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Focusing of large-wave-vector phonons in GaAs

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Focusing of 0- to 1.5-THz transverse-acoustic phonons in GaAs is studied on the basis of an extended rigid-ion model, which reproduces very accurately the observed dispersion curves of acoustic phonons. The shifts of phonon caustics due to lattice dispersion become conspicuous at frequencies above 1 THz. Calculated focusing patterns of ballistic phonons are found to be in good agreement with the characteristic features of phonon images obtained recently by Wolfe and Northrop. We also compare the dispersive shifts of caustics in GaAs with those in Ge and discuss its implication to the phonon-focusing experiments with large-wave-vector phonons.

I. INTRODUCTION

The propagation of large-wave-vector phonons photoexcited in GaAs has been a subject of great interest in recent years.1 This interest is motivated to a considerable extent by the observation by Ulbrich, Narayanamurti, and Chin of energy transport via TA (transverse-acoustic) phonons.2 However, there are some controversies whether the energy transport in high-purity GaAs occurs via long-lived dispersive TA phonons or via quasidiffusion.3,4 At present there seems to be no conclusive results. The most direct experimental method which discriminates the ballistic transport from the diffusive transport is evidently to observe the focusing patterns of phonons impinging on the detector. This attempt has recently been carried out by Wolfe and Northrop.4 By a phonon-imaging method, they have observed phonon-focusing patterns in GaAs. It is found that the phonon image of a 0.25-mm-thick sample is substantially different from the longer-path (of 1.9 mm) image, suggesting the ballistic transport of dispersive phonons (of about 1 THz) over submillimeter distances being consistent with the phonon mean-free path limited by isotope scattering.5 However, there exists no detailed analysis on the maximum frequency of phonons which constitute the ballistic component of the detected flux. The aim of this work is to predict quantitatively the dispersive effects on the TA-phonon focusing in GaAs and compare the results with experimental phonon images. We also compare the dispersive shifts of phonon caustics in GaAs with those in Ge. As a consequence it is concluded that GaAs is less dispersive than Ge as far as phonon focusing is concerned.

II. LATTICE MODEL

As in the case of Ge the dispersion relation of the TA branches in GaAs is highly nonlinear, being characterized by marked flattenings of the dispersion curves especially in the \( <111> \) direction. [The lowest zone-boundary frequency of the TA phonons is 1.87 THz at point \( \Gamma \) (Ref. 6), which is slightly lower than 1.90 THz in Ge (Ref. 7) at the same point.] These flattenings of the TA branches are attributed to long-range interatomic forces which may arise from electrostatic quadrupole interactions8 and ion-shell forces.9 In order to discuss the focusing properties of the phonons in partially ionic crystals, we need to diagonalize the dynamical matrix of the lattice for a large number of wave vectors (of more than \( 10^5 \)) after the calculation of matrix elements consisting of the short-range forces as well as long-range Coulombic forces. Within the framework of the dipole and shell models we further require several times of matrix inversions to obtain the phonon frequencies. To save computation time we employ the rigid-ion model which does not necessitate the additional matrix inversions. However, we extend this model by adding short-range forces up to fifth nearest neighbors to ensure good fitting of the theoretical dispersion curves to experimental frequencies. The 23 parameters in total (22 parameters describing force constants and one describing the static ionic charge) are then fitted to the experimental frequencies4 and elastic constants.10

GaAs is a piezoelectric material and, therefore, stiffening of effective elastic constants can be expected. In the

![FIG. 1. Calculated phonon-dispersion curves of GaAs. Experimental frequencies are from Ref. 6.](image-url)
low-frequency limit the piezoelectric effects are estimated by the velocity change
\[
\frac{\Delta c}{c} = \frac{e_p^2}{2\varepsilon_0 C_{44}} = 1.9 \times 10^{-3}, \tag{1}
\]
where \(c\) is an appropriate phase velocity, \(e_p\) is the piezoelectric constant, \(\varepsilon_0\) is the static dielectric constant, and \(C_{44}\) is a component of the compliance tensor. Because the right-hand side of Eq. (1) is much smaller than unity, the piezoelectric effects can be safely neglected in the discussion of the focusing properties of the low-frequency phonons. In the rigid-ion model, however, the static dielectric constant is fixed at a value close to unity. Hence, the piezoelectric effects are enhanced by a factor of the order of 10 if the correct value of piezoelectric constant is included in the fitting procedure because \(\varepsilon_0 = 13\) for GaAs. Therefore, we have fitted the parameters so that the piezoelectric constant may be underestimated.

