Measurements of Dental Cast Profile and Three-Dimensional Tooth Movement During Orthodontic Treatment

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Abstract—We have developed a system for measuring three-dimensional profiles of dental casts and three-dimensional tooth movement during orthodontic treatment. The profile measurement is based on the triangulation method which detects a laser spot on a cast using an image sensor. The system is computer-controlled and designed to achieve the depth and lateral resolutions of 0.05 and 0.1 mm, respectively, with a depth range of 25 mm. We have applied our system to measuring three-dimensional movement of teeth, including rotations, during orthodontic treatment. The movements have been obtained by means of three-dimensional registration of tooth profiles using a computer between casts serially taken at different stages of the treatment. Measurements over periods of 41 to 190 days on patients have revealed that this technique is capable of quantifying the difference in movements due to orthodontic therapies.

I. INTRODUCTION

A dental cast is widely used in dentistry for working on dental prostheses. Because of the problems involved in working within the mouth, tooth shape and position, which provide fundamental diagnostic information in dentistry, are also generally measured on a dental cast. This is called cast analysis and is most frequently carried out by using simple instruments such as a caliper and a ruler. These instruments, however, allow only one-dimensional measurement. In order to measure a cast in all three dimensions, X, Y, and Z, instruments of indirect and direct measurements have been attempted. As for the indirect measurement of shape, stereophotogrammetry has been applied to the morphological study of the face, the tooth, and the palate [1]-[3]. Although this technique has been used successfully to measure three-dimensional shapes, it requires a sophisticated procedure to digitize the shape.

Direct measurements employing either a contacting mechanical or noncontacting optical technique have been attempted. Van der Linden et al. [4] have described the optocom which can measure X and Y coordinates using a microscope and a Z coordinate by mechanical contact with a dental cast. The reflex optical plotter using a noncontacting optical technique has been applied to the measurement of all three coordinates [5], [6]. In this apparatus the measurement is made by aligning a movable light source to coincide with a specific point on a cast image behind a semireflecting mirror. A traveling microscope recently developed by Bhatia and Harrison [7] is based on an optical technique which has notably increased the accuracy of the measurement. However, in all cases, since the apparatus in manually operated point-to-point, little data concerning surface profiles can be obtained.

A computer-controlled profilometer using an optical probe has been developed for the measurement of cleft palate casts by Berkowitz et al. [8]. Although this apparatus scans a cast automatically and digitizes its profiles, the optical technique used does not meet the demands for the measurement of occlusal surface of a tooth because it has a fine profile. Greater spatial resolution is required for the measurement. The authors have developed a prototype of an automatic, optical profilometer equipped with a laser and an image sensor and capable of a higher degree of precision [9], [10].

In orthodontics, information concerning the positional change of a tooth is as fundamental and important as the shape. When an orthodontic force is applied to a tooth over a long period of time, the tooth moves owing to resorption of the alveolar bone on the pressurized side and apposition of new bone on the opposite side. In daily practice, orthodontists analyze tooth movement during treatment in a one-dimensional way by measuring the distance between two teeth using a caliper, or in a two-dimensional way by tracing teeth on X-ray films taken at different stages of the treatment [11]. Although the tooth moves in a three-dimensional way, no established technique to measure this movement, including rotational movement, has been reported. If the three-dimensional shape of dental casts at the different stages is digitized into a computer, three-dimensional tooth movement can be obtained by numerical calculation. In this paper, we describe a system designed for the three-dimensional measurement of dental cast profiles and tooth movement during orthodontic treatment.

