i interface.

The predictions for $A(d)$ and $\phi(d)$ are compared to experiment on a normalized scale in Fig. 3(d), assuming literature values of thermal properties.^{15,41} Thermal-boundary resistances $R_{fs} = 1.3 \times 10^{-7}$ and $R_{fi} = 1.0 \times 10^{-7}$ $\text{K m}^2 \text{W}^{-1}$ at the

f - s and f - i interfaces (the latter for $d = 0$ only) are determined by matching the contrast in A and the difference $\Delta\phi$ in and out of contact.⁴² Standard models⁴³ based on acoustic mismatch, constriction, and electron-phonon resistances give values of a similar order. However, in experiment $\phi(d)$ shows a minimum.⁴⁴ $A(d)$ also varies more slowly;⁴⁵ this points to enhanced heat transport through the gap for $d \leq 50$ nm. At 293 K and 1 atm, the molecular mean-free path and the Knudsen number are $L = 60$ nm and $\text{Kn} = L/d > 0.6$ (for $d < 100$ nm).⁴⁶ For this “near-continuum” regime, ballistic heat transport competes strongly with diffusion. The ratio of the thermal conductances in the diffusive ($K_d = \kappa_a/d$) (Ref. 41) and near-continuum (K_{nc}) regimes is

$$\frac{K_d}{K_{nc}} = 1 + \frac{4\gamma}{\gamma + 1} \frac{\alpha_f + \alpha_i - \alpha_f \alpha_i \text{Kn}}{\alpha_f \alpha_i \text{Pr}}, \quad (9)$$

with $\gamma = 7/5$ for a diatomic gas and $\text{Pr} = 0.72$ the Prandtl number in air.^{2,46} α_f and α_i are the film and indenter accommodation coefficients (< 1). Gap heat transport should therefore be overestimated ($K_d/K_{nc} \geq 3$) (Ref. 47), so kinetic theory fails to explain the anomaly in A . Another possibility is near-field thermal radiation.⁴⁸ But to account for our results would require a $K_d/4\sigma_B T^3 \sim 10^5$ enhancement compared to the blackbody value, where σ_B is the Stefan-Boltzmann constant, an implausible factor for dissimilar materials. Although Hertz theory explains the acoustically determined contact radius a , it may be that surface roughness plays a role in explaining the anomalies. The roughness parameter $\alpha \sim 0.05$ implies some contact even at radii $1.3a$.¹ Compared to the coherent acoustic phonons, the efficient transmission of the much shorter wavelength incoherent thermal phonons through the asperities should therefore broaden the thermal-wave-probed contact area. However, the anomalies in amplitude and phase occur at a gap thickness of ~ 50 nm, a value that is seemingly too large to be accounted for by the smaller rms surface roughnesses of the contacting Cr and Si_3N_4 . A theory accounting for the detailed geometry of the asperity penetration into the gap, an intermediate region in which asperities and air coexist, is required. To elucidate the thermal anomalies we observe, measurements with different indenters in evacuated chambers should be carried out to reveal the physics of asperity deformation and thermal transport through the nanowire-like connections that connect the contacting bodies.

V. CONCLUSION

In conclusion, we demonstrate that nanoscale acoustic waves excited with ultrashort optical pulses show enhanced coherent phonon transport between or enhanced scattering from solids in mechanical contact. In addition, we demonstrate that optically excited microscale thermal waves show enhanced incoherent phonon transport across the gap between solids under near-contact conditions. These findings should be investigated in the future by experiments on different contacting materials, on a range of surface roughnesses, and with a variety of gases or a vacuum in the contact region. In addition, further measurements using coated

transparent indenters with the pump and probe light incident on opposite sides of the interface will allow phonon transmission to be monitored. Accessing nanometer indentation with high-frequency phonons also opens the way to mapping

deformation or plastic flow in a wide variety of materials—whether metallic, semiconductor, or dielectric—and to direct probing of the effects of wear and friction in nanomechanical systems.

