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Control Method for a Combined Active Filter System Employing a Current Source Converter and a High Pass Filter

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Abstract—This paper describes a control method with a combined filter system which senses load current, source current, and line voltage to create reference signals for an active filter. The transfer function of the active filter is identified and is used for the control system design. It is shown that the source current feedback is most effective to suppress the harmonic-enlarging effects due to parallel resonance and the harmonic current generated by source harmonic voltages. A small setup controlled by a DSP was built, and the validity of the proposed method was demonstrated by experimental results.

I. INTRODUCTION

RECENTLY, static power converters have been widely used in many industries. With this trend wide-band current harmonics and reactive power generated by the converters are becoming a troublesome problem in ac power lines. Thus, research interest in the development of active power filters (AF) to solve the problem is growing.

Basically there are two kinds of AF's, the current source active filter (CSAF) and the voltage source active filter (VSAF). Major research efforts have been focused on VSAF because of its lower running loss compared to CSAF. CSAF is, however, superior in controllability and reliability. Furthermore, if superconducting coils could be practically used, CSAF would be promising, because it can operate in a lossless manner; absorbing not only harmonics and reactive power but active power variations. We have already proposed a combined filter system [1], [2] using a current source active filter and a high pass filter (HPF) to obtain wide-band compensation performance. With this system, however, some problems have remained unsolved:

- 1) parallel resonance between the source impedance and HPF,
- 2) inflow of harmonic currents to HPF which are produced by source harmonic voltage, and
- 3) drawbacks stem from analog control such as sensitivity to noise and temperature.

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Fig. 1. Configuration of active filter system.

It is known that source current feedback [3], [4] is useful for suppressing problems 1) and 2). If such feedback is adopted, stable control system design is required as feedback may introduce instability into the system. A control system design for VSAF has been reported in [4], but it is not valid for CSAF because the method used for creating compensation current is totally different from that of VSAF.

One target of this paper is to establish a method of control system design for CSAF. In the CSAF system under consideration, source current and line voltage feedbacks are added to load current feedforward to suppress problems 1) and 2). It is found that the transfer characteristics of CSAF are approximately represented by a first-order lag system. Then stability investigations are carried out based on a transfer function approach, and a stable feedback system design is proposed.

The other target is to adopt digital control using a digital signal processor (DSP) [2]. In this situation, however, there exists a time-lag in the output due to the computation by DSP, which causes serious deterioration in the filter performance. It is shown that the source current feedback is also very effective to suppress the influence of the time-lag.

Finally it is demonstrated by experimental and simulation results that a properly designed CSAF with load current feedforward, and source current and line voltage feedbacks, exhibits excellent compensation performance solving problems of 1) to 3) and that of the time-lag.

II. CIRCUIT CONFIGURATION

Fig. 1 shows the combined filter system using a current source converter (CSC) and a high pass filter. The AF is connected to ac power lines through a transformer with a turn

Fig. 2. Configuration of active filter control system.

ratio of 2:1. Fig. 2 shows the control circuit configuration. The DSP is used to calculate the current reference of the AF. The PWM control is a comparison-based method with triangular carrier waves [1], and the sampling and carrier frequencies are the same, 10 kHz. The functions of the AF are

- 1) compensation of low order harmonics in the load current,
- 2) suppression of parallel resonance between the source side impedance and the HPF, and
- 3) suppression of harmonic current generated by the source side harmonic voltage.

The functions of the HPF are

- 1) compensation of high order harmonics in the load current, and
- 2) elimination of carrier frequency components generated by the AF.

The constants are as follows: source side impedance $L_s = 1.0$ mH, $R_s = 0.6$ Ω , $C_1 = 2.0$ μ F, leakage inductance of the transformer $L_1 = 4.0$ mH, high pass filter $C_2 = 100$ μ F, $L_2 = 0.6$ mH, and $R_2 = 2.0$ Ω . The HPF design was described in [5].

