



Title	Evaluation of interfacial strength between fiber and matrix based on cohesive zone modeling
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1 Evaluation of interfacial strength between fiber and matrix based on cohesive zone
2 modeling

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11 **Abstract**

12 This paper presents a measurement technique of interfacial strength considering non-
13 rigid bonding on a fiber/matrix interface modeled as a cohesive surface. By focusing on
14 the stress concentration near a fiber crack obtained from a single-fiber fragmentation
15 test, the stress contours in matrix observed by photoelasticity can be related to the
16 interfacial strength by defining a characteristic length. An equation expressing the
17 relationship between the characteristic length on the stress contour and the interfacial
18 strength was derived, and validated using finite element analysis. The primary
19 advantage of proposed measurement technique is that only a single fiber crack, which
20 usually occurs within elastic deformation of matrix, is required for the evaluation of
21 interfacial strength, whereas saturated fiber fragmentation is necessary in the
22 conventional method. Herein, a sample application was demonstrated using a single
23 carbon fiber and epoxy specimen, and an average interfacial strength of 23.8 MPa was
24 successfully obtained.

25

26 **Keywords**

27 B. Interface/interphase, B. Fragmentation, B. Fiber/matrix bond, C. Cohesive interface
28 modelling

29

30 **1. Introduction**

31 The interface between fiber and matrix plays an important role in the overall load-
32 bearing performance of the composite structure. In particular, the bonding quality of the
33 interface determines the stress transfer from the matrix to the fiber and vice versa [1, 2].

34 The bonding quality of the interface has been assessed through the development of
35 interface models. An early model representing stress transfer at an interface was
36 introduced by Cox and Kelly-Tyson [3, 4]. Kim et al. then modified this model by
37 introducing the bonding quality parameter, i.e., the interfacial strength (t_o) was regarded
38 as the stress required to initiate an interfacial crack [5]. Moreover, the bonding quality
39 has also been determined using energy-based approaches [6–8].

40 The similarity between the abovementioned models is that the interface is assumed
41 to be a two-dimensional surface with a rigid bonding condition. However, recent studies
42 have shown that the interface is, in fact, a three-dimensional thin layer (also called an
43 interphase) having mechanical properties that are different from those of both the fiber
44 and the matrix [9–11]. Several studies have indicated that non-rigid bonding is formed
45 at the interface regardless of the strength of the bonding condition [12–14]. Therefore,
46 earlier models may have evaluated the bonding quality inaccurately [15, 16].

47 Recently, a surface-based cohesive model that defines the interface as a non-rigid
48 bond has been attracting attention [17–19]. It provides an improved interpretation of the

49 real interface condition by introducing the traction (t) - separation (δ) curve. However,
50 characterization of the maximum traction, which is equivalent to t_o , from the $t - \delta$ curve
51 has not been well established because it is difficult to experimentally measure the $t - \delta$
52 curve along the interface [20]. Among familiar experimental methods of push-out
53 testing [21], micro bond testing [22], and single fiber fragmentation testing (SFFT) [23],
54 SFFT is appropriate to consider the interface as a non-rigid bond because it replicates
55 actual stress transfer in real fiber/matrix composites. It also has an advantage of the
56 easier preparation of specimens [24, 25]. Our group previously proposed a method
57 based on SFFT for evaluating t_o without requiring the $t - \delta$ curve observation [26]. It
58 utilizes contours of principal stress difference ($\Delta\sigma$) in a matrix by defining a
59 characteristic length (L_t), which can be obtained directly via photoelastic analysis [27-
60 29]. Moreover, our method requires only a single fiber crack in the specimen whereas
61 conventional SFFT requires complete fiber cracks generated until saturation. Thus, the
62 influence of plastic deformation on the matrix can be significantly reduced.

