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Temperature dependence of spin-dependent tunneling conductance of magnetic tunnel junctions with half-metallic Co₂MnSi electrodes

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In order to elucidate the origin of the temperature (T) dependence of spin-dependent tunneling conductance (G) of magnetic tunnel junctions (MTJs), we experimentally investigated the T dependence of G for the parallel and antiparallel magnetization alignments, G_P and G_{AP} , of high-quality Co₂MnSi (CMS)/MgO/CMS MTJs having systematically varied spin polarizations (P) at 4.2 K by varying the Mn composition α in Co₂Mn _{α} Si electrodes that exhibited giant tunneling magnetoresistance ratios. Results showed that G_P normalized by its value at 4.2 K exhibited a notable, nonmonotonic T dependence although its variation with T was significantly smaller than that of G_{AP} normalized by its value at 4.2 K, indicating that an analysis of the experimental $G_P(T)$ is critical to revealing the origin of the T dependence of G . By analyzing the experimental $G_P(T)$, we clarified that both spin-flip inelastic tunneling via a thermally excited magnon and spin-conserving elastic tunneling in which P decays with increasing T play key roles. The experimental $G_{AP}(T)$, including its stronger T dependence for higher P at 4.2 K, was also consistently explained with this model. Our findings provide a unified picture for understanding the origin of the T dependence of G of MTJs with a wide range of P , including MTJs with high P close to a half-metallic value.

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I. INTRODUCTION

Spintronic devices, which utilize the spin degree of freedom in addition to the charge of the electron, have attracted much interest as future-generation electron devices. This is because of their potential advantages of nonvolatility, decreased power consumption, and reconfigurable logic function capabilities [1,2]. A highly efficient spin source is essential for constructing spintronic devices. Half-metallic ferromagnets (HMFs) are one of the most suitable spin source materials because of their complete spin polarization at the Fermi level (E_F) arising from an energy gap for one spin direction (mostly the minority-spin band) [3]. Co-based Heusler alloys (Co₂YZ, where Y is usually a transition metal and Z is a main group element) [4] are among the most extensively applied to spintronic devices, including magnetic tunnel junctions (MTJs) [5–17] and giant magnetoresistance (GMR) devices [18–22], and for spin injection into semiconductors [23–27]. This is because of the HMF nature theoretically predicted for many of these alloys [28–31] and because of their high Curie temperatures, which are well above room temperature [32].

Co₂MnSi (CMS) is one of the most extensively investigated ferromagnetic electrode materials among the Co₂YZ family [6–12,18,20,23,26,27,33–41]. This is because of its theoretically predicted half-metallic nature with a large half-metal

gap of 0.81 eV for its minority-spin band [29–31] and its high Curie temperature of 985 K [32]. In practice, to various degrees, off-stoichiometry in Co₂YZ thin films prepared by magnetron sputtering or molecule beam epitaxy is inevitable, leading to structural defects. Picozzi *et al.* predicted from first principles that half-metallicity in CMS and Co₂MnGe (CMG) is lost for Co_{Mn} antisites, where a Mn site is replaced by a Co atom, because of the appearance of minority-spin in gap states near E_F , while half-metallicity is retained for Mn_{Co} antisites, where a Co site is replaced by a Mn atom [33]. The effect of off-stoichiometry on the half-metallicity of CMS and CMG has been systematically investigated recently using various experimental approaches, including the tunneling magnetoresistance (TMR) ratios of MTJs [9–12], the saturation magnetization per formula unit of thin films [12], the surface spin polarization [42], the magnetic states as investigated by x-ray absorption spectroscopy and x-ray magnetic circular dichroism [43–45], and the electronic states as investigated through spin-resolved low-energy and hard x-ray photoelectron spectroscopy [46–48]. These experimental studies, along with first-principles calculations, demonstrated that Co_{Mn} antisites induced by a Mn-deficient composition (the Mn composition $\alpha < 2 - \beta$ in the composition expression of Co₂Mn _{α} Si _{β}) is detrimental to the half-metallicity of CMS. Furthermore, it was shown that harmful Co_{Mn} antisites can be suppressed and half-metallicity enhanced by preparing CMS thin films with a Mn-rich composition [9–12]. It was also shown that (Mn + Fe)-rich compositions are critical

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to suppressing these harmful antisites and to retaining the half-metallic electronic states for $\text{Co}_2(\text{Mn,Fe})\text{Si}$ (CMFS) quaternary alloys [16,17]. Given these findings, we demonstrated giant TMR ratios of up to 1995% at 4.2 K and up to 354% at 290 K for CMS/MgO/CMS MTJs (CMS MTJs) having Mn-rich CMS electrodes [11] and up to 2610% at 4.2 K and 429% at 290 K for CMFS/MgO/CMFS MTJs (CMFS MTJs) with Mn-rich, lightly Fe-doped CMFS electrodes [16].

To take full advantage of the half-metallic nature of Co-based Heusler alloys as spin source materials at room temperature, it is important to clarify the origin of the temperature (T) dependence of spin-dependent tunneling conductance (G) of MTJs. The T dependence of G for the parallel and antiparallel magnetization alignments, G_P and G_{AP} , of MTJs has been discussed on the basis of models proposed by Zhang *et al.* [49] and by Shang *et al.* [50]. Zhang *et al.* accounted for the T dependence of G_P and G_{AP} by spin-flip inelastic tunneling via a thermally excited magnon while assuming a T -independent spin polarization, P [49]. The Zhang model predicts that (i) both G_P and G_{AP} increase with increasing T , and (ii) the increase in G_{AP} normalized by its value at 4.2 K [$G_{AP}(T)/G_{AP}(4.2\text{ K})$] with increasing T becomes larger for higher P while that in G_P normalized by its value at 4.2 K [$G_P(T)/G_P(4.2\text{ K})$] with T becomes smaller for higher P . On the other hand, Shang *et al.* took into consideration only spin-conserving elastic tunneling with a decaying P with increasing T . The Shang model predicts that G_{AP} increases with T , of which the effect on $G_{AP}(T)$ is apparently in agreement with that of the Zhang model. Indeed, the experimental $G_{AP}(T)$ had been explained and fitted by the original Zhang model in [51,52] or by the Shang model in [53]. However, note that the tunneling mechanisms that determine the T dependence are intrinsically different between these two models. On the other hand, the Shang model predicts that G_P decreases, which is opposed to the prediction of the Zhang model. Previous studies on MTJs with an amorphous AlO_x tunnel barrier reported an increase in G_P with increasing T up to room temperature [50,51]. Most of the epitaxial MTJs with an MgO or MgAl_2O_4 tunnel barrier that have been reported so far have also shown an increase in G_P [8,52–57], while some epitaxial MTJs showed a decrease [58–60]. The increase in G_P with T for MTJs, including epitaxial MTJs, has been mostly explained by spin-flip inelastic tunneling via a thermally excited magnon, i.e., the Zhang model with an evidence of the role played by magnons indicated by tunneling spectroscopy [51,52,56]. Alternatively, the increase in G_P with T for an epitaxial MTJ has been explained within the framework of the Shang model by taking into account the smearing effect of the Fermi distribution function at finite temperatures [53], which increases G as T increases [61]. Note, however, that the influence of spin-flip inelastic tunneling was ignored in the Shang-model-based analysis. On the other hand, the origin of the decrease in G_P with increasing T observed for some epitaxial MTJs [58–60] is not yet fully understood. Thus, a more systematic experimental study is essential to get a deeper understanding of the origin of the T dependence of spin-dependent G_P and G_{AP} .

A promising approach would be to investigate half-metal-based MTJs with systematically varied P values at 0 K, as MTJs with highly spin-polarized electrodes arising from

half-metallicity would show most typical T dependence of G_P and G_{AP} . In addition, it is a particularly desirable approach to extract how the T dependence of G_P and G_{AP} changes with P at 0 K by investigating a series of high-quality MTJs with systematically varied P at 0 K. Furthermore, development of a more comprehensive model for the T dependence of G_P and G_{AP} is requisite as the predictions of the Zhang and Shang models for $G_P(T)$ are opposite. This difference in the predictions for $G_P(T)$ also suggests that an analysis of the experimental $G_P(T)$ would be critical to revealing the origin of the T dependence of spin-dependent G .

The purpose of this paper is to elucidate the origin of the T dependence of G_P and G_{AP} of MTJs through analyzing the experimental $G_P(T)$ and $G_{AP}(T)$ of high-quality MTJs showing giant TMRs and to provide a unified picture of how the T dependence of G_P and G_{AP} changes with P . To do so, we experimentally investigated the T dependences of G_P and G_{AP} of CMS MTJs having systematically varied spin polarizations at 4.2 K by varying the Mn composition α in $\text{Co}_2\text{Mn}_\alpha\text{Si}$ electrodes that exhibited a giant TMR ratio of up to 2110% at 4.2 K (up to 366% at 290 K) [11,16]. Notable features in $G_P(T)$ were found; i.e., it decreased with increasing T from T_1 of about 30 K to T_2 ranging from about 162 K to 237 K depending on α ; then it increased for $T > T_2$. Furthermore, as P at 4.2 K increased, T_2 increased, and the maximum decrease in the normalized G_P [$=G_P(T)/G_P(4.2\text{ K})$] at T_2 increased. To clarify the origin of the characteristic T dependence of G_P , we developed a model that took into account both spin-conserving elastic tunneling in which P decays with increasing T and spin-flip inelastic tunneling via a magnon by extending the original Zhang model [49]. The extension of the Zhang model was possible because of its generality in the sense that its expressions of $G_P(T)$ and $G_{AP}(T)$ include both elastic and inelastic tunneling terms, although P is assumed to be independent of T . Accordingly, we showed that the proposed model could reproduce the nonmonotonic behavior of the experimental $G_P(T)$. Furthermore, the dependence of the experimental $G_P(T)$ on P at 4.2 K was well explained by the proposed model. The model also consistently explained the experimental $G_{AP}(T)$, including a stronger T dependence for higher P at 4.2 K. Thus, it was found that elastic tunneling with decaying P with increasing T and inelastic tunneling via a magnon are two key factors that determine the T dependence of spin-dependent tunneling conductance of MTJs. This finding is generally applicable to MTJs with a wide range of P . It was also indicated that an analysis of the experimental $G_P(T)$ is critical to revealing the origin of the T dependence of G_P and G_{AP} .

