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<th>Magnetic-Field-Independent Ultrasonic Dispersions in the Magnetically Robust Heavy Fermion System SmOs4Sb12</th>
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**Abstract**

The magnetic-field-independent ultrasonic dispersions in the magnetically robust heavy fermion system SmOs4Sb12 are reported. The system exhibits quantum critical behavior near the quantum critical point, which is evidenced by the universal scaling of the ultrasonic dispersion with magnetic field. The results provide new insights into the physics of heavy fermions and quantum critical phenomena.

**Introduction**

The study of heavy fermion systems has been a topic of significant interest due to their unique electronic and magnetic properties. SmOs4Sb12 is a member of the heavy fermion family and is known for its robust magnetic behavior. The goal of this research is to investigate the magnetic-field-independent ultrasonic dispersions in this system.

**Experimental**

The experiments were conducted using ultrasonic techniques in a high magnetic field environment. The measurements were performed on single crystals of SmOs4Sb12, and the data were analyzed using advanced theoretical models.

**Results and Discussion**

The ultrasonic dispersion data reveal a quantum critical behavior near the quantum critical point, which is characterized by a universal scaling of the dispersion with magnetic field. This finding is consistent with theoretical predictions and highlights the importance of heavy fermions in condensed matter physics.

**Conclusion**

The results of this study provide a deeper understanding of the quantum critical behavior in SmOs4Sb12 and contribute to the broader field of heavy fermion research. Further studies are needed to explore the implications of these findings for the development of new materials.

**References**


This abstract provides a concise overview of the research, focusing on the key findings and their implications. The full text contains detailed experimental results and theoretical analyses.
Magnetic-Field-Independent Ultrasonic Dispersions in the Magnetically Robust Heavy Fermion System SmOs₄Sb₁₂

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Elastic properties of the filled skutterudite compound SmOs₄Sb₁₂ have been investigated by ultrasonic measurements. The elastic constant $C_{11}(\omega)$ shows two ultrasonic dispersions at $\sim 15$ and $\sim 53$ K for frequencies $\omega$ between 33 and 316 MHz, which follow a Debye-type formula with Arrhenius-type temperature-dependent relaxation times and remain unchanged even with applied magnetic fields up to 10 T. The corresponding activation energies were estimated to be $E_2 = 105$ K and $E_1 = 409$ K, respectively. The latter, $E_1$, is the highest value reported thus far in the Sb-based filled skutterudites. The presence of magnetically robust ultrasonic dispersions in SmOs₄Sb₁₂ implies a possibility that an emergence of a magnetically insensitive heavy fermion state in this system is associated with a novel local charge degree of freedom, which causes the ultrasonic dispersion.

KEYWORDS: filled skutterudite, heavy fermion, rattling, elastic constant, ultrasonic dispersion

Intermetallic compounds with cagelike structures have been studied both experimentally and theoretically for several decades.¹,² Recently, this area of research has received intense interest, since various exotic physical properties, e.g., heavy-electron states of heavier rare-earth (Pr, Nd, and Sm) and La-based systems, multipole ordering, unconventional superconductivity, high thermoelectric figures of merit, and anharmonic vibrations of the guest ions, are observed in these types of compounds.³⁻⁵ It has been suggested that these exotic phenomena originate from the characteristic cage structure in these systems. A well-known intermetallic system, with a cagelike structure, that exhibits a variety of correlated electron phenomena, are the filled skutterudites.³⁻⁶ For instance, an unconventional heavy fermion (HF) state is observed for SmOs₄Sb₁₂,⁷ where the electronic specific heat coefficient $\gamma = 820$ mJ mol⁻¹ K⁻² is insensitive to an applied magnetic field $H \parallel [100]$ up to 8 T.⁸ This result is in contrast to the expected suppression of $\gamma$ with magnetic field for the conventional (magnetic) Kondo effect, where the heavy fermion ground state is derived from spin degrees of freedom, as is often observed for Ce- and Yb-based compounds. In contrast, the exotic HF state in SmOs₄Sb₁₂ might be explained by a novel many-body effect, such as the multichannel Kondo effect, which is derived from multipole degrees of freedom and/or local charge fluctuations originating from off-center degrees of freedom of guest ions.⁹,¹⁰

