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Influence of macro-fractures and micro-fractures on permeability and elastic wave velocities in basalt at elevated pressure

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Abstract

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4 Fractures are ubiquitous on all scales in crustal rocks. The investigation of fractures and their
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6 influence on physical and transport properties of rocks is therefore essential for understanding of
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8 many key problems in seismology, volcanology and rock engineering. In crystalline rocks, pore
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10 water is primarily stored in and migrates through networks of cracks and fractures at all scales. It is
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12 therefore essential to know how fluid flow in such fracture networks responds to the elevated
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14 pressures found at depth. Here, we report results from an investigation of changes in fluid
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16 permeability, and associated changes in P-wave and S-wave velocities, at elevated effective
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18 pressure for intact, macro-fractured and micro-fractured samples of Seljadur basalt.
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23 In all cases, permeability decreases and both wave velocities increase with increasing effective
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25 pressure. Permeability decreases were smallest in the intact material (from approximately 10^{-19}m^2 to
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27 $3\times 10^{-20}\text{m}^2$), intermediate in the micro-fractured material (from approximately $5\times 10^{-17}\text{m}^2$ to
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29 $1\times 10^{-17}\text{m}^2$) and largest in the macro-fractured material (from approximately $3\times 10^{-15}\text{m}^2$ to
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31 $9\times 10^{-19}\text{m}^2$). For material containing both micro-fractures and macro-fractures, the closure of
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33 macro-fractures dominated the permeability reduction at low pressure, with the closure of
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35 micro-fractures exerting an increasing influence at higher pressure.
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44 **Keywords:** Permeability, Elastic wave velocities, Fractures, Pressure, Basalt
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1. Introduction

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4 Fractures are ubiquitous on all scales in crustal rocks. In the upper crust, the presence of fractures
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6 influences significantly the physical and transport properties of rock (Walsh, 1981; Gueguen et al.,
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8 1997). The existence of fractures makes rock more compliant, and also makes rock more permeable
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10 if they are connected together in a percolating network. It is therefore important to investigate how
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12 different scales and types of fracture influence the physical and transport properties of rock.
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16 This is important because knowledge of rock physical and transport properties, and their
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18 evolution with pressure and stress, is essential to understand both hazardous natural phenomena
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20 such as volcanic eruptions and earthquake ruptures, and potentially hazardous geo-engineering
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22 projects such as long-term sub-surface storage of hydrocarbons and hazardous waste. That is
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24 because the presence of water and other aqueous solutions in rock fractures leads to time-dependent
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26 deformation driven by rock-fluid chemical interactions (e.g. see reviews by Anderson and Grew,
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28 1977; Atkinson, 1982, 1984; Atkinson and Meredith, 1987). These studies have demonstrated that
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30 the growth rate (velocity) of fractures increases with increasing humidity (Meredith and Atkinson,
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32 1985; Nara and Kaneko, 2005, 2006; Nara et al., 2010a) and in the presence of liquid water (Waza
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34 et al., 1980; Sano and Kudo, 1992; Nara et al., 2009, 2010b). Since most crustal rocks contain
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36 networks of distributed fractures (Brace et al., 1972; Sprunt and Brace, 1974; Kranz, 1983), and
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38 these provide the principal pathways for fluid flow (Koudina et al., 1998; Chaki et al., 2008), it is
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40 essential to know how fluids are able to migrate through these networks. However, we also know
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42 that fractures can be closed by the application of an elevated pressure and, conversely can be
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44 extended by the application of an increased differential stress.
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52 Many efforts have therefore been made to study the change in fluid permeability associated with
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54 increasing pressure in crystalline, igneous rocks containing pre-existing networks of micro-fractures,
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56 for example in granite (Pratt et al., 1977; Kiyama et al., 1996; Kato et al., 2002; Benson et al., 2006a,
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58 b; Nasser et al., 2009) and basalt (Vinciguerra et al., 2005; Benson et al., 2006b). However,
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60 although we know that rocks contain fractures at all scales (i.e., both micro-fractures and
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macro-fractures), we know of no previous investigation of the comparative influence of
micro-fractures and macro-fractures in controlling permeability in a single rock type. In this study,
we have therefore investigated the change in permeability as a function of increasing effective stress
in a rock with no visible micro-fractures in its as-received state; Seljadur basalt from south-west
Iceland. We have made measurements on samples of intact material, on samples in which we have
introduced macro-fractures by mechanical splitting, and on samples in which we have introduced
micro-fractures by thermal stressing. As a complementary measure of the crack damage introduced
into our samples, we also measured the changes in P-wave and S-wave velocities with increasing
effective pressure during our experiments.

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2. Experimental material and methodology

2.1 Sample material

All measurements were made on samples of Seljadur basalt (SB), a fresh, columnar-jointed, intrusive basalt from south-west Iceland. A scanning electron microscope (SEM) image of intact SB is given in Fig. 1. The rock comprises plagioclase feldspar and pyroxene with some accessory minerals in a glassy matrix, and has been categorized it as a tholeitic basalt (Eccles et al., 2005). The SB used in this study has a porosity of 4 % (measured using the ISRM suggested water saturation method), but no visible pre-existing micro-fractures. This results in a low initial permeability (approximately 10^{-19} m²). Samples were cored from a single block of material to a diameter of 38.1 mm and then ground flat and parallel within ± 0.02 mm to a nominal length of 40 mm.

We should point out here that all of the samples used in this study were from a different batch of SB from that for which data are reported in Vinciguerra et al. (2005), but collected from the same quarry several years later. The earlier material had a porosity of around 1 % and a commensurately lower initial permeability of 5×10^{-21} m².

2.2 Measurement methodology

Permeabilities were measured in a servo-controlled permeameter using the steady-state flow method. A schematic diagram of the permeameter system used in this study is presented in Fig. 2 (see also, Benson et al., 2005). It comprises a 100 MPa hydrostatic pressure vessel equipped with dual 70 MPa servo-controlled pore fluid intensifiers. Rubber-jacketed samples are set inside the pressure vessel between two stainless steel end-caps. The end-caps contain ports to allow pore fluid to be introduced and distributed to one end of the sample, and to be received and expelled at the other end. The end-caps also house piezoelectric P-wave and S-wave transducers for the

measurement of axial elastic wave velocities by the ultrasonic transmission method (Birch, 1960).

1 During permeability measurement, the upstream and downstream intensifiers are set to slightly
2 different control pressures in order to maintain a small, constant pressure difference across the
3 sample. Once steady-state flow is established, permeability can be determined from the rate of fluid
4 flow, the pressure gradient, and the sample dimensions via direct application of Darcy's law. To
5 minimise any temperature-induced pressure fluctuations, the equipment is located within a
6 temperature-controlled laboratory. The temperature was kept constant at 20 °C during all
7 experiments.
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9 In this study, we use the simple effective pressure law, $P_{\text{eff}} = P_c - a.P_p$, with $a = 1$, where P_c is
10 the applied confining pressure, P_p is the mean pore pressure and P_{eff} is the effective pressure. We
11 varied the effective pressure, P_{eff} , during our experiments by holding the mean pore pressure
12 constant at 4 MPa, and increasing the confining pressure in a series of steps. We estimate that the
13 accuracy of our permeability and wave velocity measurements is 2 % and 1 %, respectively.
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16 2.3 Measurements on sequentially damaged samples

17 Measurements of permeability and elastic wave velocities were first made, as a function of
18 effective pressure, on an intact sample prepared from the as-received material. Following these
19 initial measurements, we induced macro-fractured samples by splitting the initially intact samples in
20 half axially using a modified Brazil test apparatus at an axial strain rate of 10^{-5}s^{-1} . These
21 macro-fractured samples were then re-inserted into the permeameter and a second series of
22 permeability measurements made under the same effective pressure conditions. Great care was
23 taken to ensure that the halves of the macro-fractured samples were fully mated with no shear offset.
24 On insertion, the macro-fractures were aligned normal to the polarization direction of the S-wave
25 transducers to better than 5°.
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28 Finally, in order to produce micro-fractured samples we thermally stressed previously intact and
29 macro-fractured samples by heating them slowly to 600°C or 800°C inside a tube furnace at
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1°C/min to induce thermal cracking. Samples were held at the maximum temperature for 1 hour before cooling to ambient temperature at the same rate. Measurements of permeability and elastic wave velocities were then made on the micro-fractured samples over the same range of effective pressures.

2.4 Imaging macro-fractured samples

Before proceeding to measure the permeabilities and elastic wave velocities of our macro-fractured samples, we used a micro-focus X-ray CT scanner with a spatial resolution of 5 μm to image the induced macro-fractures. The scanner used was the same instrument as that for which results are reported by Kawaragi et al. (2009) and Fukuda et al. (2010). Cross-sectional images were taken across the mid-plane of the samples using the minimum thickness setting of 0.065 mm.

X-ray CT images of two macro-fractured sample of SB are presented in Fig. 3. In these images, darker and lighter shades represent lower and higher densities, respectively. Fractures and pores therefore appear darker than the surrounding matrix. We observe that Brazil test splitting has produced two patterns of macro-fracturing; either a single dominant macro-fracture (Fig. 3a) or a set of three macro-fractures comprising a relatively straight central fracture and two adjacent fractures forming an hour-glass shape (Fig. 3b). We have commonly observed the fracture pattern seen in Fig. 3b in previous Brazil tests on fine-grained, brittle rocks in our laboratory. Use of the minimum thickness setting has also allowed individual pores to be observed. These are relatively sparse and unconnected.

During subsequent permeability measurements, the direction of fluid flow was parallel to the macro-fracture planes. For the elastic wave velocity measurements, P-waves propagated parallel to the macro-fracture planes and S-waves also propagated parallel to the macro-fractures but with their polarization direction normal to the macro-fracture planes.