63 This paper introduces a theoretical analysis of $\Delta\sigma$ contours to establish a novel
64 technique of evaluating t_o at the debonding interface. First, an equation showing the
65 relationship between the $\Delta\sigma$ contour and t_o is derived from the stress distribution of the
66 matrix near the fiber crack during SFFT. FEA is then conducted to examine the derived
67 equation. The application of L_t for the measurement of t_o is finally demonstrated using a
68 carbon fiber/epoxy sample. A photoelastic image representing the $\Delta\sigma$ concentration in
69 the matrix is analyzed by an image processing technique [30], to determine t_o from the
70 L_t value using the derived equation.

71 **2. Theory**

72 **2.1. Surface-based cohesive model for interface**

73 Strain (ε_a) was imposed on a SFFT specimen consisting of a single fiber surrounded
74 by a matrix to initiate fiber fragmentation, as shown in Figs. 1a and 1b. Shear traction
75 (t_s) and separation (δ_s) developed in the interface soon after a fiber crack was generated,
76 and then increased in response to the applied ε_a . When the relationship between t_s and δ_s
77 is assumed to be simply expressed by the $t_s - \delta_s$ curve as shown in Fig. 2, three
78 interfacial properties can be defined: interfacial stiffness (K_o), t_o , and the interfacial
79 fracture toughness (G_c). K_o is a parameter that relates t_s and δ_s in a bonding condition,
80 where

$$81 \quad t_s = K_o \delta_s. \quad (1)$$

82 The real interface condition can be more suitably represented by the definition of K_o
83 than the assumption of rigid bonding, because it implies that the interface can undergo
84 separation even though t_s does not exceed t_o . Here, t_o is defined as the t_s required to
85 initiate the debonding process, represented by degradation of K_o . Further, G_c , which can
86 be obtained from the total area below the $t_s - \delta_s$ curve, is defined as the energy release
87 rate required to cause debonded interface.

88 The position on the interface where t_s reaches a maximum can be found by
89 examining the stress distribution in the matrix. Although it is difficult to observe the t_s
90 distribution along the interface directly, t_o can be obtained by observing the $\Delta\sigma$ contour
91 near the interface. It simply corresponds to the point of maximum $\Delta\sigma$ because $\Delta\sigma$ is a
92 representative of principal shearing stress. Therefore, $\Delta\sigma$ can be an indicator of the
93 maximum t_s , which is equal to t_o .

94 In order to confirm the relationship between t_s and the $\Delta\sigma$ contour, FEA using
95 Abaqus 6.14 was conducted for an axisymmetric model, as shown in Fig. 3. It
96 represents a region near a fiber crack, indicated by the dashed line in Fig. 1b. The single

97 fiber and matrix were assumed to be linearly elastic materials, because the first fiber
 98 crack usually appears in the elastic range of the matrix. The mechanical properties of
 99 the fibers and matrices used in the FEA are shown in Table 1. The model geometry and
 100 the number of elements are shown in Table 2. Three sample cases with the different
 101 interfacial properties shown in Table 3 were examined. The range of t_o was determined
 102 based on previous study [9]. The values of G_c and K_o were suitably selected so that FEA
 103 calculation converges under ε_a of less than 3%, which is comparable to experimental
 104 results. Note that stress state of matrix for SFFT can be represented by axisymmetric
 105 model because of low volume fraction of fiber ($a \ll b$) even though the actual cross
 106 section of SFFT specimen is not axisymmetric [26, 31].

107 Fig. 4a shows the t_s and dt_s/dz distribution along the interface obtained from a
 108 simulation result for a carbon fiber-hard epoxy composite with case-1 interfacial
 109 properties in Table 3. The t_s becomes maximum value of 30 MPa, which is identical to
 110 t_o defined in case-1, at the boundary (z_o) between the bonded and debonding regions. It
 111 almost linearly decreases in the bonded region, resulting in almost constant dt_s/dz near
 112 the fiber crack. The $\Delta\sigma$ contours in the matrix shown in Fig. 4b clearly show that t_o
 113 causes a highly concentrated $\Delta\sigma$ near the fiber crack. The black points on each contour
 114 in Fig. 4b indicate the positions located farthest from the interface, represented by the
 115 maximum radius (r_{max}). Subtracting the fiber radius (a), it can be used as an indicator of
 116 t_o since our previous work found a linear relationship between them [26]. Therefore, it
 117 was defined as a characteristic length, L_t .

$$L_t = r_{max} - a \quad (2)$$

118 Among the contours in Fig. 4b, those with a $\Delta\sigma$ of 50 MPa or higher are ideal to find the
 119 maximum t_s , because the location of L_t corresponds well to the z_o . The L_t -based

120 approach is not effective when the $\Delta\sigma$ contours are far from the interface because the
 121 maximum radius on contours gradually shift to the left due to the edge effects of the
 122 calculation area.