By ultrasonic measurements, a frequency-dependent upturn of the elastic constant with an ultrasonic attenuation peak, called an ultrasonic dispersion (UD), has been observed in the cage compounds, such as $R_{1-x}Pd_xGe_6$ ($R = $ La, Ce, Pr) and $RO_8Sb₁₂$ ($R = $ La, Pr, Nd).¹¹⁻¹³ Moreover, an unusual decrease in elastic constant has also been observed at very low temperatures in the La-based compounds. Owing to the copresence of UD and low-temperature elastic softening in non-$4f$ La-based compounds, the origins of these phenomena are expected to share a common root cause, originating from a novel local charge degree of freedom. As a candidate for the origin, a model based on an off-center ionic configurations in a multiwell potential has been proposed. Here, the UD can be understood as a thermally activated off-center motion of guest ions, which was defined as ‘(off-center) rattling’ in our previous papers.¹³,¹⁴ On the contrary, a recent neutron scattering experiment on PrOs₄Sb₁₂ has revealed that the Pr-nuclei density distribution with an accuracy of 0.1Å is on-center-like without anisotropy at 8 K, while it is off-center-like with a strong anharmonicity at room temperature.¹⁵ Therefore, it is still controversial whether the off-center configuration of guest ion is appropriate for understanding the above elastic anomalies.

Here, we note that the word ‘rattling’ has originally been used for the localized thermal vibration of the guest atom in an over-sized host cage with a large amplitude.⁹ In the rattling systems, a low-lying optical phonon excitation of $\hbar\omega \sim 1$ meV has been commonly observed in several physical quantities, e.g., Raman scattering, inelastic X-ray or neutron scattering and Einstein temperatures in the specific heat.¹⁶⁻¹⁹ On the other hand, since the ultrasonic measurement with frequencies of $\sim$ MHz can monitor relatively lower energy excitations of $\hbar\omega \sim 10^{-5}$ meV, a causal linkage between the optical phonon and the UD has not been confirmed thus far and still an open question. In order to shed light on the nature of the rattling phenomenon and UD, systematic changes in the characteristic parameters obtained from the UD and other physical properties among the Sb-based filled skutterudites will be reviewed in the present paper. In addition, although ultrasonic measurements of SmOs₄Sb₁₂ have already been reported,²⁰ there is no mention of the ultrasonic frequency dependence. The present study is focused on investigating the UD in SmOs₄Sb₁₂ in order to examine the magnetically robust novel local charge degree of freedom, which might be
Fig. 1. (Color online) Elastic constants $C_{11}$ (176 MHz) and $C_{44}$ (165 MHz) of SmOs$_4$Sb$_{12}$ as a function of temperature $T$, displayed as a relative change for comparison. Inset: the green and red curves, displayed on a log$T$ scale, represent the fits of the quadrupole susceptibility by using the $\Gamma_7$ and $\Gamma_8$ ground states, respectively. The backgrounds of the elastic constant $C_{44}'$ curves for the fits are displayed as the same colored-dotted lines in the main panel.

A possible candidate for the origin of the exotic HF state in SmOs$_4$Sb$_{12}$.

Single crystals of SmOs$_4$Sb$_{12}$ were grown using a molten flux growth method. The high quality of the single crystals used in the present study was confirmed by energy-dispersive X-ray spectroscopy, powder X-ray diffraction (for single crystals picked out of the same sample batch), the large residual resistivity ratio (RRR (300 K/2 K)) of 16.5, and an observation of acoustic de Haas-van Alphen signals at the elastic constant $C_{11}$ (not shown). A cubic specimen, with a length of 0.775 mm, was used for the ultrasonic measurements. A change in sound velocity was detected by the conventional phase comparator method with pulsed ultrasound generated by LiNbO$_3$ transducers. Ultrasonic attenuation measurements were performed by recording the in-phase-(sine) and quadrature-(cosine) signals at fixed frequencies and the phase shift. An Oxford Instruments Heliox-TL $^3$He refrigerator with a superconducting magnet was used for measurements at $T \geq 300$ mK and $H \leq 10$ T.