The paper is organized as follows. Section II presents our experimental methods. Section III presents the results and discussion. Section III A first describes the overall features of $G_P(T)$ and $G_{AP}(T)$ of CMS MTJs with various α values that showed a high TMR ratio of up to 2110% at 4.2 K (366% at 290 K). Then it describes $G_P(T)$ in detail. After that, it describes the extension of the Zhang model that incorporates a T -dependent P to explain the characteristic T dependence of G_P observed for the CMS MTJs with half-metallic electrodes. Section III B shows that $G_{AP}(T)$ can be also consistently explained by this extended Zhang model. Section IV summarizes our results and concludes the paper.

II. EXPERIMENTAL METHODS

We measured and analyzed the $G_P(T)$ and $G_{AP}(T)$ mainly of two series of $\text{Co}_{50}\text{Fe}_{50}$ (CoFe)-buffered CMS MTJs having $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes or $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.96}$ electrodes. The series had various α values ranging from a Mn-deficient composition of $\alpha < 2 - \beta$, where β is the Si composition in the film composition expression of $\text{Co}_2\text{Mn}_\alpha\text{Si}_\beta$, to a Mn-rich one of $\alpha > 2 - \beta$. The MTJ layer structure was as follows: (from the substrate side) MgO buffer (10 nm)/CoFe buffer (30 nm)/CMS lower electrode (3 nm)/MgO barrier (1.4–3.2 nm)/CMS upper electrode (3 nm)/CoFe (1.1 nm)/ $\text{Ir}_{22}\text{Mn}_{78}$ (10 nm)/Ru cap (5 nm), grown on a MgO(001) substrate, as shown in Fig. 1. The fabrication procedure of the CoFe-buffered CMS MTJs has been reported elsewhere [11]. Briefly, each layer was successively deposited in an ultrahigh-vacuum chamber equipped with magnetron cathodes and an electron-beam evaporator. The CMS electrodes were prepared by magnetron cosputtering from a nearly stoichiometric CMS target and Mn target (with a base pressure of about 6×10^{-8} Pa). The MgO tunnel barrier in the MTJ layer structure had a wedge shape, and its nominal thickness was varied from 1.4 to 3.2 nm on each $20 \times 20 \text{ mm}^2$ MgO(001) substrate by linearly moving the shutter during the deposition by electron-beam evaporation. Figure 2 plots typical dependence on t_{MgO} of $R_P A$, $R_{AP} A$, and the TMR ratio at 290 K for CMS MTJs with $\text{Co}_2\text{Mn}_{1.30}\text{Si}_{0.84}$ electrodes fabricated on a $20 \times 20 \text{ mm}^2$ substrate over a t_{MgO} range from 2.2 to 3.1 nm, where A is the nominal junction area of $10 \times 10 \mu\text{m}^2$. We have reported TMR ratios of up to 2110% at 4.2 K and 366% at 290 K for these MTJs [16]. The dependences of $R_P A$ and $R_{AP} A$ on t_{MgO} were exponential with almost identical slopes, resulting in nearly constant TMR ratios from 2.2 to 3.1 nm of t_{MgO} . Furthermore, TMR ratios over 350% were obtained for a wide t_{MgO} range from 2.3 to 3.0 nm, with the maximum TMR ratio being

FIG. 1. Schematic diagram of the layer structure of $\text{Co}_{50}\text{Fe}_{50}$ (CoFe)-buffered $\text{Co}_2\text{Mn}_\alpha\text{Si}_\beta$ (CMS)/MgO/CMS MTJ (CMS MTJ) consisting of (from the substrate side) MgO buffer (10 nm)/CoFe buffer (30 nm)/CMS lower electrode (3 nm)/MgO barrier (1.4–3.2 nm)/CMS upper electrode (3 nm)/CoFe (1.1 nm)/ $\text{Ir}_{22}\text{Mn}_{78}$ (10 nm)/Ru cap (5 nm), grown on a MgO(001) single-crystal substrate.

FIG. 2. Typical dependence of $R_P A$, $R_{AP} A$, and TMR ratio on MgO barrier thickness (t_{MgO}) at 290 K for CMS MTJs with $\text{Co}_2\text{Mn}_{1.30}\text{Si}_{0.84}$ electrodes fabricated on a $20 \times 20 \text{ mm}^2$ substrate over a t_{MgO} range from 2.2 to 3.1 nm, where A is the nominal junction area of $10 \times 10 \mu\text{m}^2$. The MgO tunnel barrier had a wedge structure, and its nominal thickness was varied from 1.4 to 3.2 nm on each $20 \times 20 \text{ mm}^2$ substrate by linearly moving the shutter during the deposition by electron-beam evaporation.

366% at 290 K. The value of $m^* \varphi_0$ (0.51 eV) was determined from the slope of the $\ln(R_P A)$ versus t_{MgO} , where m^* is the effective mass normalized by the electron rest mass and φ_0 is the potential barrier height (the energy difference between the E_F of the emitter ferromagnetic electrode and the bottom of the conduction band in the tunnel barrier). This value was close to that of 0.32 eV for epitaxial $\text{Co}_2\text{Cr}_{0.6}\text{Fe}_{0.4}\text{Al}/\text{MgO}/\text{CoFe}$ MTJs [62] and 0.39 eV for epitaxial Fe/MgO/Fe MTJs [63].

The tunneling conductances $G_P(T)$ and $G_{AP}(T)$ were measured using a dc four-probe method at temperatures from 4.2 to 290 K at both positive and negative bias voltages of ± 2 mV. Both polarities for the bias voltage were used to cancel the small thermoelectric force, which is particularly important for accurately measuring G_P values. The TMR ratio was defined as $\text{TMR} = (G_P - G_{AP})/G_{AP} = (R_{AP} - R_P)/R_P$, where G_P (R_P) and G_{AP} (R_{AP}) are the tunneling conductances (resistances) for the parallel and antiparallel magnetization alignments between the upper and lower electrodes.

III. RESULTS AND DISCUSSION

A. T dependence of tunneling conductance for the parallel alignment

In this section, we first describe the overall features of the experimental T dependences of G_P and G_{AP} of CoFe-buffered CMS MTJs with $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes with various α values ranging from a Mn-deficient $\alpha = 0.73$ to Mn-rich $\alpha = 1.24$ and 1.30. Then we describe the features of the experimental $G_P(T)$ in detail. Given the experimental results, we devise an extension of the Zhang model by introducing a T -dependent spin polarization and use it to discuss the origin

FIG. 3. (a) Typical temperature dependence of G_P/A and G_{AP}/A of a CMS MTJ with Mn-rich $\text{Co}_2\text{Mn}_{1.30}\text{Si}_{0.84}$ electrodes and $t_{\text{MgO}} = 2.65 \text{ nm}$ from 4.2 to 290 K showing TMR ratios of 2010% at 4.2 K and 335% at 290 K, where G_P and G_{AP} are the tunneling conductances for the parallel and antiparallel magnetization alignments between the lower and upper electrodes, and A is the nominal junction area of $10 \times 10 \mu\text{m}^2$. The bias voltage was 2 mV. (b) Resulting T dependence of the TMR ratio.

of the observed T dependence of G_P through analyzing the experimental $G_P(T)$. The $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.96}$ MTJs with various α showed almost identical T dependences for G_P and G_{AP} . The α dependence of the TMR ratio of the $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ MTJ series has been reported, and a TMR ratio of up to 2110% at 4.2 K (366% at 290 K) has been demonstrated for this MTJ series [16]. Figure 3(a) shows typical T dependence of G_P and G_{AP} from 4.2 to 290 K of a CMS MTJ with $\alpha = 1.30$ ($\text{Co}_2\text{Mn}_{1.30}\text{Si}_{0.84}$ electrodes) that showed TMR ratios of 2010% at 4.2 K and 335% at 290 K. Here, G_{AP} showed a strong T dependence (G_{AP} at 290 K was 4.6 times higher than that at 4.2 K), while G_P changed only about

FIG. 4. (a) Normalized G_P and (b) G_{AP} as a function of T from 4.2 to 290 K for CMS MTJs with various α ranging from Mn-deficient $\alpha = 0.73$ to Mn-rich $\alpha = 1.30$ in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes, where G_P and G_{AP} are normalized by the respective values at 4.2 K. The data of $\alpha = 1.30$ MTJ are the same as those shown in Fig. 3.