123 2.2. Equation relating L_t and t_o

124 The equation relating L_t and t_o is derived by the $\Delta\sigma$ equation from stress state in the
 125 bonding region near the interface ($z \geq z_0$) where the deformations of matrix is linearly
 126 elastic. It is expressed by the axial (σ_z), radial (σ_r), and shear stress on the rz axis (τ_{rz}).

$$\frac{\Delta\sigma}{2} = \sqrt{\left(\frac{1}{2}(\sigma_z - \sigma_r)\right)^2 + \tau_{rz}^2} \quad (3)$$

127 In an axisymmetric model of the bonding region, the above stresses are related with
 128 hoop stress (σ_θ) and axial displacement (u_z) by equilibrium and the stress-strain relations
 129 for perfectly elastic and isotropic matrices.

$$\frac{\partial\sigma_z}{\partial z} + \frac{\tau_{rz}}{r} + \frac{\partial\tau_{rz}}{\partial r} = 0 \quad (4)$$

$$\frac{\partial\sigma_r}{\partial r} + \frac{\partial\tau_{rz}}{\partial z} + \frac{1}{r}(\sigma_r - \sigma_\theta) = 0 \quad (5)$$

$$\frac{\partial u_z}{\partial z} = \frac{1}{E}[\sigma_z - \nu(\sigma_r + \sigma_\theta)] \quad (6)$$

$$\frac{\partial u_z}{\partial r} = \frac{2(1 + \nu)}{E}\tau_{rz} \quad (7)$$

130 where E and ν are the elastic modulus and Poisson ratio, respectively. It should be noted
 131 that the radial displacement (u_r) was assumed to be zero near the interface because a is
 132 very small compared with the matrix radius (b). The boundary conditions of the matrix
 133 model shown in Fig. 3 are expressed as

$$\tau_{rz}(a, z) = t_s ; \tau_{rz}(b, z) = 0, \quad (8)$$

$$\sigma_r(a, z) = -q ; \sigma_r(b, z) = 0, \quad (9)$$

$$u_z(b, z) = \varepsilon_a z, \quad (10)$$

134 where q is the stress due to the Poisson ratio difference of the fiber and matrix. This can
 135 be calculated from the following equation [32].

$$q = \frac{\varepsilon_a (v_m - v_f)}{\left(\frac{1-v_f-2v_f^2}{E_f}\right) + \left(\frac{1+v_m}{E_m}\right)}, \quad (11)$$

136 where f and m refer to the fiber and matrix, respectively.

137 Intensive studies have been conducted by Zhao et al. and Nair et al. regarding the
 138 decay function of τ_{rz} along r axis [31, 33]. These studies have shown that, for a very low
 139 fiber-volume fraction model ($a \ll b$) such as in the case of an SFFT specimen, the
 140 simplest τ_{rz} that satisfies Eq. 4 and the boundary condition of Eq. 8 became the
 141 following equation.

$$\tau_{rz} = \frac{a}{r} t_s \quad (12)$$

142 Here, the t_s is assumed to be a linear function of z based on the FEA result shown in Fig.
 143 4a. Considering a constant value of dt_s/dz near the fiber crack, the radial and hoop
 144 stresses can be obtained from Eq. 5 with the boundary conditions of Eq. 9 under the
 145 assumption of uniform axial stress along z direction and low fiber-volume fraction ($a \ll$
 146 b).

