The WB-SAR is estimated from the absorption power of investigate the same subject have been reported [9], [10].

Advancements in the side of theoretical estimations are being achieved steadily. On the other hand, some experiments to software tools or original program codes [5]–[9]. Thus, ad-numerical simulations have become possible through the use of precise estimations based upon realistic shaped and anatomical exposure situations might be complicated, more accurate and precise estimations based upon realistic shaped and anatomical human models are expected. Recently, high resolution numerical simulations have become possible through the use of advanced high-speed computers and 3-D EMF analysis software tools or original program codes [5]–[9]. Thus, advancements in the side of theoretical estimations are being achieved steadily. On the other hand, some experiments to investigate the same subject have been reported [9], [10]. The WB-SAR is estimated from the absorption power of the human body phantom model which is exposed to the plane-wave of known EMF strength in the anechoic chamber. For the absorption power measurements, 3-D scanning techniques using electric probes inserted into the phantom [10] or thermographic techniques [11] have been applied. One of the scanning techniques is widely used as an IEC standard system for the SAR measurement on hand-held devices. However, at microwave frequencies these techniques have a substantial problem that it is difficult to scan precisely all over the entire phantom body required for the WB-SAR measurements.

Our solution is to propose a novel WB-SAR estimation method based on the external cylindrical field scanning technique [12]. This method measures electric field strength by scanning a cylindrical surface of the closed region containing the phantom and the plane-wave radiation source inside. The similar scanning techniques have been employed to obtain the antenna radiation patterns [13], [14]. A key characteristic of the proposed method is that it can be easily applied to human phantoms that have different postures or sizes, because it is not necessary to obtain the electromagnetic components distributed inside of the human phantom.

This paper describes the experimental set-up for WB-SAR estimations of scaled homogeneous human phantoms that have 2/3 muscle-equivalent complex permittivity material and same standing posture. Whole-body absorption power is measured at 4 GHz using a male adult or a child phantom. In addition, in order to confirm the applicability of the proposed method, numerical estimations of inhomogeneous human phantoms exposed to an ideal plane-wave are performed with the FDTD (Finite-difference Time-domain) method. The human phantom parameters are designed based upon Virtual Family Product series [15].

2. Methodology

2.1 Whole-Body Averaged SAR Estimation Method

It is a technique that assesses WB-SAR by measuring the radiation power on closed surface including human phantom and some radiation source. This method is based on scanning the EMF data in the near-field of the antenna when the radiation characteristic of the antenna is measured [13]. The principle of radiation energy balance of the system is shown in Fig.1. In the figure, the absorption power (W_{ab}) of the lossy material (phantom) is given by the following expression from the law of the conservation of energy:

SUMMARY

The aim of this study is to develop a new whole-body averaged specific absorption rate (SAR) estimation method based on the external-cylindrical field scanning technique. This technique is adopted with the goal of simplifying the dosimetry estimation of human phantoms that have different postures or sizes. An experimental scaled model system is constructed. In order to examine the validity of the proposed method for realistic human models, we discuss the pros and cons of measurements and numerical analyses based on the finite-difference time-domain (FDTD) method. We consider the anatomical European human phantoms and plane-wave in the 2 GHz mobile phone frequency band. The measured whole-body averaged SAR results obtained by the proposed method are compared with the results of the FDTD analyses.

**key words:** whole-body averaged SAR, field measurement, scaled model, mobile phone frequency, plane-wave exposure system

1. Introduction

The whole-body averaged Specific Absorption Rate (WB-SAR) of 0.4 W/kg is one of the vital physical quantities to specify the basic restrictions on human exposure to electromagnetic fields (EMF) regarding the adverse health effects prevention [1]. The reference levels as guidelines to control and estimate EMF exposure environments at frequencies above 10 MHz are basically derived from the WB-SAR associated with the plane-wave exposure condition [1]. Same process is applied in the telecommunications technology council report of MIC Japan [2] and the ANSI/IEEE C95.1-1999 standard [3].

