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Breaking of unsteady lee waves generated by diurnal tides

T. Nakamura,1 Y. Isoda,2 H. Mitsudera,1 S. Takagi,3 and M. Nagasawa4

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[1] Diapycnal mixing caused through breaking of large-amplitude internal lee waves generated by sub-inertial diurnal tides, which are modulated with a 18.6-year period, is hypothesized to be fundamental to both the intermediate-layer ventilation and the bi-decadal oscillation around the North Pacific Ocean. The first observational evidence of such wave breaking is presented here. The breaking wave observed had ~200 m height and ~1 km width, and its associated diapycnal mixing was estimated to be ~1.5 m² s⁻¹, with a temporal average ~10⁷ times larger than typical values in the open oceans. Our estimate suggests that a similar mixing process occurs globally, particularly around the Pacific and Antarctic Oceans. Citation: Nakamura, T., Y. Isoda, H. Mitsudera, S. Takagi, and M. Nagasawa (2010), Breaking of unsteady lee waves generated by diurnal tides, Geophys. Res. Lett., 37, L04602, doi:10.1029/2009GL041456.

1. Introduction

[2] Diapycnal mixing induced by oceanic internal waves is a driving force of the global thermohaline and material circulations and affects the climate. A major energy source of internal waves is tides. Diurnal tides, however, have been paid much less attention than semidiurnal tides in terms of diapycnal mixing. This may be because semidiurnal tides are dominant in most regions, and because diurnal tides are subinertial at latitudes higher than ≈30°, and hence diurnal internal tides cannot be internal waves. Nevertheless, subinertial diurnal tides are also important around the North Pacific rim and the Antarctic Ocean. In these regions, nearly half of the kinetic energy of barotropic diurnal tides is concentrated [Egbert and Ray, 2003], and diurnal tidal currents often dominate the local current field through resonant generation of topographically trapped waves [e.g., Chapman, 1989]. Also, with high current speed, subinertial diurnal tides can generate unsteady lee waves, which can have an intrinsic frequency higher than the local inertial frequency and hence can be internal waves [Nakamura et al., 2000].

[3] In particular, numerical studies suggested that diurnal tides cause strong diapycnal mixing through the generation and breaking of large-amplitude unsteady lee waves in the Kuril Straits, located between the North Pacific and the Okhotsk Sea (Figure 1a), and that this mixing enhances the ventilation of the North Pacific intermediate layer through the following process [Nakamura et al., 2004]. First, the diapycnal mixing in the Kuril Straits causes both direct water-mass modification in the Straits and strengthened convection in the Okhotsk Sea—i.e., saline subsurface water brought up to the surface by mixing is subsequently transported by the wind-driven gyre to the northern part of the Sea, where the resulting salt flux increases the density of the Dense Shelf Water, which is produced as a result of cooling and sea-ice formation in winter and is the major source of North Pacific Intermediate Water. Second, the effects of tidal mixing are spread by a dynamical adjustment through coastally trapped waves and Rossby waves and by advective transport of heat, salt, and materials, leading to modification of the circulation and water mass properties in the North Pacific.

[4] Another reason why diapycnal mixing caused by diurnal tides is of interest is that the 18.6-year nodal cycle significantly modulates diurnal lunar tidal forces (K₁, ±14%; O₁, ±19%) [e.g., Ray, 2007]. The associated modulation of the barotropic tidal currents is expected to modulate the amplitude of lee waves generated, thus leading to the 18.6-year variation in the resulting mixing. Because the modulation of semidiurnal lunar tidal forces is smaller (M₂, ±4%), the effects of the 18.6-year cycle occur more significantly in regions where diurnal tides are dominant. In particular, a combination of recent studies suggests the hypothesis that the mixing due to diurnal tides in the Kuril Straits could induce 18.6-year oscillations, which are found both in the ocean and the atmosphere around the North Pacific [e.g., Wilson et al., 2007], through the following process: (1) the modulation in the mixing strength causes the 18.6-year variation in the tidally enhanced ventilation process described above [Yasuda et al., 2006], (2) the coastally trapped waves generated through this process reach the equator and vary the subsurface temperature there, thus regulating El Niño Southern Oscillation [Hasumi et al., 2008], and (3) atmospheric teleconnections, such as the Pacific North American pattern, spread its influence [McKinnell and Crawford, 2007].

[5] Previous observations have found breaking events of internal waves caused by semidiurnal tides in fjords [e.g., Farmer and Freeland, 1983], off Hawaii [Klymak et al., 2008], and off Oregon [Nash et al., 2007], as well as density inversion associated with hydraulic jumps in the Strait of Gibraltar [e.g., Wesson and Gregg, 1994]. However, large-amplitude unsteady lee waves generated by diurnal tides and their breaking—i.e., a major mixing mechanism for subinertial diurnal tides—have not been observed in the real ocean.

