Quasi-unidirectional shrinkage of gels with well-oriented lipid bilayers upon uniaxial stretching†

Tasuku Nakajima,⁎a Corentin Durand,bc Xu Feng Li,c Md. Anamul Haque,ad Takayuki Kurokawaa and Jian Ping Gong*a

PDGI–PAAm gels with well oriented lipid bilayers show a quasi-unidirectional shrinkage upon uniaxial stretching along the bilayers. They shrink largely parallel to the bilayer but slightly perpendicular to it in order not to increase the bilayer area and its interfacial energy. Such an anisotropic deformation can be well-modelled based on classical theories for gel networks and lipid layers.

Generally, gels have an isotropic network structure and show an isotropic deformation as shown in Fig. 1(a). One of the typical examples is free swelling. When isotropic gels are immersed in solvents, the deformation (swelling) ratio of each direction α is ideally same. Another example is uniaxial stretching experiment. Note that gels’ Poisson’s ratio is very close to 0.5 if solvent exchange is not accompanied by deformation. ¹ When gels are uniaxially stretched along the x-axis with the deformation ratio of λₓ, they similarly shrink along the y and z-axes with the deformation ratio of λ⁻⁰.⁵. On the other hand, if any restriction is introduced to the gels, the deformation of such gels does not follow the formulas of isotropic gels.²⁻⁵ For example, when a hydrogel having a liquid crystalline structure is put under a magnetic field, the orientation of the liquid crystal induces an anisotropic swelling of the gel.² A spherical gel surrounding a hard core shows a water content distribution at the equilibrium state due to the swelling constraint near the core.³ If a gel with a patterned cross-linking distribution swells, many bumps are formed on its surface due to the swelling degree distribution.⁴ One kind of gel having such restrictions, the PDGI–PAAm gel with thousands of monodomain lamellar bilayers, has been reported.⁶⁻⁹ This gel consists of hard, uniaxially-oriented sheet-like poly(dodecyl glycidyl itaconate) (PDGI) lipid bilayers fixed within soft PAAm gel as the matrix. The structure of a PDGI–PAAm gel is shown in Fig. 1(b). The monodomain PDGI bilayer structure is realized by applying a strong shear when the gel precursor solution is poured into a mould.⁶ This gel shows brilliant structural colour due to its well-oriented and periodic lamellar structure. This colour can be modulated by external stimuli such as mechanical force,⁶,⁸ pH and temperature.⁹

One of the most remarkable behaviours of a PDGI–PAAm gel is unidirectional swelling, shown in Fig. 1(b).⁶ When the PDGI–PAAm gel with an oriented PDGI bilayer in the x–y plane is swollen in water, this gel swells only along the z-axis, which is perpendicular to the bilayer plane. Such unidirectional swelling of gels with a layered structure has been also reported by Kang et al.¹⁰ This strange phenomenon is because increasing the area

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Fig. 1 (a) Size change of an isotropic gel upon swelling and uniaxial stretching. (b) The structural model and unidirectional swelling behaviour of a PDGI–PAAm gel with hard monodomain lipid bilayers in the soft gel matrix.
of the bilayer is energetically unfavourable. The amorphous PAAm gel layers tend to keep their “shape” during swelling as explained above, whereas lipid bilayers tend to keep their “area” upon deformation to maintain a low surface energy. If a PDGI–PAAm gel swells along the x or y-axes, this process is always accompanied by an area expansion of the bilayer, which is energetically unfavourable. As a result, a PDGI–PAAm gel tends to swell only along the z-axis. More precisely, Wang and Hong have proposed a simple theoretical model to explain this anisotropic swelling of PDGI–PAAm gels.11

As such anisotropic PDGI–PAAm gels show anisotropic swelling due to the bilayers, they also should show anisotropic deformation upon uniaxial stretching. Although this prediction is interesting from the physical point of view, no study for this subject has been reported. Thus, the aim of this study is to investigate how PDGI–PAAm gels deform anisotropically upon uniaxial stretching. In this paper, we investigate the deformation behaviour of PDGI–PAAm gels upon uniaxial stretching by experiments first, then we establish the theoretical model to explain these experimental phenomena.