II. THREE-DIMENSIONAL MEASUREMENT OF DENTAL CASTS

Instrumentation and Measurement

A triangulation method is a conventional technique for the measurement of a distance. This method has recently been applied to noncontacting three-dimensional measurement using an optical probe. A biomedical application of this technique to the surface profile measurement of the trunk has been reported in recent years [12]. Based on a similar technique, we have developed a prototype of our system for measuring dental cast profiles [9], [10]. The measurement system including a personal computer is now more compact than the prototype, as shown in Fig. 1. The depth is measured with an optical system composed...
The system developed for measuring dental cast profiles. The system is constructed with the optical equipment composed of a laser, an image sensor, and lenses (1), the X-Y table (2), the specially designed interface with a personal computer (3), and the computer (4). The computer is also used for calculating three-dimensional tooth movement.

of a laser and an image sensor, as illustrated in Fig. 2. A small spot of light is formed on a dental cast with a 0.6 mW He-Ne laser and a lens \( L_1 \) (\( f = 100 \) mm). This lens is employed to sharpen the laser beam to a point in order to raise the power of lateral resolution, because the diameter 0.8 mm of the unfocused beam from the laser is too thick to measure the fine occlusal surface of a tooth. Scattered light from the spot is focused, with the other lens \( L_2 \) (\( f = 75 \) mm), onto an image sensor (Sharp L2Z2020) which has a one-dimensional array of 2048 photoelements aligned in a pitch of 14 \( \mu \)m. From the position of the spot on the array the depth of the cast surface can be obtained. Scanning required for profile measurement is accomplished by moving the cast in a horizontal plane with an X-Y table, for which a conventional X-Y plotter (Graphtec FD5311) controlled by a personal computer (NEC PC-9801) was substituted for ease of instrumentation. The image sensor is placed on an optical axis \( W \) making an angle of \( \alpha \) (35°) with the incident optical axis \( Z \) of the laser beam. The sensor is also tilted by \( \beta \) (45°) with respect to the axis \( W \) in such a way that the spot image is always focused on the array of photoelements.

The intensities of light stimulating 2048 photoelements are sequentially read from the sensor with a 1-MHz clock and fed into a specially designed interface with the computer. The interface detects the rising and falling edges of the spot signal using a voltage comparator and obtains the position of the edges on the array, \( P_1 \) and \( P_2 \) shown in Fig. 2, by counting the clock pulses from the beginning of a read-out cycle to the edges. The two counted binary data are transferred to the computer via a digital input. The center of the two edges is determined and defined as the peak position, because it almost coincides with the actual position of the peak intensity. The peak position is then converted into the corresponding depth with a calibration curve obtained prior to the measurement, as described in the next section.

A plaster dental cast is fixed with pieces of double-sided adhesive tape to select one rectangular scanned area which covers all the teeth and the palate concerned. However, this method requires the complicated image processing for identifying the boundaries between tightly connected teeth. To eliminate this problem, the scanned area including the boundaries is predetermined on each tooth and the palate, prior to the measurement. An operator can easily adjust the scanned area with a joystick linked to the computer. After setting the scanned areas the apparatus automatically and successively digitizes teeth and palate profiles. Teeth and the palate were typically scanned at a pitch of 0.2 and 0.4 mm, respectively. All the data are stored on a flexible disk and used for the calculation of tooth movement by the method described in the next chapter.

An example of the computer graphic display of measured profiles of a dental cast is shown in Fig. 3. The shape of the occlusal surface, which is necessary for the calculation of three-dimensional tooth movement, is almost completely measured except for the lateral portion of the teeth. The lack of data in this portion is because the laser spot is not formed due to anatomical arrangement of the dental arch.

**Measurement Speed and Resolution**

The time required for measuring a point was 25 ms and was mostly consumed by mechanical scanning with the plotter. The number of sampled data per tooth amounts to nearly 2000 on the average, and it takes about 50 s per tooth.

We calibrated the apparatus and examined depth resolution in the following manner. Details have been described in our previous study [10]. The relationship between the peak position of the sensor and the depth of an object surface was measured by moving vertically, at an interval of 0.5 mm in the region of...
Fig. 3. Computer graphic display, using a shading method, of cast profiles of the patient's maxilla measured by the present system. Teeth and the palate were measured in a pitch of 0.2 and 0.4 mm, respectively. The first premolars of this patient were extracted prior to orthodontic treatment.

