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<td>Kawaguchi, Yuki; Saitoh, Kunimasa; Koshiba, Masanori</td>
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Analysis of Leakage Losses in One-Dimensional Photonic Crystal Coupled Resonator Optical Waveguide Using 3-D Finite Element Method

Yuki Kawaguchi, Student Member, IEEE, Kunimasu Saitoh, Member, IEEE, and Masanori Koshiba, Fellow, IEEE

Abstract—We have evaluated leakage losses of one-dimensional photonic crystal coupled resonator optical waveguides (1-D PC-CROW) by using three-dimensional finite element method (3-D FEM). We propose structure of 1-D PC-CROW with shifted position of air-hole, changed size of air-hole, and changed air-hole depth. We have also proposed air-bridge 1-D PC-CROW and evaluated group velocity and leakage losses of these CROWs. Our numerical results show that 1-D PC-CROW has large leakage losses, especially for vertical direction, and the proposed structure can reduce leakage losses. Leakage loss of 1-D PC-CROW with changed air-hole depth is two order of magnitude lower compared with normal structure.

Index Terms—Coupled resonator optical waveguides, finite element method, leakage loss, photonic crystals.

I. INTRODUCTION

COUPLED RESONATOR OPTICAL WAVEGUIDES (CROWs) are highly attractive for integrated delay lines [1]–[3] and nonlinear effects enhancement [4]. Especially, optical delay lines have emerged as key components for future optical networks and information processing systems. There is a wide range of applications of optical delay lines, such as optical buffers [5], optical regenerators [6], wavelength converters [7], and optical delay-line filters [8]. CROWs are attractive for these applications because of their specific small group velocity and zero group velocity dispersion (GVD) at the transmission mininband [9]–[19]. CROW can be classified in details by using three-dimensional finite element method (FEM) for periodic structure analysis [27].

The remainder of this paper is structured as follows. In Section 2, we describe a model and fundamental characteristics of 1-D PC-CROW. We show that leakage losses of the vertical direction is quite high and 3-D analysis is important to examine waveguide characteristics of 1-D PC-CROW. In Section 3, we characterize four types of 1-D PC-CROW to achieve low-loss structure, 1-D PC-CROW with shifted air-hole or changed air-hole size, air-bridge 1-D PC-CROW, and 1-D PC-CROW with shallow etched air-hole. In Section 4, findings in the numerical analysis are summarized.

II. STRUCTURE OF NORMAL 1-D PC-CROW

We consider a 1-D PC-CROW as shown in Fig. 1. We set structural parameters as follows. The lattice constant \( a \) of 1-D PC is 400 nm, the waveguide width \( w \) is 1,2\( a \) = 480 nm, the air hole radius \( r \) is 0.3\( a \) = 120 nm, the distance between air holes across the defect \( b \) is 2.5\( a \) = 1000 nm [26], and the waveguide height \( h \) is 0.5\( a \) = 200 nm. In this case, the intercavity distance \( \Delta \) becomes 5.5\( a \) = 2200 nm. We assume silicon, silica, and air as core, under cladding, and over cladding materials, respectively. We set the refractive index of 3.5 as silicon and 1.45 as silica.

In Figs. 2(a) and (b), we show the dispersion curve and the group velocity in 1-D CROW for quasi-TE mode calculated by 3-D FEM for periodic structure waveguides [27] with solid curves, where \( \lambda \) is the operating wavelength, \( \beta \) is the propagation constant along the propagation direction (\( z \) direction), \( v_g \) is the group velocity, and \( c \) is the velocity of light in vacuum. Here we give some details about numerical implementation. The analysis region is divided into linear tangential/quadratic normal...
III. DESIGN OF LOW-LOSS 1-D PC-CROW

A. 1-D PC-CROWs With Shifted Air-Holes

Next, we address to reducing the leakage losses in 1-D PC-CROW. If the reflection of the electromagnetic field is weakened at the cavity edge, the change of electromagnetic field becomes gentler and its envelope function gets close to Gaussian function. As a result, the tangential components of wavevector in the leaky region are reduced, leading to the suppression of leakage losses [26]. In order to weaken the reflection of the electromagnetic field at the cavity edge, we shift two air holes’ position neighboring cavities to outside as shown in Fig. 3(a), where the displacement of the air holes at the cavity edges is set as $S_i$. In Figs. 3(b), (c), and (d), we show dispersion curves, group velocity, and leakage losses, respectively, where $S_i$ is a variable parameters. By increasing the displacement of the air holes, dispersion curve shifts to lower frequency side and group velocity becomes large. As was expected, the leakage losses are reduced to 0.4 dB per period at the central wavelength, however, the suppression of the leakage losses is not enough.