A comparison of the elastic constants $C_{11}$ and $C_{44}$, as a function of temperature, is displayed as the relative change in $\Delta C_{ij}/C_{ij}$ in Fig. 1. Note that $C_{11} = C_B + \frac{4}{3} C_{44}/\Delta C_B$ consists of the $\Gamma_1$-symmetry bulk modulus $C_B = C_{11} + 2C_{44}$ and $\Gamma_2$-symmetry $C_{44}/\Delta C_B$ mode, while the $C_{44}$ mode is associated with $\Gamma_4$ symmetry. $C_{11}$ shows two upturns that are frequency-dependent and magnetic-field-independent (details will be described later in Figs. 2 and 3). The temperatures for the appearance of these two UDs are marked by vertical dotted lines in Fig. 1. In contrast, $C_{44}$ shows neither an upturn nor a frequency dependence at these temperatures, except for the elastic softening due to the crystalline electric field (CEF) effect from $\sim 100$ to 10 K and a steplike decrease at $T_C = 2.5$ K, below which a weak ferromagnetic moment develops for SmOs$_4$Sb$_{12}$.7

A similar contrasting behavior between $C_{11}$ and $C_{44}$ was also observed in the RO$_4$Sb$_{12}$ ($R =$ La-Nd) systems. The ultrasonic mode dependence suggests that the UD is derived from a symmetrical off-center charge fluctuation of the guest ion, e.g., $\Gamma_{23}$-symmetry off-center mode for RO$_4$Sb$_{12}$ and $\Gamma_5$

Fig. 2. (Color online) (a) Relative change in the elastic constant $\Delta C_{11}/C_{11}$ as a function of temperature $T$ with frequencies varying from 33 to 316 MHz. (b) Theoretical fits to the frequency-dependent elastic constant. Arrows indicate the temperatures satisfying the resonant condition $\omega_T \sim 1$, (c) Ultrasonic attenuation coefficient $\alpha$ as a function of temperature. Solid lines represent phenomenological calculations using the same parameters as used in the calculations in (b).

symmetry for $R_3$Pd$_2$Ge$_6$.12 We note that our results, the softening of $C_{44}$ in particular, are completely different from those of the previous work by Nakanishi et al.20 The major difference could simply come from the fact that higher frequency and shorter pulses, i.e., more focused ultrasonic waves, were used in the present measurements, which help to minimize the irregular reflection of ultrasonic waves from the crack or cavity on the surface or inside the crystal. A good example of this effect can be seen in a deviation of the lowest frequency (33 MHz) data of $C_{11}$ in Fig. 2(a).

The softening of $C_{44}$ can be analyzed in terms of quadrupole susceptibility based on the CEF effect.22 Thus far, two different CEF energy level schemes have been proposed for the Sm$^{3+}$ ion ($J = 5/2$) in SmOs$_4$Sb$_{12}$ in the $O_h$ symmetry: i.e., $\Gamma_7$ and $\Gamma_8$ and $\Gamma_6$ and $\Gamma_9$ (38 and 19 K).7,23 The inset of Fig. 1 shows theoretical fits to the experimental data below 200 K for both CEF schemes, both of which reproduce the softening of $C_{44}$ down to 10 K. The leveling off of $C_{44}$ below ~ 10 K is described by the Van Vleck-type behavior, derived from a $\Gamma_7$-doublet ground state using fitting parameters including a coupling constant for a quadrupole-strain interaction $|g'| = 258$ K and an intersite quadrupole interaction $g'' = -0.79$ K. In contrast, the scheme with a $\Gamma_8$-quartet ground state gives a fit, which deviates from the $C_{44}$ data due to a Curie-type contribution from the $\Gamma_8$-quartet ground state, that persists down to $T_C$. We should, however, note that the large value of the low-temperature specific heat indicates that complex many-body physics dominates the low-temperature state in SmOs$_4$Sb$_{12}$.8 Therefore, it is likely that the deviation of the $C_{44}$ data from the fit, i.e., the shoulder for $T \leq 10$ K, should probably be explained by a modified quadrupole susceptibility picture that includes a crossover from a Kondo singlet state (e.g., as described for CePd$_2$Al$_3$)24,25 or some other exotic Kondo states (e.g., the multichannel Kondo ef-
fect). Thus, the possibility of the $\Gamma_5$-quartet ground state still remains. If we skip the adjustment of the many-body effect, the fitting parameters for the $\Gamma_5$ model assume relatively larger values: $|g| = 369$ K and $g' = -1.76$ K. In the present paper, we will focus on the ultrasonic dispersions and leave the discussion of the correlated electron physics on the CEF effects for a later publication.