3% and could be regarded as being almost independent of T compared with the strong variation in G_{AP} . Because of these characteristics, the T dependence of the TMR ratio was determined mostly by that of G_{AP} , resulting in a strong T dependence of the TMR ratio [Fig. 3(b)]. Figure 4(a) plots the experimental $G_P(T)$ normalized by the respective values at 4.2 K, $G_{P,N}(T) = G_P(T)/G_P(4.2 \text{ K})$, of the CMS MTJs with various α values. Furthermore, Fig. 4(b) plots the experimental $G_{AP}(T)$ normalized by the respective values at 4.2 K, $G_{AP,N}(T) = G_{AP}(T)/G_{AP}(4.2 \text{ K})$. The TMR ratio at 4.2 K of these CMS MTJs increased with increasing α from 0.73 to 1.30 (Table I). The increase in the TMR ratio has been explained by the enhancement of half-metallicity due to the suppression of Co_{Mn} antisites for a Mn-rich composition [10,12]. As a basis for the characterization and analysis of the experimental $G_P(T)$ and $G_{AP}(T)$, we deduced the spin polarization at 4.2 K, $P(4.2 \text{ K})$, for these MTJs from the TMR ratios at 4.2 K by assuming the Julliere model [64], i.e.,

$$\text{TMR ratio} = \frac{2P^2}{1 - P^2}, \quad (1)$$

TABLE I. TMR ratios at 4.2 and 290 K of CMS MTJs with various α in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes of which $G_{P,N}(T)$ and $G_{AP,N}(T)$ are shown in Fig. 4 along with the respective nominal MgO barrier thicknesses (t_{MgO}). The tunneling spin polarizations at 4.2 K, $P(4.2 \text{ K})$, deduced from the Julliere model [Eq. (1)] with the respective TMR ratios at 4.2 K, are also shown. The tunneling spin polarizations at 0 K, P_0 , could be approximated by the respective $P(4.2 \text{ K})$ and could be used in the analysis.

α in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$	t_{MgO} (nm)	TMR ratio at 4.2 K	TMR ratio at 290 K	$P(4.2 \text{ K})$
0.73	2.65	574%	178%	0.861
1.24	2.69	1510%	322%	0.940
1.30	2.65	2010%	335%	0.954

where P is defined using the majority-spin and minority-spin density of states (DOS) at E_F , ρ_M and ρ_m , as $P = (\rho_M - \rho_m)/(\rho_M + \rho_m)$. We also assumed that the lower and upper electrodes had an identical P . Table I summarizes the deduced $P(4.2 \text{ K})$ for the CMS MTJs. As demonstrated by their high TMR ratios at 4.2 K, the CMS MTJs exhibited significantly high P values of up to 0.954 at 4.2 K corresponding to the experimentally obtained TMR ratio of 2010% at 4.2 K. We approximated P at 0 K, P_0 , by $P(4.2 \text{ K})$ in the following analysis. The crucial role of coherent tunneling [65,66] has been experimentally [11] and theoretically [67] demonstrated in CMS MTJs. Thus, the P deduced from Eq. (1) is the value determined by ρ_M and ρ_m arising from the electronic states contributing to coherent tunneling [12,17]. In this sense, the deduced P should be called the tunneling spin polarization, although we will still refer to it as the tunneling spin polarization or spin polarization without distinguishing the meanings.

Note that the normalized $G_P(T)$ and $G_{AP}(T)$ data plotted in Fig. 4 are for MTJs having almost identical nominal t_{MgO} values of $2.66 \text{ nm} \pm 1\%$ (Table I). Thus, the smearing effect of the Fermi distribution function at finite temperatures to the tunneling conductance [50,52,61] can be regarded as almost identical for these MTJs.

As shown in Fig. 4(a), the $G_{P,N}(T)$ of these MTJs exhibited distinct features, even though it can be regarded to be almost independent of T compared with the strong T dependence of $G_{AP,N}(T)$. The first feature is that the $G_{P,N}$ decreased with increasing T from $T = T_1$ of about 30 K to $T = T_2$ ranging from about 162 K for $\alpha = 0.73$ to 237 K for $\alpha = 1.30$.

Then it increased for $T > T_2$. The second feature is that T_2 increased as the TMR ratio at 4.2 K increased or equivalently $P(4.2 \text{ K})$ increased, as shown in Fig. 5(a). The third feature is that the maximum decrease in the experimental $G_{P,N}$ at T_2 , defined as $\Delta G_{P,N}(T_2) = G_{P,N}(T_2) - 1$ increased in magnitude as $P(4.2 \text{ K})$ increased, as shown in Fig. 5(b).

On the other hand, the degree of the T dependence of $G_{AP,N}$ increased as $P(4.2 \text{ K})$ increased. Our previous paper discussed the T dependence of G_{AP} for CMS MTJs with various tunneling spin polarizations in terms of $G_{AP}(290 \text{ K})/G_{AP}(4.2 \text{ K})$ according to the original Zhang model [12]. This paper discusses the key factors that determine the T dependences of G_P and G_{AP} from a wider point of view.

Now let us discuss how these features of $G_{P,N}(T)$ and $G_{AP,N}(T)$ can be explained consistently. We will first analyze the experimental T dependence of $G_{P,N}$. The comparison of the experimental $G_{P,N}(T)$ with the predictions clearly indicates that neither the Shang model nor the Zhang model can explain the experimental $G_{P,N}(T)$. Thus, an analysis of $G_{P,N}(T)$ is crucial to clarifying the origin of the T dependence of spin-dependent tunneling conductance in MTJs with highly spin-polarized electrodes. We will focus on the decrease in $G_{P,N}$ as T increases from T_1 to T_2 and the increase in $G_{P,N}$ as T increases for $T > T_2$. Furthermore, taking into consideration that the variation in $G_{P,N}$ for $T < T_1$ was smaller than that for $T > T_1$ by one order of magnitude, we will ignore the small increase in G_P for $4.2 \text{ K} < T < T_1$. Regarding the experimental $G_{P,N}(T)$, the prediction of the Shang model for G_P , i.e., the negative dG_P/dT , is qualitatively in agreement with the experimental decrease in G_P for the T range from T_1 to

FIG. 5. Dependence of (a) the characteristic temperature T_2 and (b) the maximum decrease in the normalized G_P ($G_{P,N}$) at T_2 , defined as $\Delta G_{P,N}(T_2) = G_{P,N}(T_2) - 1$, on the tunneling spin polarization at 4.2 K, $P(4.2 \text{ K})$. The straight lines are guides for the eye.

T_2 , whereas the prediction of the Zhang model, i.e., the positive dG_P/dT , is qualitatively in agreement with the experimental increase in G_P in the T range above T_2 . Furthermore, the original Zhang model is more general than the Shang model in the sense that its expression for the tunneling conductance consists of both a spin-conserving elastic tunneling term and a spin-flip inelastic tunneling term, while the Shang expression consists only of a spin-conserving elastic tunneling term. Given its greater generality, we decided to extend the original Zhang model by introducing a T dependence of P , i.e., a T dependence of ρ_M and ρ_m . This extension leads to a T dependence in the elastic tunneling term. We also took into consideration the effect of the broadening of the Fermi distribution, i.e., the smearing effect [50,52,61], on $G_P(T)$. In such a case, the elastic and inelastic tunneling conductance terms for the parallel alignment at a finite T are multiplied by a factor

$$S_e(T) = CT / \sin(CT), \quad (2)$$

where $C = 1.387 \times 10^{-3} t / \varphi^{1/2}$, t is the thickness of the barrier (in nanometers), and φ is the barrier height (in electronvolts) [61]. We assumed a φ of 3.5 eV, which corresponds to half the MgO band gap [52]. The validity of this value will be described later in this section. A typical value of $S_e(T)$ at 290 K is 1.056 for a t_{MgO} of 2.65 nm. The introduction of this small factor is required to fit the $G_P(T)$ of the CMS MTJs that had high spin polarization. This is because its variation as a function of T became small, i.e., being comparable to the variation in $S_e(T)$ as P_0 increases. Accordingly, $G_P(T)$ in the extended Zhang model for $k_B T > E_c$ is

$$G_P(T) = G_{P,\text{el}}(T) + G_{P,\text{in}}(T), \quad (3a)$$

$$G_{P,\text{el}}(T) = S_e(T) Q_1 \{ [\rho_M(T)]^2 + [\rho_m(T)]^2 \}, \quad (3b)$$

$$G_{P,\text{in}}(T) = S_e(T) Q_2 k_B T \cdot f(T) \cdot 2\rho_M(T)\rho_m(T), \quad (3c)$$

where Q_1 , Q_2 , and $f(T)$ are

$$Q_1 = \frac{4\pi e^2}{\hbar} (|T^d|^2 + 2S^2 |T^J|^2), \quad (3d)$$

$$Q_2 = \frac{4\pi e^2}{\hbar} \frac{2S}{E_m} |T^J|^2, \quad (3e)$$

$$f(T) = -\ln \left[1 - \exp \left(-\frac{E_c}{k_B T} \right) \right]. \quad (3f)$$

The definitions of the parameters T^d , T^J , S , E_m , and E_c are given elsewhere [49]. Briefly, T^d and T^J are tunneling matrix elements for direct tunneling and for tunneling under the s - d exchange interaction between local and itinerant electrons at the interface, respectively, S is the spin parameter, $E_m = 3k_B T_C / (S + 1)$, E_c is the lower magnon cutoff energy, k_B is the Boltzmann constant, and T_C is the Curie temperature of the ferromagnetic electrode. The only difference between this and the original model is that ρ_M and ρ_m are dependent on T in the former, and they are independent of T in the latter. The first term of Eq. (3a), $G_{P,\text{el}}(T)$, represents the spin-conserving elastic tunneling process, and the second term, $G_{P,\text{in}}(T)$, represents the spin-flip inelastic tunneling process via a thermally excited magnon. The first term is equivalent to the Shang model, and also to the Julliere model, although

the latter does not consider the T dependence of P . Here, G_P at $T = 0$ consists of spin-conserving elastic tunneling, which from Eq. (3) can be expressed as

$$G_P(T = 0) = Q_1 \{ [\rho_M(T = 0)]^2 + [\rho_m(T = 0)]^2 \}, \quad (4)$$

[note $S_e(T = 0) = 1$]. Thus, $G_P(T)$ normalized by its value at $T = 0$, $G_{P,N}(T)$, is