$$\sigma_r = -\frac{a^2}{r^2} q \quad (13)$$

$$\sigma_\theta = \frac{a^2}{r^2} q + a \frac{dt_s}{dz} \quad (14)$$

147 The σ_z is derived by obtaining u_z from Eqs. 6 and 7, and then substituting the stresses of
 148 Eqs. 12, 13, and 14.

$$\sigma_z = E_m \varepsilon_a + a \frac{dt_s}{dz} \left(v_m + 2(1 + v_m) \ln \frac{r}{b} \right) \quad (15)$$

149 It is reasonable that the σ_r , σ_θ , and σ_z , are only functions of r (uniform along z direction)
 150 because they actually have little effect to the overall stress state compared with shear
 151 stress. Substituting Eqs. 12, 13, and 15 into Eq. 3, t_s can be expressed as a function of
 152 $\Delta\sigma$ and the distance from the interface to the $\Delta\sigma$ contour (r).

$$t_s = \frac{r}{2a} \sqrt{\Delta\sigma^2 - \left(E_m \varepsilon_a + a \frac{dt_s}{dz} \left(v_m + 2(1 + v_m) \ln \frac{r}{b} \right) + \frac{a^2}{r^2} q \right)^2} \quad (16)$$

153 Focusing on the maximum radius on a $\Delta\sigma$ contour near the interface, where $r = L_t + a$
 154 and $t_s = t_o$, t_o can be expressed in terms of L_t .

$$t_o = \frac{(L_t + a)}{2a} \sqrt{\Delta\sigma^2 - \left(E_m \varepsilon_a + a \frac{dt_s}{dz} \left(v_m + 2(1 + v_m) \ln \frac{L_t + a}{b} \right) + \frac{a^2}{(L_t + a)^2} q \right)^2} \quad (17)$$

155 Further, the constant dt_s/dz parameter must be obtained to apply Eq. 17 for evaluating t_o ,
 156 but it is difficult to theoretically derive the value. Therefore, FEM results were utilized
 157 to estimate dt_s/dz parameter. As an example of t_s and dt_s/dz distributions along the
 158 interface shown in Fig. 4a, $dt_s/dz = -249$ MPa/mm at a point of $t_o = 30$ MPa was
 159 obtained by approaching from the bonding region. The L_t values corresponding to $\Delta\sigma$
 160 contours between 40 and 65 MPa were then measured and substituted into Eq. 17 in
 161 order to obtain t_o . The same procedure was repeated for other parameters in Table 3.

162 Results were calculated for both the carbon fiber/hard epoxy and glass fiber/soft
 163 epoxy models, and are plotted in Figs. 5 and 6, respectively. The dashed lines indicate
 164 the actual t_o input in the FEA, whereas the data-points indicate the estimated t_o using Eq.
 165 17 with L_t and dt_s/dz values. Measurements excluding dt_s/dz effect ($dt_s/dz = 0$) are also
 166 plotted here, because it has been neglected in a large number of theoretical analyses due
 167 to simplification [5–10]. These figures clearly show that more accurate t_o values are
 168 obtained when dt_s/dz is included in the equation. Specifically, t_o values are

169 overestimated when dt_s/dz is neglected. These results show that t_o can be accurately
 170 evaluated by measuring L_t . Moreover, these findings indicate that the assumptions
 171 applied in the derivation of Eq. 17 are reasonable and yield good agreement with the
 172 FEA results.

173 2.3. Non-dimensional analysis for practical use

174 Although Eq. 17 produces good results regarding evaluation of t_o , it is not
 175 practically useful if FEA must be conducted to obtain dt_s/dz parameter. Therefore, Eq.
 176 17 was rearranged to a non-dimensional form to identically evaluate dt_s/dz term. Both
 177 sides of Eq. 17 were divided by $\Delta\sigma$ in order to obtain a general form that is independent
 178 of material properties.

$$t' = \frac{(L' + 1)}{2} \sqrt{1 - \left(\frac{E_m \varepsilon_a}{\Delta \sigma} + \frac{a}{\Delta \sigma} \frac{dt_s}{dz} \left(v_m + 2(1 + v_m) \ln \frac{a(L' + 1)}{b} \right) + \frac{1}{(L' + 1)^2} \frac{q}{\Delta \sigma} \right)^2} \quad (18)$$

179 where $t' = t_o / \Delta\sigma$ and $L' = L_t / a$.