The original relationships between the WB-SAR and the EMF reference levels were obtained through the theoretical analyses using the simple geometrical or block structure model with homogeneous tissue for human body [4]. However, since these relationships for practical human exposure situations might be complicated, more accurate and precise estimations based upon realistic shaped and anatomical human models are expected. Recently, high resolution numerical simulations have become possible through the use of advanced high-speed computers and 3-D EMF analysis software tools or original program codes [5]–[9]. Thus, advancements in the side of theoretical estimations are being achieved steadily. On the other hand, some experiments to investigate the same subject have been reported [9], [10]. The WB-SAR is estimated from the absorption power of the human body phantom model which is exposed to the plane-wave of known EMF strength in the anechoic chamber. For the absorption power measurements, 3-D scanning techniques using electric probes inserted into the phantom [10] or thermographic techniques [11] have been applied. One of the scanning techniques is widely used as an IEC standard system for the SAR measurement on hand-held devices. However, at microwave frequencies these techniques have a substantial problem that it is difficult to scan precisely all over the entire phantom body required for the WB-SAR measurements.

Our solution is to propose a novel WB-SAR estimation method based on the external cylindrical field scanning technique [12]. This method measures electric field strength by scanning a cylindrical surface of the closed region containing the phantom and the plane-wave radiation source inside. The similar scanning techniques have been employed to obtain the antenna radiation patterns [13], [14]. A key characteristic of the proposed method is that it can be easily applied to human phantoms that have different postures or sizes, because it is not necessary to obtain the electromagnetic components distributed inside of the human phantom.

This paper describes the experimental set-up for WB-SAR estimations of scaled homogeneous human phantoms that have 2/3 muscle-equivalent complex permittivity material and same standing posture. Whole-body absorption power is measured at 4 GHz using a male adult or a child phantom. In addition, in order to confirm the applicability of the proposed method, numerical estimations of inhomogeneous human phantoms exposed to an ideal plane-wave are performed with the FDTD (Finite-difference Time-domain) method. The human phantom parameters are designed based upon Virtual Family Product series [15].
\[ W_{ab} = W_{in} - W_{out} \]  
where, \( W_{in} \) (in watt) is a antenna output power and \( W_{out} \) (in watt) is a total radiation power from the closed region. The power \( W_{out} \) from the closed region is yielded as a surface integral of the Poynting vector \( \mathbf{P} \) (in watts per square meter) over a closed surface \( S \):

\[ W_{out} = \int_{S} \mathbf{P} \cdot \mathbf{n} \, dS \]  
where, 

\[ \mathbf{P} = \frac{1}{2} \mathbf{E} \times \mathbf{H}^* \]  

Moreover, the WB-SAR can be derived from the absorption power \( W_{ab} \) and weight of the lossy material as follows:

\[ \text{Whole-body averaged SAR} = \frac{W_{ab}}{\text{Weight}} \]  

2.2 Field Scanning Method

Three major approaches have been advanced for scanning EMFs. The types of scanning surfaces used are planar, cylindrical, and spherical. The advantages and disadvantages of using the different surfaces have been previously discussed [13]. The technique that used most often is spherical scanning. Spherical scanning makes highly accurate measurements possible since it can obtain the EMFs that are measured at the same length from the center position of the scanning surface. However, it is not suitable for an experimental system targeting the WB-SAR since this system requires an increase in the estimation space and for the measured object to be suspended in midair.

Cylindrical scanning and planar scanning are, however, suitable for practical experimental systems. This paper examines the application of cylindrical scanning.

The cylindrical scanning system has two dimensions: height interval \( \Delta z \) and circumferential interval \( \Delta \phi \). For these sampling intervals, the following expressions are applied [16].

\[ \Delta z \leq \frac{\lambda}{2 \rho}, \quad \Delta \phi \leq \frac{\pi}{k \rho} = \frac{\lambda}{2 \rho} \]  

Thus, \( k \) (in per meter) is shown as a wave number, \( \lambda \) (in meter) is shown as wavelength, \( \rho \) (in meter) is the radius of the minimum sphere surrounding the measured object and \( a \) (in meter) is the radius of the cylindrical scanning surface. In this report, the sampling intervals are decided referring to the value derived from these conditions.

In order to include areas not usually considered, such as the upper and lower parts of the cylinder, the absorption power is subtracted from the radiation power when the lossy material is in the scanning surface as well as when the material is not in the scanning surface. Equation (2) is redefined (for cylindrical scanning) as follows:

\[ W_{out} = \int_{S} \mathbf{P} \cdot \mathbf{n} \, dS = \sum_{i=0}^{N} \sum_{j=0}^{M} P_r \Delta z_i \left( \frac{a \Delta \phi_j}{\pi} \right) \]  

3. Validation of Proposed Method Using Numerical Analysis

3.1 Numerical Model

The numerical human model is shown in Fig. 2. This model is an enhanced high-resolution magnetic resonance imaging whole-body human model and was made as one of the Virtual Family Product series [15]. This represents a 34-year-old male adult. It consists of 77 inhomogeneous tissues; its height is about 1.74 m and weight is 70 kg. The resolution of the model used is 2 mm.

