NMR Study of Carrier Doping Effects on Spin Gaps in the Spin Ladder $\text{Sr}_{14-x}\text{A}_x\text{Cu}_{24}\text{O}_{41} (A = \text{Ca}, \text{Y}, \text{and La})$

Ken-ichi Kumagai and Sigenori Tsuji

Department of Physics, Graduate School of Science, Hokkaido University, Sapporo 060, Japan

Masatsune Kato and Yoji Koike

Department of Applied Physics, Faculty of Engineering, Tohoku University, Sendai 980-77, Japan

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Carrier doping effects on spin dynamics in $\text{Sr}_{14-x}\text{A}_x\text{Cu}_{24}\text{O}_{41} (A = \text{Ca}, \text{Y}, \text{and La})$ are investigated by Cu NMR and NQR. The energy gaps in the spin excitation spectra (spin gap) are confirmed to be $\Delta = 140 \text{ K}$ for the CuO$_2$ chain and $\Delta = 470 \text{ K}$ for the Cu$_2$O$_3$ ladder in Sr$_{14}$Cu$_{24}$O$_{41}$. The spin gap for the ladder increases with the Y and La substitutions for Sr (up to $x = 3$), while it decreases with increasing $x$ in Sr$_{14-x}$Ca$_x$Cu$_{24}$O$_{41}$ and seems to collapse around $x = 13$ of the Ca substitution. Hole-doping effects on the spin gaps for the ladder configuration are interpreted in terms of magnon and hole-depairing excitations for the spin $S = \frac{1}{2}$ ladder. [S0031-9007(97)02578-7]

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The discovery of high-$T_c$ superconductivity in lightly doped antiferromagnets has provided much interest in low-dimensional quantum spin systems. In order to obtain insight into the physics of the high-$T_c$ superconductivity, the Heisenberg spin-ladder systems, which consist of two (or more) chains of magnetic coupled ions, have been investigated intensively, since novel quantum phenomena appear in spin-ladder system [1–6]. The spin degree of freedom in the single ladder is well described by the Heisenberg Hamiltonian

$$H = J\sum S_i S_{i+1} + J'\sum S_i S_j,$$

where $J$ and $J'$ are exchange couplings along the legs and the rungs of the ladder, respectively. Recent theories predicted that the $S = \frac{1}{2}$ antiferromagnetic spin ladder forms a spin liquid state and has an energy gap in the spin excitation spectra (spin gap) for ladders with even numbers of leg, but has no gap for odd-numbered leg systems. Theories [3,4] predicted also that the frustrated spin liquid state with a spin gap translated into the superconducting state for hole doping.

The magnetic and electronic properties have been investigated in ladder systems of a vanadyl prypophosphate, (VO)$_2$P$_2$O$_7$ [7–9], and a cuprate Sr$_{n-1}$Cu$_{n+1}$O$_{2n}$ ($n = 3, 5, \ldots$) [10,11], though carrier doping into those systems has not been successfully achieved yet. Magnetic susceptibility [7,10], neutron scattering [8], and NMR studies [9,11] on those undoped ladder systems have provided a clear evidence for the formation of gaps for the low lying spin excitations. We have investigated Cu-NMR and Cu-nuclear quadrupole resonance (NQR) of a newly disclosed ladder system of Sr$_{14}$Cu$_{24}$O$_{41}$ [12,13] in which carriers are possibly controlled [14]. The Sr$_{14}$Cu$_{24}$O$_{41}$ system forms a unique structure with CuO$_2$, Cu$_2$O$_3$, and Sr layers. The CuO$_2$ layers consist of 1D chains of edge-sharing CuO$_4$ clusters and the Cu$_2$O$_3$ layers form 2D planes with two-leg ladder configurations [12,13]. Carriers in the Cu$_2$O$_3$ ladders and the CuO$_2$ chains are controlled by the substitution of other divalent (Ca$^{2+}$, Ba$^{2+}$) or trivalent (La$^{3+}$, Y$^{3+}$) elements for Sr$^{2+}$ [15–17]. Very recently, superconductivity of $T_c \sim 10 \text{ K}$ was observed in the highly doped sample of the Ca substitution for Sr, when high pressure of $\sim 3 \text{ GPa}$ was applied [18].