±12 mm, a spot on a plaster block fixed on a mechanical Z-stage. Since the relation is slightly curvilinear in principle, the regression curve of the 50 measured data was obtained and used for converting the peak position into depth. The standard deviation of the data around the curve was 0.024 mm, and 92% of the data distributed with an error of less than 0.05 mm. The present apparatus is, therefore, able to detect a depth with an approximate accuracy of 0.05 mm.

We also tested the lateral resolution by scanning a plaster block on which thin grooves were cast using metal plates of known thickness (0.1 and 0.2 mm) and confirmed that our system attained the lateral resolution of at least 0.1 mm. In our current system, actual resolution is not determined by the sharpened laser beam but by the minimum scanning pitch 0.1 mm of the plotter used.

III. MEASUREMENT OF THREE-DIMENSIONAL TOOTH MOVEMENT

Numerical Registration of Three-Dimensional Image

Our principle of measuring the three-dimensional movement of a tooth during orthodontic treatment is based on the registration, using a computer, of three-dimensional tooth images measured by the present profilometer at different stages of treatment. Namely, tooth profiles taken at the initial stage of treatment are numerically moved and superimposed on those of a certain later stage. The numerical movement of each tooth which attains to the close matching of the images gives the actual movement of the tooth.

In order to represent changes in position of a rigid body in three-dimensional space, we must introduce six parameters. These are defined, as illustrated in Fig. 4, by the translations \( \Delta x \), \( \Delta y \), and \( \Delta z \), and by the rotations \( \phi \), \( \theta \), and \( \psi \) which denote the tipping direction, the tipping angle and the rotation angle with respect to the Z-axis, respectively. In conformity with the terms tipping and rotation defined in dentistry, the present definition of the angles were modified from Euler's angles conventionally used for describing the amount of rotation in three-dimensional space, i.e., \( \psi \) was redefined by \( \phi + \psi \) of Euler's angles. According to this definition, a tooth tips by \( \theta \) to the direction of \( \phi \) and then rotates by \( \psi \) around the Z'-axis, as shown in Fig. 4. The coordinate system was fixed on each tooth of the initial stage and its origin was chosen as the centroid of the occlusal surface determined from the tooth profiles of the initial stage.

New coordinates necessary for carrying out the registration were calculated by the following equation:

\[
\mathbf{r}' = \mathbf{R} \cdot \mathbf{r} + \Delta \mathbf{r}
\]

where \( \mathbf{r'} \) is the coordinates \([x', y', z']^T\) after the numerical moving, \( \mathbf{R} \) is a rotation matrix, \( \mathbf{r} \) is the original \([x, y, z]^T\) before the moving, and \( \Delta \mathbf{r} \) is the translations \([\Delta x, \Delta y, \Delta z]^T\). The \( \mathbf{R} \) is given by the matrix:

\[
\begin{bmatrix}
\cos \theta \cos \phi \cos (\psi - \phi) & -\cos \theta \cos \phi \sin (\psi - \phi) & \sin \theta \cos \phi \\
-\sin \phi \sin (\psi - \phi) & -\sin \phi \cos (\psi - \phi) & \sin \phi \cos \theta \\
\cos \theta \sin \phi \cos (\psi - \phi) & -\cos \theta \sin \phi \sin (\psi - \phi) & \sin \theta \sin \phi \\
+\cos \phi \sin (\psi - \phi) & +\cos \phi \cos (\psi - \phi) & \cos \theta \\
-\sin \theta \cos (\psi - \phi) & \sin \theta \sin (\psi - \phi) & \cos \theta
\end{bmatrix}
\]
The registration was carried out automatically by searching for an optimal combination of $H$ and $\Delta \gamma$ until the amount of mismatching of the tooth images of the initial and the later stages became minimum. The mismatching was evaluated from the averaged value of difference $u$ in the $z$-coordinate.