Numerical EMF analyses were performed using the FDTD method [17] since this method well suits the computation of large scale and high precision inhomogeneous programs. The FDTD numerical analysis was performed by commercial software SEMCAD X [18] which incorporates a number of advanced tools for the visualization and treatment of simulation results.

The numerical model of the SAR experiment evaluation system including the numerical human model is shown
in Fig. 3. This calculation model assumes a plane-wave generated by a 2.1 GHz cellular phone impacting the human body. The male adult is located at the center of the plane-wave irradiation area.

Table 1 describes the parameters of FDTD calculation and the dielectric properties. The cell size of the analysis model is 2.0 mm. The computational space is 1000 × 1000 × 2000 mm³ (500 × 500 × 1000 cells). The absorbing boundary condition is a uniaxial perfectly matched layer (UPML) having 10 layers. The human model is composed of homogeneous tissue of 2/3 muscle-equivalent or inhomogeneous tissues [19]. 2/3 muscle-equivalent tissue means that its conductivity and permittivity are 2/3 times of the muscle’s ones.

The frequency of the plane-wave is 2.1 GHz and the plane-wave has uniform E polarization. The radiation power given as a power density is 1 mW/cm² based on ICNIRP public exposure reference levels [1] from the front side of the human body.

### 3.2 Estimation Condition of Proposed Method

The radiation power in a closed region was calculated using the EMF distributions given by the numerical analysis. In numerical analysis, an ideal probe that does not disturb the EMF distribution is assumed. Since the plane-wave source is located outside of the closed surface, the antenna input power (Wₚ) is 0 W. The absorbed power (Wₘ) equals to the radiation power (Wₚ) from the closed region. The FDTD analysis results are initially given in Cartesian coordinates. Accordingly, those results are converted into Cylindrical Polar Coordinates and the Poynting vector distributions on the cylindrical surface are obtained.

The sampling intervals on the cylindrical surface are derived from the sampling assumption of expression (5). The height interval is 20 mm and the circumferential interval is 4 degrees. Here, the sampling intervals are 20 mm × 20 mm.

### 3.3 Result

The Poynting vector distribution obtained when using homogeneous male adult phantom is shown in Fig. 4. The horizontal axis is angle φ and the vertical axis is height z of the cylindrical scanning surface. The plane-wave comes from 270 degrees direction perpendicular to the closed surface. In this numerical model, the Poynting vectors take negative values on the surface where the plane-wave enters from outside of the closed region.

The absorbed power and WB-SAR estimation results derived from the Poynting vector distribution for the male adult phantom are shown in Table 2. This table includes the WB-SAR estimation result using FDTD dosimetric calculation based on IEEE Standard C95.3 [20]. In this standard technique, the WB-SAR is evaluated by averaging the SAR distributions inside of the phantom. The human phantom weight is 68.55 kg (homogeneous tissue) and 72.24 kg (inhomogeneous tissues) as calculated from FDTD cells of the
numerical analysis model. The WB-SAR of the homogeneous phantom is 0.0587 W/kg using the proposed method and 0.0516 W/kg by the IEEE calculation technique. In addition, the WB-SAR of the inhomogeneous phantom is 0.0672 W/kg using the proposed method and 0.0598 W/kg by the IEEE calculation technique. The WB-SAR using the proposed method is within 13% of the IEEE calculation results. This confirms that the proposed method is suitable for both homogeneous and inhomogeneous phantoms.

As mentioned in Sect. 2.2, it is difficult for the WB-SAR estimation method using cylindrical field scanning method to experimentally estimate the Poynting vectors on the top and bottom surfaces. However, the numerical estimation result of the absorbed power including the top and bottom areas using cylindrical scanning is 3.813 W for the homogeneous phantom. This means that the error attributed to this incompleteness is less than 8%. Thus, the validity of the field scanning proposal has been confirmed.

4. Measurement Condition and System

The experimental set-up based on the proposed method is described. The far-field relationship between E and H is assumed. This makes it possible to conduct power estimations using the wave impedance of free space (377 Ω) and the electric field distributions. When the radiation source is located inside the closed region, some amount of the radiation power leaks from the top and bottom surfaces. Assuming the leak power difference is negligible between the situations with and without the phantom, the antenna input power should be corrected by the leak power. Accordingly, the leak power without the phantom is measured in advance.