III. CONTROL METHOD OF THE ACTIVE FILTER

A per-phase equivalent circuit of the AF and the load system for harmonics are shown in Fig. 3, where I_{Lh} and I_{sh} denote the load and source harmonic currents, respectively, and V_{sh} denotes the source harmonic voltage. The transfer function G_{z1} from the AF current I_{AF} to I_{sh} is given by

$$G_{z1} = \frac{I_{sh}}{I_{AF}} = \frac{\frac{Z_H}{j\omega C_1}}{(Z_H + Z_s)Z_1 + Z_s Z_H} \quad (1)$$

where ω is the fundamental angular frequency of the source. Z_s , Z_H , and Z_1 denote the source impedance, the resultant HPF impedance, and the series impedance of C_1 and L_1 , respectively. The Bode plot of G_{z1} is shown in Fig. 4 where it has two crests due to the parallel resonance between $L_2 + L_s$ and C_2 at 400 Hz, and between L_1 and C'_1 (referred to the line side) at 3560 Hz. In particular, the former resonance is a problem, as it enlarges harmonics around 400 Hz. The transfer function from I_{Lh} to I_{sh} is defined as $G_{z2} = I_{sh}/I_{Lh}$. $G_{z2} = G_{z1}$ in the low-frequency range (<1 500 Hz).

Fig. 3. Equivalent circuit for harmonics per phase.

Fig. 4. Gain characteristic of G_{z1} .

A. Harmonic Current Sensing

The instantaneous real and imaginary power theory [6] is used for harmonic calculation. There are three current sensing methods, as shown in Fig. 5.

Load current sensing is shown in Fig. 5(a), in which the AF output current is controlled in the feedforward way

$$I_{AF} = I_{Lh}. \quad (2)$$

Thus the source current will be given by

$$I_{sh} = (G_{z2} - G_{AF}G_{z1})I_{Lh} + \frac{V_{sh}}{Z_{H1} + Z_s} \quad (3)$$

where G_{AF} is the transfer function of AF, and Z_{H1} is the parallel combination of the impedances Z_H and Z_1 . Since $G_{z2} = G_{z1}$ in the low-frequency region, the harmonic current originating from the load current would be zero in the same region if $G_{AF} = 1$. In practice, however, as $G_{AF} = 1$, some harmonics remain uncompensated for. In particular, the resonant frequency components in the remainder are enlarged in the source current by the parallel resonance, which causes a problem. The harmonic current generated by V_{sh} will not be compensated for at all, which causes another problem. However reactive power compensation is easy.

Source current sensing is shown in Fig. 5(b), in which I_{AF} is controlled by the I_{sh} feedforward through the transfer function G_i in the following manner assuming $G_{AF} = 1$:

$$I_{AF} = G_i I_{sh}. \quad (4)$$

Thus we have

$$I_{sh} = \frac{G_{z2}I_{Lh} + \frac{V_{sh}}{Z_{H1} + Z_s}}{1 + G_i G_{AF} G_{z1}}. \quad (5)$$

Fig. 5. Block diagram of three harmonic currents sensing methods. (a) Load current sensing. (b) Source current sensing. (c) Load and source currents sensing.

Fig. 6. Bode plots of I_{sh}/I_{Lh} .

A phase-lead element is used for G_i to compensate for the phase-lag property of G_{z1} as

$$G_i = \frac{K_i T_i s}{1 + T_i s} \quad (6)$$

From (5) it is seen that harmonics generated by V_{sh} as well as I_{Lh} can be suppressed if the gain, K_i , is higher than unity. The gain, I_{sh}/I_{Lh} , is illustrated in Fig. 6 under $G_{AF} = 1$ and $V_{sh} = 0$. In the figure, the crests disappear as K_i becomes high, which means that the parallel resonance is suppressed. However, as I_{Lh} is not sensed, reactive power compensation is difficult.

Load and source current sensing is shown in Fig. 5(c). In this case I_{AF} is controlled by the I_{Lh} feedforward and I_{sh} feedback in the following manner:

$$I_{AF} = I_{Lh} + G_i I_{sh} \quad (7)$$

Therefore we have

$$I_{sh} = \frac{(G_{z2} - G_{AF} G_{z1}) I_{Lh} + \frac{V_{sh}}{Z_{H1} + Z_s}}{1 + G_i G_{AF} G_{z1}} \quad (8)$$

This sensing method exhibits the best filtering performance because it has advantages of both I_{Lh} feedforward and I_{sh} feedback, that is, compensation for load harmonics and reactive power is possible by the I_{Lh} sensing, and suppression of the effects of parallel resonance and V_{sh} is also possible by I_{sh} sensing.