180 The relationship between t' and L' is plotted in Eq. 18 for both the carbon fiber/hard
 181 epoxy and glass fiber/soft epoxy models. It was found that the relationship is identical
 182 regardless of materials and can be approximated by a simple linear equation, which was
 183 implied in our previous work [26].

$$t_o = \left(0.21 \frac{L_t}{a} + 0.45 \right) \Delta\sigma \quad (19)$$

184 Through a linear approximation of Eq. 18, expressed by Eq. 19, the dt_s/dz value is no
 185 longer required for the t_o estimation. By selecting the appropriate $\Delta\sigma$ contour, which
 186 should be as close as possible to the interface, and by measuring L_t from the SFFT
 187 experiment, the t_o can be evaluated directly. Thus, Eq. 19 contributes significantly
 188 towards the effective and efficient measurement of t_o . Moreover, it can be applied to any

189 relationship of $t_s - \delta_s$ curve on the interface since our proposed method only focuses on
190 the location of z_o .

191 **3. Experiment**

192 3.1. Experimental procedure

193 SFFT was conducted to estimate t_o by proposed method of L_t measurement. Single
194 carbon fiber (HTS30 3K, TOHO Tenax) and epoxy resin (KONISHI Chemical Co.,
195 Ltd.) were prepared to create an SFFT specimen with 2-mm thickness (h). The
196 experimental setup consists of a polychromatic light and a microscope with a digital
197 camera attached. A micro-tensile testing machine was located under the microscope so
198 that the specimen was placed at the center of two polarizers. The retarders were also
199 used to create circularly polarized light for the elimination of isoclinic and isochromatic
200 interaction noise. A detailed schematic of the apparatus is shown in Fig. 8.

201 Stress contours can be observed because epoxy has two refraction indexes, as it is a
202 birefringence material. The presence of two refraction indexes generates relative
203 retardation expressed in the fringe order (N). Thus, N indicates $\Delta\sigma$, which is connected
204 to the stress-optic coefficient (f_σ).

$$\Delta\sigma = \frac{f_\sigma N}{h} \quad (20)$$

205 First, f_σ of the pure-epoxy specimen, meaning no carbon fiber embedded, was
206 obtained from a bending test [34]. $\Delta\sigma$ distribution under bending load and an image of
207 continuous colored band corresponding to N can be simultaneously recorded. f_σ was
208 then calculated by using Eq. 20. Next, ε_a was applied to a specimen of single fiber-
209 embedded epoxy to capture the $\Delta\sigma$ contours near the fiber crack. On a certain ε_a , a fiber
210 crack appeared and caused a $\Delta\sigma$ concentration near the interface. An image of colors

211 corresponding to $\Delta\sigma$ contours was then captured by the camera through the microscope,
 212 and then the colors were extracted and converted to hue-saturation-value (HSV) system
 213 values. The conversion of colors to these values eliminates errors in color comparison,
 214 so that accurate results can be assured. Finally, L_t was measured from the $\Delta\sigma$ contours
 215 near the interface, and applied to Eq. 19 to obtain t_o .

216 3.2. Results and Discussion

217 Fig. 9a shows captured color image from bending test correspond to N with bending
 218 load of 6.2 N. The black color band in the specimen indicates no stress. Focusing on
 219 tensile stress distribution in the upper side of specimen, the $\Delta\sigma - N$ curve of the epoxy,
 220 shown in Fig. 9b, indicated that the f_σ of the epoxy specimen was 7.9 MPa.mm. The E_m
 221 of 0.67 GPa was also obtained from a tensile test.