3. Experimental results

3.1 Macro-fractured samples

Changes in the permeability, P-wave velocity and S-wave velocity of intact and macro-fractured samples of SB as a function of increasing effective pressure are shown in Fig. 4. Fig. 4a shows that the initial permeability of intact SB (sample SB(I)) is very low at approximately 10^{-19} m^{-2} , and that it decreases only marginally as P_{eff} is increased from 5 to 90 MPa. These observations reflect the paucity of pre-existing fractures in the as-received material. By contrast, the permeability of the sample with a single macro-fracture (SB(1F)) (Fig. 3a) is some 3.5 orders of magnitude higher at $P_{\text{eff}} = 5 \text{ MPa}$, while the sample with the three macro-fractures (SB(3F)) (Fig. 3b) is about 4.5 orders of magnitude higher at the same pressure. As might be expected, the permeabilities of the macro-fractured samples decrease much more rapidly with increasing P_{eff} than that for the intact sample, so that at the higher pressures the permeabilities of the two macro-fractured samples are essentially equal and less than 2 orders of magnitude greater than that of the intact sample.

Fig. 4b shows that the P-wave velocity increases only slightly with increasing pressure for all three samples. Not only are the increases very similar for both intact and macro-fractured samples, at around 3 %, but the absolute velocity values are also very similar. These similarities are entirely as expected, since both the propagation direction and the particle motion of the P-waves are parallel to the macro-fracture planes. Hence, the macro-fractures exert little influence on P-wave propagation in this direction.

Similarly, Fig. 4c shows that the S-wave velocity in sample SB(I) also increases by only about 4 % as effective pressure is increased from 5 to 90 MPa. However, in contrast to the P-wave velocities, the S-wave velocities for the both macro-fractured samples are demonstrably lower than that for the intact sample at every pressure. Furthermore, the S-wave velocity for sample SB(3F) is consistently lower than that for sample SB(1F). Again, these observations are entirely as expected, since although the S-wave propagation direction is parallel to the macro-fracture planes, the particle

1 motion is polarized normal to those planes. Hence, the macro-fractures exert a significantly greater
2 influence on S-wave propagation than for P-wave propagation. Not only that, but we also found that
3 we could not get sufficient signal amplitude to measure the S-wave velocity at the lower effective
4 pressures because of signal attenuation caused by the presence of the macro-fracture(s). For sample
5 SB(1F), we could not get a good signal below 20 MPa, and for sample SB(3F), we could not get a
6 good signal below 40 MPa (Fig. 4c).
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12 These results are therefore all consistent with the idea that the macro-fractures close
13 progressively with increasing effective stress. The macro-fracture apertures exert a large influence
14 on fluid permeability and a significant influence on S-wave velocities for waves polarized normal to
15 their length.
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25 3.2 Micro-fractured samples 26

27 Since X-ray CT scanning does not have sufficient resolution to allow us to observe the
28 micro-fractures induced in our samples of SB subjected to thermal stressing, we measured the
29 P-wave velocities of unsaturated intact and thermally-stressed samples at ambient pressure, as an
30 indicator of increased micro-fracture damage, before commencing measurements at pressure in the
31 permeameter. The intact sample had an axial P-wave velocity of 5.65 km.s^{-1} . After heating to 600°C ,
32 the velocity decreased markedly to 4.69 km.s^{-1} and, after heating to 800°C , the velocity decreased
33 further to 4.33 km.s^{-1} . This suggests that significantly more thermal micro-fracture damage was
34 induced in the sample heated to 800°C than in the sample heated to 600°C .
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49 Changes in the permeability, P-wave velocity and S-wave velocity of intact and micro-fractured
50 samples of SB as a function of increasing effective pressure are shown in Fig. 5 (the data for the
51 intact sample is the same as presented in Fig. 4). Fig. 5a shows that, once again, the introduction of
52 cracks leads to increases in fluid permeability; albeit micro-fractures rather than macro-fractures in
53 this case. The initial permeability of the sample heated to 600°C (SB(600)) is some 20 times higher
54 than that for sample SB(I), and that for the sample heated to 800°C (SB(800)) is close to 500 times
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1 higher. As for the macro-fractured samples, the permeabilities of the micro-fractured samples
2 decreased with increasing effective pressure, indicating crack closure.
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4 Fig. 5b shows that the pattern of behaviour of P-wave velocities in the micro-fractured rock
5 samples is significantly different from that seen for the macro-fractured samples (Fig. 4b). The
6 P-wave velocity in sample SB(600) is about 6 % lower than that for sample SB(I) at $P_{\text{eff}} = 5$ MPa,
7 while that for sample SB(800) is close to 12 % lower at the same pressure. These velocity
8 differences decrease in an essentially identical manner with increasing effective pressure so that by
9 90 MPa the P-wave velocity in SB(600) is only about 1 % lower than in SB (I) and in SB(800) it is
10 about 6 % lower. This supports the suggestion that thermal stressing to 800°C induces far more
11 micro-fracturing than thermal stressing to 800°C. However, while the micro-fractures exert a
12 smaller influence on permeability than the macro-fractures, it is clear from the changes in both
13 permeability and P-wave velocity with increasing effective pressure that the micro-fractures
14 are considerably more difficult to close. Fig. 5c shows that the pattern of behaviour of S-wave
15 velocities in the micro-fractured samples is essentially the same as that seen for P-wave velocities in
16 Fig. 5b.
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34 The similarities between the changes observed in P-wave and S-wave velocities occur even
35 though the particle motions are orthogonal. This suggests that, in contrast to the highly oriented
36 macro-fractures (Fig. 3), the micro-fractures induced by thermal stressing in our samples are
37 essentially isotropically distributed. This suggestion is entirely consistent with the results of
38 Vinciguerra et al. (2005), who reported an isotropic distribution of thermal microcracks and
39 isotropic elastic wave velocities in their thermally stressed samples of Seljadur basalt.
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4. Discussion

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4 We have seen from the results presented in Figs. 4 and 5 how the introduction of macro-fractures
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6 and micro-fractures into a rock with an essentially unfractured matrix can change the fluid
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8 permeability quite dramatically. It is clear that a few, long, low-aspect-ratio macro-fractures
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10 increase permeability much more than a much greater number of shorter, high aspect-ratio
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12 micro-fractures. However, the dominant influence of the macro-fractures is greatest at low effective
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14 pressure and when fluid flow is parallel to their long axes. Due to their low aspect ratio,
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16 macro-fractures are relatively easily closed by an increase in effective pressure, so that their overall
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18 influence declines at higher pressures. In contrast, while a distributed network of micro-fractures
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20 exerts a smaller influence on permeability overall, that influence appears to be maintained even at
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22 the highest effective pressures because their high aspect ratio makes them more difficult to close.
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24 However, we know that many natural materials, including rocks, contain fractures at different scales
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26 (i.e., both micro-fractures and macro-fractures).
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33 Ideally, therefore we would like to understand the interplay between these two fracture
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35 populations and how that may influence the change in permeability with increasing effective
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37 pressure (c.f. increasing depth in the crust). We therefore prepared a further sample of SB
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39 containing both macro-fractures and micro-fractures by thermally stressing sample SB(3F) by slow
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41 heating to 800°C. We then measured the fluid permeability and elastic wave velocities for this
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43 sample as a function of effective pressure in exactly the same way as described above for our other
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45 samples.
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50 The results of these measurements are presented in Fig. 6. The data for the intact sample, the
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52 macro-fractured sample and the micro-fractured sample in Fig. 6 are the same as those for sample
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54 SB(I) and sample SB(3F) in Fig. 4 and SB(800) in Fig. 5. We note in Fig. 6a that the permeability
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56 for the macro- and micro-fractured sample (SB(MM)) is essentially the same as that for sample
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58 SB(3F) at the lowest effective pressure (5 MPa). This observation confirms our earlier suggestion
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60 that low-aspect-ratio macro-fractures dominate fluid flow under these conditions. The addition of a
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population of high-aspect-ratio micro-fractures appears to contribute nothing to the fluid flow.

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2 However, this situation changes dramatically by the time we reach the highest effective pressure (90
3 MPa). Here, the macro-fractures and micro-fractures appear to contribute essentially equally to the
4 increase in permeability with respect to the intact sample. This is because the rate of permeability
5 decrease with increasing effective pressure is much lower for sample SB(MM) than for sample
6 SB(3F). We suggest that this occurs simply because the high-aspect-ratio micro-fractures are more
7 difficult to close than the low-aspect-ratio macro-fractures. We further observe that the permeability
8 for sample SB(800) is much lower than for sample SB(MM) at low pressure, but that the
9 permeabilities are virtually the same at the highest effective pressure, confirming the above
10 suggestion that the open micro-fractures increasingly dominate the permeability as effective
11 pressure is increased. However, it is also clear from Fig. 6a that both the macro-fractures and the
12 micro-fractures are still open at 90 MPa. We therefore suggest that if such measurements were
13 continued to even higher effective pressures then the micro-fractures would become even more
14 dominant over the macro-fractures in controlling fluid permeability. In the same way as for Figs. 4
15 and 5, the wave velocity data of Figs. 6b and 6c support this interpretation of permeability
16 evolution.

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18 However, while these are robust observations, it is also important to quantify how different
19 fractures populations influence fluid permeability in rocks. First we consider the influence of
20 micro-fractures using the model of Gueguen and Dienes (1989), who proposed the following
21 relationship:

$$k = \frac{2}{15} fw^2\zeta\varphi \quad (1)$$

22 where, k is the permeability, f is the percolation factor, w is the mean micro-fracture aperture, ζ is
23 their mean aspect ratio, and φ is their volume density. For $0.14 < \varphi < 0.4$, the percolation factor f
24 can be approximated by the following relation follows (Benson et al., 2006b):

$$f \approx \frac{9}{4} \left(\frac{\pi^2}{4} \varphi - \frac{1}{3} \right)^2 \quad (2)$$

Hence the permeability of a micro-fractured solid can be related to the aperture, aspect ratio and density of the micro-fractures.

There are several methods of determining the micro-fracture density of a solid. Here we compare two different methods; Hudson's model (Hudson, 1980, 1981) and the New Self Consistent Scheme (NSCS) (Yamamoto, 1981; Nara and Kaneko, 2006). Since Hudson's model is a "dilute solution", we can use it only for the case where the micro-fracture density is low and fractures are non-interacting. By contrast, the NSCS can be used for higher micro-fracture densities because it takes account of micro-fracture interactions. In order to determine the NSCS micro-fracture density we need an estimate of the aspect ratio of the micro-fractures. For simplicity, we make use of previously measured parameters for micro-fractured basalt. Vinciguerra et al. (2005) showed that the P-wave velocity in experimentally thermally fractured Seljadur basalt was very similar to that in naturally thermally fractured Etnean basalt, and Benson et al. (2006b) showed that the aspect ratio of micro-fractures in Etnean basalt remained essentially constant at approximately 0.001 when the permeability was lower than 10^{-16} m^2 and the crack density was lower than 0.4. Since both of these conditions are met in our case, we assume a micro-fracture aspect ratio of 0.001 in our calculations.

