Fano resonance in a multimode tapered fiber coupled with a microspherical cavity

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Fano resonance in a tapered optical fiber in contact with a high-Q microsphere is demonstrated. Multimode waves propagating in a 2.3 \( \mu \)m diameter taper were coupled with a single whispering gallery mode of a 220 \( \mu \)m sphere, and their coherent interaction resulted in Fano resonance. The asymmetric line shapes of the transmission spectra changed periodically with scanning of the coupling position along the taper. The observed 24 \( \mu \)m period was due to modal dispersion in the tapered fiber. © 2005 American Institute of Physics. [DOI: 10.1063/1.1951049]

Fano resonance, originating in the interference between a discrete energy state and a continuum of states, is observed as a characteristically asymmetric line shape in transmission and reflection spectra. Anomalies occurring in diffractive gratings and photonic crystal spectra have been explained by the Fano effect. Fano resonance leads to a drastic change in transmittance and reflectance over a narrow spectral range, the Fano effect. The asymmetric line shape is expressed as

\[
E_i = \sum_j (t_j E_0 + q_j E_c),
\]

where \( t_j, q_j \) are the complex transmittances of the fields passing through the individual taper modes without coupling to the cavity and \( q_j \) are the complex coupling coefficients from the cavity to the output field through the multimodes. From Eqs. (1) and (2), the intensity transmittance is given by

\[
T = \left| \frac{E_i}{E_0} \right|^2 = \frac{\left| \frac{\rho}{\omega - \omega_c^0} + C_1 + C_2(\omega - \omega_c) \right|^2}{\left| \frac{\rho}{\omega - \omega_c} \right|^2 + \left( 1 - \alpha_c t_c \right)^2 \nu_c^2},
\]

where \( \rho = \sum_{j} \rho_j \) and \( \nu_c \) denotes a complex conjugate. The first and second terms in the numerator of Eq. (3) represent a symmetric Lorentzian dip of the whispering gallery mode, while the last term exhibits an asymmetric line shape. In the case of a single-mode tapered fiber, the asymmetric component does not appear \( C_2 = 0 \), while the interaction among the multiple taper modes gives \( C_2 \neq 0 \), which induces the Fano resonance.

When the coupling position is shifted by the distance \( x \) along the fiber axis, \( t_j \) is not changed but \( p_j \) and \( q_j \) are phase shifted as \( \left| q_j \right|^2 \) for \( j \), \( \exp(-i(\beta_j - \beta_i) x), \) where

\[
E_c = \frac{i \alpha_c \nu_c}{(\omega - \omega_c) + i(1 - \alpha_c t_c) \nu_c} \sum_j p_j E_0,
\]

where \( \alpha_c \) and \( t_c \) are the round-trip factor and the transmittance in the coupling region of the microsphere, respectively. The output field from the fiber waveguide is expressed as

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E_i = \sum_j (t_j E_0 + q_j E_c),
\]

where \( t_j, q_j \) are the complex transmittances of the fields passing through the individual taper modes without coupling to the cavity and \( q_j \) are the complex coupling coefficients from the cavity to the output field through the multimodes. From Eqs. (1) and (2), the intensity transmittance is given by

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The propagation constants \( \beta_j \) \((j = 1, 2, \ldots)\) are the propagation constants of the taper modes. Supposing that two taper modes are coupled with the cavity, the asymmetric line shape is periodically changed with the shifting of the coupling position, with the period being given by \(2\pi|\beta_1 - \beta_2|^{-1}\). It is noted that the coefficient \(C_1\) containing the parameter \(\tilde{p}\tilde{q}\) also changes with the displacement \(x\).

A tapered fiber was prepared from a fused-silica single-mode optical fiber. After stripping the polymer coating, the fiber was heated using a ceramic heater and stretched into a fine thread with a waist diameter of 2.3 \(\mu\text{m}\). This permitted the propagation of not only the fundamental propagation mode (HE\(_{11}\)), but also some higher-order propagation modes.\(^{12}\) Scanning electron micrographs indicated that there was no appreciable variation \(<0.1\ \mu\text{m}\) in the taper diameter over a 100 \(\mu\text{m}\) length. A microsphere having a stem was also fabricated from a single-mode fiber as follows. The tip of a fiber from which the coating had been stripped was irradiated with a CO\(_2\) laser causing the fiber to melt and, due to surface tension, to form into a sphere. A sphere with a diameter of 220 \(\mu\text{m}\) was used. The lowest radial-order modes of such a sphere satisfy the phase matching condition for coupling with the HE\(_{11}\), HE\(_{21}\), TM\(_{01}\) and TE\(_{01}\) modes of the 2.3 \(\mu\text{m}\) tapered fiber.\(^{12,13}\) A micrograph of the spherical microcavity attached to the multimode tapered fiber is shown in the inset of Fig. 1.