222 On the SFFT, a fiber crack appeared at the ε_a of a 1.4%, which is still within the
 223 elastic range. The color distribution near the fiber crack visualized through an image
 224 processing was shown in Fig. 10a. The colors of every pixel related to N values of 2.56,
 225 2.52, and 2.50 were extracted, and then plotted as contours in the rz axis, as shown in
 226 Fig. 10b. Three contours were selected for the measurement of t_o . Through application
 227 of Eq. 20, these contours were found to be $\Delta\sigma$ values of 10.1, 9.9, and 9.8 MPa,
 228 respectively. These $\Delta\sigma$ values must be corrected to compensate for the axisymmetric
 229 effect because the carbon fiber has a circular shape that leads to axisymmetry in the
 230 projection. The corrected $\Delta\sigma$ (σ_c) can be calculated from [27, 29, 35] as

$$\sigma_c = \frac{h(\Delta\sigma - E_m\varepsilon_a)(b - a)}{2 \left\{ bm - \frac{1}{2} \left(mb + (a + L_t)^2 \ln \frac{(m+b)}{(a+L_t)} \right) \right\}} + E_m\varepsilon_a, \quad (21)$$

231 where m is obtained from

$$m = [b^2 - (L_t - a)^2]^{0.5}. \quad (22)$$

232 σ_c values of 32.6, 29.3, and 26.9 MPa were obtained from the calculations for the $\Delta\sigma$
233 values of 10.1, 9.9, and 9.8 MPa, respectively. The L_t , a , and σ_c were measured and
234 substituted into Eq. 19. As a result, the t_o values of 23.4, 29.3, and 31.5 MPa were
235 finally obtained. The same procedure was repeated for 26 other stress contours from
236 three specimens, and resulted in an average value of 23.8 MPa.

237 A conventional SFFT that considers the interface as being a rigid bond was also
238 conducted for the same specimens. Fig. 11 shows fragmentation process of fiber on
239 initial and saturated conditions. The images were captured without installing retarders
240 on photoelastic tools in order to observe location of fiber cracks. The analysis of
241 conventional SFFT follows Ref. 36 which clearly explain the procedure. The averaged
242 t_o value from the conventional SFFT was 33.7 MPa. The detail comparison of t_o
243 evaluation between our analysis and conventional SFFT analysis is shown in Fig. 12. It
244 is confirmed that t_o is overestimated unless non-rigid bonding is considered.
245 Furthermore, our proposed procedure to evaluate t_o is easier and more straightforward
246 compared to the conventional SFFT, because it requires only measurement of L_t based
247 on the stress response of the matrix to the interface.

248

249 **Conclusion**

250 A method to evaluate the interfacial strength (t_o) between fiber and matrix has been
251 developed based on the cohesive damage model. The characteristic length (L_t)
252 indicating t_o was introduced and measured from a $\Delta\sigma$ contour in epoxy matrix. Hence, a
253 theoretical analysis was conducted to obtain the relationship between t_o and L_t . From a
254 non-dimensional analysis, it was found that the normalized t_o (t') and L_t (L') have a

255 linear relationship independently determined from material properties. A sample
256 application to carbon fiber-epoxy composite was demonstrated to evaluate the proposed
257 technique. A photoelastic analysis in conjunction with an SFFT experiment was
258 conducted to capture the stress contours, clearly visualized through image processing
259 techniques. The calculated result yielded an average t_o value of 23.8 MPa, which is
260 almost 30% lower than one obtained from conventional SFFT analysis. The
261 overestimation of conventional method implies the importance of debonding process of
262 the interface.

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267

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- 363

364 **Figure Legends**

365 Fig. 1. Fiber fragmentation process; (a) before and (b) after.

366 Fig. 2. Shear traction (t_s)-separation (δ_s) curve.

367 Fig. 3. Axisymmetric model of fiber/matrix composite near fiber crack.

368 Fig. 4. FEA result for carbon fiber-hard epoxy composite with case-1 interfacial
369 properties: (a) t_s and dt_s/tz curves along simulated interface; (b) $\Delta\sigma$ contours in matrix.