As reported above, the P-wave velocities in samples SB(800), SB(600) and SB(I), in dry conditions and ambient pressure, are 4.33, 4.69 and 5.65 km/s, respectively. Using these values and assuming that the Young's modulus and Poisson's ratio of the unfractured basalt matrix are 100 GPa and 0.22, respectively (following Benson et al., 2006b), the crack densities of samples SB(800), SB(600) and SB(I) were determined using both Hudson's model and the NSCS method. The calculated values are summarized in Table 1. Following this, the relations between permeability k and micro-fracture density ϕ were calculated for different values of crack aperture w from Eqs. (1) and (2), within the range of $0.14 < \phi < 0.4$.

The results are shown in Fig. 7, together with the permeabilities for SB(800) and SB(600) measured at the lowest effective pressure (5 MPa). Using the value for ϕ determined from the NSCS model, we see in Fig. 7 that the predicted micro-fracture apertures for samples SB(600) and SB(800) are in the range of $0.4 \sim 1.1 \text{ }\mu\text{m}$, which is very similar to the range of $0.5 \sim 0.8 \text{ }\mu\text{m}$

1 reported for basalt by Benson et al. (2006b) from SEM observations. By contrast, the Hudson
2 model predicts considerably larger apertures in the range 1.5 ~ 4.0 μm . We therefore suggest that
3 the NSCS method provides better estimates of fracture density and aperture because it takes account
4 of interactions between micro-fractures. It is also apparent from Fig. 7 that the higher permeability
5 of sample SB(800) over sample SB(600) is due to it having a higher micro-fracture density.
6
7 However, for the NSCS data, the fracture density increases by only 30 % from 0.30 to 0.39 while
8 the fracture aperture increases by 175 % from 0.4 to 1.1 μm . This suggests that the higher fracture
9 density (and associated higher permeability) is primarily due to an increase in fracture aperture.
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11 Second, we consider the influence of macro-fractures on permeability using the model of Walsh
12 (1981) who proposed the following expression to describe the effect of pressure on fluid flow
13 through macro-fractures:
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$$15 \quad k^{1/3} = A - B \ln P_{\text{eff}} \quad (3)$$

16 where A and B are empirical constants. The relations between $k^{1/3}$ and P_{eff} for macro-fractured
17 samples SB(3F) and macro- plus micro-fractured sample SB(MM)) are presented in Fig. 8. As noted
18 earlier, we see that the permeability for sample SB(MM) is essentially the same as that for sample
19 SB(3F) at the lowest effective pressure, suggesting the dominance of macro-fractures over
20 micro-fractures. However, the relative slopes of the $k^{1/3}$ vs. P_{eff} curves show that the permeability
21 for SB(3F) decreases much more rapidly with increasing effective pressure. We also note that there
22 is a significant change in the slope for SB(3F) at an effective pressure of around 20 MPa, and
23 interpret this as due to closure of the low-aspect-ratio macro-fractures in this sample. For sample
24 SB(MM), containing both micro- and macro-fractures, we also observe a significant change in slope
25 at a slightly higher effective pressure of around 30 MPa. Since we have seen that the
26 low-aspect-ratio macro-fractures are essentially closed at this pressure, we suggest that the
27 high-aspect-ratio micro-fractures increasingly dominate the fluid permeability at higher pressure.
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29 Due to this closure of the macro-fractures, we suggest that the Walsh model breaks down at
30 effective pressures greater than 20 ~ 30 MPa as micro-fractures start to dominate the fluid flow
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behaviour.

1 Overall, the results reported here clarify how different fracture populations within the same rock
2 influence the permeability and elastic wave velocities in that rock. While permeability always
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4 decreases as a function of increasing effective pressure in fractured rock (whether macro-fractures,
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6 micro-fractures or a combination of the two), the rate of change of permeability is also generally
7
8 seen to decrease with increasing effective pressure. However, that rate of change can alter
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10 significantly when there is a change in the dominance of one fracture population over another. We
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12 therefore suggest that any attempt at predicting permeability evolution in rock must first quantify
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14 and characterize the size and orientation of fracture populations in the rock and their sensitivity to
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16 changes in effective pressure.
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5. Conclusions

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4 For all samples studied, we found that permeability always decreased with increasing effective
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6 pressure. The decreases were smallest for intact samples, intermediate for the micro-fractured
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8 samples, and largest for the macro-fractured samples. For the sample with both macro-fractures and
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10 micro-fractures, we found that closure of the macro-fractures dominated the permeability reduction
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12 at the lower effective pressures, but that closure of the micro-fractures exerted an increasing relative
13
14 influence on permeability reduction with increasing effective pressure. We therefore conclude that
15
16 macro-fractures with low aspect ratios close more easily with increasing pressure, so that
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18 micro-fractures with high aspect ratios increasingly dominate the permeability at higher pressures
19
20 because they are more difficult to close. The associated variations measured in P-wave and S-wave
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22 velocities support this interpretation.
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12 obtaining the SEM images.
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Figure captions

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4 Fig. 1. Scanning Electron Microscope photomicrograph of intact Seljadur basalt.
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9 Fig. 2. Schematic diagram of the permeameter and elastic wave velocity measurement system used
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11 for all measurements in this study.
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16 Fig. 3. Micro-focus X-ray CT images of macro-fractured Seljadur basalt samples.
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18 (a): sample SB(1F) with a single axial macro-fracture, (b): sample SB(3F) containing three
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20 axial macro-fractures
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25 Fig. 4. Measurements of: (a) permeability, (b) P-wave velocity and (c) S-wave velocity with
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27 increasing effective pressure for intact and macro-fractured samples of Seljadur basalt; SB(I),
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29 SB(1F) and SB(3F), respectively.
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35 Fig. 5. Measurements of: (a) permeability, (b) P-wave velocity and (c) S-wave velocity with
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37 increasing effective pressure for intact and micro-fractured samples of Seljadur basalt; SB(I),
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39 SB(600) and SB(800), respectively.
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45 Fig. 6. Measurements of: (a) permeability, (b) P-wave velocity and (c) S-wave velocity with
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47 increasing effective pressure for intact, macro-fractured, micro-fractured and macro-fractured plus
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49 micro-fractured samples of Seljadur basalt; SB(I), SB(3F), SB(800) and SB(MM), respectively.
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54 Fig. 7. Relation between permeability and micro-fracture density calculated from the
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56 Gueguen-Dienes model for different crack apertures (w). Open symbols use micro-fracture densities
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58 from Hudson's model, and solid symbols use micro-fracture densities from the NSCS model.
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61 Triangles are measured permeabilities for sample SB(600), and circles are measured permeabilities
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for sample SB(800).

Fig. 8. Plots of the relation between the cube route of permeability and effective pressure from Walsh's model. Open symbols are measured data for the samples indicated.

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Table

Table 1. Density of micro-fracture in intact and micro-fractured basalt

| | φ (Hudson's model) | φ (NSCS) |
|---------|----------------------------|------------------|
| SB(I) | 0.082 | 0.10 |
| SB(600) | 0.19 | 0.30 |
| SB(800) | 0.23 | 0.39 |

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Figure1

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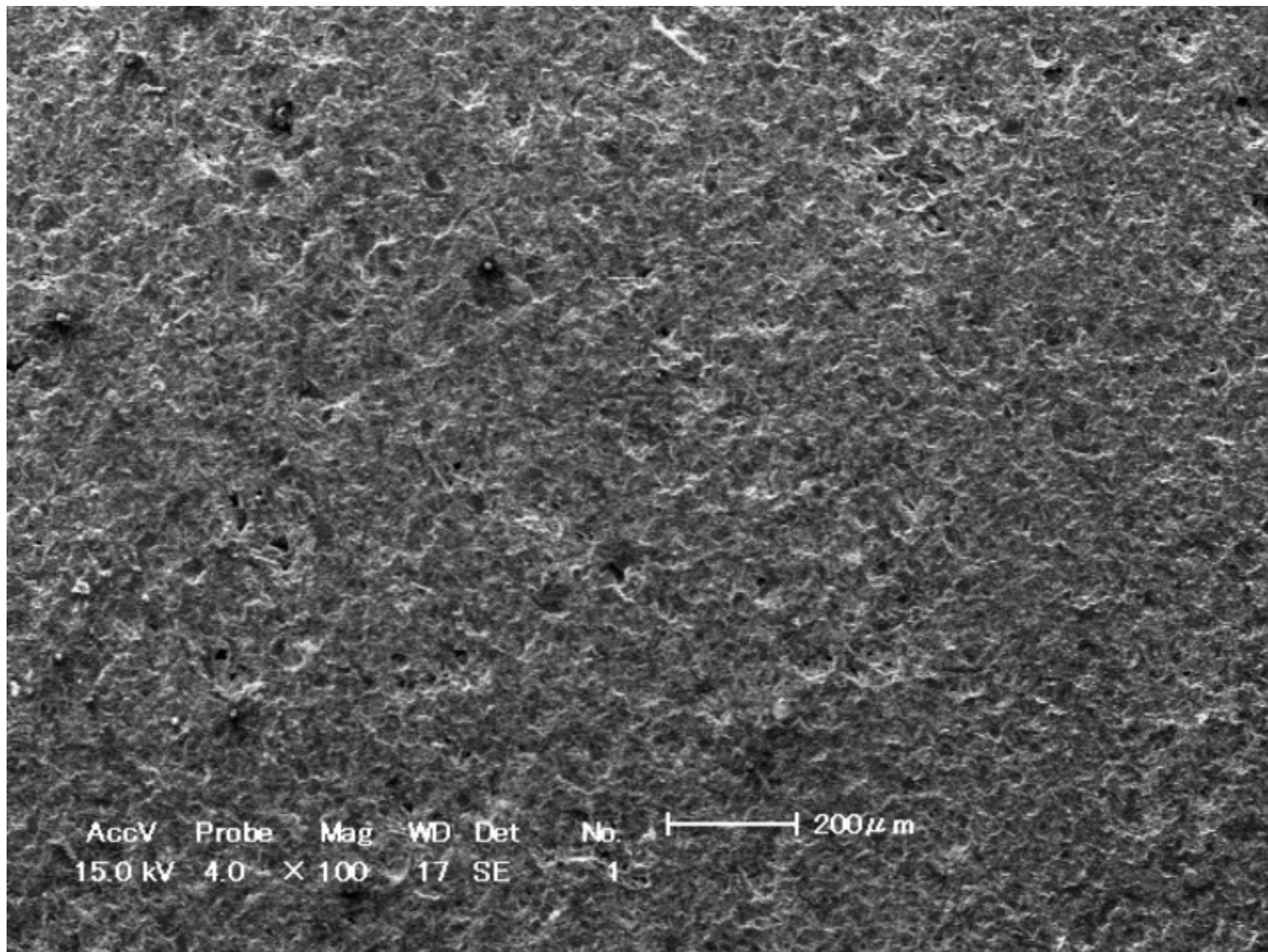