Fig. 2(a) shows the changes of λx, λy, and λz of the uniaxially-stretched PDGI–PAAm gel upon changing the deformation ratio along the x, y and z-axes caused by uniaxial stretching. Both sides of the gel samples were fixed by two clips and uniaxially stretched along the x-axis slowly by hand to several desired deformation ratios, λx. Here, it should be noted that the following measurements of λy and λz have been done after waiting for more than 90 s until complete relaxation (see Fig. S1 of the ESI† for stress relaxation tests). λy was determined by direct measurement of the gel width analysed from the pictures of the deformed gels shown in Fig. 2(a). λz was determined by reflection spectrum measurements of the gels with a Hamamatsu Photonics KK, C10027 device. The distance of two adjacent lamellar sheets, d, for each λz was calculated from the peak wavelength of the reflection spectra by using Bragg’s law (concept for the measurement and raw spectra are shown in Fig. 2(b) and (c), respectively). As a change of d should be proportional to a change of gel thickness along the z-axis, λz can be calculated as λz = d/d0, where d0 is d in the reference state. At any λx, the calculated change of gel volume λxλyλz is almost 1, which verifies the accuracy of our measurements of λy and λz (see Fig. S2 of the ESI†).

Fig. 3(a) shows the changes of λy and λz of the uniaxially-stretched PDGI–PAAm gel upon changing the deformation ratio along the x-axis, λx. The anisotropic PDGI–PAAm gel did not follow the formula for determining λx, λy, and λz can be indirectly determined from the layer distance, d, which can be measured by the reflection spectra with Bragg’s law. (c) Reflection spectra of the deformed gels with several λx values. In this experiment θ was 60°.
unidirectional shrinkage has been also reported by Finkelmann and Nishikawa using a monodomain thermotropic liquid crystal (LC) elastomer. As their elastomer has modulus anisotropy, it mainly shrinks along the soft direction when stretched uniaxially. Our system, which can be called a monodomain lyotropic LC gel having modulus anisotropy, seems to show a similar shrinkage to Finkelmann’s system. However, surprisingly, our gel shrinks along the ‘hard’ direction, which is the opposite to their system.

To understand the reason for the unidirectional shrinkage and the difference in shrinking direction of PDGI–PAAm gels, we studied the changes of the PDGI bilayer area. This is because not the uniaxial deformation ratio but the area expansion ratio is important when considering the mechanics of lipid membranes. For this reason, we also calculated the change of $\lambda_x\lambda_y$, which corresponds to the area expansion ratio of the PDGI bilayer with changes of $\lambda_x$. The results are also shown in Fig. 3(a). Though isotropic gels should follow $\lambda_x\lambda_y \propto \lambda_y^{0.5}$, the anisotropic PDGI–PAAm gel followed the different relationship of $\lambda_x\lambda_y \propto \lambda_y^{0.07}$, which has quite a small value of the exponent. This strange deformation behaviour of the PDGI–PAAm gel suggests that it deforms while keeping the change of bilayer area to a minimum. This conclusion is convincing if we imagine the expansion of conventional lipid layers. Generally, an expansion of layer area requires a large energy due to the generation of an expansion of conventional lipid layers. Generally, an expansion of layer area requires a large energy due to the generation of an expansion of conventional lipid layers.

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Based on these findings, we tried to establish simple theoretical models for such a quasi-unidirectional shrinkage of the PDGI–PAAm gels upon uniaxial stretching. The Helmholtz free energy change per unit volume, $\Delta F_{\text{total}}$ (J m$^{-3}$), of conventional neutral gels upon deformation is the sum of two contributions: the mixing term and elastic term of the network. In our case, as the volume change of the gels due to elongation is negligible, the mixing term can be ignored. In addition, as the PDGI–PAAm gel contains bilayers, the elastic term of the bilayers also should be considered. As a result, we obtain $\Delta F_{\text{total}}$ (J m$^{-3}$) of the PDGI–PAAm gels upon uniaxial deformation as:

$$\Delta F_{\text{total}} = \Delta F_{\text{el,g}} + \Delta F_{\text{el,d}}$$

where $\Delta F_{\text{el,g}}$ and $\Delta F_{\text{el,d}}$ are the elastic terms of the gels and PDGI bilayers, respectively. For $\Delta F_{\text{el,d}}$, we simply adopt classical neo-Hookean rubber elasticity theory as:

$$\Delta F_{\text{el,d}} = \frac{E_{\text{gel}}}{6} \left( \lambda_x^2 + \lambda_y^2 + (\alpha'\lambda_z)^2 - (2 + \alpha') \right) \times \frac{d_0 - d_{\text{gel}}}{d_0}$$

where $E_{\text{gel}}$ (Pa) is Young’s modulus of the PAAm layer, $\alpha'$ is the swelling ratio of the PDGI–PAAm gels along the $z$-axis (see Fig. 1) and $d_{\text{gel}}$ (m) is the thickness of a single PDGI bilayer. The reason for the presence of the $\alpha'$ coefficient before $\lambda_z$ is because the PAAm network is already pre-stretched along the $z$-axis at the reference state due to unidirectional swelling. The final $(d_0 - d_{\text{gel}})/d_0$ indicates the volume fraction of the PAAm matrices in the PDGI–PAAm gels.