*assp@kino-ap.eng.hokudai.ac.jp

- ¹K. L. Johnson, *Contact Mechanics* (Cambridge University Press, Cambridge, 1985).
- ²C. V. Madhusudana, *Thermal Contact Conductance* (Springer, New York, 1996).
- ³M. V. Swain, *Mater. Sci. Eng., A* **253**, 160 (1998).
- ⁴P. W. O’Callaghan and S. D. Probert, *Wear* **29**, 120 (1987).
- ⁵A. Ovcharenko, G. Halperin, G. Verberne, and I. Etsion, *Tribol. Lett.* **25**, 153 (2007).
- ⁶K. Kendall and D. Tabor, *Proc. R. Soc. London, Ser. A* **323**, 321 (1971).
- ⁷B. W. Drinkwater, R. S. Dwyer-Joyce, and P. Cawley, *Proc. R. Soc. London, Ser. A* **452**, 2613 (1996).
- ⁸Y. Ohson, G. Wu, J. Dryden, F. Zok, and A. Majumdar, *ASME J. Heat Transfer* **121**, 954 (1999).
- ⁹M. S. Bobji, J. B. Pethica, and B. J. Inkson, *J. Mater. Res.* **20**, 2726 (2005).
- ¹⁰From Toshiba Materials Co. datasheet (2008).
- ¹¹The respective rms surface slopes are 4°, 11°, and 1°.
- ¹²C. Thomsen, H. T. Grahn, H. J. Maris, and J. Tauc, *Phys. Rev. B* **34**, 4129 (1986).
- ¹³O. B. Wright and K. Kawashima, *Phys. Rev. Lett.* **69**, 1668 (1992).
- ¹⁴T. Saito, O. Matsuda, and O. B. Wright, *Phys. Rev. B* **67**, 205421 (2003).
- ¹⁵ $\rho_i=3.2$, $\rho_f=7.2$, and $\rho_s=4.0$ g cm⁻³; $\nu_i=0.29$, $\nu_f=0.21$, and $\nu_s=0.23$; $E_i=320$, $E_f=280$, and $E_s=440$ GPa; $\nu_i=10.6$, $\nu_f=6.62$, and $\nu_s=11.1$ km s⁻¹; $\kappa_i=28$, $\kappa_f=14$, and $\kappa_s=45$ W m⁻¹ K⁻¹; $C_i=2.1 \times 10^6$, $C_f=3.2 \times 10^6$, and $C_s=3.4 \times 10^6$ J m⁻³ K⁻¹ (taken at 300 K). κ_f is 1/7 of the single-crystal value. See Refs. **10**, **14**, **22**, **49**, and **50**.
- ¹⁶In the contact region, R_0 increases by ~5%.
- ¹⁷S. Kashiwada, O. Matsuda, J. J. Baumberg, R. Li Voti, and O. B. Wright, *J. Appl. Phys.* **100**, 073506 (2006).
- ¹⁸O. B. Wright and T. Hyoguchi, *Opt. Lett.* **16**, 1529 (1991).
- ¹⁹Refractive indices of Cr 2.6+2.6i at 405 nm and 3.8+2.0i at 810 nm were measured by ellipsometry.
- ²⁰O. B. Wright, *Opt. Lett.* **20**, 632 (1995).
- ²¹D. Lide, *CRC Handbook of Chemistry and Physics* (CRC, Boca Raton, 1999).
- ²²O. L. Anderson, in *Physical Acoustics*, edited by W. P. Mason (Academic, New York, 1965), Vol. 3B, pp. 43–95.
- ²³The amplitude decreases by $1/e^2$ over this range of f .
- ²⁴O. Matsuda and O. B. Wright, *J. Opt. Soc. Am. B* **19**, 3028 (2002).
- ²⁵Echo smoothing $\propto \exp[-2(\pi f \delta h / v_f)^2]$ by reflection from nm rms variations δh in h is negligible. See S. A. Akhmanov and V. E. Gusev, *Sov. Phys. Usp.* **35**, 153 (1992).
- ²⁶H. Y. Yu, S. C. Sanday, and B. B. Rath, *J. Mech. Phys. Solids* **38**, 745 (1990).