4.1 Experimental Set-Up

A block diagram of the proposed experimental set-up for WB-SAR estimation is shown in Fig. 5. The experimental set-up consists of the radiation system, the electric field measurement system, and the physical phantom whose dielectric properties match those of the human body.

This set-up assumes a human exposed to a 2 GHz E-polarized plane-wave. The power density of the plane-wave is 1 mW/cm². To estimate plane-wave exposure at mobile radio frequencies on the human body, the direct approach is to use a full-size model. Instead, this study uses a scaled model to minimize the estimation space requirements and so permit the use of practical anechoic chambers. In an evaluation that includes lossy materials such as the human phantom, both the electric constant and the scale of the lossy material should change. In this study, a 1/2 scale model is used. The measurement systems are automatically controlled by program code through GPIB.

4.2 Scaled Modeling

In order to subject the human body to uniform plane-wave excitation in the cellular phone frequency band (2.0 GHz), a large-scale evaluation area (of the order of 10’s of meters) is required.

Accordingly, the evaluation area was reduced by scaling both antenna size and frequency. In an evaluation system including lossy materials such as human bodies, both the dielectric constant and the scale of the lossy material should change appropriately. The reduced scale relation between the full-scale model and a model with a scale factor of $k$ [21],[22] is shown in Table 3. For a scaled model with a scale factor of $k$, the dielectric constants of the scaled model are the equal relative permittivity and the $1/k$ times conductivity.

In this paper, a 1/2 scale model is used. Since a 1/2 scale factor is used, object sizes are reduced by a half and the antenna radiation frequency is 4.0 GHz.

4.3 Radiation System

The radiation source outputs a 4 GHz continuous wave. A plane-wave radiation system that generates a uniform plane-wave is required, since the guideline of the EMF strength assumes an ideal plane-wave that vertically enters the human body.

In order to easily generate a plane-wave with sharp directivity, horn antennas with sharp directivity are used as radiators. Figure 6 illustrates the plane-wave radiation system that was used. Only a localized surface of the human phantom could be exposed without any measures since the electric field strength in front of the horn antenna is comparatively high. Thus a dielectric lens was designed and set in front of the horn antenna. The relative permittivity of the dielectric lens is 3.7. The dielectric lens aligns the amplitude and phase of the wave from the horn antenna.

We used a double ridge horn antenna in order to realize wideband characteristic. The nominal frequency range of the antenna is from 1 GHz to 5 GHz. The overall size of the radiation system is $800 \times 750 \times 1300 \text{ mm}^3$. The radiation system irradiates a plane-wave whose excitation area is

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Full scale model</th>
<th>Scale model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Length</td>
<td>$l$</td>
<td>$l' = k l$</td>
</tr>
<tr>
<td>Frequency</td>
<td>$f$</td>
<td>$f' = (1/k)f$</td>
</tr>
<tr>
<td>Permittivity</td>
<td>$\epsilon$</td>
<td>$\epsilon' = \epsilon$</td>
</tr>
<tr>
<td>Conductivity</td>
<td>$\sigma$</td>
<td>$\sigma' = (1/k)\sigma$</td>
</tr>
</tbody>
</table>

![Fig. 5 Block diagram of the proposed experimental set-up for WB-SAR estimation.](image-url)
The radiation power from the cylindrical closed surface is obtained by electric field distribution measurement using a 3-axis optical electric-field sensor (SEIKOH GIKEN OEFS-H-S1B). The optical sensor has uncertainty values in the range of \( \pm 0.5 \) dB. The translation error of Poynting vector is ignored. The cylindrical scanning system is composed of the antenna tower (DEVICE DM2224B1) and the turntable (DEVICE DM3352BV1/O-1.5). The minimum steps of the antenna tower and the turntable are 10 mm and 0.1 degrees, respectively. The sampling intervals in cylindrical scanning are 20 mm in height and 1 degree in circumference. The human phantom is separated by 0.5 m from the front surface of the lens.

The optical sensor is mounted on the antenna tower. The optical sensor output is connected to the sensor controller through 20 m of optical fiber cable. The controller output is fed to the input of spectrum analyzer (Agilent E4440A).

4.4 Field Sensor and Positioner

The measured electric-field components on the planer surface at the position of 500 mm from the dielectric lens are shown in Figs. 7(a)–(c). The main polarized component of the radiation system is vertical polarization (Ez). The antenna input power is 23 dBm. The Ez strength of the area-irradiated plane-wave is within 3 dB. The field strength of cross-polarized components decreases by 10 dB compared to the field strength of the main polarized component.