370 The black dots indicate the maximum radius (r_{max}) with respect to the r -axis.

371 Fig. 5. Measurement of t_o for carbon fiber-hard epoxy composite. The black and white
372 marks indicate measurements with and without considering dt_s/dz respectively.

373 Fig. 6. Measurement of t_o for glass fiber-soft epoxy composite. The black and white
374 marks indicate measurements with and without considering dt_s/dz respectively.

375 Fig. 7. Linear relationship approximation between t' and L' .

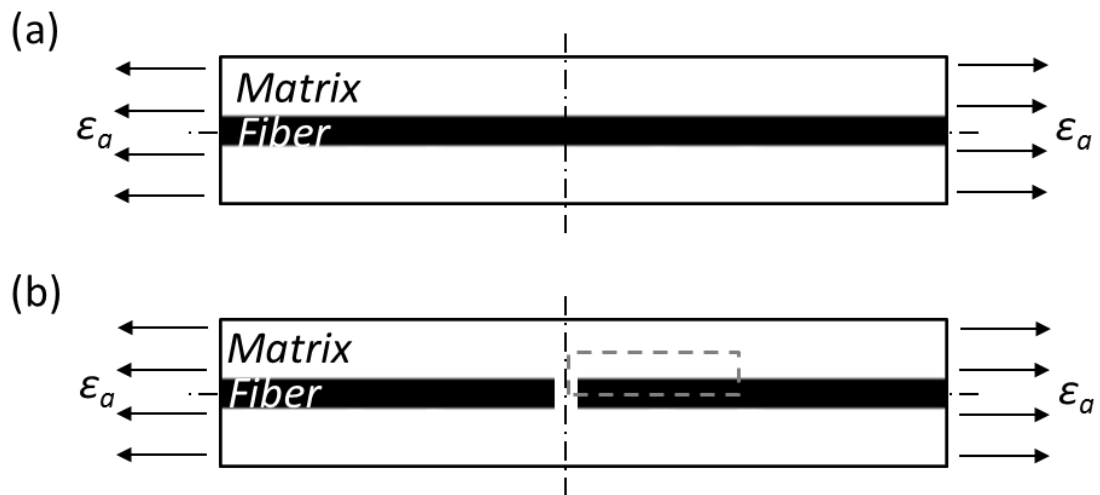
376 Fig. 8. Schematic of apparatus used for photoelastic analysis.

377 Fig. 9. (a) colored band observed under bending load and (b) epoxy stress-fringe order
378 curve.

379 Fig. 10. (a) color captured near fiber crack using photoelastic technique and (b) plotted
380 $\Delta\sigma$ contours from experiment.

381 Fig. 11. Fiber cracks appearance on SFFT (a) initial and (b) saturated conditions.

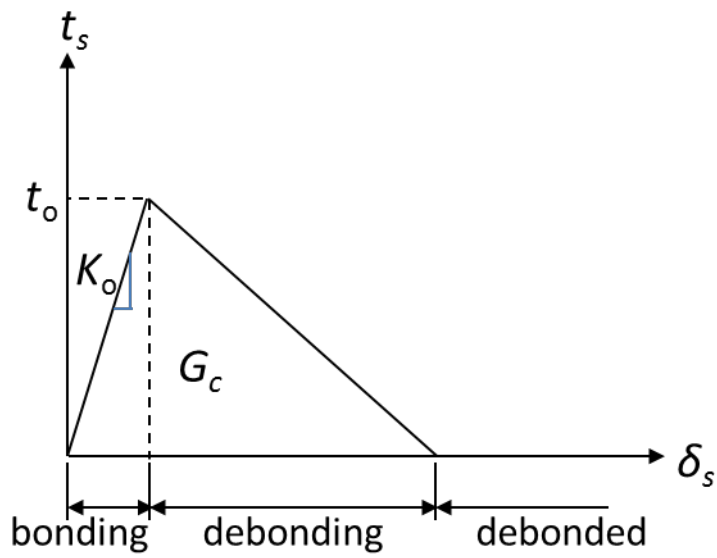
382 Fig. 12. Comparison of t_o evaluation between conventional SFFT and our experimental
383 analysis.