[6] To look for evidence of such wave generation and breaking, observations were conducted in the Amchitka Pass, the Aleutian arc (Figure 1), where the dynamical conditions for tidally generated internal waves are similar to those in the Kuril Straits: Diurnal tides are subinertial and
dominant (Figures 1c and 1d); a ridge of ~10 km width and 
~35 km length is present (Figure 1b); and the density 
stratification is similar in the sense that both areas are in 
the subarctic Pacific. In addition, mixing in the Amchitka Pass 
might affect the ventilation and variability around the 
Bering Sea and the North Pacific, as is similar to mixing in the 
Kuril Straits. The Pass allows a significant water exchange 
between the two basins [Stabeno et al., 1999], which would 
spread the effects of mixing, and the energy flux of baro-
tropic tides through the Pass has been estimated to increase 
by 36% due to the 18.6-year cycle [Foreman et al., 2006].
Motivated by the observational results obtained, we then 
made a global estimate of the occurrence of a similar process 
due to the $K_1$ tide.

2. Observation

[9] According to numerical experiments [Nakamura et al., 
2000], breaking of unsteady lee waves tends to occur around 
the time when the barotropic tidal flow in the cross-ridge 
direction ceases. To estimate the time of zero cross-ridge 
flow, we first measured currents in the cross-ridge (i.e., 
meridional) section shown in Figure 1b six times, and in 
three of these measurements (indicated by i–iii in Figure 1e), 
the vertical sections of temperature and salinity were also 
measured. The results suggested that cross-ridge barotropic 
flow over the top of the ridge stops near the time of high/low 
water. Extensive observations were thus conducted around 
the time of high water (indicated by iv in Figure 1e). As it 
turned out, the cross-ridge barotropic flow was well corre-
lated with a tidal model prediction (TPXO7.1 [Egbert and 
Erofeeva, 2002]) and agreed well after fitting (Figure 1e), 
indicating the dominance of tidal currents.

[8] The measurements were conducted using a ship-board 
acoustic Doppler current profiler (ADCP, Furuno Electric 
CI-3500AD), 44 expendable conductivity temperature 
depths (XCTDs, Tsurumi-Seiki XCTD-1), and 41 expend-
able bathythermographs (XBTs, Tsurumi-Seiki XBT-7). 
The ADCP has a nominal depth range of 10–706 m with a 
vertical resolution of 6 m. XCTD and XBT data was visu-
ally checked for spikes, low-pass filtered, corrected for the 
finite-time responses of the sensors and their mismatches,

and then averaged into 1-m bins. The XBT data was further 
calibrated and utilized to calculate potential temperature 
using the adjacent XCTD data. Errors associated with the 
latter calculation were within 0.001°C. To exclude spurious 
overturns resulting from observation errors, tests of vertical 
and density resolutions, run length, and water mass 
[Galbraith and Kelley, 1996] were carried out with revised 
criteria for run length tests [Johnson and Garrett, 2004] and 
water mass tests [Martin and Rudnick, 2004]. The main 
upturn discussed below cleared all the tests.

3. Breaking Wave

[9] The extensive observations captured a breaking wave 
having a height of ~200 m (Figure 2a) and causing inversion 
of the potential density ($\sigma_0$, hereafter referred to as density; 
Figure 2b). The horizontal scale of the major density in-
version reached ~1.5 km with a core width of ~500 m in the 
cross-ridge direction. Its density ranged from 26.48 to 26.71 
$\sigma_0$ (kg m $^{-3}$) in the meridional range of 51°34.75′– 
35.25′N. The breaking wave had various-scale structures and 
contained smaller-scale density inversions (Figures 2a and 
2b), indicating the occurrence of instability and associated 
energy transfer from the wave to turbulent motion.

[10] The time evolution of isopycnal surfaces suggests that 
the breaking wave was tidal in origin (Figure 3). After the 
barotropic current flowed southward (leftward in Figure 3), 
isopycnal surfaces were lifted over the northern slope of the 
ridge and depressed over the southern slope (Figure 3a). As 
the barotropic current changed direction and flowed north-
ward, isopycnal surfaces began to rise on the southern side 
and to descend on the northern side (Figure 3b). A large-
amplitude elevation appeared over the ridge top as water 
(or the crest of the wave generated by the southward flow) 
crossed the ridge (Figure 3c). When the northward barotropic 
flow nearly ceased, internal waves generated during the 
 nordthward flow grew (Figure 3d), resulting in the wave 
breaking shown in Figure 2. Similar wave generation was 
also seen over a small peak at 51°37.5′N and over a lower 
peak at 51°40.5′N (Figure 3e).