In a previous paper [19], we have confirmed the existence of the energy gaps in spin excitation spectra in both Cu sites by NMR/NQR measurements, as we have observed Cu-NMR/NQR signals of the chain and ladder site separately. We assign the gap energy of $\Delta = 140 \text{ K}$ for the CuO$_2$ chains and $\Delta = 470 \text{ K}$ for the Cu$_2$O$_3$ ladder in Sr$_{14}$Cu$_{24}$O$_{41}$. The value of 140 K is close to the 11 meV peak and $\Delta = 470 \text{ K}$ is close to the 35 meV peak for inelastic neutron experiments [20,21]. The difference in the spin gap between the chain and the ladder is attributed to the large exchange coupling in the ladder and the small one in the chain, which may be owing to the different atomic bond configurations; namely 180° Cu-O-Cu bond for the ladder and the nearly 90° Cu-O-Cu bond for the chain [12,13].

In this Letter, we report carrier doping effects on the spin gaps in both sites in Sr$_{14-x}$A$_x$Cu$_{24}$O$_{41} (A = \text{Ca}, \text{Y}, \text{and La})$. The main results are as follows. The spin gap for the ladder increases with Y and La substitutions for Sr, decreases with increasing $x$ in Sr$_{14-x}$Ca$_x$Cu$_{24}$O$_{41}$, and seems to collapse around $x = 13$ of the Ca substitution. We will discuss hole-doping effects on the gap energy of spin excitation spectra in terms of magnon and hole-depairing excitations.

Polycrystalline samples were prepared by a conventional solid state reaction under ambient pressure [15–17]. NMR and NQR were measured by a conventional phase coherent pulse method. Two kinds of Cu-NQR signals were obtained separately around 30–34 MHz (Cu(1) chain signals) and 13–15 MHz (Cu(2) ladder signals) under zero applied field [19], corresponding to the two
Cu sites of the chain and the ladder configurations in Sr$_{14}$Cu$_{24}$O$_{41}$. The split Cu-NMR spectrum of Sr$_{14}$Cu$_{24}$O$_{41}$ was analyzed well by taking into account the quadrupole interactions for both sites as reported previously [19].

From the edge position of the quadrupole split central transition (due to the second order perturbation effect) of Cu(1)-NMR, we evaluate the NMR shift $K$ of Cu(1) in Sr$_{14}$Cu$_{24}$O$_{41}$ and show its temperature dependence in Fig. 1. $K$ shows a maximum near 70 K and changes rapidly with decreasing temperature. The NMR shift consists of both orbital and spin parts $K = K_{\text{orb}} + K_{\text{spin}}$ for the transition metal element. $K_{\text{orb}}$ is considered to be temperature independent in general and is estimated to be in the range of $(+1 \sim +2)\%$ for Cu$^{2+}$ [22]. Therefore, the observed positive $K$ of $+1.74\%$ at $T \to 0$ can be reasonably attributed to $K_{\text{orb}}$, for the Cu$^{2+}$ configuration, and the temperature-dependent part of $K$ is attributed to $K_{\text{spin}}$. As shown in the inset of Fig. 1, the temperature dependence of $K_{\text{spin}}$ of Cu(1) obeys a linear relation of magnetic susceptibility $\chi_{\text{corr}}$ (after subtracting the Curie-Weiss type contribution from impurity- or isolated-Cu$^{2+}$ spins [15]) with an implicit parameter of temperature. Below 100 K, only the susceptibility from the chain site is dominant as the contribution from the ladder is considered to be negligible due to the large energy gap as discussed below. Thus, the transferred hyperfine constant $H_{hf}^{\text{spin}}$ for Cu(1) is obtained to be $-82$ kOe/$\mu_B$ from the relation of $H_{hf}^{\text{spin}} = N_A\mu_BK(T)/\chi_{\text{corr}}$.

We measured $T_1$ of Cu(1)-NQR (at 33 MHz) and Cu(2)-NMR in Sr$_{14}$Cu$_{24}$O$_{41}$ by a conventional recovery method from a saturation pulse. Recovery of the nuclear magnetization after a saturation pulse for Cu(1)-NQR and Cu(2)-NMR spectra does not follow a recovery relation expected for a unique $T_1$ process. Instead, the recovery $R(t)$ of spin echo intensity in both Cu sites was well fitted to the relation of $R(t) = \{[M(\infty) - M(t)]/M(\infty)]\exp[-(t/T_1)^n]\}$ with $n = \frac{1}{2}$, indicating the Gaussian-like distribution of the $T_1$ process. Figure 2 shows the temperature dependence of $1/T_1$ of Cu(1)-NQR at 33 MHz in Sr$_{14-x}A_x$Cu$_{24}$O$_{41}$ ($A = \text{Ca, Y, and La}$). $1/T_1$ decreases rapidly with decreasing temperature, showing an activation type behavior above 20 K. As the deviation at low temperatures is owing to additional contributions from impurity- or isolated-Cu$^{2+}$ spins, we evaluate the gap value at high temperatures above 20 K and obtain the activation gap of $\Delta = 140$ K for the chain site. As can be seen in Fig. 2, the temperature dependence of $1/T_1$ of the Cu(1) site is similar for Ca, Y, and La substitutions.