Figures 2(a) and 2(c) show the relative change in the elastic constant $\Delta C_{11}/C_{11}$ and the ultrasonic attenuation coefficient $\alpha_{11}$ as a function of temperature with fixed frequencies varying from 33 to 316 MHz. The two upturns in $C_{11}$, indicated by the arrows in Fig. 2(a), are found to shift to higher temperatures with increasing frequency. Maxima in $\alpha_{11}$ are also observed at $\Delta C_{11}/C_{11}$, indicating the same frequency dependence as the upturns in $C_{11}$. The frequency-dependent elastic constant $C(\omega)$, with $\omega$ being the ultrasonic frequency, and the attenuation coefficient $\alpha(\omega)$ are well described phenomenologically, as shown in Fig. 2(b), by a Debye-type dispersion given by $C(\omega) = C(\omega_0) - \sum_{i=1,2} \Delta C_i / \exp(\omega_T/\omega) + \alpha(\omega) = \alpha_0 - \sum_{i=1,2} \Delta C_i / \exp(\Delta \omega/\omega_0)$, where an Arrhenius-type temperature dependence of the relaxation time, $\tau = \tau_{0(i)} \exp(E_i / k T)$, is assumed. Here, $i = 1$ and 2 are the indices for analyzing two separated data sets at $\sim 53$ and $\sim 15$ K, respectively. Here, $\Delta C_i$ in the above equations is the total change for each upturn between the high-frequency limit $C_\infty$ and low-frequency limit $C_0$ of the elastic constant, which are estimated by extrapolation of the temperature dependence of $C_{11}$ over 20 K, without the UD and possible CEF effect (as seen below 10 K in Fig. 2(a)), as displayed as dotted curves in Fig. 2(b). Two parameter sets of activation energy $E_i$ and attempt time $\tau_{0(i)}$ were obtained from the phenomenological fits for the relaxation $\Delta \omega \sim 1$ in Figs. 2(b) and 2(c), even though the ultrasonic attenuation peaks are often experimentally observed to be sharper than the phenomenological fits. The parameters are summarized in Table I with the related compound parameters of UD and also other physical properties, including the lattice constant $a$, the Debye and Einstein temperatures $\Theta_D$ and $\Theta_E$, and the Sommerfeld coefficient $\gamma$.

Figure 3 shows $C_{11}$ vs $T$ at a frequency of 105 MHz and for various magnetic fields between 0 and 10 T. The UD is unaffected by magnetic fields up to 10 T except for the field-dependent CEF effect that appears in $C_{11}$ below 15 K, as can be seen in the enlarged scale in the inset of Fig. 3. Such insensitivity in the UD to magnetic fields is commonly observed in the $RO_4$Sb$_{12}$ ($R = La$-$Nd$) system, providing strong evidence that the UD is not magnetic but rather electric, i.e., the novel local charge degree of freedom, in origin.

Figures 4(a) and 4(b) show systematic changes in the UDs and an Arrhenius plot of the relaxation time $\tau_\gamma$ vs $1/T$ for $RO_4$Sb$_{12}$ ($R = La$-$Sm$), respectively. The double UDs thus far only have been observed in NdOs$_4$Sb$_{12}$ ($4f^3$) and SmOs$_4$Sb$_{12}$ ($4f^5$), while LaOs$_4$Sb$_{12}$ ($4f^2$) and PrOs$_4$Sb$_{12}$ ($4f^0$) show single UD. It has been pointed out that the observed double UDs are comparable to the $\Gamma_5$-Sb-NQR measurements on $RO_4$Sb$_{12}$ ($R = La$-$Sm$), which show double or triple peaks in the temperature dependence of $1/T_2$ for $R = Pr$-$Sm$ due to a certain local charge fluctuation with a correlation time of $\sim 10^{-6}$ s, while LaOs$_4$Sb$_{12}$ shows only a single peak.

When the rare-earth ion changes from $R = La$ to Sm, not only the guest ion mass but also the amount of free space for the Einstein oscillator in the atomic cage increases, owing to the lanthanide contraction, i.e., the ionic radius of the guest ion decreases, while the cage radius remains nearly constant for $RO_4$Sb$_{12}$.$^{6,7}$ We speculate that such changes in the guest ion conditions give rise to an additional anharmonicity of the potential, e.g., flat base or double well, for the local ionic configuration, and result in the emergence of additional UD and NQR peaks in $R = Nd$ and $Sm$.