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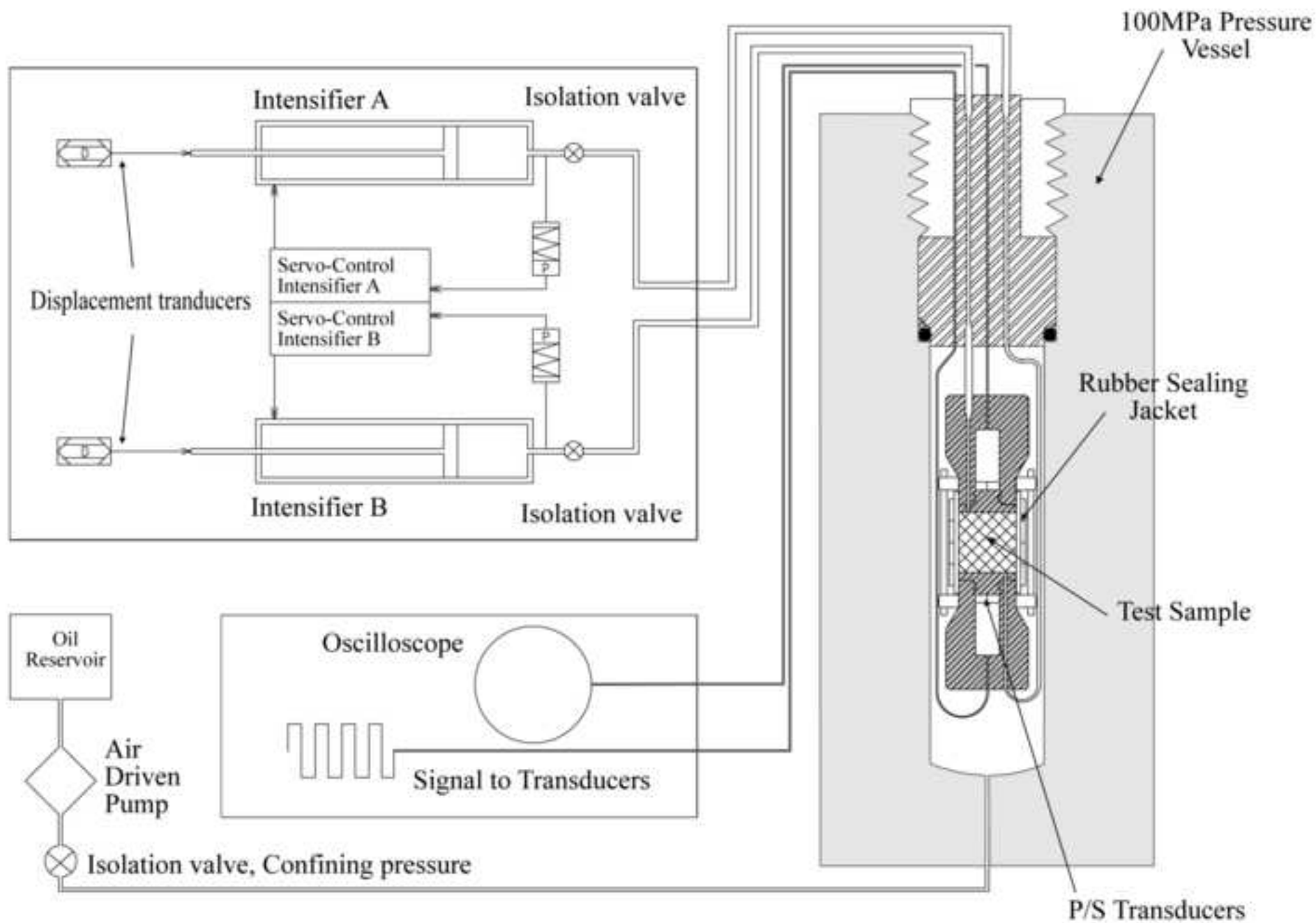
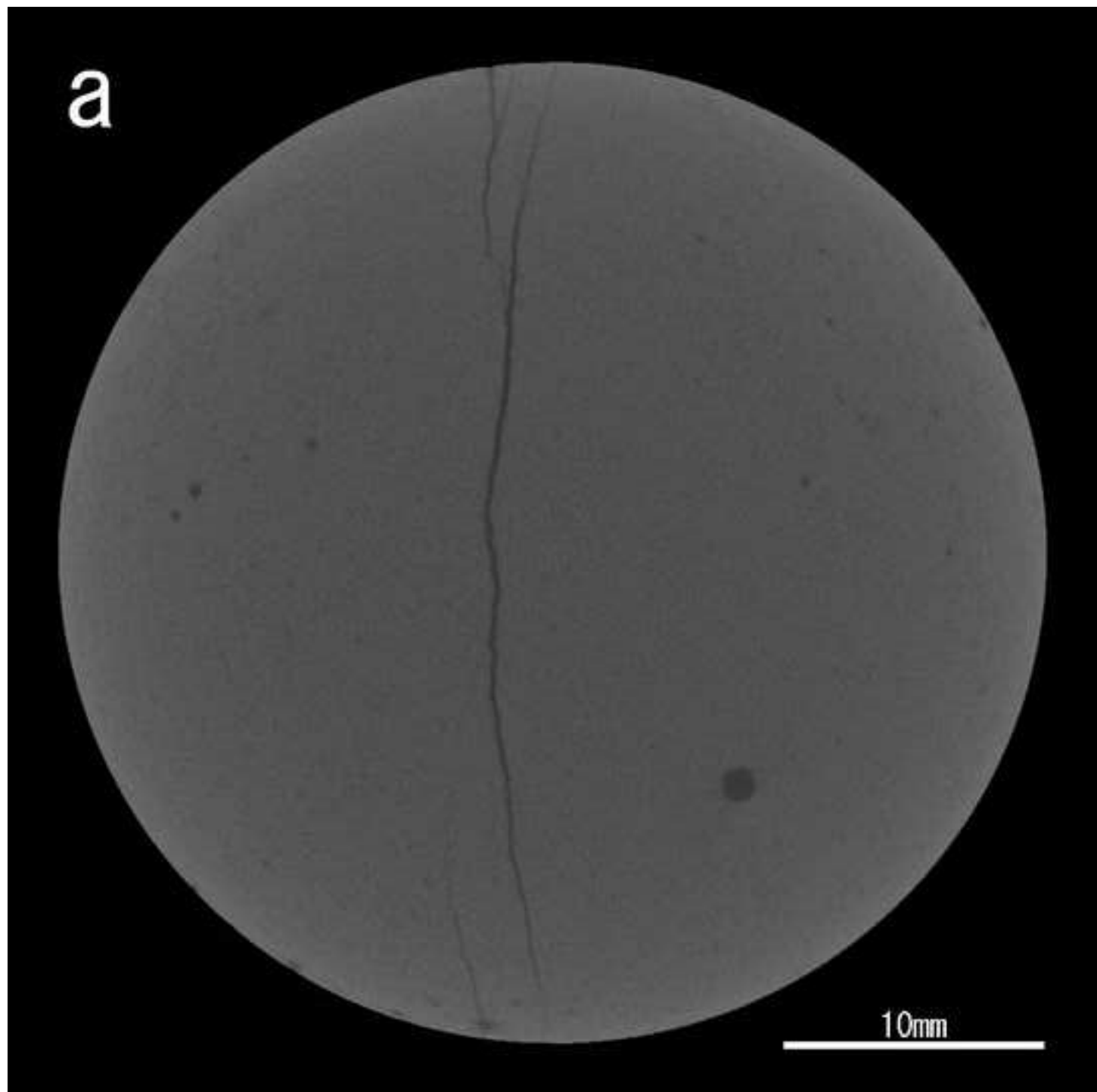