B. Line Voltage Harmonics Sensing

Here the line voltage feedback is added to I_{Lh} feedforward and I_{sh} feedback. The sensed harmonic voltage V'_{sh} will be

$$V'_{sh} = V_{sh} - Z_s I_{sh} \quad (9)$$

This voltage is used for creating the compensation current reference by

$$I_{AF} = I_{Lh} + G_i I_{sh} + G_v V'_{sh} \quad (10)$$

The control block diagram is shown in Fig. 7. Thus we have

$$I_{sh} = \frac{(G_{z2} - G_{AF} G_{z1}) I_{Lh} + \left(\frac{1}{Z_{H1} + Z_s} - G_v G_{AF} G_{z1} \right) V_{sh}}{1 + (G_i - G_v Z_s) G_{AF} G_{z1}} \quad (11)$$

Order k	Residual Current J_{sk} $\Delta T=0.1\text{ms}$	$\Delta T=0.2\text{ms}$
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where V'_{sh} is used through the transfer element G_v . From simulation-based stability investigations it has been found that G_v should be a proportional gain as

The voltage-sensing method is not useful if it is used alone, but if used together with I_{Lh} and I_{sh} sensing the compensation characteristics can be improved further.

Here the influence of a time-lag in the AF output due to the computation time needed by DSP is examined [5]. Consider the compensation of the k -th order harmonic current with the unity amplitude, $i_{Lk} = \sin k\omega t$, under an ideal AF gain characteristic, $|G_{AF}| = 1$, with I_{Lh} sensing. If the time-lag is ΔT , the residual harmonic current after compensation, j_{sk} , will be expressed by

where

$$J_{sk} = 2 \sin(k\omega\Delta T/2).$$

J_{sk} values for 10-kHz and 5-kHz samplings are shown in Table I. It is seen that compensation performance gets worse as the harmonic order becomes higher or the sampling frequency becomes lower. In particular, with our AF, the residual harmonics between the 5th and 11th orders are serious because they are close to the resonant frequency 400 Hz. As AF characteristics are practically not ideal, the situation becomes more serious. Equation (8), however, indicates that the source current feedback is effective to suppress the residual harmonics.

The dc current of AF should be the minimum necessary value because too little dc current results in poor filter performance and too much dc current results in excess loss in the dc reactor. Therefore, the maximal value of the AF current reference in one period of the source frequency is chosen as the dc current reference in the next period, which is useful to reduce AF running loss. The control is based on a $P-I$ algorithm as

where $K_P = 0.4$ and $T_I = 50$ ms. The dc current control is carried out every period of the source frequency.

It is expected that higher G_i gains may result in better AF performance. However, too much gain may cause instability in the system. Here feedback control system design is based on a transfer function approach [7].

Identification of the transfer function of AF is essential for the control system design. Responses of a current source converter (CSC) to sinusoidal current references with various frequencies were simulated under the modulation index, $M = 1$ ($M = I^*/I_d$, I^* : amplitude of the reference, I_d : dc current of CSC equal to 10 A) and $f_s = f_c$ (f_s : sampling frequency, f_c : carrier frequency). The CSC output includes many harmonics but the relation of input to output at the fundamental frequency was examined. Then the transfer characteristics, G_{AF}^* , shown in Fig. 8 were obtained [7]. In the figure, significant phase lag is observed in the high-frequency region because reference values are kept constant during the sampling interval. Simulation was also done under various M values but it did not result in much difference in the responses. It is concluded with these simulation results that the transfer characteristic of the

Fig. 9. Bode plots of loop transfer function $(G_i - G_v Z_s)G_{AF}G_{z1}$.

Fig. 10. Simulation results under I_{Lh} and I_{sh} sensing.