The averaged electric power density in the plane-wave excitation area is 0.154 W/m². Hence, the electric power density is 1/65 times the reference level of ICNIRP (1 mW/cm² at 2 GHz).

4.5 Solid Phantom Made from Silicone Rubber

Two physical human phantoms were made based on enhanced high-resolution European human CAD data [15]. A 34-year-old male adult and a 6-year old male child model were used, as shown in Fig. 8. The full-size male child has
about 1.17 m in height and 19.5 kg in weight. The phantom parameters are summarized in Table 4. The human phantom is composed of 2/3 muscle-equivalent tissue [19]. The phantoms used in this study consist of carbon nanotubes embedded in silicone rubber [23]. This material has a specific gravity below 1.3 g/cm³. The measured complex dielectric constants of the male adult phantom is 31.3 in relative permittivity and 1.93 S/m in conductivity. The variations of the complex dielectric constants are within 20%.

5. Result

5.1 Validity of Experimental Set-Up Using Simplified Rectangular Phantom

Basic geometrical phantoms must be examined when confirming the experimental set-up. Such phantoms are a sphere, rectangular or spheroid, and so on. As for the basic geometrical structure, a theoretical analysis based on electromagnetic theory has already been done [24], [25].

In this paper, a rectangular phantom is used. The phantom model offers highly accurate WB-SAR estimations, because this phantom has a simplified structure that is affected by the staircase approximation employed in the FDTD method.

The square planar shape phantom used for the numerical calculations and the measurements is shown in Fig. 9. It has dimensions of 400 mm × 400 mm × 50 mm. Its weight is 8.0 kg based on the fact that mass density of the phantom is regarded as 1000 kg/m³. The target values of relative permittivity and conductivity for the rectangular phantom are 45.0 and 8.0 S/m, respectively.

The WB-SAR estimation result using the proposed method is 0.111 W/kg. The WB-SAR result using FDTD analysis with ideal plane-wave is 0.093 W/kg. These values are normalized to the reference level of the ICNIRP Guideline. The difference of these results is within 20%.

5.2 WB-SAR Estimation Result

The experimental set-up for the male adult human phantom in the anechoic chamber is shown in Fig. 10. The electric power of the plane-wave radiation system was 23 dBm. Thus, the averaged electric power density of the plane-wave excitation space of the radiation system is 0.154 W/m². The electric field distributions on the cylindrical scanning area without and with the male adult phantom are shown in Fig. 11 and Fig. 12, respectively. However, the component of Er not used in the power evaluation is omitted. The evaluation cylinder has a height of 1.8 m and diameter of 3.0 m.

Next, the Poynting vector on cylindrical surface is derived based on the electric field data. The measured absorption power and WB-SAR estimation results for the male adult and male child models are summarized in Table 5. The WB-SARs are calculated using the weight of the numerical human phantom models. The absorbed power is normalized for the power density of exposed plane-wave of 1 mW/cm².

The measured WB-SAR for the male adult is
Table 5 Comparison of measurement results based on proposed method and IEEE C95.3 calculation results.

<table>
<thead>
<tr>
<th></th>
<th>Male adult</th>
<th>Male child</th>
</tr>
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<tbody>
<tr>
<td>Normalized $W_{ob}$ [W]</td>
<td>4.825</td>
<td>3.873</td>
</tr>
<tr>
<td>WB-SAR [W/kg]</td>
<td>0.0704</td>
<td>0.0565</td>
</tr>
</tbody>
</table>

0.0704 W/kg. A numerical estimated WB-SAR for the male adult model exposed to ideal plane-wave is 0.0565 W/kg obtained by the IEEE standard calculation method. In addition, the measured and calculation result for the male child is 0.131 W/kg and 0.100 W/kg, respectively. The measured WB-SAR results are 30% larger than calculated results for both the adult and child phantom cases. Improvement of these uncertainties is one of the future study issues.

6. Conclusions

This paper introduces an actual experimental set-up for WB-SAR measurements based on the cylindrical field scanning method. Several measurement results of WB-SAR exposure were reported. The experimental results agree with the numerical ones in terms of a simplified rectangular phantom and a few human phantoms. This technique supports numerical ones in terms of a simplified rectangular phantom model. Additionally, the experimental WB-SAR estimation of human phantoms that have different postures or sizes will be conducted.

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