For $\Delta F_{\text{el,d}}$ we consulted elastic lipid membranes. According to the literature, the Helmholtz free energy change per single lipid molecule upon membrane extension, $\Delta \mu$ (J), can be roughly estimated as:

$$\Delta \mu = \frac{\gamma}{\alpha} (a - a_0)^2$$

where $\gamma$ (N m$^{-1}$) is the interfacial tension, $a$ (m$^2$) is the interfacial area occupied by a single lipid molecule and $a_0$ is $a$ in the initial state, which should be the optimum interfacial area. Under the assumption that the area expansion ratio of a whole membrane $\lambda_x\lambda_y$ is equal to that of each single molecule $a/a_0$, eqn (3) can be rewritten as:

$$\Delta \mu = \frac{\gamma}{\lambda_x\lambda_y} (a - a_0)^2.$$ 

A single PDGI bilayer sheet having a unit surface area at the initial state consists of 2/$a_0$ PDGI molecules (the coefficient 2 is because of the ‘bi’-layer). Also, the volume of a single PDGI bilayer sheet with unit surface area is $1 \times 1 \times d_{\text{gel}}$. Hence, $\Delta F_{\text{el,d}}$ (J m$^{-3}$), which is the free energy change of the PDGI bilayers per unit volume of the PDGI–PAAm gel, can be calculated as:

$$\Delta F_{\text{el,d}} = \frac{\Delta \mu}{a_0} \frac{1}{d_{\text{gel}}} \times \frac{d_{\text{gel}}}{d_0} = \frac{2\gamma}{\lambda_x\lambda_y} \frac{d_0}{a_0} (\lambda_x\lambda_y - 1)^2.$$ 

The $d_{\text{gel}}/d_0$ in the second term indicates the volume fraction of the PDGI bilayers in the PDGI–PAAm gel. By substituting eqn (2) and eqn (5) into eqn (1) and using the relationship $\lambda_x\lambda_y = 1$, we finally obtain:

$$\Delta F_{\text{total}} = \frac{E_{\text{gel}}}{6d_0} \left( \lambda_x^2 + \lambda_y^2 + (\alpha'\lambda_z)^2 - (2 + \alpha') \right) \left( d_0 - d_{\text{gel}} \right)$$

$$+ \frac{2\gamma}{\lambda_x\lambda_y} \lambda_x\lambda_y (\lambda_x\lambda_y - 1)^2.$$ 

Using the experimental parameters $d_0 = 251$ nm, $d_{\text{gel}} = 4.7$ nm, $\alpha' = 2.1$ and $E_{\text{gel}} = 0.01$ MPa (roughly estimated from the compression test shown in ref. 6), we calculated the $\lambda_x$ which gives the lowest $\Delta F_{\text{total}}$ for various $\lambda_x$ values using a numerical calculation technique with $\gamma$ as the fitting parameter. Fig. 4 shows the fitting results of the $\lambda_x$, $\lambda_y$ and $\lambda_x\lambda_y$ dependence on $\lambda_z$. If $\gamma = 10.0$ mN m$^{-1}$ was used, the fitting lines almost overlapped with the experimental results. This value of $\gamma$ is comparable to the reported values of $\gamma \approx 10$–100 mN m$^{-1}$ for some synthetic or natural lipid membranes. These facts confirm the adequacy of our simple theory.
Finally, we should comment on the difference between the results of this work and our previous work. This time we observed almost no colour change upon stretching. On the other hand, in our previous work, we have shown uniaxial deformation-induced colour changes. The reason for this difference is probably that in the previous work we measured the reflection spectra before relaxation, whereas in this work we did it after relaxation. We have confirmed that the colour of the gel changes upon fast uniaxial deformation, while it slightly changes upon slow deformation.

In conclusion, we have found a quasi-unidirectional shrinkage of the PDGI–PAAm gels with well-oriented lipid bilayers. When they are stretched parallel to the bilayer, they tend to deform along the direction perpendicular to it without increasing the bilayer area. A simple theoretical model based on the elasticity of the gel network and lipid layer can well explain such an anisotropic deformation. In the future, the design and creation of novel lipid layer-gel composites showing unique and anisotropic deformations based on this theory are expected. Such materials could possibly be applied to artificial muscles with unique motions.

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Notes and references