[11] The breaking wave had a characteristic feature of lee 
waves, that is, co-phase lines slanted to the upstream side

Figure 1. Locations and times of observations. Topographic maps showing (a) the location of the Amchitka Pass and 
(b) the observation sites in the Pass. Tidal height (TPXO7.1) in the Amchitka Pass during (c) 2008, (d) June 2008, and 
(e) around 16 June 2008 (UTC). Figure 1e also shows the durations of XCTD/XBT observations (shaded areas), vertically-
averaged cross-ridge flow observed over the ridge top (crosses), and northward tidal velocity (dashed line) predicted based on 
TPXO7.1, which was lagged by ~1.35 hours, amplified 1.94 times, and had a mean value of 0.055 m s $^{-1}$ added.


Figure 2. Breaking internal wave seen in the extensive observations (iv in Figure 1e). (a) Cross-ridge section of potential temperature and the XCTD (○) and XBT (+) sites. White areas represent the bottom or missing data. The observations took 38 min for this whole section and 14 min for the main part of the wave (34.75°–35.5°N), during which the wave may have moved 0.2 km or less. The potential temperature behaves almost as a passive tracer in this area below the seasonal thermocline, where the density stratification is determined mostly by salinity. It was nevertheless correlated with density, except for the alternating layers located 100–300 m deep on the left hand side of the ridge top, which did not show associated density inversions of this vertical scale. (b) Vertical profile of potential density ($\sigma_\theta$) at 51°35′N. (c) Cross-ridge (northward) baroclinic currents (the deviation from the vertically averaged flow over the ridge top) and the horizontal resolution of the temporally averaged ADCP data (▽). Selected isotherms are superimposed.

(i.e., south), as seen in both current and density fields (Figures 2c and 3d). In fact, the ratio of the Doppler shift (or lee wave frequency) to tidal frequency ($kU/\omega$) was estimated to be 11, suggesting that the wave was an unsteady lee wave [Nakamura et al., 2000], where $U$, $\omega$, and $k$ are barotropic tidal flow speed, tidal frequency, and horizontal wavenumber estimated from Figure 2. Also, the intrinsic frequency estimated from the dispersion relation ($8 \times 10^{-4} \text{ rad s}^{-1}$) roughly agreed with the lee wave frequency ($kU = 7.9 \times 10^{-4} \text{ rad s}^{-1}$). Actually, the observed time evolution had similarities to those of unsteady lee waves seen in numerical experiments [Nakamura et al., 2000]. In addition, the inverse Froude number ($N^2/\Omega U$) and the wave Froude number ($U/ND$) were estimated to be 3 and 0.2, respectively, where $N$ is the depth average of buoyancy frequency, and $D$ is the water depth at the ridge top, and wave height, $\eta$, was used instead of topographic height because the tidal excursion is finite. The two estimated numbers suggest that the wave generating force was strong enough for the wave to break but that the flow was not hydraulically controlled [e.g., Baines, 1995]. All of these indicate that the breaking wave was an unsteady lee wave generated by tides.

[12] Diapycnal mixing associated with the main overturn at 51°35.0′N (Figure 2) was estimated by two approaches. One is the Thorpe scale method [e.g., Thorpe, 2005]. The turbulence dissipation rate was estimated as $c N^2 L_T^2$, where $c \sim 1$, $N_i$ is the mean sorted buoyancy frequency, and $L_T$ is the Thorpe scale. The diapycnal diffusivity coefficient, $\kappa_{\rho}$, was then estimated as $\kappa_{\rho} = \gamma c N_i^2$, where the conventional value of $\gamma$ is 0.2. This approach yields $\kappa_{\rho}$ of 1.5 m$^2$ s$^{-1}$ with calculated values of $L_T$ (60 m), $N_i$ (0.0021 rad s$^{-1}$), and $c$ (3.1 $\times$ 10$^{-5}$ W kg$^{-1}$). The other approach assumed that the statically unstable region will be vertically mixed, following past numerical experiments [e.g., Scinocca and Peltier, 1993]. Equating the resulting density flux to a vertical diffusive flux, $\kappa_{\rho} \rho_i \partial \sigma_i / \partial z$ where $\rho_i$ is sorted density, we obtain a vertical diffusivity coefficient, $\kappa_{\rho}$, that almost corresponds to $\kappa_{\rho}$. Here, the density flux was estimated as the density transport divided by the time required for mixing.