As shown in Fig. 3, the temperature dependence of $1/T_1$ of the Cu(2) site obtained from the central peak in the NMR spectrum also shows an activation type behavior at high temperatures, except below 50 K where $T_1$ tends to be constant. The gap of $\Delta = 470$ K for the Cu(2) ladder site is obtained from the simple relation of $1/T_1 \propto \exp(-\Delta/T)$ for Sr$_{14}$Cu$_{24}$O$_{41}$ [23]. For the Ca-substitution case, $1/T_1$ becomes smaller with decreasing temperature compared to the case of Sr$_{14}$Cu$_{24}$O$_{41}$, indicating the gap

![FIG. 1. Temperature dependence of NMR shift $K$ of Cu(1)-NMR spectrum of Sr$_{14}$Cu$_{24}$O$_{41}$. Note that $K$ is shown by the negative direction. The inset shows Knight shift $K$ vs magnetic susceptibility $\chi_{\text{corr}}$ as a function of temperature as an implicit parameter.](image1.png)

![FIG. 2. Temperature and inverted-temperature dependence of $1/T_1$ of $^{63}$Cu(1)-NQR in Sr$_{14-x}A_x$Cu$_{24}$O$_{41}$ ($A = \text{Ca, Y, and La}$). The solid lines correspond to the $\exp(-\Delta/T)$ relation with a gap of 140 K.](image2.png)
energy decreases with $x$ of Ca. Figure 4 shows the $x$ dependences of gap energy for both Cu sites obtained from the temperature dependence of $1/T_1$. We would like to stress that the spin gaps of the Cu(1) chain site up to $x$ of Ca, up to $x = 2$ of Y, and up to $x = 1$ of La are nearly identical to (or a little smaller than) that of nondoped Sr$_{14}$Cu$_{24}$O$_{41}$. However, the spin gap of the Cu(2) ladder site increases with $x$ of Y and La, and decreases with $x$ of Ca. From the linear extrapolation with $x$, the spin gap for the ladder site seems to disappear at around $x = 13$ in Sr$_{14-x}$Ca$_x$Cu$_{24}$O$_{41}$. This finding suggests that the spin gap for the ladder site collapses with hole doping at a sufficient level where the ladder system is expected to be metallic [15] and superconducting [18].

First, we discuss the spin gap for the chain site. According to the electrical resistivity measurement, Sr$_{14}$Cu$_{24}$O$_{41}$ is semiconductive in spite of an average valence of Cu ions of $\frac{5}{2}$. This system becomes more insulating with increasing $x$ for $A =$ Ba, Y, and La, while it becomes more conductive for $A =$ Ca, [15–17]. The bond-valence-sums calculation [16] has shown that most holes are localized dominantly in the CuO$_2$ chains and do not enter the Cu$_2$O$_3$ ladder planes for the nondoped Sr$_{14}$Cu$_{24}$O$_{41}$. In fact, the average valency of the chain Cu ions is estimated to be 2.55 by an iodometry titration and to be 2.53 from the analysis of magnetic susceptibility [17], values that are close to 2.60 expected when all holes are located in the chain of Cu ions. Thus, most holes are considered to be situated in the chain site and to be localized.

The number of Cu$^{2+} S = \frac{1}{2}$ spins in the chain is $\sim 40\%$ of the Cu ions of the chain in Sr$_{14}$Cu$_{24}$O$_{41}$. As two neighboring Cu$^{2+}$ spins in the 1D chains couple antiferromagnetically to form a singlet, most of Cu$^{2+} S = \frac{1}{2}$ spins (40% of the Cu ions) among the comparable amount of Cu$^{3+} (S = 0)$ ions may form dimers, a finding that has been supported by the recent neutron scattering experiment [21]. For the 1D chain spins with alternating interactions (dimerized spins), theory has shown the existence of the gap for magnon excitation spectra [24]. This may be an interpretation for the origin of the spin gap for the CuO$_2$ chains in Sr$_{14}$Cu$_{24}$O$_{41}$. The relatively small gap of 140 K is attributed to the small exchange interaction owing to the edge-sharing CuO$_4$ bond for the chain configuration in Sr$_{14}$Cu$_{24}$O$_{41}$. As the NMR result shows the spin gap for the chain persists without notable change in the range of $x$ for the Ca, Y, and La substitution for Sr, the AF exchange interaction between Cu$^{2+}$ spins of the dimerized singlet pairs is not affected by increase or decrease in the number of singlet spin pairs in the chains under randomly distributed and localized holes.