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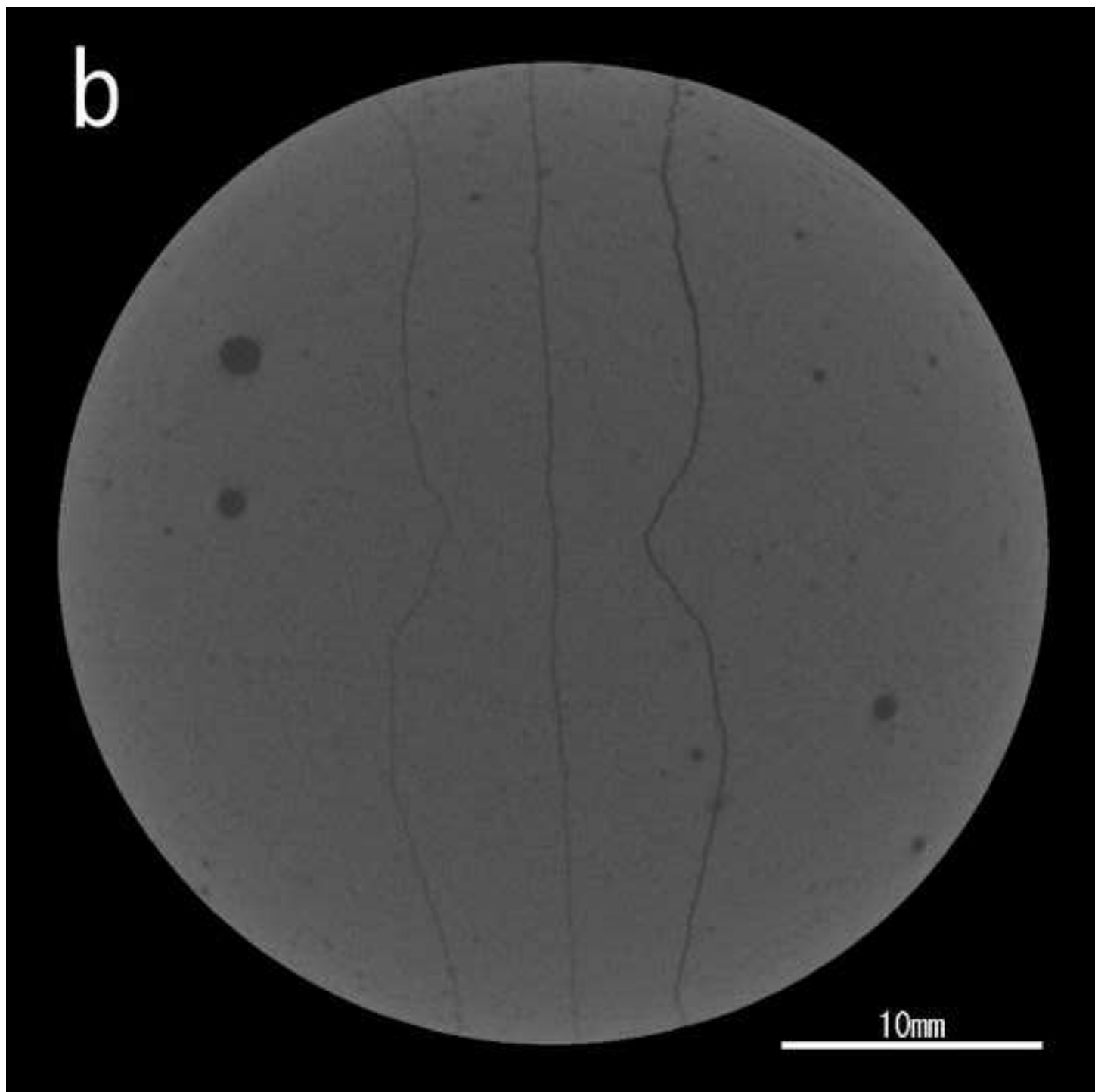


Figure4a

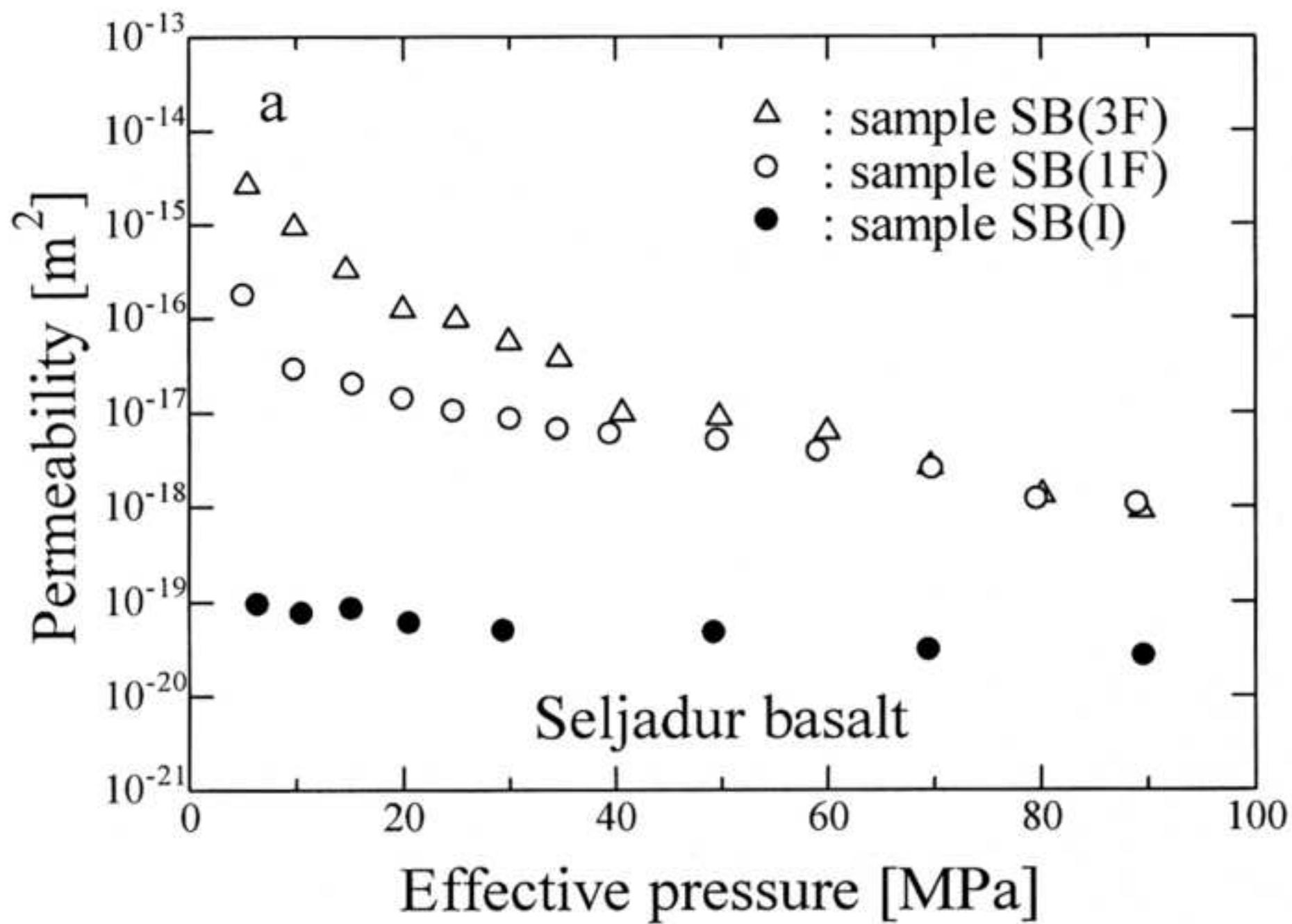
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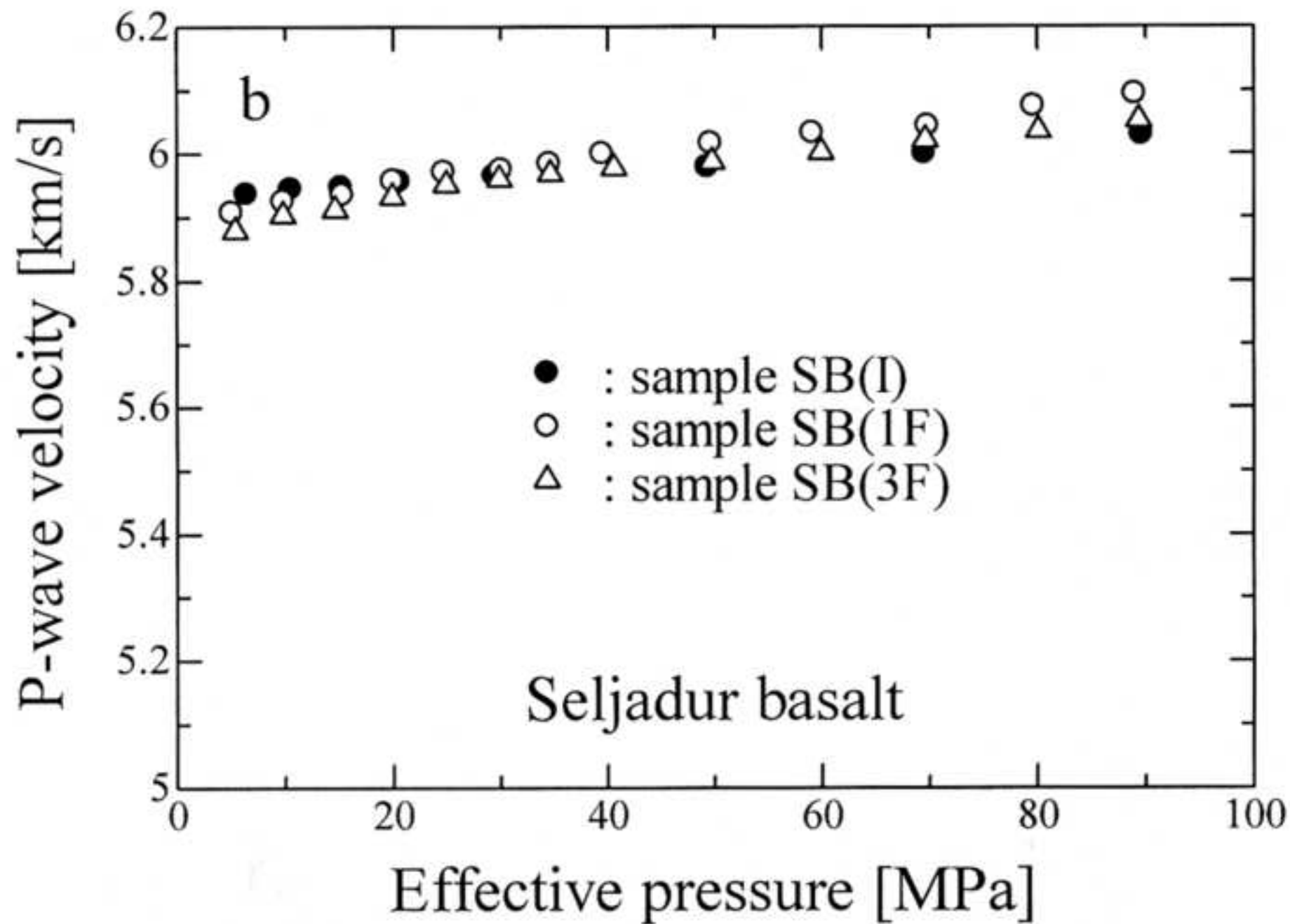