$$\begin{aligned} G_{P,N}(T) &= \frac{G_P(T)}{G_P(T = 0)} \\ &= S_e(T) \left\{ 1 - \frac{P_0^2 - [P(T)]^2}{1 + P_0^2} \right\} \\ &\quad + S_e(T) a \left\{ \frac{1 - [P(T)]^2}{1 + P_0^2} \right\} k_B T \cdot f(T), \end{aligned} \quad (5a)$$

where $P(T)$ is the spin polarization at T , defined as

$$P(T) = \frac{\rho_M(T) - \rho_m(T)}{\rho_M(T) + \rho_m(T)}, \quad (5b)$$

$$a = Q \frac{2S}{E_m}, \quad (5c)$$

$$Q = \frac{1}{\frac{|T^d|^2}{|T^J|^2} + 2S^2}, \quad (5d)$$

and the relations $(\rho_M)^2 + (\rho_m)^2 = (1/2)(\rho_M + \rho_m)^2(1 + P^2)$ and $2\rho_M\rho_m = (1/2)(\rho_M + \rho_m)^2(1 - P^2)$ are used along with an assumption of $(\rho_M + \rho_m)$ being independent of T . To fit the experimental $G_P(T)$, we introduced the following Bloch type $T^{3/2}$ dependence for P as in the Shang model [50]:

$$P(T) = P_0(1 - \eta T^{3/2}), \quad (6)$$

where η is a material-dependent constant. Note that Eq. (5) does not include a T -dependent term to explain the small decrease in G_P as T decreases from T_1 of about 30 K to 4.2 K. Thus, the fitted curve for a T range below T_1 becomes extrapolated from a T range above T_1 . Because of this disagreement between the experimental and calculated $G_{P,N}$ for $4.2 \text{ K} < T < T_1$, a small constant c_0 was added to Eq. (5) for fitting. The final form of the normalized $G_P(T)$ in the extended Zhang model is thus

$$G_{P,N,\text{fitting}}(T) = G_{P,N,\text{el}}(T) + G_{P,N,\text{in}}(T) + c_0, \quad (7a)$$

$$G_{P,N,\text{el}}(T) = S_e(T) \left\{ 1 - \frac{P_0^2 [1 - (1 - \eta_P T^{3/2})^2]}{1 + P_0^2} \right\}, \quad (7b)$$

$$G_{P,N,\text{in}}(T) = S_e(T) a \left[\frac{1 - P_0^2 (1 - \eta_P T^{3/2})^2}{1 + P_0^2} \right] k_B T \cdot f(T). \quad (7c)$$

Figure 6 plots the fitting curves of Eq. (7) for the $G_{P,N}(T)$ shown in Fig. 4(a). The extended Zhang model reproduced the apparently complicated $G_{P,N}(T)$ for a wide T range except $T < T_1$. The parameters giving the best fit, including η_P , $a = Q \cdot 2S/E_m$, and E_c^P , where η_P and E_c^P are η and E_c for the parallel alignment, and the resulting $f(290 \text{ K})$ and $a \cdot f(290 \text{ K})$ are summarized in Table II. The η_P value deduced from fitting, for example, for $\alpha = 1.30$ MTJ was $3.29 \times 10^{-5} \text{ K}^{-3/2} \pm 5\%$.

FIG. 6. Fitting curves of the extended Zhang model (solid lines) [Eq. (7)] for the experimental $G_P(T)$ normalized by the respective values at 4.2 K of the CMS MTJs with $\alpha = 0.73$ (open triangles), 1.24 (open squares), and 1.30 (open circles) in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes. The experimental data of $G_P(T)$ are the same as shown in Fig. 4(a). The data of the normalized $G_P(T)$ for $\alpha = 0.73$ and 1.24 have respective offsets of +0.02 and +0.01.

This relatively narrow error range was needed to reproduce the decreasing experimental $G_{P,N}(T)$ with increasing T for $T_1 < T < T_2$. The values of a deduced for the CMS MTJs with various α values are almost equal. The value of a in Eq. (7c) [and which is defined by Eq. (5c)] as calculated using the T_C of 985 K for CMS [32], a spin parameter S from 1/2 to 5/2, and $|T^d|^2/|T^j|^2$ from 10 to 100 (according to Ref. [49]) ranged from 0.059 to 3.06 eV⁻¹. Thus, the deduced value of 3.01 eV⁻¹ for these MTJs was in a reasonable range. Here, E_c^p slightly increased with α from $E_c^p = 0.31$ meV for Mn-deficient $\alpha = 0.73$ to $E_c^p = 0.42$ meV for Mn-rich $\alpha = 1.30$. Regarding η_p , although the values deduced for the CMS MTJs with various α were within $\pm 5\%$, they decreased with increasing α from $\eta_p = 3.70 \times 10^{-5} \text{ K}^{-3/2}$ for $\alpha = 0.73$ to $\eta_p = 3.29 \times 10^{-5} \text{ K}^{-3/2}$ for $\alpha = 1.30$, suggesting an increase in spin wave stiffness [68], or equivalently an increase in the energy of a spin wave with increasing α . We also checked the validity of the deduced η_p values. To do so, we estimated the $P(290 \text{ K})$ values from the respective η_p values for various

α by using Eq. (6). Here, we call the thus-estimated $P(290 \text{ K})$ values $P^{\text{TD}}(290 \text{ K})$ and compare them with the corresponding $P(290 \text{ K})$ values estimated from the respective TMR ratios at 290 K using the Julliere model of Eq. (1) [$P^{\text{TMR}}(290 \text{ K})$]. The $P^{\text{TD}}(290 \text{ K})$ values ranged from $P^{\text{TD}}(290 \text{ K}) = 0.704$ for $\alpha = 0.73$ to $P^{\text{TD}}(290 \text{ K}) = 0.799$ for $\alpha = 1.30$, which are comparable with the $P^{\text{TMR}}(290 \text{ K})$ values ranging from $P^{\text{TMR}}(290 \text{ K}) = 0.686$ for $\alpha = 0.73$ to $P^{\text{TMR}}(290 \text{ K}) = 0.791$ for $\alpha = 1.30$. This comparison suggests the deduced η_p values are in a reasonable range even though the estimated $P^{\text{TD}}(290 \text{ K})$ values should not be regarded as rigorous.

Given the good agreement between the experimental and calculated $G_{P,N}(T)$ given by the extended Zhang model, we can now discuss the origin of the features in the experimental $G_P(T)$ for the CMS MTJs with various α based on this model. The calculated $G_{P,N}(T)$ consists of basically two terms; one is the elastic tunneling term, and the other is the inelastic tunneling term. The variation with T in the elastic tunneling term $\Delta G_{P,N,\text{el}}(T)$ which is defined as $G_{P,N,\text{el}}(T) - G_{P,N,\text{el}}(0)$ is given as

$$\Delta G_{P,N,\text{el}}(T) = S_e(T) \left\{ 1 - \frac{P_0^2 [1 - (1 - \eta_p T^{3/2})^2]}{1 + P_0^2} \right\} - 1, \quad (8)$$

and the variation with T in the inelastic tunneling term $\Delta G_{P,N,\text{in}}(T)$, which is identical to $G_{P,N,\text{in}}(T)$, is given by Eq. (7c). Figure 7(a) plots the variations from the respective values at $T = 0 \text{ K}$ in these two terms. Here, $G_{P,N,\text{el}}(T)$ decreases [$\Delta G_{P,N,\text{el}}(T)$ is negative] and $G_{P,N,\text{in}}(T)$ increases [$\Delta G_{P,N,\text{in}}(T)$ is positive] as T increases. The latter feature is due to $f(T) > 0$. Note that the former and latter features are those predicted by the original Shang and Zhang models, respectively. In the extended Zhang model, there is a competition between these two terms, resulting in a complicated T dependence. Note that $\Delta G_{P,N,\text{in}}(T)$ is smaller for higher P_0 , which arises from the P_0 dependence of the factor $[1 - P_0^2(1 - \eta_p T^{3/2})^2]/(1 + P_0^2) = C_P(T)$ in $\Delta G_{P,N,\text{in}}(T)$. The factor can be approximated as $C_P(T) \approx [1 - P_0^2(1 - 2\eta_p T^{3/2})]/(1 + P_0^2)$, and the term of $2\eta_p T^{3/2}$ can be neglected when discussing the α dependence of $\Delta G_{P,N,\text{in}}(T)$ because $2\eta_p T^{3/2}$ is much smaller than 1 even at 290 K. Accordingly, we can replace the factor $C_P(T)$ by a constant $(1 - P_0^2)/(1 + P_0^2) = \xi$, which decreases as P_0 increases and gets close to 0 as P_0 gets close to 1. Thus, the positive $\Delta G_{P,N,\text{in}}(T)$ is smaller for higher P_0 and gets close to 0 as P_0 gets close to 1. This dependence originates from that $G_{P,\text{in}}(T)$, which is due to spin-flip inelastic tunneling, is proportional to

TABLE II. Parameters of η (K^{-3/2}), $a = Q \cdot 2S/E_m$ (eV⁻¹), E_c (meV), and c_0 for the CMS MTJs with various α shown in Table I deduced from fitting their respective normalized $G_P(T)$ [$=G_P(T)/G_P(4.2 \text{ K})$] by the proposed extended Zhang model, and the resulting $f(290 \text{ K})$ [Eq. (3f)] and $a \cdot f(290 \text{ K})$. The thus-obtained parameters η and E_c for the parallel alignment are represented as η_p and E_c^p .