CSC, G_{CSC} , can be approximated as a first order lag element in the frequency region, $f < f_c/3$, and is given by

$$G_{CSC} = \frac{K}{1 + Ts} \quad (15)$$

where $K = 1.0$ and $T = 1/(2f_c)$. It has been reported that the transfer function of a voltage source converter is also approximated by a first order lag element [4], but it exhibits strong nonlinearity, i.e., the delay time T in (15) depends on the amplitude of the AF reference current. However, T is independent of the amplitude of AF reference with the CSC unless the reference exceeds the dc current I_d .

Taking the computational time-lag ΔT and the anti-aliasing filter with its cutoff frequency 4.8 kHz into consideration, the transfer function of CSAF, G_{AF} , will be expressed by

$$G_{AF} = \frac{G_{CSC}}{1 + T_a s} \exp(-\Delta T s) = \frac{K}{1 + Ts} \frac{1}{1 + T_a s} \exp(-\Delta T s) \quad (16)$$

where $T = f_c/2 = 0.05$ ms, $T_a = 0.03$ ms, and $\Delta T = 1/f_c = 100$ μ s.

Fig. 11. Simulation results indicating instability.

B. Stability Investigation and Control System Design

Bode plots of the loop transfer function, $G_i G_{AF} G_{z1}$ in (8) are calculated under various K_i and T_i values. As a result when $K_i = 4.0$ and $T_i = 0.7$ ms, the phase margin of 21.0° at 1141 Hz and the gain margin of 1.9 dB at 1467 Hz are obtained. Further increase in K_i makes it difficult to stabilize the system.

Again simulation of the loop transfer function, $(G_i - G_v Z_s)G_{AF}G_{z1}$ in (11) is done with various K_v values. Its frequency characteristics under $K_i = 4.0$, $T_i = 0.7$ ms and $K_v = -0.1$ are shown in Fig. 9. With this value, the phase margin of 25.8° at 1227 Hz and the gain margin of 2.1 dB at 1678 Hz are obtained, which means that the line voltage feedback provides us with a more stable system.

V. SIMULATION RESULTS

Fig. 10 shows a simulation result under I_{Lh} and I_{sh} sensing with $K_i = 4$ and $T_i = 0.7$ ms, and a three-phase diode rectifier. Sinusoidal source current is obtained after AF starts operation. Fig. 11 shows simulation results under the same conditions as in Fig. 10 except for $K_i = 5.0$. Stability examination of this case reveals that the phase margin is 1.2° at 1485 Hz, and the gain margin is 0.1 dB at 1467 Hz. It is seen that the source current diverges at the frequency around 1550 Hz, which proves that the stability investigation is reasonable.

Fig. 12. Comparison of measured voltage and current waveforms in steady state under four current sensing methods. Upper: source current I_s , 10 A/div; middle: load current I_L , 10 A/div; lower: line voltage V'_s , 177 V/div; 5 ms/div. (a) Without AF. (b) With I_L sensing. (c) With I_s sensing, $K_i = 0.4$, $T_i = 0.7$ ms. (d) With I_L and I_s sensing, $K_i = 0.4$, $T_i = 0.7$ ms.

Because experimental confirmation of the effects of the V'_{sh} feedback is difficult, it was done by simulation. The conditions were: the source voltage of $V_s = 100$ V was assumed to include 5, 7, and 11th harmonics with each amplitude being 7% of V_s , and $I_{Lh} = 0$ to make clear the effects of the V'_{sh} feedback alone. The THD value of the source current without feedback was 114%, but it was reduced to 33.1% with the I_{sh} feedback and to 26.7% with the I_{sh} and V'_{sh} feedbacks. From these results it was confirmed that the I_{sh} feedback is the most effective but the V'_{sh} feedback is also effective to compensate for harmonics generated by V_{sh} .