![Figure 3. (a–d) Temporal evolution of potential density surfaces. The observation times of Figures 3a, 3b, 3c, and 3d are shown by shaded areas numbered i, ii, iii, and iv in Figure 1e, respectively. Arrows show the direction of barotropic cross-ridge flow at the ridge top. (e) The measured bottom topography.](image-url)
vector, \( \mathbf{k} \), was estimated from the horizontal scale of the vertical velocity amplitude \( \left( W_o = - \mathbf{U}_0 \cdot \nabla \mathbf{D}, \text{where } D \text{ is depth} \right) \). Note that lee wave generation is likely to be underestimated particularly in areas of weak tidal currents, because of the horizontal resolution \( (1' \times 1') \) of the topographic data used (ETOPO1 [Amante and Eakins, 2008]). For \( \left| \mathbf{U}_0 \right| \sim 0.01 \text{ m s}^{-1} \), the condition \( \mathbf{k} \cdot \mathbf{U}_0 / \omega \gtrsim 1 \) requires a topographic length scale of less than 1 km, which is hardly resolved because 1' in latitude is 1.852 km.

[15] The global map suggests that lee waves are expected in other regions along the Aleutian and Kuril Islands, and also around the Antarctic and Pacific Oceans. The generation condition is also met in the Indian Ocean, the Indonesian Seas, the northwest of Canada, and around the Caribbean and Svalbard Islands.

[16] As a rough measure of the significance of the lee wave process, an upper limit of the wave height of tidally generated lee waves \( (\eta_{\text{max}}) \) was estimated together with the Froude number \( (\left| \mathbf{U}_0 \right| / \mathbf{N} D) \). The upper limit was estimated as the minimum of the vertical excursion of barotropic tidal flow estimated at a fixed point \( (2W_o / \omega, D, \mathbf{A}) \) in a Boussinesq fluid; and (2) the wave height of internal waves should be less than or comparable to \( \lambda \omega / 2 \), as long as the wave ray slope is small and the horizontal scale of the density inversion is smaller than the horizontal wavelength. Here, \( \lambda \) was approximated as the vertical wavelength of hydrostatic lee waves \( (2\pi(\mathbf{k} \cdot \mathbf{U}_0 / |\mathbf{k}| / N \lambda)) \). \( \mathbf{A} \) was estimated together with the topographic mean slope \( (\mathbf{H} - \mathbf{H}_0) \), where the overbar denotes the horizontal average and \( \mathbf{H} \) is horizontal displacement). The calculations for \( \mathbf{A} \) and \( \mathbf{H} \) were performed within the distance of the local horizontal tidal excursion from each point.

[17] Estimated values of \( \eta_{\text{max}} \) exceed 100 m along the Aleutian and Kuril Islands, and around the Pacific and Antarctic Oceans, particularly around the Ross and Weddell Seas. The distribution is similar to that of \( \mathbf{k} \cdot \mathbf{U}_0 / \omega \), but is more concentrated in areas of a sharp change in depth, such as shelf breaks, ridges, and seamounts. The distribution of the Froude number is quite similar to that of \( \eta_{\text{max}} \). In regions of strong tidal currents (e.g., the Kuril and Aleutian Islands), areas having large \( \eta_{\text{max}} \) are interwoven with areas where the jump condition is met \( (\left| \mathbf{U}_0 \right| / \mathbf{N} D > 1/\omega) \). Vigorous mixing might be caused in such areas by the \( K_1 \) tide, though estimation of the mixing strength needs future work.

[18] In contrast to the \( K_1 \) case, \( \eta_{\text{max}} \) for the \( M_2 \) tide, the largest semiidiurnal constituent, is insignificant around the Antarctic, except for the Weddell Sea, but is significant in the Atlantic Ocean, according to the map of \( W_o \) calculated by Legg and Klymak [2008].

4. Global Distribution

[14] Figure 4a shows values of \( \mathbf{k} \cdot \mathbf{U}_0 / \omega \) estimated for the largest diurnal constituent, the \( K_1 \) tide, where lee wave generation is expected when \( \mathbf{k} \cdot \mathbf{U}_0 / \omega \gtrsim 1 \) and \( N \lambda \gtrsim 1 \). \( \mathbf{U}_0 \) is the amplitude vector of horizontal, barotropic tidal velocity, \( \omega \) is the corresponding tidal frequency, and \( N \lambda \) is buoyancy frequency averaged from the bottom in one vertical wavelength of hydrostatic lee waves \( (2\pi(\mathbf{k} \cdot \mathbf{U}_0 / |\mathbf{k}|)/N \lambda) \) [e.g., Baines, 1995]. Horizontal wavenumber