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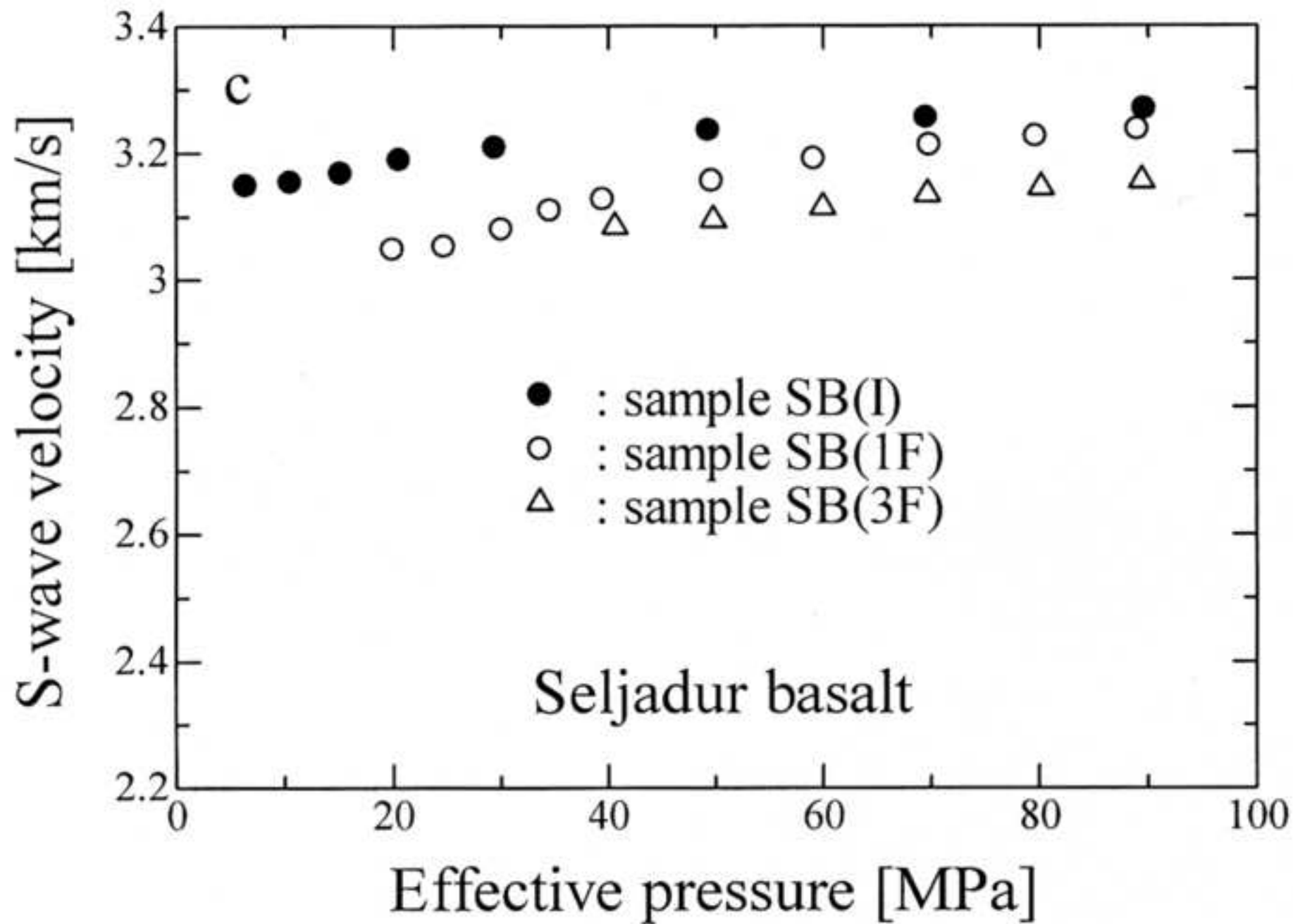


Figure5a

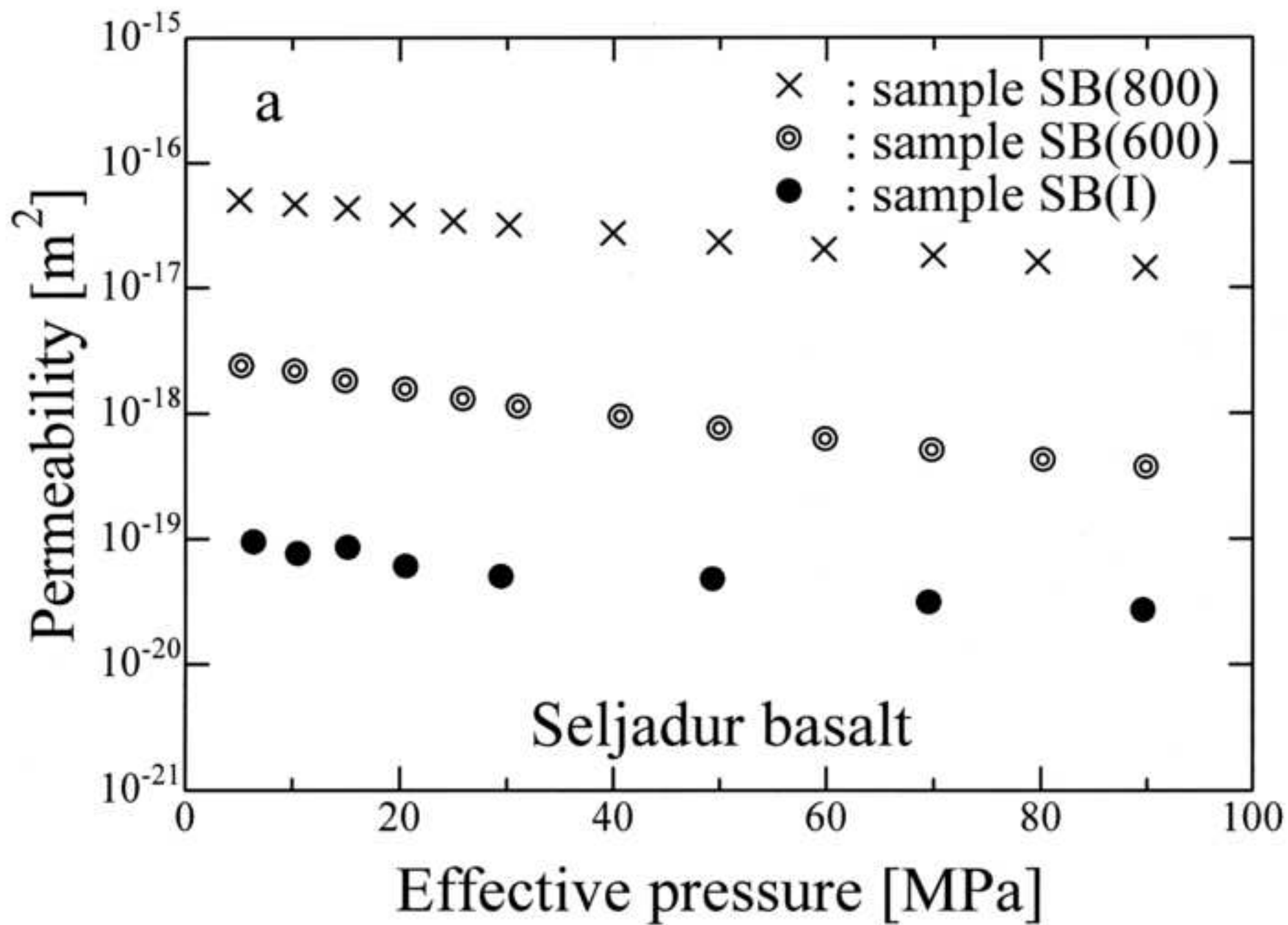
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Figure5b
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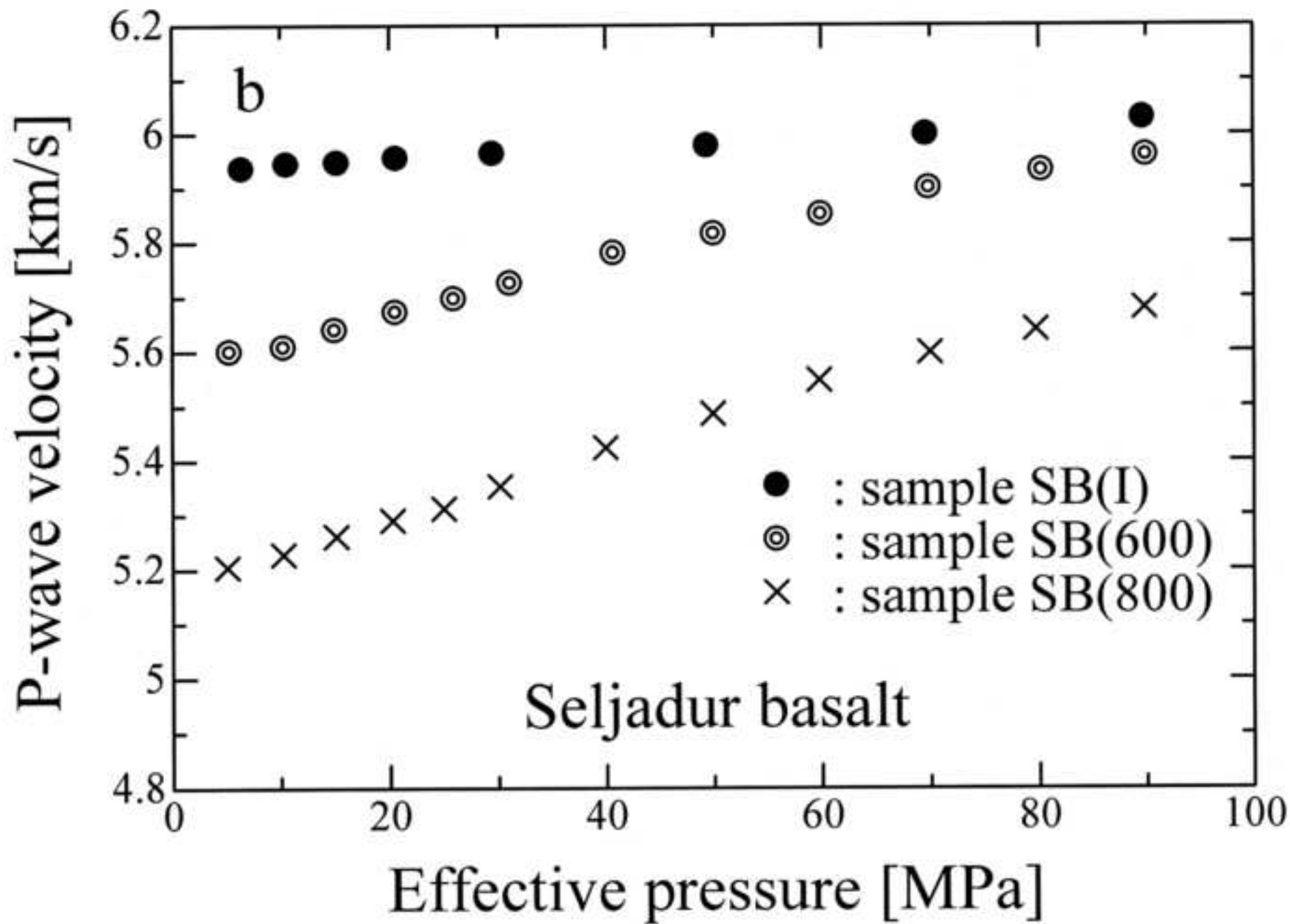