VI. EXPERIMENTAL RESULTS

A prototype 1-kVA active filter was built and experiments were done using it. Fig. 12 shows the waveforms of source current I_s , load current I_L , and line voltage V'_s ; and the spectra of I_s , where the vertical is with a linear scale and the horizontal is with a logarithmic scale. The load was a three-phase thyristor rectifier with the control angle $\alpha = 0^\circ$. Fig. 12(a) shows the waveforms before compensation. It can be seen that the 5th and 7th harmonics are enlarged by the parallel resonance, and that the THD of V'_s is increased up to 8.0% while it was

TABLE II
COMPARISON OF SOURCE CURRENT SPECTRA UNDER VARIOUS SENSING METHODS

Order k	None	Sensed Variables			
		I_{Lh}	I_{sh}	$I_{Lh}+I_{sh}$	$I_{Lh}+I_{sh}+V_{sh}'$
5	24.15%	7.67%	2.97%	1.66%	1.61%
7	13.24	3.99	2.51	1.13	0.65
11	1.61	1.06	1.24	0.64	0.46
13	0.89	0.51	1.16	0.80	0.46
17	0.41	0.27	0.66	0.33	0.35
19	0.35	0.27	0.54	0.33	0.16
THD	27.62	8.83	4.35	2.49	1.98

Fig. 13. Measured voltage and current waveforms in transient state with I_L and I_s sensing. $K_i = 0.4$, $T_i = 0.7$ ms.

Fig. 14. Measured three-phase current waveforms for unbalanced load compensation, with a single phase diode rectifier load connected between phase "b" and "c." (a) Load currents, 10 A/div. (b) Source currents, 7.5 A/div, with I_L , I_s and V_{sh}' sensing. $K_i = 0.4$, $T_i = 0.7$ ms, $K_v = -0.1$, 7.5 A/div, and 5 ms/div.

0.82% at no load. Fig. 12(b)–(d) show the waveforms and the source current spectra after the compensation with three-way sensing control. In the I_{Lh} feedforward of Fig. 12(b), suppression of the parallel resonance around 400 Hz is not great enough and influence of the computational time-lag is seen. In the I_{sh} feedback of Fig. 12(c), suppression of the 5th and 7th harmonics is better but the other harmonics are larger than the I_{Lh} feedforward. In the $I_{Lh} + I_{sh}$ sensing of Fig. 12(d) and $I_{Lh} + I_{sh} + V_{sh}'$ sensing (photo is not shown in this case), excellent compensation results are observed. The source current harmonic list under various variable sensing conditions is summarized in Table II.

The compensation results when the control angle of the rectifier was changed continuously and periodically under the $I_{Lh} + I_{sh}$ sensing are shown in Fig. 13. The dc current follows the variations in I_L behind the time around 50 ms. As the purpose of the I_d control is to minimize running loss in the

TABLE III
COMPARISON OF CURRENT SPECTRA

Order k	Load Current	Source Current
1	100%	100%
3	12.8	1.30
5	8.14	0.87
7	5.52	0.24
9	4.14	0.47
11	3.11	0.32
13	2.35	0.20
15	1.79	0.24
17	1.38	0.08
19	1.07	0.18
THD	17.3	1.79

steady state, the response delay of 50 ms is no problem. The load current is almost sinusoidal, which indicates that the proposed AF system is useful in the transient state as well.

Fig. 14 shows compensation for an unbalanced load when a single phase diode rectifier was connected between phase "b" and "c," and phase "a" was left open. Fig. 14(a) shows the load current waveforms of each phase, and (b) shows the source current ones of each phase. Balanced three-phase source currents are seen after compensation. The load and source current harmonic lists of phase "b" are given in Table III.

VII. CONCLUSION

The CSAF control method, which senses load current, source current, and line voltage, was described. The transfer characteristics of CSAF were examined and it was found that it could be approximately represented by a first order lag function. Stability investigation was then carried out and a control system design based on the transfer function approach was proposed. It was pointed out that if a microprocessor is used in the control system, the time-lag in the output caused by the computation time results in serious deterioration in the compensation performance. It was shown by experiment as well as simulation that an appropriate control system design using load current feedforward, source current feedback, and line voltage feedback can compensate for not only the harmonics generated by load harmonic current and/or source harmonic voltage but the time-lag problems as well. With the proposed control method, almost every kind of harmonics of current source nature can be compensated for as long as the system parameters remain constant.

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