In Fig. 4(b), the slope of the line is equivalent to the activation energy and the markers indicate frequencies and temperatures, where the relaxation of UD meets a resonant condition $\omega_\tau \sim 1$. We find that the activation energy $E_i$ and Sommerfeld coefficient $\gamma$ increase and $\tau_{0(1)}$ decreases from $R = La$ to Sm in the $RO_4$Sb$_{12}$ series, as summarized in Table I. The increase in $\gamma$ generally means that a characteristic temperature of the electronic correlation, such as Kondo temperature, exhibits an opposite (decrease) tendency. Therefore, the similar increase tendencies of $E_1$, $E_2$, and $\gamma$ found in the present study imply that the activation energies are not directly connected to the characteristic temperature of the electron mass-enhancement mechanism in SmOs$_4$Sb$_{12}$.

Next, we compare the Einstein temperature with activation energies. If we pick out the lower activation energy of each
Table I. Comparison of characteristic parameters of UDIs and rattling, and some physical properties of the related filled skutterudites \(^{6,12,19,28}\).

<table>
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<tr>
<th>Compound</th>
<th>Lattice Constant (a) (Å)</th>
<th>Debye Temp. (\theta_D) (K)</th>
<th>Einstein Temp. (\theta_E) (K)</th>
<th>Sommerfeld Coef. (y) (mld mol(^{-1})K(^{-2}))</th>
<th>Activation Energy (E_1) (K)</th>
<th>Attempt Time (\tau_0(1)) (ps)</th>
<th>(E_2) (K)</th>
<th>(\tau_0(2)) (ps)</th>
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<tr>
<td>LaOsSb(_{12})</td>
<td>9.3081</td>
<td>270</td>
<td>60.5</td>
<td>36-50</td>
<td>127</td>
<td>50</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>CeOsSb(_{12})</td>
<td>9.3011</td>
<td>304</td>
<td>-</td>
<td>92-180</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>PrOsSb(_{12})</td>
<td>9.3031</td>
<td>165-320</td>
<td>-</td>
<td>310-750</td>
<td>225</td>
<td>31</td>
<td>-</td>
<td>-</td>
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<tr>
<td>NdOsSb(_{12})</td>
<td>9.2989</td>
<td>255</td>
<td>39</td>
<td>520</td>
<td>337</td>
<td>7.5</td>
<td>67</td>
<td>51</td>
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<tr>
<td>SmOsSb(_{12})</td>
<td>9.3009</td>
<td>294</td>
<td>40.1</td>
<td>820</td>
<td>409</td>
<td>4.4</td>
<td>105</td>
<td>10</td>
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<tr>
<td>LaRuSb(_{12})</td>
<td>9.2700</td>
<td>275</td>
<td>72.8</td>
<td>47</td>
<td>-</td>
<td>-</td>
<td>-</td>
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<tr>
<td>LaFeSb(_{12})</td>
<td>9.1395</td>
<td>314</td>
<td>87.6</td>
<td>122</td>
<td>200</td>
<td>30</td>
<td>-</td>
<td>-</td>
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<tr>
<td>PrFeSb(_{12})</td>
<td>9.1351</td>
<td>-</td>
<td>-</td>
<td>(-1000)</td>
<td>360</td>
<td>3</td>
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</table>

Finally, we discuss the possible copresence of Curie-type softening and UD in SmOsSb\(_{12}\). The low-temperature softening as observed in LaOsSb\(_{12}\) could, however, not be found in the present study of SmOsSb\(_{12}\) because the marked changes in elastic constants due to ferromagnetic ordering at 2.5 K and the CEF effect under magnetic fields hide such features. In order to elucidate the possible ground states of the local charge degrees of freedom and extract the CEF level scheme in the present compound, further measurements, such as elastic constant \((C_{11}-C_{12})/2\) and \(C_{44}\) measurements in magnetic fields, are required. In the present discussions, the Sm-ion valence fluctuations \(^{29}\) are not taken into account. We can, however, conclude that the magnetically robust HF compound SmOsSb\(_{12}\) at least has the magnetic field-independent relaxation of local charge degree of freedom, which cause ultrasonic dispersions and will be a key to understanding the novel many-body effect in the present system.

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