Next, we discuss the change of spin gap in the ladders. Additional doping of holes induces the oxidation state and introduces effective Cu$^{3+} (S = 0)$ ions in either chain or ladder sites. Kato et al. [15] suggest that the hole transfer from the CuO$_2$ chain to the Cu$_2$O$_3$ ladder planes occurs by the Ca substitution due to the shortening of the lattice constants. The hole transfer from the chain to the ladder sites is supported also by the bond-valence-sums calculation [16]. As a result, hole carriers situated in the ladder planes may participate in conducting without
localization, when sufficient holes are doped. For the \( \text{Y}^{3+} \) and \( \text{La}^{3+} \) substitution, holes in the ladder as well as in the chains decrease owing to the difference of the charged state of \( \text{Ca}^{2+} \).

As pointed out theoretically [6], the ground state of the ladder is a spin liquid state with a gap \( \Delta \) for the isotropic \( J'/J = 1 \) and also the strong \( J'/J > 1 \) coupling. The excited state in the doped ladder can involve spin-triplet rungs, similar to the nondoped ladder case. In addition, hole doping in the ladder creates the single-hole rungs or two-hole rungs. In the ground state for two holes, holes enter the bound state of two holes in the same rungs [6]. Therefore, in the doped ladder, there exist two different types of magnetic excitations, i.e., the singlet-triplet (magnon) excitations and the excitations in which a pair of holes is scattered into two separated quasiparticles. The former one is inherited from the undoped spin ladder. The collective magnon excitations which evolve continuously from the nondoped limit can be influenced by the quasiparticle excitations, especially when quasiparticles start to move along the legs. The mean field theory [3] shows an increase of the gap for the magnon excitations upon small doping, while numerical studies for the ladder indicate a decrease of the gap when quasiparticles start to move along the legs. The decrease of the gap can be reasonably estimated by a simple exponential relation at low temperature.

In summary, the spin gap of the order of 140 K for the Cu\( ^{2+} \) spins of the singlet pairs along the rungs is not affected by the increase or decrease in the number of singlets in the ladder, similar to the case of the chains, the spin gap for singlet-triplet magnon excitations is expected to persist for light hole doping. The large decrease of the spin gap for the ladder suggests an important influence of the hole-depairing excitations on the gap energy. Low-lying excitations for the hole depairing cause the suppression of the gap. The NMR results show the spin gap seems to collapse around \( x \approx 13 \) of the Ca substitution, at which range holes can move (become metallic). Though the binding pairs of holes are considered to be favorable for the superconducting condensation, it should be noted that recently discovered superconductivity \( (T_c \approx 10 \text{ K}) \) under high pressure [18] appears in the doped range where the spin gap seems to disappear in the ladder. Needless to say, to confirm conclusively the important point whether or not the spin gap and the hole-pairing state for the Cu\( ^{2+} \), ladder persists in the superconducting state, we need to investigate NMR and neutron scattering experiments for the highly doped ladder samples under high pressure.

In summary, the spin gap of the order of 140 K for the Ca is nearly independent of the substitution of \( \text{Ca} \) (up to \( x = 9 \)), Y (up to \( x = 2 \)), and La (up to \( x = 1 \)) for Sr, but the spin gap for the ladder decreases with \( x \) and seems to disappear around \( x = 13 \) of the Ca substitution for Sr in Sr\( _{14-x} \text{A}_x\text{Cu}_2\text{O}_4 \). The decrease of the spin gap energy upon hole doping in the ladder can be attributed to the evolution of spin excitations, which is owing to the increase of the excitations from bound holes into separated quasiparticles in the ladder planes.

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[23] Troyer et al. [5] predicted \( 1/T_1 A^2 \exp(-\Delta/T)(a + \ln T) \) at low temperature for the ladder. As the main feature is the exponential drop with temperature, the magnitude of the spin gap can be reasonably estimated by a simple exponential relation at low temperature.