B. 1-D PC-CROW With Changed Air-Hole-Size

As another approach to weaken electromagnetic field reflection at the cavity edges, we consider changing two air holes’ radius neighboring cavities $r$ to $r'$ as shown in Fig. 4(a). In Figs. 4(b), (c), and (d), we show dispersion curves, group velocity, and leakage losses, respectively, where the modified air-hole radius is set as $r' = 0.3a (= r), 0.25a$, and $0.2a$. As in the case of previous approach, the dispersion curve shifts to lower frequency side and group velocity becomes large by decreasing the air-hole radius. We can see that the leakage losses are reduced by adjusting two air holes’ radius neighboring cavities. Specifically, when we set $r' = 0.2a$, the leakage losses are reduced to about 0.2 dB per period at the central wavelength.
In this structure, calculated normalized group velocity $v_g/c$ is about 0.13.

C. Air-Bridge 1-D PC-CROW

We consider weakening the reflection of electromagnetic field at the cavity edge to reduce the leakage losses so far, however, they need to be decreased further for practical applications. For designing low-loss 1-D PC-CROW structure, we consider another approach for reducing leakage losses. We can expect that leakage losses for vertical direction are suppressed by making relative refractive index difference higher, therefore, next we evaluate leakage losses of air-bridge 1-D PC-CROW as shown in Fig. 5(a). Red curves in Figs. 5(b), (c), and (d) show dispersion curve, group velocity, and leakage loss, respectively, for the air-bridge structure ($r' = 0.3a$). We can see that the dispersion curve of air-bridge 1-D PC-CROW shifts to higher frequency region. And we can also see that the group velocity becomes smaller. This is because air-bridge structure can confine light stronger in the cavity than silica cladding CROW. Leakage loss is decreased to about 0.33 dB per period. This leakage loss can be further reduced by applying previously introduced technique. For example, we consider air-bridge 1-D PC-CROW with changed air-hole radius neighboring the cavities. In this case, we
set $r'$ as $0.2a$. Blue curves in Figs. 5(b), (c), and (d) show dispersion curve, group velocity, and leakage loss, respectively, for air-bridge 1-D PC-CROW with changed air-hole radius. We can see that the leakage loss is reduced to 0.023 dB per period and normalized group velocity is 0.105. Air-bridge 1-D PC-CROW can achieve small group velocity and low-loss characteristics simultaneously, however, we note that simplicity, which is advantage of 1-D PC-CROW, is lost in air-bridge 1-D PC-CROW because some additional fabrication processes are needed.
D. 1-D PC-CROW With Shallow Etched Air-Hole

The another method to reduce the leakage loss is weakening the refractive index modulation of CROW. It is expected that such structures can realize small leakage loss, however, group velocity becomes larger. If one assumes to apply CROW to pulse delay devices, leakage loss should be as small as possible even if group velocity is not small because delay time becomes longer by multiplying resonators. In order to weaken the refractive index modulation, we consider 1-D PC-CROW with shallow etched air-hole as shown in Fig. 6(a). We set air-hole depth as $h_{\text{hole}}$. Red and blue curves in Figs. 6(b), (c) and (d) show dispersion curves, group velocity, and leakage losses of 1-D PC-CROW for $r' = 0.3a$, respectively. Black curves show those of normal 1-D PC-CROW. We note that the air-hole radius are set as $r = r' = 0.3a$. We can see that by reducing the air-hole depth, the dispersion curve shifts to lower frequency region and the group velocity becomes larger. When we choose $h_{\text{hole}}$ as 0.25h, leakage loss is reduced to 0.07 dB per period. Next, in order to achieve much lower leakage loss structure, we set $r'$ as 0.2a. Red and blue curves in Figs. 6(e), (f) and
(g) show dispersion curves, group velocity, and leakage losses of 1-D PC-CROW for $h_{\text{hole}} = 0.5h$ and $0.25h$, respectively ($\nu' = 0.2\alpha$). If we set $\nu' = 0.2\alpha$ and $h_{\text{hole}} = 0.25h$, leakage loss can be reduced by 2 orders of magnitude lower compared with normal structure ($h_{\text{hole}} = h$ and $\nu' = r = 0.3\alpha$). However, we note that this structure has also problem in terms of simplicity in fabrication process as air-bridge structure.