The comparison of the theory with experimental frequency data is shown in Fig. 1. Our model reproduces the frequencies of the acoustic branches relevant to the present discussion quite well, although there exist some deviations for the frequencies of the optical branches. The predicted elastic constants are \(C_{11} = 12.18\) (12.26), \(C_{12} = 5.74\) (5.71), and \(C_{44} = 5.95\) (6.00) in units of \(10^{11}\) dyn cm\(^{-2}\), which should be compared with the experimental values (extrapolated to 0 K) in the parentheses. More details of the results derived from this model, such as the one-phonon and two-phonon densities of states will be given elsewhere in relation to the study of anharmonic decay of the TA phonons in GaAs.

III. CONSTANT-FREQUENCY SURFACES

The focusing of phonons results from the fact that the constant-frequency surface (\(\omega\) surface) of each phonon mode spanned in the wave-vector space (\(k\) space) is distorted from a spherical shape due to the crystal anisotropy. The direction of the energy flow of the phonons is determined by the outward normal of the \(\omega\) surface or group-velocity vector. Hence, the phonons accumulate, in general, along some directions as compared to other directions in the real space, even if the phonons are distributed uniformly in the \(k\) space. In Figs. 2(a)–2(d) we have plotted the \(\omega\) surfaces of the TA phonons in GaAs at 0 and 1.5 THz frequencies. (We refer to the lower and upper TA branches as T1 and T2 branches, respectively.) Even at 0 THz these surfaces are highly nonspherical and consist generally of the concave and convex regions with positive Gaussian curvature and the saddle regions with negative Gaussian curvature, which are separated from each other by the zero-curvature parabolic lines indicated by dashed lines. When the dispersive effects are turned

FIG. 2. Constant-frequency surfaces (\(\omega\) surfaces) of TA phonons in GaAs. Dashed lines indicate zero Gaussian curvature and they separate convex, saddle, and concave regions. (a) T1 mode, 0 THz; (b) T2 mode, 0 THz; (c) T1 mode, 1.5 THz; and (d) T2 mode, 1.5 THz.
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on, ω surfaces are noticeably deformed. Similar to the case in Ge (Ref. 15) the narrowing (spreading) of the saddle regions can be seen on the T1 (T2) surface at the higher frequency. These changes should lead to the significant variations of the phonon-focusing patterns at near-zone-boundary frequencies.

Here, we remark on one of the qualitative differences of the shape of the ω surfaces for GaAs from those for Ge being shown in an earlier work. 15 At 0 THz the T1 surface of GaAs possesses a continuous concave area extended around the ⟨100⟩ axis [Fig. 2(a)]. For Ge the corresponding concave region forms a four-leafed clover extended about the ⟨100⟩ axis, which contracts with increasing frequency and vanishes at a frequency about 1.2 THz (see also Fig. 5). In the continuum approximation the characteristics of the shape of the ω surfaces for cubic crystals have been examined extensively by Every.16 He has found that the topologies of the ω surface are classified into several sets by the relative magnitude of elastic-constant ratios \( x = C_{11}/C_{44} \) and \( y = C_{12}/C_{44} \). On a plot of \( x \) versus \( y \), GaAs is located slightly below the line determined by the equation

\[
(x - 1)(x + y) + (x - y - 2)(y + 1)^2 = 0, \tag{2}
\]

whereas Ge is located slightly above the same line. This is the reason for the above-mentioned difference of the shapes of the T1 surfaces in the vicinity of the fourfold axis at 0 THz. However, as the frequency increases, the above continuous concave region of the T1 surface in GaAs is deformed also into the four-leafed-clover form, which survives even at near-zero-boundary frequencies, although it becomes more slender at high frequencies. All of these distortions of the ω surfaces due to the phonon dispersion should be directly reflected in the spatial patterns of the ballistic-phonon flux which will be shown in the next section.