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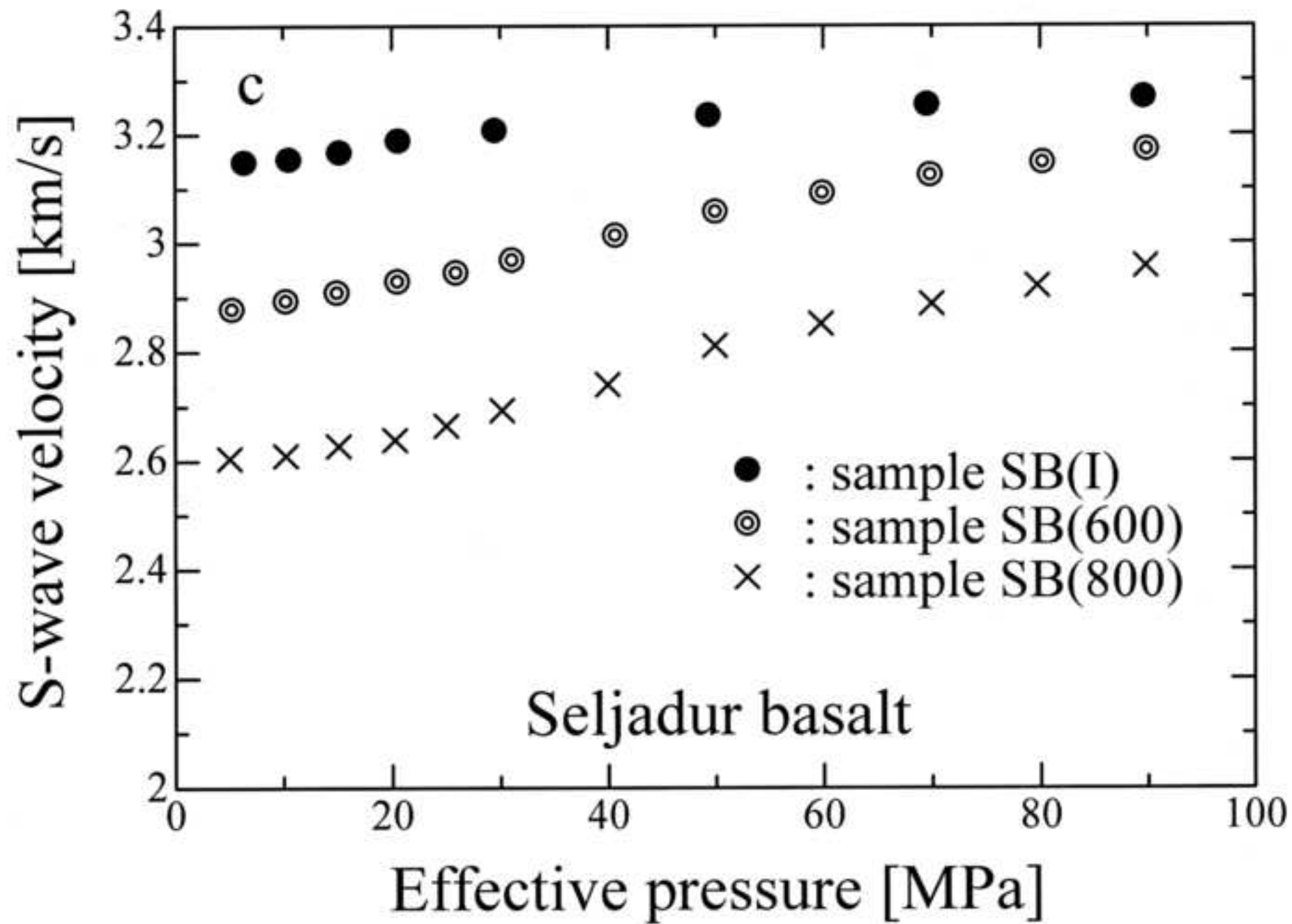