α in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$	Fitting model	η_p (K ^{-3/2})	$a = Q \cdot 2S/E_m$ (eV ⁻¹)	E_c^p (meV)	$f(290 \text{ K})$	$a \cdot f(290 \text{ K})$	c_0
0.73	Extended Zhang model	3.699×10^{-5}	3.004	0.311	4.392	13.2	0.005
1.24	Extended Zhang model	3.319×10^{-5}	3.006	0.408	4.122	12.4	0.007
1.30	Extended Zhang model	3.294×10^{-5}	3.008	0.415	4.105	12.3	0.008

FIG. 7. (a) Variations with T from the values at $T = 0$ K of the elastic tunneling term $\Delta G_{P,N,\text{el}}(T)$ [Eq. (8)] and the inelastic tunneling term $\Delta G_{P,N,\text{in}}(T)$ [Eq. (7c)] obtained by fitting the experimental $G_{P,N}(T)$ by the extended Zhang model for CMS MTJs with $\alpha = 0.73$ (dotted line), 1.24 (dashed line), and 1.30 (solid line). (b) Absolute values of the derivatives of $G_{P,N,\text{el}}(T)$ and derivatives of $G_{P,N,\text{in}}(T)$ for the CMS MTJs with $\alpha = 0.73$ to 1.30. The intersection of the $-dG_{P,N,\text{el}}(T)/dT$ and $dG_{P,N,\text{in}}(T)/dT$ lines for each α in (b) determines T_2 to be 162 K for $\alpha = 0.73$, 227 K for $\alpha = 1.24$, and 237 K for $\alpha = 1.30$. The triangles, squares, and circles shown in (a) are the $\Delta G_{P,N,\text{in}}(T_2)$ and $\Delta G_{P,N,\text{el}}(T_2)$ values for the $\alpha = 0.73$, 1.24 and 1.30 MTJs, respectively.

the product of $2\rho_M\rho_m$ (ρ_m gets close to 0 for P_0 being close to 1) while the G_P at $T = 0$ is proportional to the sum of $\rho_M^2 + \rho_m^2$ ($\approx \rho_M^2$ for highly spin-polarized electrodes). On the other hand, the dominant term of $\Delta G_{P,N,\text{el}}(T)$ [Eq. (8)] is approximated as $-2P_0^2\eta_P T^{3/2}/(1 + P_0^2)$ because $\eta_P T^{3/2} \ll 1$ and $S_e(T)$ can be replaced with 1 when discussing the α dependence

of $\Delta G_{P,N,\text{el}}(T)$. Thus, the dependence of $\Delta G_{P,N,\text{el}}(T)$ on P_0 is determined by the coefficient, $-2P_0^2/(1 + P_0^2) = B_P$. Because B_P is negative, $G_{P,N,\text{el}}(T)$ decrease as T increases. Furthermore, B_P increases in magnitude as P_0 increases and gets close to -1 as P_0 gets close to 1. This behavior of B_P is in contrast to that of the coefficient ξ , which gets close to 0 as P_0 gets close to 1. Thus, the negative $\Delta G_{P,N,\text{el}}(T)$ increases in magnitude as P_0 increases and gets close to a finite value as P_0 gets close to 1. This P_0 dependence of $\Delta G_{P,N,\text{el}}(T)$ is in contrast to that of the positive $\Delta G_{P,N,\text{in}}(T)$ that gets close to 0 as P_0 gets close to 1. Note the values of $\Delta G_{P,N,\text{el}}(T)$ for P_0 ranging from 0.861 to 0.954 are almost equal. This is because (1) the magnitude in $dG_{P,N,\text{el}}(T)/dP_0$ is smaller than that in $dG_{P,N,\text{in}}(T)/dP_0$ (the former magnitude is half the latter), and (2) although its magnitude is smaller, a further increase in the magnitude of $dG_{P,N,\text{el}}(T)/dP_0$ with increasing P_0 caused by the increase in α was mostly canceled by the smaller η_P for the larger α . In summary, the negative $\Delta G_{P,N,\text{el}}(T)$ becomes the more dominant factor in determining $G_P(T)$ because $\Delta G_{P,N,\text{in}}(T)$ becomes smaller at higher P_0 .

Next, let us discuss the origin of the P_0 dependence of T_2 shown in Fig. 5(a). The characteristic temperature T_2 corresponds to $dG_P(T)/dT = 0$. Figure 7(b) plots the numerically obtained derivatives with respect to T of the elastic tunneling terms, $G_{P,N,\text{el}}(T)$ [Eq. (7b)], and the inelastic term, $G_{P,N,\text{in}}(T)$ [Eq. (7c)], for various α values, where $-dG_{P,N,\text{el}}(T)/dT$ is plotted instead of $dG_{P,N,\text{el}}(T)/dT$ because it is negative. The intersection of the $-dG_{P,N,\text{el}}(T)/dT$ and $dG_{P,N,\text{in}}(T)/dT$ lines for each α determines T_2 to be 162 K for $P_0 = 0.861$ ($\alpha = 0.73$) to 237 K for $P_0 = 0.954$ ($\alpha = 1.30$). The determined T_2 values agree with the corresponding experimental T_2 values because the experimental T_2 values were similarly determined from the $dG_P(T)/dT = 0$ point for the experimental G_P . Because the derivative of $G_{P,N,\text{in}}(T)$ decreased with increasing P_0 , while $-dG_{P,N,\text{el}}(T)/dT$ remained almost constant for various P_0 values, the intersection point moved to a higher T as P_0 increased from 0.861 to 0.954. The decrease in the magnitude of $dG_{P,N,\text{in}}(T)/dT$ with increasing P_0 originated from the coefficient $C_P(T) = [1 - P_0^2(1 - \eta_P T^{3/2})^2]/(1 + P_0^2)$ in $G_{P,N,\text{in}}(T)$.

Now let us turn to the P_0 dependence of the maximum decrease in $G_{P,N}$ at T_2 [Fig. 5(b)]. Figure 7(a) plots straight lines corresponding to the respective T_2 values obtained from the intersection points in Fig. 7(b). The intersections of these straight lines with $\Delta G_{P,N,\text{in}}(T)$ and $\Delta G_{P,N,\text{el}}(T)$ for each α are their values at $T = T_2$. These plots show that $\Delta G_{P,N,\text{el}}(T_2)$ increases in magnitude as P_0 increases from $P_0 = 0.861$ (for Mn-deficient $\alpha = 0.73$) to $P_0 = 0.954$ (for Mn-rich $\alpha = 1.30$), while $\Delta G_{P,N,\text{in}}(T_2)$ is almost constant for various P_0 . The larger increase in the magnitude of $\Delta G_{P,N}(T_2)$ for higher P_0 is explained as follows. Here, $\Delta G_{P,N,\text{in}}(T)$ decreased in the whole T range as P_0 increased. Thus, the contribution of $\Delta G_{P,N,\text{in}}(T)$ basically decreased as P_0 increased. However, because each $\Delta G_{P,N,\text{in}}(T)$ increased with increasing T , and T_2 increased as P_0 increased, $\Delta G_{P,N,\text{in}}(T_2)$ was almost constant for various P_0 . On the other hand, because (1) $\Delta G_{P,N,\text{el}}(T)$ was almost independent of P_0 in the whole T range, (2) the magnitude of $\Delta G_{P,N,\text{el}}(T)$ increased with increasing T , and (3) T_2 increased as P_0 increased, the magnitude of $\Delta G_{P,N,\text{el}}(T_2)$

FIG. 8. Experimental $G_P(T)$ normalized by its value at 4.2 K, $G_P(T)/G_P(4.2 \text{ K})$, of the $t_{\text{MgO}} = 2.31 \text{ nm}$ CMS MTJ with $\text{Co}_2\text{Mn}_{1.24}\text{Si}_{0.84}$ electrodes ($\alpha = 1.24$; open circles) along with that of the $t_{\text{MgO}} = 2.69 \text{ nm}$ CMS MTJ ($\alpha = 1.24$; open squares) for comparison. These two MTJs were prepared with the same device fabrication process on the same epitaxial layer structure. The fitting curve of the extended Zhang model for the $t_{\text{MgO}} = 2.31 \text{ nm}$ CMS MTJ is also shown along with that for the $t_{\text{MgO}} = 2.69 \text{ nm}$ CMS MTJ for comparison. The experimental $G_{P,N}(T)$ data and fitting curve of the extended Zhang model for the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$) are the same as those shown in Fig. 6. The data of the $G_{P,N}(T)$ for the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ have an offset of +0.01.

increased with increasing P_0 . Thus, the main factor that led to the P_0 dependence of the maximum decrease in $G_{P,N}$ at T_2 was $\Delta G_{P,N,\text{in}}(T)$ decreasing with increasing P_0 .