A tunable external-cavity laser diode with a linewidth of 300 kHz was coupled to the tapered fiber waveguide and the output light at the other end of the fiber was detected using a photodiode. The output intensity from the fiber when not coupled to the microsphere was 50 \(\mu\text{W}\). The laser frequency was scanned over a range of 18 GHz around a wavelength of 780 nm in order to observe the transmission spectra. The frequency was precisely calibrated by simultaneous measurement of the 5\(^2\)S\(_{1/2}\) (\(F = 3\)) \(-\rightarrow\) 5\(^2\)P\(_{3/2}\) transition peak of \(^{85}\)Rb set to the origin of frequency detuning. In order to control the relative position of the sphere and the tapered fiber in three dimensions, the microsphere was mounted on a piezoelectric stage. The microsphere was kept in contact with the taper waist and the contact point was scanned along the tapered fiber. The microsphere/tapered-fiber-waveguide system was placed in a chamber which was filled with dry air (humidity < 1.0\%) to reduce water adsorption that may cause adhesion forces at the surfaces. The chamber was kept at a stable temperature, which is necessary to avoid any resonant frequency shift in the microspherical cavity.\(^{14}\)

Figure 2 shows typical transmission spectra of the multimode tapered fiber/microsphere coupling system. These spectra were measured at different coupling positions, \(x = (a) 0\ \mu\text{m}, \ (b) 6\ \mu\text{m}, \ (c) 12\ \mu\text{m}, \) and \((d) 18\ \mu\text{m}\). The spectral intensity was normalized using the signal at off-resonant frequency. The spectra exhibit an intense resonance at a detuning frequency of 4.7 GHz, as well as two small dips at 3.8 GHz and 4.0 GHz. The shapes of the resonant dips are dependent on the coupling position. The dip at 4.7 GHz in Fig. 2(a) has a symmetric line shape with a linewidth of 160 MHz corresponding to a \(Q\) value of \(2.4 \times 10^6\). Characteristically asymmetric Fano resonance line shapes were clearly observed in Figs. 2(b) and 2(d). One shoulder of the dip comprises a steep slope including an overshoot, while the other shoulder has a moderate slope followed by a long tail. The dip in Fig. 2(c) is symmetric and much deeper than that of Fig. 2(a). The width of the left-side shoulders, which are defined as the frequency width required for a change in transmission from 90\% to 10\% of the dip depth, are (a) 320 MHz, (b) 130 MHz, (c) 290 MHz, and (d) 550 MHz. The two small dips at 3.8 and 4.0 GHz, which possess \(Q\) values of \(4.1 \times 10^6\) and \(1.0 \times 10^7\), respectively, exhibit the same change in shape as the dips described above, in spite of the difference in their widths and depths. It was confirmed that the spectral shapes did not change on increasing and decreasing the laser power. This indicates that, in the present experiment, thermal nonlinear effects caused by the introduction of the laser were negligibly small.

The coupling-position dependence of the resonant spectra is shown as a three-dimensional plot in Fig. 3. Transmission spectra were measured at every 1 \(\mu\text{m}\) displacement within a scan range of 45 \(\mu\text{m}\). The shapes of the spectra gradually change over the scan range. Clearly, the three-dimensional plot shows a periodicity in the change in the spectra with respect to the displacement. The intensity at the dip and the side peaks varies sinusoidally with a period of 24 \(\mu\text{m}\). The data were highly reproducible on backward scanning.

Theoretical analysis\(^ {12}\) has shown that, at a 780 nm wavelength, the fundamental HE\(_{11}\) mode and the HE\(_{21}\), TM\(_{01}\) and TE\(_{01}\) modes were observed.
TE$_{01}$ modes of the 2.3 $\mu$m tapered fiber possess propagation constants of $1.154 \times 10^7$ m$^{-1}$, $1.129 \times 10^7$ m$^{-1}$, $1.127 \times 10^7$ m$^{-1}$, and $1.131 \times 10^7$ m$^{-1}$, respectively. For the mode pairs HE$_{11}$/HE$_{21}$, HE$_{11}$/TM$_{01}$ and HE$_{11}$/TE$_{01}$, the calculated periods $2\pi[\beta_j - \beta_k]^{-1}$ are 24.5 $\mu$m, 23.1 $\mu$m, and 27.1 $\mu$m, respectively. Since a single whispering gallery resonance is either a TM or TE mode, coupling from both TM$_{01}$ and TE$_{01}$ taper modes into a single cavity mode of the microsphere cannot occur simultaneously. The experimental results show the period to be 24 $\mu$m, falling between 23.1 and 24.5 $\mu$m. This suggests that the dip observed in Fig. 3 can be ascribed to the TM microspherical resonance mode coupled with the HE$_{11}$, HE$_{21}$ and TM$_{01}$ taper modes but not coupled with the TE$_{01}$ wave. Furthermore, this suggests that the period is determined by the amplitude ratio between the HE$_{21}$ and TM$_{01}$ mode waves which are coupled to the cavity. The details of this analysis, which is based on the theory developed for multiple-input-output cavity systems, will be presented elsewhere.

In conclusion, Fano resonance in a multimode taper waveguide coupled with a microspherical cavity has been demonstrated. Dependent on the coupling position, the asymmetric line shape of the transmission spectrum was observed to change. This phenomenon is due to the modal dispersion in the tapered fiber and the multimode coupling between the taper and the microsphere. The steep transmission change originating from the high quality factor of a microsphere can be further enhanced by the Fano effect. In comparison to the single-mode-waveguide/cavity system using partially reflecting elements, the present system has the advantages of simplicity of device fabrication and controllability of the Fano resonance line shapes.

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