$$u = \frac{1}{n} \sum_{i=1}^{n} |z_i - z_i'|$$

where $z_i'$ denotes the numerically moved datum $z'(x', y')$, calculated by (1), of the initial stage, $z_i$ is the datum of the later stage, and $n$ is the number of data used for the registration. For the coincidence of horizontal coordinates of $z_i$ and $z_i'$, $z_i'$ was interpolated; $z(x', y')$ was obtained from four values of $z(x, y)$ around the point $(x', y')$. Mathematically the registration is regarded as a procedure searching for a point of minimum of a function of multivariable. Such a procedure was executed by an iterative method of calculation, changing the value of one of the six parameters back and forth, and repeating the same algorithm is turn on the parameters to reach the final minimum of the function $u$. At the beginning of the iteration we set the initial values of the parameters to 1 mm in translations, $5^\circ$ in $\theta$ and $\gamma$, and $15^\circ$ in $\phi$. These initial values were not so critical in finding the minimum. But, coarse alignment in translations using the centroid of the profiles before the iteration was effective in preventing the above procedure from reaching a false, local minimum.

Prior to the registration of teeth, the three-dimensional position of casts to be compared must be normalized, because the position cannot be adjusted accurately when casts are measured. For this purpose, the palate was employed as a reference. Namely, the palates were first superimposed by the same algorithm as that of teeth. As described later in “Discussion,” profile details of the palate are rather stable during orthodontic treatment and therefore appropriate for an immovable reference.

The error in the calculated movement by the above procedure was evaluated through the simulation study, in which actual measured data of a molar were numerically moved by substituting random numbers for the parameters and then the registration was performed between the measured and the moved data. The 36 movements calculated in all showed sufficiently small errors less than 0.1 mm in translation and 0.5$^\circ$ in rotation. It should be noted that the error in translation is less than the scanning pitch 0.2 mm of a tooth because the procedure in the registration was designed to interpolate the data.

**Clinical Measurement**

Various types of springs are in common use as an orthodontic appliance to produce a force on teeth. In order to quantify the effect of spring configurations on tooth movement, we measured upper canine movements on patients over periods of 41 to 190 days when the canines were moved by two types of springs conventionally used: an open single loop (referred to as spring A) and a closed loop with multiple helices (spring B), which are illustrated in Fig. 5. After extracting the first premolars, canine retraction was commenced on three males and seven females. Patients were 11-15 years of age, with the exception of a 23-year-old male. A force of 150 g was applied so that the posterior teeth pulled the canine by the sectional retraction method. As the force decreases with space closure, the springs were reactivated to 150 g almost every month. At that time a dental cast was taken from a patient and the canine movement from the initial stage to that stage was measured by the procedure mentioned in the previous section.

Data were collected under four groups according to the treatment conditions classified below. In connection with this, two kinds of bends incorporated in a spring should be referred to. When a single force is placed on the lateral portion of the crown of a tooth, the tooth rotates and tips owing to the moment of rotation resulting from the force. Against such a rotational tendency antiarotation and gable bends are commonly set up in a spring to create a moment of counter-rotation. The magnitude of this effective force is adjusted by an angle of bending. Classified treatment conditions are the following. In all groups the angle of a gable bend was set to 20-35$^\circ$.

- **Group 1**: spring A with an antiarotation angle of 20$^\circ$.
- **Group 2**: spring B with the same bend as the above.
- **Group 3**: spring A without an antiarotation bend.
- **Group 4**: spring B without an antiarotation bend.

As shown in Fig. 5, the spring B (group 2) is capable of moving the canine almost twice as fast as the spring A (group 1) because spring B, which has the multiple helices and numerous flexibility, conserves most of the activated force even if a certain amount of space closure occurs. However, spring B (groups 2 and 4) shows no significant effect of the antiarotation bend on tooth rotation $\gamma$, as shown in Fig. 6. On the contrary, spring A, which has less flexibility than spring B, has the greater ability to protect the rotation when incorporating the antiarotation bend (group 1), as shown in Fig. 7.