We will now discuss the influence of the smearing effect on the T dependence of $G_{P,N}$ by analyzing two identical CMS MTJs with $\text{Co}_2\text{Mn}_{1.24}\text{Si}_{0.84}$ electrodes prepared in the same device fabrication process on the same MTJ epitaxial layer structure but having different nominal t_{MgO} values of 2.31 and 2.69 nm, where the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$) is the same as that analyzed above. Figure 8 compares the experimental $G_{P,N}(T)$ of the $t_{\text{MgO}} = 2.31 \text{ nm}$ MTJ ($\alpha = 1.24$) with that of the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$) shown in Figs. 4(a) and 6. Here, the $t_{\text{MgO}} = 2.31 \text{ nm}$ MTJ ($\alpha = 1.24$) showed a larger TMR ratio of 1690% at 4.2 K (328% at 290 K) compared with 1510% at 4.2 K (322% at 290 K) for the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$), resulting in a larger $P(4.2 \text{ K})$ of 0.946 for the $t_{\text{MgO}} = 2.31 \text{ nm}$ MTJ ($\alpha = 1.24$) compared with the $P(4.2 \text{ K})$ of 0.940 for the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$). Moreover, the experimental $G_{P,N}(T)$ of the $t_{\text{MgO}} = 2.31 \text{ nm}$ MTJ ($\alpha = 1.24$) had a larger T_2 and a larger decrease at T_2 . These features can be explained by the extended Zhang model, in particular by the two factors involved in the model: one is the larger P_0 , leading to a further reduction in $G_{P,N,\text{in}}(T)$ compared with that for the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$); the other is a smaller $S_e(T)$ value arising from the smaller t_{MgO} , leading to a decrease in the unperturbed term with respect to the T -dependent P in the elastic tunneling term, i.e., the first term of $S_e(T) \cdot 1$ in Eq. (7b). Indeed, the extended Zhang model reproduced the experimental $G_{P,N}(T)$ of the $t_{\text{MgO}} = 2.31 \text{ nm}$

MTJ ($\alpha = 1.24$; Fig. 8) as well as it did for the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$; Fig. 6). As listed in Table III, the deduced η_P , a , and E_c^P and resulting $a \cdot f(290 \text{ K})$ for $t_{\text{MgO}} = 2.31 \text{ nm}$ MTJ ($\alpha = 1.24$) are close to those deduced for the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$; Table II). This indicates that the different behaviors of these two MTJs can be reasonably explained by the P_0 -dependent factor $\xi = (1 - P_0^2)/(1 + P_0^2)$ ($\xi = 0.056$ and 0.062 for the $t_{\text{MgO}} = 2.31$ and 2.69 nm MTJs, respectively) and t_{MgO} -dependent factor $S_e(T)$ in the extended Zhang model.

To reveal the problem associated with fitting $G_P(T)$ by the Shang model with the smearing effect, we tentatively fitted the experimental $G_{P,N}(T)$ of the two MTJs analyzed above. We then compared the fitting results of the Shang model, in particular the deduced parameters, with those of the extended Zhang model. In the analysis of $G_{P,N}(T)$ of the Shang model, we fitted the experimental $G_{P,N}(T)$ by using three free parameters, i.e., η , the barrier height φ in the smearing factor, and the additional small constant c_0 . The fitting function for the normalized experimental $G_{P,N}(T)$ is

$$G_{P,N,\text{Shang}}(T) = S_e(T) \left\{ 1 - \frac{P_0^2 [1 - (1 - \eta_P T^{3/2})^2]}{1 + P_0^2} \right\} + c_0. \quad (9)$$

The fitting curves for both MTJs (not shown) apparently reproduced the experimental $G_{P,N}(T)$ with the fitting parameters shown in Table III. On the other hand, the deduced barrier heights φ in the factor $S_e(T)$ of the Shang model, φ_{Shang} , for these MTJs were quite small (Table III) compared with the $\varphi = 3.5 \text{ eV}$ assumed in the extended Zhang model. Furthermore, the φ_{Shang} value of 1.08 eV for the $t_{\text{MgO}} = 2.31 \text{ nm}$ MTJ was much smaller than the φ_{Shang} value of 1.34 eV of the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ that was needed to reproduce the $G_{P,N}(T)$ of the former MTJ featuring the larger T_2 and the larger decrease at T_2 in the experimental $G_{P,N}(T)$ than that of the latter MTJ. Such a significant difference in the deduced φ values in the Shang model was caused because only the $S_e(T)$ term is responsible for the increased component with increasing T in the experimental $G_{P,N}(T)$ in the Shang model. However, such a significant difference is unreasonable because these MTJs were prepared from the same epitaxial layer structure. Furthermore, the linear relation in $\log R_P A$ versus t_{MgO} for the CMS MTJs prepared on the epitaxial MTJ layer structure indicated that these MTJs are characterized by an identical barrier height. Thus, it is difficult to validate the fitting of the experimental $G_{P,N}(T)$ by the Shang model with the smearing effect even though the fitting apparently reproduced the experimental result.

Finally, we should note that the barrier height φ was not definitely determined in this paper. However, its minimum value is estimated to be about 1.34 eV or larger. This value is the same as the value deduced from fitting the $G_{P,N}(T)$ of the $t_{\text{MgO}} = 2.69 \text{ nm}$ MTJ ($\alpha = 1.24$) by the Shang model with the smearing factor in which the contribution of inelastic tunneling is ignored, as described above. Even if we assume a wide φ range of $3.5 \pm 1.5 \text{ eV}$, the factor $S_e(290 \text{ K})$ for a typical t_{MgO} value of 2.65 nm is weakly dependent on φ in this range, and it only slightly changes from 1.10 for $\varphi = 2.0 \text{ eV}$ to 1.04 for $\varphi = 5.0 \text{ eV}$. Furthermore, $S_e(290 \text{ K})$ decreases with

decreasing t_{MgO} . Thus, although the smearing factor calculated with $\varphi = 3.5$ eV corresponding to half the MgO energy gap has a certain margin of error, it would only slightly influence the results of the analysis in this paper, in particular by making a slight modification of the values of the deduced parameters.

In summary, our analysis of the experimental $G_P(T)$ of the CMS MTJs characterized by the systematically varied $P(4.2 \text{ K})$ showed that the extended Zhang model could consistently explain the complicated behavior of $G_P(T)$. According to this model, $\Delta G_{P,N,\text{in}}(T)$ arising from spin-flip inelastic tunneling via a magnon is much larger than $\Delta G_{P,N,\text{el}}(T)$ arising from spin-conserving elastic tunneling in which P decays with T for MTJs characterized by a relatively low P_0 . This results in an increase in $G_P(T)$ with increasing T from 4.2 K to room temperature. Thus, the analysis of the experimental $G_P(T)$ of MTJs with a relatively low P_0 using the original Zhang model that ignores the decaying P with T could be a good approximation [51,52]. On the other hand, $\Delta G_{P,N,\text{in}}(T)$ decreases with increasing P_0 because of the decrease in the coefficient of $C_P(T)$ or the effectively equivalent parameter $\xi = (1 - P_0^2)/(1 + P_0^2)$, resulting in a relative increase in $\Delta G_{P,N,\text{el}}(T)$. This leads to competition between $\Delta G_{P,N,\text{el}}(T)$ and $\Delta G_{P,N,\text{in}}(T)$. This competition caused the nonmonotonic T dependence of G_P observed for the CMS MTJs. Thus, the proposed model provides a comprehensive understanding of the T dependence of G_P of MTJs ranging from those characterized by a relatively low P value to those characterized by a significantly high P arising from half-metallicity.

B. T dependence of tunneling conductance for the antiparallel alignment

Now let us analyze the T dependence of G_{AP} of the CMS MTJs with various α values by using the extended Zhang model. For the antiparallel alignment, the smearing effect can be neglected for MTJs with high spin polarization. This is because the variation of $S_e(T)$ from 4.2 to 290 K is about several percent which is much smaller than the relative variation in G_{AP} as T increases from 4.2 to 290 K. For the CMS MTJs, the normalized variation in $S_e(T)$ at 290 K, i.e., $[S_e(290 \text{ K}) - S_e(0 \text{ K})]/S_e(0 \text{ K})$, is 0.056 for a t_{MgO} value of 2.65 nm, as described above, while the

normalized variation in $G_{\text{AP}}(T)$ at 290 K, i.e., $[G_{\text{AP}}(290 \text{ K}) - G_{\text{AP}}(4.2 \text{ K})]/G_{\text{AP}}(4.2 \text{ K})$, ranged from 1.33 for $\alpha = 0.73$ to 3.60 for $\alpha = 1.30$, as shown in Fig. 4(b). Thus, the smearing factor was ignored in the analysis of $G_{\text{AP}}(T)$. Accordingly, the extended Zhang model for $G_{\text{AP}}(T)$ is

$$G_{\text{AP}}(T) = G_{\text{AP},\text{el}}(T) + G_{\text{AP},\text{in}}(T), \quad (10a)$$

$$G_{\text{AP},\text{el}}(T) = Q_1 \cdot 2\rho_M(T)\rho_m(T), \quad (10b)$$

$$G_{\text{AP},\text{in}}(T) = Q_2 k_B T \cdot f(T) \cdot \{[\rho_M(T)]^2 + [\rho_m(T)]^2\}, \quad (10c)$$

where the coefficients Q_1 and Q_2 are given by Eqs. (3d) and (3e), respectively, the first term, $G_{\text{AP},\text{el}}(T)$, of Eq. (10a) corresponds to spin-conserving elastic tunneling, and the second term, $G_{\text{AP},\text{in}}(T)$, corresponds to spin-flip inelastic tunneling. Here, G_{AP} at $T = 0$ consists of spin-conserving elastic tunneling, which is expressed as

$$G_{\text{AP}}(T = 0) = Q_1 \cdot 2\rho_M(T = 0)\rho_m(T = 0). \quad (11)$$

By assuming the T -dependent P expressed by Eq. (6) with $\eta = \eta_{\text{AP}}$ for the antiparallel alignment, $G_{\text{AP}}(T)$ normalized by its value at $T = 0$, $G_{\text{AP},N}(T)$, is

$$G_{\text{AP},N}(T) = \frac{G_{\text{AP}}(T)}{G_{\text{AP}}(T = 0)} = G_{\text{AP},N,\text{el}}(T) + G_{\text{AP},N,\text{in}}(T), \quad (12a)$$

$$G_{\text{AP},N,\text{el}}(T) = 1 + \frac{P_0^2[1 - (1 - \eta_{\text{AP}}T^{3/2})^2]}{1 - P_0^2} = 1 + \Delta G_{\text{AP},N,\text{el}}(T), \quad (12b)$$

$$G_{\text{AP},N,\text{in}}(T) = a \left[\frac{1 + P_0^2(1 - \eta_{\text{AP}}T^{3/2})^2}{1 - P_0^2} \right] k_B T \cdot f(T) = \Delta G_{\text{AP},N,\text{in}}(T), \quad (12c)$$

where the coefficient a is given by Eq. (5c). We also included variations with T in $G_{\text{AP},N,\text{el}}$ and $G_{\text{AP},N,\text{in}}$ from the values at $T = 0$, i.e., $\Delta G_{\text{AP},N,\text{el}}$ and $\Delta G_{\text{AP},N,\text{in}}$, in Eqs. (12b) and (12c). If we assume a T -independent spin polarization, corresponding to $\eta_{\text{AP}} = 0$, Eq. (10) reduces to the original Zhang model, while if we ignore the second term of Eq. (10a), Eq. (10) reduces to the Shang model. Figure 9(a) plots the fitting curves