Figure 4. (a) The condition for lee-wave generation \( (\mathbf{k} \cdot \mathbf{U}_0 / \omega) \), (b) maximum possible wave height \( (\eta_{\text{max}}) \), and (c) the condition for hydraulic jump \( (\left| \mathbf{U}_0 \right| \mathbf{N} / \mathbf{D}) \) for the \( K_1 \) tide. Here, \( \mathbf{k} \cdot \mathbf{U}_0 / \omega \) and \( \eta_{\text{max}} \) are set to zero, where \( N \lambda \leq 1 \). The calculation used ETOPO1 bathymetric data, TPXO7.1 tidal data, and density data \( (\sigma_0, \sigma_2, \sigma_4) \) of WOCE Global Hydrographic Climatology [Gouretski and Koltermann, 2004]. Abnormal values found in the last in some marginal seas were corrected. The calculation was conducted on \( 1' \times 1' \) grids and maximum values in \( 15^\circ \times 15^\circ \) boxes are shown.

where the density transport was calculated as the vertical integration of the magnitude of the difference between the density observed and the density that would be achieved by vertical mixing to a statically stable state. This approach gave \( k_c \) of 1.2 m$^2$ s$^{-1}$ when mixing occurred in the mean buoyancy period \( (2\pi / N \lambda) \) of 3000 s.

[13] Both approaches gave diffusivity \( \sim 10^4 \) times larger than typical values found in the open oceans. (The estimates yield a temporal average of 0.08 - 0.1 m$^2$ s$^{-1}$ if the mixing lasts for the buoyancy period and occurs twice a day, while observational estimates are \( \sim 0.1 \times 10^4 \) m$^2$ s$^{-1}$ away from topographic features or at latitudes higher than \( \sim 30^\circ \), for example, Gouretski et al., 2003; Hibiya et al., 2006.) The rough agreement of the two estimates together with the wide applicability of the Thorpe scale method [Wesson and Gregg, 1994] supports these estimates, though the estimates should have a margin of error.

4. Global Distribution

[14] Figure 4a shows values of \( \mathbf{k} \cdot \mathbf{U}_0 / \omega \) estimated for the largest diurnal constituent, the \( K_1 \) tide, where lee wave generation is expected when \( \mathbf{k} \cdot \mathbf{U}_0 / \omega \gtrsim 1 \) and \( N \lambda \gtrsim 1 \). \( \mathbf{U}_0 \) is the amplitude vector of horizontal, barotropic tidal velocity, \( \omega \) is the corresponding tidal frequency, and \( N \lambda \) is buoyancy frequency averaged from the bottom in one vertical wavelength of hydrostatic lee waves \( (2\pi(\mathbf{k} \cdot \mathbf{U}_0 / |\mathbf{k}|)/N \lambda) \) [e.g., Baines, 1995]. Horizontal wavenumber

5. Summary and Discussion

[19] This study showed evidence that subinertial tides are causing vigorous diapycnal mixing through the breaking of unsteady lee waves in the real ocean. This process is fundamental to the tidally enhanced ventilation and the tidally
induced bi-decadal oscillation around the North Pacific. We also made global maps of the areas where lee waves or hydraulic jumps are expected. These revealed further implications: (1) Mixing due to lee waves might be significant for a global estimate of diapycnal mixing because such areas are distributed globally. (2) Diurnal tides could affect the formation of the Antarctic Bottom Water (AABW) through the generation of lee waves or hydraulic jumps, which is expected around the Ross and Weddell Seas, two of the major sources of the AABW. (3) The 18.6-year variation could be significant in areas having a large Froude number or $r_{\max}$. (4) The combination of the last two suggests the possibility that the 18.6-year cycle could affect the formation of the AABW. A quantitative understanding of these possible effects could be obtained from a global estimate of diapycnal mixing caused by lee wave breaking (and jumps), although problems concerning nonlinearity of waves and tidal currents still remain, and higher resolution data of the topography, tides, and stratification are desired.

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M. Nagasawa, Department of Earth and Planetary Science, Graduate School of Science, University of Tokyo, Tokyo 113-0033, Japan.

T. Nakamura and H. Mitsudera, Institute of Low Temperature Science, Hokkaido University, Sapporo 060-0033, Japan. (nakamura@lowtem.hokudai.ac.jp)

Y. Isoda, Faculty of Fisheries, Hokkaido University, Hakodate 041-8611, Japan.

S. Takagi, School of Fisheries, Hokkaido University, Hakodate 041-8611, Japan.