IV. SPATIAL DISTRIBUTION OF PHONONS AND CAUSTICS

For the comparison with experimental phonon images, it is useful to make a simulation of the phonon flux. A large number of TA-phonon wave vectors (of about \( 3 \times 10^5 \)) are randomly generated in an isotropic distribution and their corresponding group-velocity vectors are computed and projected onto the ⟨001⟩ surface of GaAs. Figures 3(a)–3(d) are the TA-phonon images calculated for 0, 0.7, 1.1, and 1.5 THz frequencies. The characteristics of the focusing patterns in GaAs are the presence of heavy accumulation regions of the T1 phonons around the [100] axis and of the T2 phonons spreading about the [100] plane. In addition, the structures extending from the ⟨100⟩ to ⟨111⟩ axes due to the T1 phonons do exist. Comparing these structures in the images of the selected frequencies, the dispersive effects on the focusing pattern are really discernible in the image of 0.7 THz and

FIG. 3. Simulated ballistic-phonon focusing patterns projected onto the ⟨001⟩ plane of GaAs extending ±39° horizontally and ±29° vertically in propagation angle. (a) 0 THz, (b) 0.7 THz, (c) 1.1 THz, and (d) 1.5 THz.
they become significant at frequencies higher than 1 THz. More specifically, as the frequency increases the typical square structure of the T1 phonons being present at 0 THz becomes gradually round (see especially the image of 1.1 THz) and four pairs of the T2-phonon-focusing region become rapidly wider. Incidentally, we note that the accumulation of the phonons tends to be rather gentle at high frequencies as the focusing regions develop in the real space.

To aid in analyzing further the structures of the focusing patterns shown in Fig. 3, it is helpful to identify the directions along which the enhancement factor of the phonon flux diverges. Such directions originate from the parabolic points on the \( \omega \) surfaces and are distributed on the continuous lines or surfaces called caustics in the real space. The caustics distinctively separate the focusing region from the defocusing region of the phonons. In Figs. 4(a)–4(d) the caustics of the TA phonons in the (001) plane of GaAs are illustrated. The coincidence of the calculated caustic directions with the boundaries of the focusing regions is remarkable. Hence, by measuring the locations of the caustics we can identify, in principle, the maximum frequency of the ballistic phonons detected in the experimental phonon images. In Fig. 5 the theoretical frequency dependences of three loci of the caustics (denoted by polar angles \( \theta_{T1}, \theta_{T2}, \) and \( \theta_{T3} \)) in the (110) plane of GaAs together with those of Ge (see also Sec. V below) have been plotted. Generally, for the T1 mode, there exist four intersections of the caustics with this plane, i.e., two near the [001] axis and other two near the [111] axis, whereas the T2 mode has only one intersection in the vicinity of the [110] axis (cf. Fig. 4). For the T1 mode the loci of the former two are displayed. The measurement of the locations in the (110) plane of the T2 caustic (\( \theta_{T2} \)) and the T1 caustic (\( \theta_{T1} \)) situated outside, should be best suited for determining the maximum value of the ballistic-phonon frequency. This is because in these directions the phonon intensity suddenly jumps an order of magnitude, and in addition, their locations are quite sensitive to the phonon frequency. For instance, at 0 THz \( \theta_{T2}=3.7^\circ \) and \( \theta_{T1}=9.3^\circ \) but at 1.5 THz they become \( \theta_{T2}=16.1^\circ \) and \( \theta_{T1}=17.8^\circ \) where \( \theta_{T1} \) and \( \theta_{T2} \) are measured from the [001] and [110] directions, respectively.