**IV. DISCUSSION**

An apparatus using an optical probe, developed by Berkowitz et al. [8], is the first and the only automatic apparatus, to our knowledge, for three-dimensional measurement of dental casts. Although it was successfully applied to cleft palate cast analysis, it has the limitation of the minimum detectable depth interval of 0.5 mm and the lateral resolution of about 1 mm under the total measuring depth range of 18 mm. It is because the measurement is based on utilizing the relationship between the depth and the light intensity change due to defocusing. The recent development of the travelling microscope by Bhata and Harrison [7] has notably increased the accuracy of measurement in Z-dimension. The claimed accuracy is 0.024 mm, but this apparatus has to be operated manually as well as the others [4-6]. The present apparatus is automated and its accuracy is, at least, 0.05 mm in depth and 0.1 mm on a horizontal plane within
The spring with the antirotation bend

Negative values mean the counter-rotation caused by the antirotation bend.

Fig. 7. Effect of an antirotation bend in spring $A$ on the tooth rotation $\psi$. The spring with the antirotation bend $\theta$ of $20^\circ$ (solid lines) showed the marked effect in comparison with the spring without a bend (broken lines). Negative values mean the counter-rotation caused by the antirotation bend.

the depth range of 25 mm. The problem to be overcome is that data of the lateral portion of a tooth are unavailable because the optical equipment is placed on the side above a dental cast, as is most apparatus developed up to now.

Previous studies with respect to the measurement of tooth movement over a long period of orthodontic treatment were restricted to one or two dimensions. As for the three-dimensional measurement, only the instantaneous translation and rotation, observed immediately after applying an orthodontic force to a tooth, have been measured using laser hologram interferometry [13]-[16]. This technique measures movement with the highest degree of sensitivity but is restricted to short-term observations.

Our approach is based on registration of profiles of serial casts, and consequently enables long-term movement to be followed. An interesting method also using registration for the measurement of two-dimensional tooth movement during orthodontic treatment has recently been reported [17] where a cast and a holographic image representing different stages are manually superimposed within an X-Y plane by mechanical stages.

The accuracy of movement measurement with the present method depends on the registration and the irrenovable error. The error in the registration examined by the simulation study was less than 0.1 mm in translation and 0.5° in rotation. These are, however, the minimum errors resulting only from the calculation. Actual accuracy is mostly determined by the reproducibility of plaster casts. Therefore, care should be taken in the process of making a cast. The effect of the reproducibility on the error is now being studied. To confirm the morphological stability of the palate employed as a reference, we evaluated its deformation during orthodontic treatments of 6-21 months in nine patients of 8-14 years of age. The "averaged" value of difference in depth on each patient before and after treatment was only 0.05-0.13 mm, which were calculated by (2) except for the palate data around realigned teeth. The deformation of the palate around the teeth is much larger than that of the bottom. In practice we have used palata data within 5 mm from the bottom as the reference. The palate is thus, an appropriate reference. However, it has limitation of applicability only to the maxilla because of the presence of the tongue in the mandible.

Despite the above limitation, the results in the time course analysis of tooth movement on the patients suggest the usefulness of the present technique in quantifying the action of a spring upon tooth movement. The importance of such a technique is easily understood from the fact that it is quite difficult to detect three-dimensional tooth movement with the eyes. The present technique also shows promise of presenting useful quantitative information to the orthodontist, who is then able to optimize a treatment procedure by readjustment of the magnitude and direction of the force and of the antirotation and gable bends of a spring in response to the tooth movement due to treatment. The automatic digitization of cast profiles will permit further application to computerization of cast analysis [18], which is now performed on manually digitized data.

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REFERENCES


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