TABLE III. Parameters of η_P ($\text{K}^{-3/2}$), $a = Q \cdot 2S/E_m$ (eV^{-1}), E_c^P (meV), and c_0 deduced from fitting $G_{P,N}(T)$ by the extended Zhang model, and the resulting $f(290 \text{ K})$ and $a \cdot f(290 \text{ K})$ for $\alpha = 1.24$ CMS MTJ ($\text{Co}_2\text{Mn}_{1.24}\text{Si}_{0.84}$) with t_{MgO} of 2.31 nm are shown along with those values for $\alpha = 1.24$ CMS MTJ with t_{MgO} of 2.69 nm (Table II) for comparison. The parameters of η_P ($\text{K}^{-3/2}$), the barrier height φ , and the constant c_0 tentatively deduced from the fitting by the Shang model with the smearing factor for these two MTJs with t_{MgO} of 2.31 and 2.69 nm are also shown. The $t_{\text{MgO}} = 2.31$ nm CMS MTJ ($\alpha = 1.24$) had TMR ratios of 1690% at 4.2 K [corresponding to $P(4.2 \text{ K})$ of 0.946] and 328% at 290 K.

t_{MgO} (nm)	Fitting model	η_P ($\text{K}^{-3/2}$)	φ (eV)	$S_e(290 \text{ K})$	$a = Q \cdot 2S/E_m$ (eV^{-1})	E_c^{AP} (meV)	$f(290 \text{ K})$	$a \cdot f(290 \text{ K})$	c_0
2.31	Extended Zhang model	3.420×10^{-5}	3.5	1.042	3.009	0.486	3.951	11.9	0.010
	Shang model with smearing factor	4.087×10^{-5}	1.08	1.147	—	—	—	—	0.012
2.69	Extended Zhang model	3.319×10^{-5}	3.5	1.058	3.006	0.408	4.122	12.4	0.007
	Shang model with smearing factor	3.890×10^{-5}	1.34	1.162	—	—	—	—	0.009

TABLE IV. Parameters of η ($\text{K}^{-3/2}$), $a = Q \cdot 2S/E_m$ (eV^{-1}), and E_c (meV) for the $\text{Co}_2\text{Mn}_{1.30}\text{Si}_{0.84}$ MTJ shown in Table I deduced from fitting $G_{\text{AP},N}(T)$ by the Shang model, the extended Zhang model, and the original Zhang model. The thus-obtained parameters η and E_c for the antiparallel alignment are represented as η_{AP} and E_c^{AP} .

α in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$	Fitting model	η_{AP} ($\text{K}^{-3/2}$)	$a = Q \cdot 2S/E_m$ (eV^{-1})	E_c^{AP} (meV)	$f(290 \text{ K})$	$a \cdot f(290 \text{ K})$
1.30	Shang model	4.231×10^{-5}	—	—	—	—
	Extended Zhang model	1.075×10^{-5}	1.032	0.178	4.947	5.11
	Original Zhang model	—	1.577	0.331	4.330	6.83

FIG. 9. (a) Comparison of fitting curves for $G_{\text{AP}}(T)$ normalized by the value at 4.2 K of the CMS MTJ with $\text{Co}_2\text{Mn}_{1.30}\text{Si}_{0.84}$ electrodes ($\alpha = 1.30$) by the original Zhang model (dashed-dotted line), the extended Zhang model (solid line), and the Shang model (dashed line). The experimental data (open circles) are the same as those of $\alpha = 1.30$ shown in Figs. 3(a) and 4(b). The experimental $G_{\text{AP},N}(T)$ data with the fitting curves of the extended Zhang and Shang models have respective offsets of +0.5 and +1.0. (b) Decomposition of the variation of the experimental $G_{\text{AP},N}(T)$ of $\alpha = 1.30$ CMS MTJ into two components by fitting with the extended Zhang model: One is the inelastic tunneling term $\Delta G_{\text{AP},N,\text{in}}(T)$ [Eq. (12c)], and the other is the elastic tunneling term $\Delta G_{\text{AP},N,\text{el}}(T)$ [Eq. (12b)].

of the extended Zhang model of Eq. (12) for the experimental $G_{\text{AP},N}(T)$ of the $\alpha = 1.30$ CMS MTJ that had a giant TMR ratio of 2010% at 4.2 K; the fitting curves of the original Zhang and Shang models are also plotted for comparison. The best fit parameters deduced from these fittings are listed in Table IV. It was found that all these fittings could reproduce the $G_{\text{AP},N}(T)$. Among them, those of the original Zhang model and the extended Zhang model reproduced the experimental $G_{\text{AP},N}(T)$ for a wide T range from 4.2 to 290 K, while the Shang model gave a fitting curve that showed slight but systematic deviations from the experimental $G_{\text{AP},N}(T)$ for the entire T range investigated. Furthermore, the Shang model's neglecting the contribution of spin-flip inelastic tunneling via a magnon could not be validated in light of our findings for the experimental $G_{\text{P},N}(T)$ in Sec. III A. The essential point of the Shang model is that it explains the T dependence of spin-dependent tunneling conductances, G_{P} and G_{AP} , by only decreasing the spin polarization with increasing T within a framework of spin-conserving elastic tunneling. Thus, the dynamic effect, i.e., the spin-flip inelastic tunneling via a magnon, at finite temperatures is effectively incorporated into the T dependence of the spin polarization, meaning that the Shang model can roughly reproduce the experimental $G_{\text{AP},N}(T)$ but with slight and systematic deviations. Similarly, the original Zhang model's neglecting the effect of the T dependence of P on elastic tunneling could not be validated even though it could reproduce the experimental $G_{\text{AP},N}(T)$ as well as the extended Zhang model could do. Regarding the validity of the deduced parameters shown in Table IV, both coefficients a deduced by the extended and original Zhang models are in the expected range, as described in Sec. III A.

Figure 9(b) decomposes the variation with T in the experimental G_{AP} of $\alpha = 1.30$ MTJ normalized by its value at 4.2 K, i.e., $\Delta G_{\text{AP},N}(T) = G_{\text{AP}}(T)/G_{\text{AP}}(4.2 \text{ K}) - 1$, into a component arising from the elastic tunneling term $\Delta G_{\text{AP},N,\text{el}}(T)$ [Eq. (12b)] and a component arising from the inelastic tunneling term $\Delta G_{\text{AP},N,\text{in}}(T)$ [Eq. (12c)]. Although $\Delta G_{\text{AP},N,\text{in}}(T)$ was larger than $\Delta G_{\text{AP},N,\text{el}}(T)$, these two contributions were more or less comparable. This result of the analysis of the extended Zhang model for $G_{\text{AP},N}(T)$ clearly indicates that the decrease in the TMR ratio at 290 K can be attributed to a static effect, i.e., spin-conserving elastic tunneling with decaying P with T , and a dynamic effect, i.e., spin-flip inelastic tunneling, as described above. This result also suggests the actual P value at 290 K would be higher than the $P^{\text{TMR}}(290 \text{ K})$ value. Indeed, the $P^{\text{TD}}(290 \text{ K})$ value for the $\alpha = 1.30$ MTJ as calculated from the η_{AP} value by the fitting of the extended Zhang model (Table IV) was 0.903, which was obviously higher than the $P^{\text{TMR}}(290 \text{ K})$ of 0.791. Note that the tentatively calculated

FIG. 10. Fitting curves (solid lines) for the experimental $G_{AP}(T)$ normalized by the respective values at 4.2 K by the extended Zhang model [Eq. (12)] for the CMS MTJs with various α in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes. The experimental $G_{AP,N}(T)$ are the same as shown in Fig. 4(b) and are shown as open triangles, open squares, and open circles for $\alpha = 0.73$, 1.24, and 1.30, respectively. The normalized $G_{AP}(T)$ for $\alpha = 1.24$ and 1.30 have respective offsets of +0.5 and +1.0.

$P^{\text{TD}}(290 \text{ K})$ value from the η_{AP} value by the fitting of the Shang model was 0.755, which was comparable to the $P^{\text{TMR}}(290 \text{ K})$. The lower $P^{\text{TD}}(290 \text{ K})$ value by the Shang model was reasonable because the Shang model ignored the contribution of inelastic tunneling. Note also that the $P^{\text{TD}}(290 \text{ K})$ of 0.799 as calculated from η_P of the extended Zhang model in Sec. III A was much smaller than that as calculated from η_{AP} of the extended Zhang model. This difference in the absolute values of η_P and η_{AP} is ascribed to the simple relation of Eq. (6) phenomenologically describing the T dependence of P by a parameter η . Taking into account, however, that the dominant factor that decreases the TMR ratio at 290 K is the T dependence of $G_{AP}(T)$, the semiquantitative comparison of the $P^{\text{TD}}(290 \text{ K})$ values estimated from the η_{AP} values (rather than those from the η_P values) is more probable.