IV. CONCLUSION

We have evaluated leakage losses of 1-D PC-CROW by using 3-D vector FEM for periodic structure analysis. We have shown that the leakage losses are quite high especially for vertical direction, however, it was shown that the leakage losses can be reduced by adjusting the air-hole position and radius neighboring cavities. We have also shown that the leakage losses are reduced from 0.5 dB per one period to 0.023 dB per one period by applying air-bridge structure to 1-D PC-CROW with changed air-hole radius. Moreover, we have proposed 1-D PC-CROW with shallow etched air-hole and shown that the leakage loss can be decreased by 2 orders of magnitude lower compared with normal structure. Since such structure’s modulation of refractive index is weak, group velocity becomes larger. Air-bridge 1-D PC-CROW or 1-D PC-CROW with shallow etched air-hole can achieve low-loss characteristics, however, additional fabrication processes may be needed. Therefore, designing small group velocity and low-loss 1-D PC-CROW with simple structure is next issue.

REFERENCES

Kunimasa Saitoh (S’00–M’01) was born in Hokkaido, Japan. He received the B.S., M.S., and Ph.D. degrees in electronic engineering from Hokkaido University, Sapporo, Japan, in 1997, 1999, and 2001, respectively. From 1999 to 2001, he was a Research Fellow of the Japan Society for the Promotion of Science. From 2001 to 2005, he was a Research Associate of Graduate School of Engineering at Hokkaido University. In 2005, he became an Associate Professor at Graduate School of Information Science and Technology, Hokkaido University. He has been engaged in research on fiber optics, nano-photonics, integrated optical devices, and computer-aided design and modeling of guided-wave devices using finite element method, beam propagation method, and so on. He is an author or coauthor of more than 100 research papers in refereed international journals.

Prof. Saitoh is a member of the Institute of Electronics, Information and Communication Engineers (IEICE) and the Optical Society of America (OSA). In 1999 and 2002, he was awarded the Excellent Paper Award and the Young Scientist Award from the IEICE, respectively, and in 2008, the Young Scientists’ Prize of the Commendation for Science and Technology from the Ministry of Education, Culture, Sports, Science, and Technology (MEXT), Government of Japan.

Masanori Koshiba (M’76–SM’87–F’03) was born in Sapporo, Japan. He received the B.S., M.S., and Ph.D. degrees in electronic engineering from Hokkaido University, Sapporo, Japan, in 1971, 1973, and 1976, respectively. In 1976, he joined the Department of Electronic Engineering, Kitami Institute of Technology, Kitami, Japan. From 1979 to 1987, he was an Associate Professor of Electronic Engineering at Hokkaido University, and in 1987, he became a Professor there. He has been engaged in research on wave electronics, including microwaves, millimeter-waves, lightwaves, surface acoustic waves (SAW), magnetostatic waves (MSW), and electron waves, and computer-aided design and modeling of guided-wave devices using finite element method, boundary element method, beam propagation method, and so on. He is an author or coauthor of more than 300 research papers in refereed international journals. He is an author of books Optical Waveguide Analysis (New York: McGraw-Hill, 1992) and Optical Waveguide Theory by the Finite Element Method (Tokyo, Japan: KTK Scientific/Dordrecht, The Netherlands: Kluwer Academic, 1992), and is a coauthor of the books Analysis Methods for Electromagnetic Wave Problems (Boston, MA: Artech House, 1990), Analysis Methods for Electromagnetic Wave Problems, Vol. Two (Boston, MA: Artech House, 1996), Ultrafast and Ultra-parallel Optoelectronics (Chichester, U.K.: Wiley, 1995), and Finite Element Software for Microwave Engineering (New York: Wiley, 1996).

Prof. Koshiba is a fellow of the Institute of Electronics, Information and Communication Engineers (IEICE), and is a member of the Institute of Electrical Engineers of Japan, and the Institute of Image Information and Television Engineers of Japan. In 1987, 1997, and 1999, he was awarded the Excellent Paper Awards from the IEICE, in 1998, the Electronics Award from the IEICE-Electronics Society, and in 2004, the Achievement Award from the IEICE. From 1999 to 2000, he served as a President of the IEICE-Electronics Society, and in 2002, he served as a Chair of the IEEE-LEOS (Lasers and Electro-Optics Society) Japan Chapter. Since 2009, he has served as a Vice-President of the IEICE and a Chair of the IEEE Sapporo Section.