Figure6a

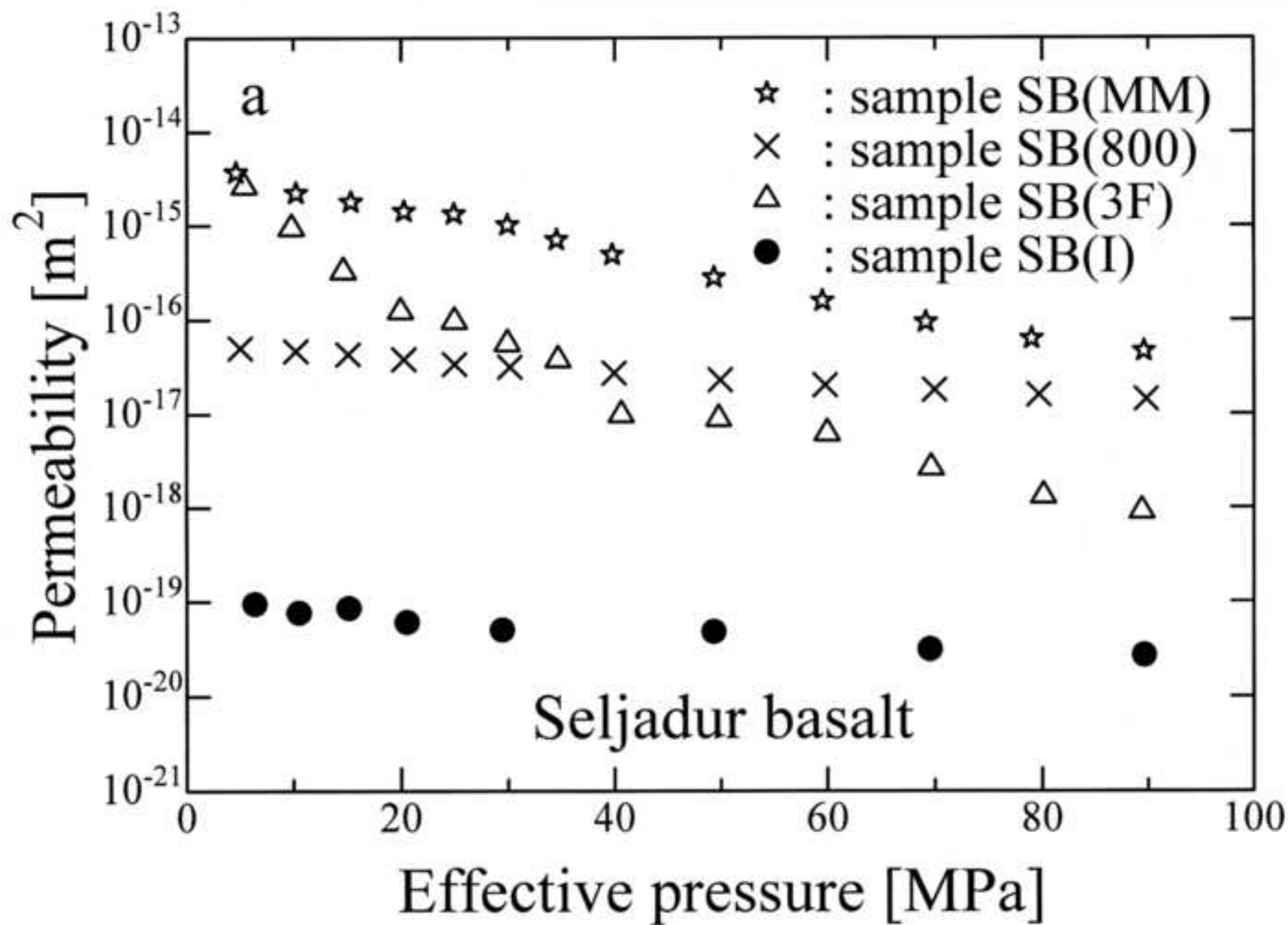
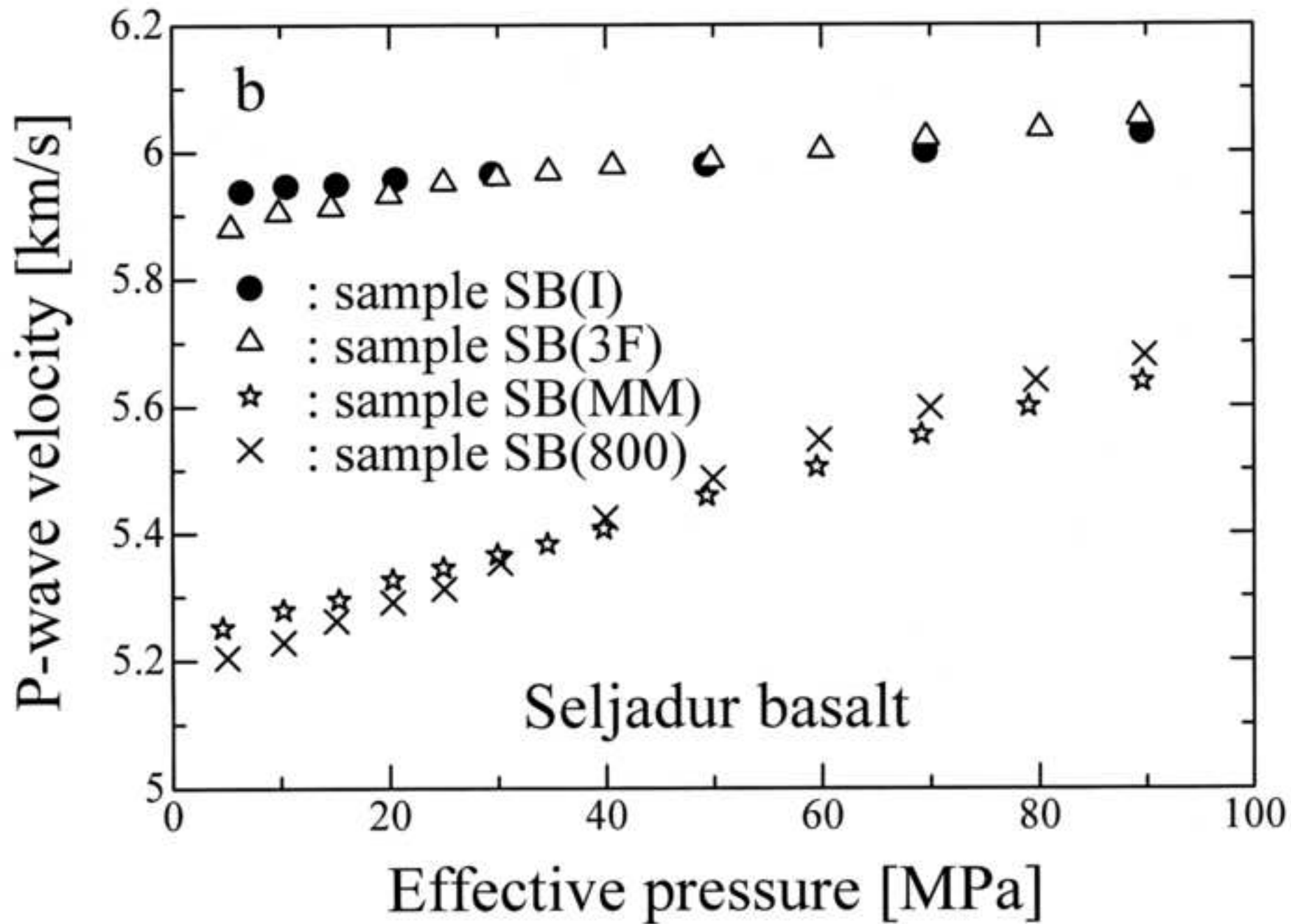
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Figure6b
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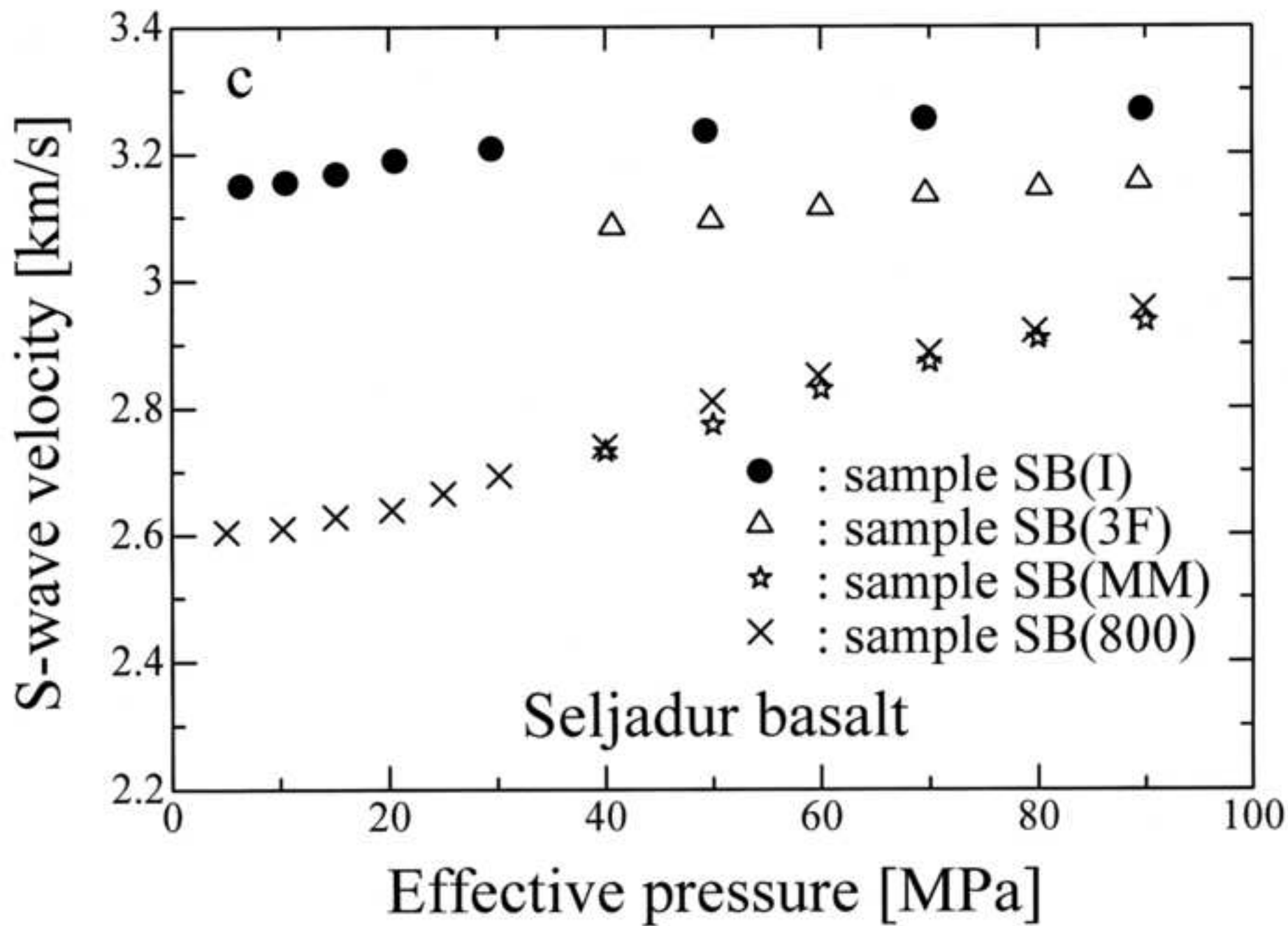


Figure7

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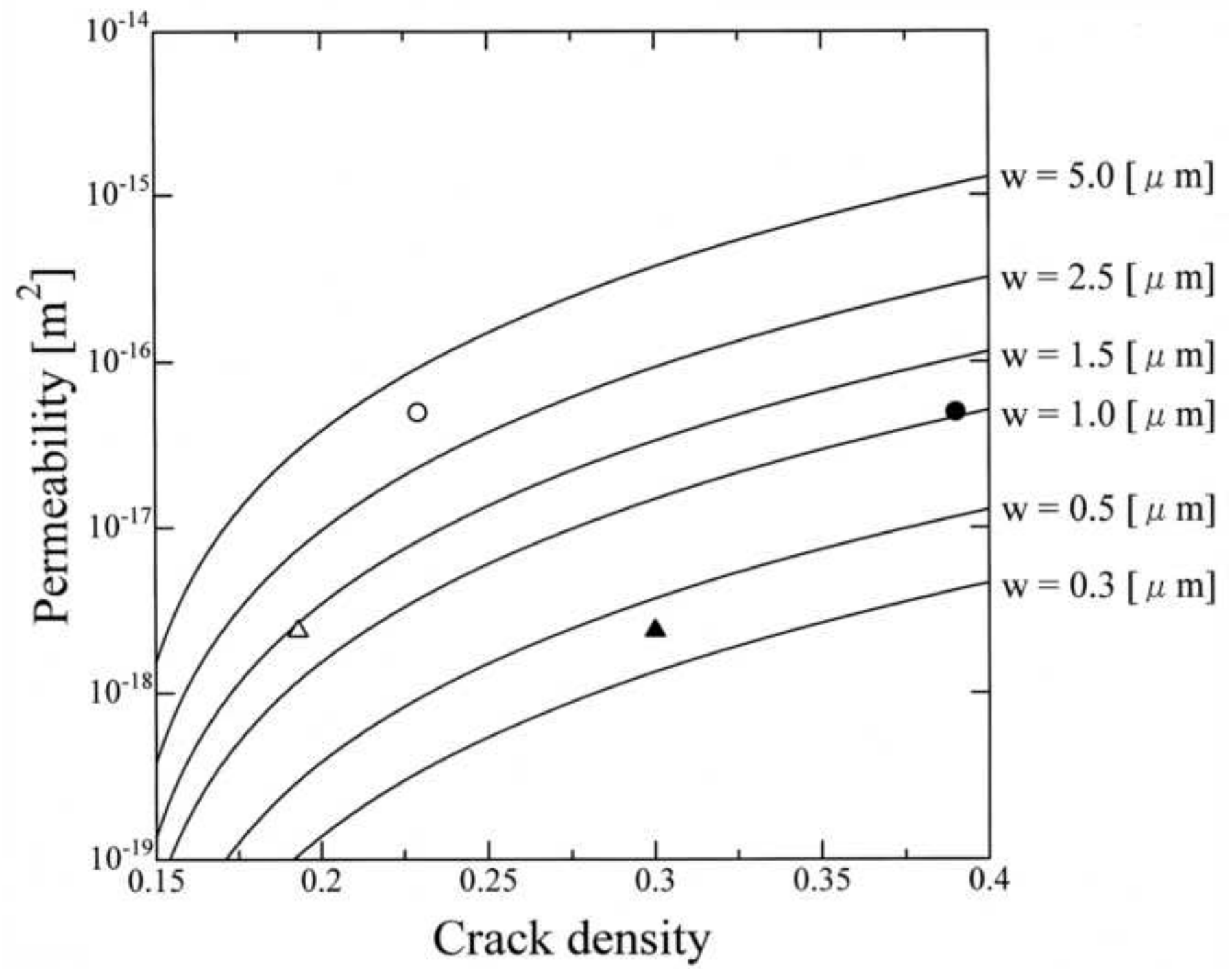


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