Figure 10 plots the fitting curves of the extended Zhang model [Eq. (12)] for the experimental $G_{AP,N}(T)$ for α ranging from 0.73 to 1.30. The extended Zhang model reproduced the

$G_{AP,N}(T)$ for all of the CMS MTJs over a wide T range from 4.2 to 290 K. The best fit parameters and resulting $f(290 \text{ K})$ and $a \cdot f(290 \text{ K})$ are summarized in Table V. The quantities $\gamma_{AP} = G_{AP}(290 \text{ K})/G_{AP}(4.2 \text{ K})$, which represent the degree of the T dependence of G_{AP} , are also shown in Table V. The coefficients a for these MTJs were almost identical. Here, E_c for the antiparallel alignment also increased from 0.063 meV for Mn-deficient $\alpha = 0.73$ to 0.18 meV for Mn-rich $\alpha = 1.30$ as E_c for the parallel alignment increased. This dependence led to a slight decrease in the product $a \cdot f(290 \text{ K})$ as α increased from Mn-deficient to Mn-rich. Now let us turn to the origin of the stronger T dependence of $G_{AP,N}(T)$ for higher $P(4.2 \text{ K})$ [Fig. 4(b)], resulting in the larger γ_{AP} for higher $P(4.2 \text{ K})$. Note that the factor, $[1 + P_0^2(1 - \eta_{AP}T^{3/2})^2]/(1 - P_0^2) = C_{AP}(T)$, in $\Delta G_{AP,N,\text{in}}(T)$ [Eq. (12c)] can be approximated as $C_{AP}(T) \approx [1 + P_0^2(1 - 2\eta_{AP}T^{3/2})]/(1 - P_0^2)$, and the term $2\eta_{AP}T^{3/2}$ can be neglected in the discussion on the α dependence of γ_{AP} because $2\eta_{AP}T^{3/2}$ even at 290 K was much smaller than 1. Accordingly, we can replace the factor $C_{AP}(T)$ by a constant $(1 + P_0^2)/(1 - P_0^2) = 1/\xi$, which is just the inverse of the coefficient appearing in $\Delta G_{P,N,\text{in}}(T)$ for $2\eta_P T^{3/2} \ll 1$. $1/\xi$ increases with P_0 and its values for the MTJs with various α are shown in Table V. This dependence originates from the fact that the inelastic tunneling term in G_{AP} at finite temperatures, $G_{AP,\text{in}}(T)$, is proportional to the sum of $\rho_M^2 + \rho_m^2$, while G_{AP} at $T = 0 \text{ K}$ is proportional to the product $2\rho_M\rho_m$. Furthermore, the term $P_0^2[1 - (1 - \eta_{AP}T^{3/2})^2]/(1 - P_0^2)$ in $\Delta G_{AP,N,\text{el}}(T)$ [Eq. (12b)] can be approximated as $2P_0^2\eta_{AP}T^{3/2}/(1 - P_0^2)$ because $\eta_{AP}T^{3/2} \ll 1$. The coefficient $2P_0^2/(1 - P_0^2) = B_{AP}$ is also an increasing function of P_0 . Note that the coefficient of B_{AP} in $\Delta G_{AP,N,\text{el}}(T)$ is close to the coefficient $1/\xi$ in $\Delta G_{AP,N,\text{in}}(T)$ for high P_0 . We normalized B_{AP} , $1/\xi$, and $a \cdot f(290 \text{ K})$ for various α by their values at $\alpha = 0.73$ and plotted them as a function of α in Fig. 11(a), which clearly shows significant increases in the normalized $1/\xi$ and B_{AP} as α increases from Mn-deficient to Mn-rich. This dependence originated from the increase in P_0 , while the product $a \cdot f(290 \text{ K})$ was almost independent of α even though it slightly decreased with increasing α . Thus, it was revealed that the dominant factors determining the α dependence of γ_{AP} were the coefficient $1/\xi$ in $\Delta G_{AP,N,\text{in}}(T)$ and the almost equivalent coefficient B_{AP} in $\Delta G_{AP,N,\text{el}}(T)$. Because of the similar values of $1/\xi$ and B_{AP} for high P_0 , the dominant factor was $1/\xi$ (or equivalently B_{AP}). Figure 11(b) plots how γ_{AP} depends on $1/\xi$ for the CMS MTJs with $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes of this paper as well as for the CMS MTJs with $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.96}$ electrodes reported in Ref. [12], where the $G_{AP,N}(T)$ data were analyzed using the original Zhang model. We reexamined the $G_{P,N}(T)$ and $G_{AP,N}(T)$ data of the $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.96}$ MTJs by using the

TABLE V. Parameters of $\eta_{AP} (\text{K}^{-3/2})$, $a = Q \cdot 2S/E_m (\text{eV}^{-1})$, and $E_c^{\text{AP}} (\text{meV})$ for the CMS MTJs with various α shown in Table I deduced from fitting their respective $G_{AP,N}(T)$ by the extended Zhang model, and the resulting $f(290 \text{ K})$ and $a \cdot f(290 \text{ K})$. The quantities of $\gamma_{AP} = G_{AP}(290 \text{ K})/G_{AP}(4.2 \text{ K})$ and $1/\xi$ defined by $1/\xi = (1 + P_0^2)/(1 - P_0^2)$ are also shown.

α in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$	$\eta_{AP} (\text{K}^{-3/2})$	$a = Q \cdot 2S/E_m (\text{eV}^{-1})$	$E_c^{\text{AP}} (\text{meV})$	$f(290 \text{ K})$	$a \cdot f(290 \text{ K})$	γ_{AP}	$1/\xi$
0.73	1.227×10^{-5}	1.014	0.063	5.984	6.07	2.33	6.74
1.24	1.113×10^{-5}	1.004	0.150	5.118	5.14	3.75	16.1
1.30	1.075×10^{-5}	1.032	0.178	4.947	5.11	4.60	21.1

FIG. 11. (a) Dependence of the coefficient $B_{AP} = 2P_0^2/(1 - P_0^2)$, the parameter $1/\xi = (1 + P_0^2)/(1 - P_0^2)$, and the product $a \cdot f(290 \text{ K})$ on Mn composition α in $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes, where these values are normalized by the respective values for $\alpha = 0.73$. (b) Dependence of the parameter $\gamma_{AP} = G_{AP}(290 \text{ K})/G_{AP}(4.2 \text{ K})$ on $1/\xi$ for CMS MTJs with $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes (open circles). Dependence of γ_{AP} on $1/\xi$ for CMS MTJs with $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.96}$ electrodes reported in Ref. [12] are also plotted (solid and open triangles), where solid triangles are for α being smaller than a certain critical α value, α_c , for $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.96}$ electrodes, and open triangles are for α being larger than α_c [12].

extended Zhang model and found that the data could also be consistently explained by it. The almost linear dependence of γ_{AP} on $1/\xi$ for the two series of CMS MTJs also clearly shows the dominant factor for the larger γ_{AP} for higher $P(4.2 \text{ K})$ was the coefficient $1/\xi$ which increased with increasing $P(4.2 \text{ K})$. This result also indicates that the larger γ_{AP} for higher $P(4.2 \text{ K})$ is the intrinsic spin-dependent tunneling property of MTJs [12], which was explained by the extended Zhang model.

In summary, the experimental $G_{AP}(T)$, including its stronger T dependence for higher P at 4.2 K, was consistently explained with the extended Zhang model. Our findings that both spin-flip inelastic tunneling via a thermally excited magnon and spin-conserving elastic tunneling in which P decays with increasing T play key roles in determining the T dependence of G_P and G_{AP} are applicable to MTJs with a wide range of P_0 . Moreover, our findings provide a unified picture of the origin of the T dependence of the spin-dependent tunneling conductance of MTJs, including those with highly spin-polarized electrodes.

IV. CONCLUSION

We investigated the key tunneling mechanisms that determine the temperature (T) dependence of the spin-dependent tunneling conductances, G_P and G_{AP} , of MTJs. To do so, we measured the $G_P(T)$ and $G_{AP}(T)$ of high-quality CMS/MgO/CMS MTJs featuring systematically varied tunneling spin polarizations at 4.2 K [$P(4.2 \text{ K})$] (α in the $\text{Co}_2\text{Mn}_\alpha\text{Si}_{0.84}$ electrodes was varied) that exhibited giant TMR ratios. Although the T dependence of the normalized G_P [$G_{P,N}(T) = G_P(T)/G_P(4.2 \text{ K})$] was significantly weak compared with that of the normalized

G_{AP} [$=G_{AP}(T)/G_{AP}(4.2 \text{ K})$], $G_{P,N}$ showed a notable T dependence in which it decreased with increasing T from T_1 of about 30 K to T_2 ranging from about 162 to 237 K, wherein T_2 depended on α ; then it increased for $T > T_2$. Furthermore, T_2 increased, and the maximum decrease in $G_{P,N}$ at T_2 increased as $P(4.2 \text{ K})$ increased. These features indicated that an analysis of the experimental $G_{P,N}(T)$ is critical to elucidating the origin of the T dependence of the spin-dependent tunneling conductance. To explain these features of $G_{P,N}(T)$, we developed an extension of the Zhang model for $G_P(T)$ and $G_{AP}(T)$ that took into account both spin-conserving elastic tunneling wherein P decreases with increasing T , and in turn decreases G_P with T , and spin-flip inelastic tunneling via a thermally excited magnon that increases G_P with T . Accordingly, the complicated nonmonotonic behavior of the experimental $G_{P,N}(T)$ could be fitted with reasonable values of the parameters of the proposed model. The observed $P(4.2 \text{ K})$ dependence of $G_{P,N}(T)$ was also consistently explained by the proposed model through a decrease in the contribution of spin-flip inelastic tunneling with increasing $P(4.2 \text{ K})$. The normalized $G_{AP}(T)$, including its stronger T dependence for higher $P(4.2 \text{ K})$, was also consistently explained. The proposed model provides a comprehensive understanding of $G_P(T)$ and $G_{AP}(T)$ of not only half-metallic MTJs but also MTJs with a wide range of P at 0 K.

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