Now we shall compare our results with the characteris-

FIG. 4. Theoretical maps of the caustics of GaAs in the (001) plane centered on the [001] direction for both the T1 phonons (solid lines) and the T2 phonons (dashed lines). Frequencies are (a) 0 THz, (b) 0.7 THz, (c) 1.1 THz, and (d) 1.5 THz. \( \theta_v \) indicates the polar angle of group-velocity vector.
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V. COMPARISON WITH DISPERSIVE EFFECTS ON THE FOCUSING IN Ge

We shall briefly compare the results obtained above for GaAs with the results for Ge. We may expect that the similar dispersive effects on the TA-phonon focusing should be present in both GaAs and Ge because the dispersion relations for the acoustic branches of these crystals are nearly identical as remarked in Sec. I. To convince ourselves of this expectation, we have plotted in Figs. 6(a)—6(c) the caustic patterns of the TA phonons.
projected also on the (001) crystal plane of Ge for 0, 0.7, and 1.0 THz, respectively. At 0 THz, characteristic square shapes surrounding the fourfold axis are constructed by the caustics of the T1 phonons. Equivalently, this is also seen in GaAs in the low-frequency limit [Fig. 4(a)], although their locations are slightly shifted from each other due to the different magnitudes of the elastic anisotropy.20 Surprisingly, however, for Ge these structures of the T1 phonons are deformed by dispersion and make a circle at a frequency as low as 0.7 THz [Fig. 6(b)]. For GaAs such a round shape of the caustics is yielded at a much higher frequency about 1.1 THz [Fig. 4(c)]. Moreover, the predicted shape for the T2-phonon caustics in GaAs at 1.5 THz is very similar to that in Ge at 1.0 THz. These results imply that the distinctive features of the dispersive shifts of the T1-phonon-focusing patterns can adequately be observed at 0.7 THz in Ge but they become detectable at a much higher frequency in GaAs. We also find from Fig. 5 that the shift of the T2-phonon caustics in Ge depends on the frequency more abruptly than that in GaAs.

In these respects GaAs may be regarded as less dispersive than Ge as far as the focusing properties of the TA phonons are concerned. As a result, our model suggests that the distortion of the ballistic-focusing patterns in GaAs is slightly difficult to observe experimentally, as compared to Ge, because the phonons are subject to scattering, very efficiently, at high frequencies.

VI. CONCLUDING REMARKS

In this paper the dispersive effects on the TA-phonon focusing in GaAs have been investigated on the basis of an extended rigid-ion model. Our analysis implies that the dispersive effects on the directional properties of the phonons in GaAs are less pronounced than in Ge despite the apparent coincidence of the dispersion curves of the TA branches in these crystals. Calculated results exhibit, however, good agreement with the dispersive shifts of the focusing patterns in GaAs obtained by Wolfe and Northrop.4 Our results also make it possible to analyze quantitatively the maximum frequency of the phonons which constitute the ballistic component of the experimental images. In the experiment of Wolfe and Northrop the Al bolometer which is sensitive to the phonons of all frequency range has been used as a detector.4 For more precise understanding of the dispersive effects on the phonon focusing a detector such as the Pb—oxide-Pb tunnel junction which may selectively respond to the near-zone-boundary phonons should be employed.21

In this work only spatial distribution of ballistically propagating dispersive phonons is studied. To resolve further the substantial features of the experiment of Ulbrich et al.,2 the analysis of temporal behaviors of the phonon flux (i.e., line shapes) should be performed by incorporating more rigorous scattering effects (which include anisotropy and dispersion) than those discussed in the literature.

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FIG. 3. Simulated ballistic-phonon focusing patterns projected onto the (001) plane of GaAs extending ±39° horizontally and ±29° vertically in propagation angle. (a) 0 THz, (b) 0.7 THz, (c) 1.1 THz, and (d) 1.5 THz.