- ²⁷The variation in v_f with pressure is negligible here.
- ²⁸M. J. Jaffar, *Proc. Inst. Mech. Eng., Part C: J. Mech. Eng. Sci.* **211**, 549 (1997).
- ²⁹B. Jönsson and S. Hogmark, *Thin Solid Films* **114**, 257 (1984).
- ³⁰J. A. Greenwood and J. B. P. Williamson, *Proc. R. Soc. London, Ser. A* **295**, 300 (1966).
- ³¹Y. Kimura, *Wear* **15**, 47 (1970).
- ³²J.-Y. Kim, A. Baltazar, and S. I. Rokhlin, *J. Mech. Phys. Solids* **52**, 1911 (2004).
- ³³A. I. Lavrentyev and S. I. Rokhlin, *J. Acoust. Soc. Am.* **103**, 657 (1998).
- ³⁴J. M. Baik and R. B. Thompson, *J. Nondestruct. Eval.* **4**, 177 (1984).
- ³⁵Such theories have also been applied in picosecond ultrasonics to ultrathin layers. See, Ref. **13** or G. Tas, J. J. Loomis, H. J. Maris, A. A. Bailes, and L. E. Seiberling, *Appl. Phys. Lett.* **72**, 2235 (1998).
- ³⁶Conversion to shear is negligible. See, e.g., Y. C. Angel and J. D. Achenbach, *ASME J. Appl. Mech.* **52**, 33 (1985).
- ³⁷J. Christensen, L. Martin-Moreno, and F. J. Garcia-Vidal, *Phys. Rev. Lett.* **101**, 014301 (2008).
- ³⁸Acoustic transmission at ~50 GHz only occurs for air gaps <0.1 pm (see Ref. **7**). Intermittent contact at our acoustic displacements ~0.1 nm has negligible influence as does a ~2 nm water layer under our conditions of 35% humidity. See J. Israelachvili, *Intermolecular and Surface Forces* (Academic, London, 1985).
- ³⁹This data was taken at $t=40$ ps. The contrast at this time is mainly determined by the temperature changes.
- ⁴⁰See A. J. Schmidt, X. Chen, and G. Chen, *Rev. Sci. Instrum.* **79**, 114902 (2008). Harmonics contribute <40% to normalized A and a shift of <4° in ϕ .
- ⁴¹For air at 300 K, $\rho_a=1.01$ kg m⁻³, $\kappa_a=0.026$ W m⁻¹ K⁻¹, and $C_a=1.02 \times 10^3$ J m⁻³ K⁻¹ (see Ref. **21**).
- ⁴²Reduction in R_{fi} leads to similar results, consistent with the observed saturation in A and ϕ for $F \geq 1.1$ N.
- ⁴³R. S. Prasher and P. E. Phelan, *J. Appl. Phys.* **100**, 063538 (2006).
- ⁴⁴The predicted ϕ in and out of contact are -14.4° and -17.9°.
- ⁴⁵Preliminary measurements of $A(d)$ for an $h=215$ nm and $\sigma_f=7$ nm film [T. Dehoux, R. Li Voti, and O. B. Wright (unpublished)] showed similar trends.
- ⁴⁶E. H. Kennard, *Kinetic Theory of Gases* (McGraw-Hill, New York, 1938).
- ⁴⁷P. M. Patel, D. P. Almond, and H. Reiter, *Appl. Phys. B: Lasers Opt.* **43**, 9 (1987).
- ⁴⁸J.-P. Mulet, K. J. Joulain, R. Carminati, and J.-J. Greffet, *Microscale Thermophys. Eng.* **6**, 209 (2002).
- ⁴⁹W. C. Oliver and G. M. Pharr, *J. Mater. Res.* **7**, 1564 (1992).
- ⁵⁰M. Tomoda, O. B. Wright, and R. Li Voti, *Appl. Phys. Lett.* **91**, 071911 (2007).