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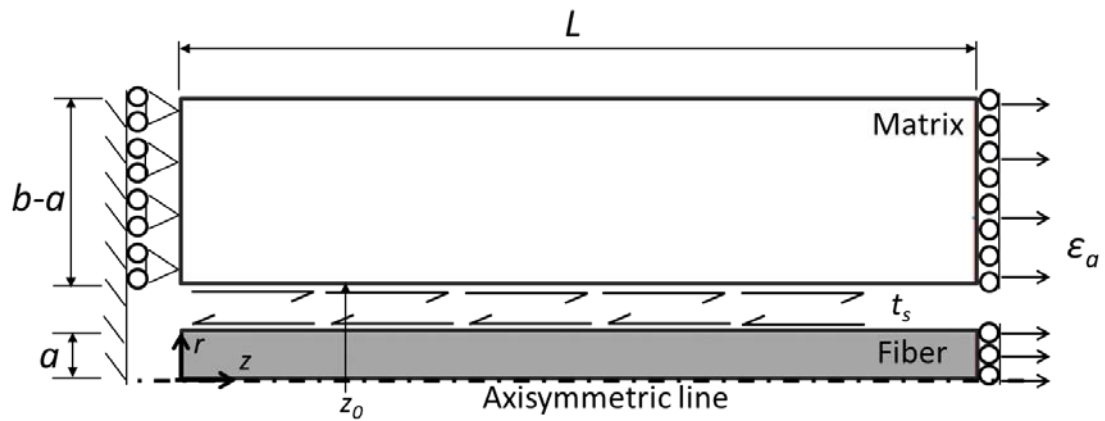
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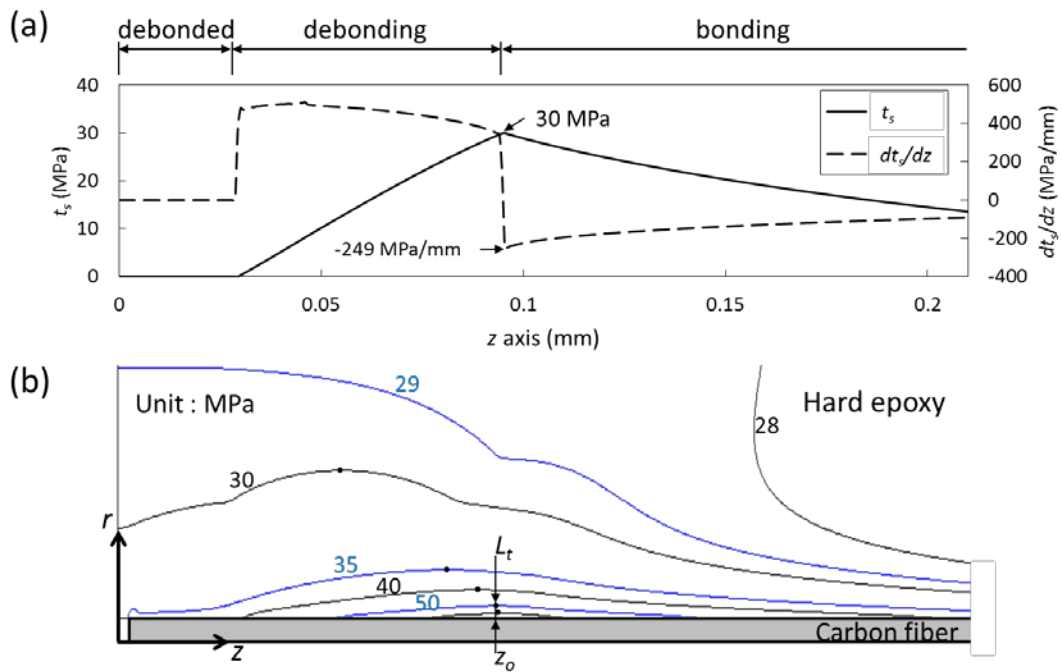
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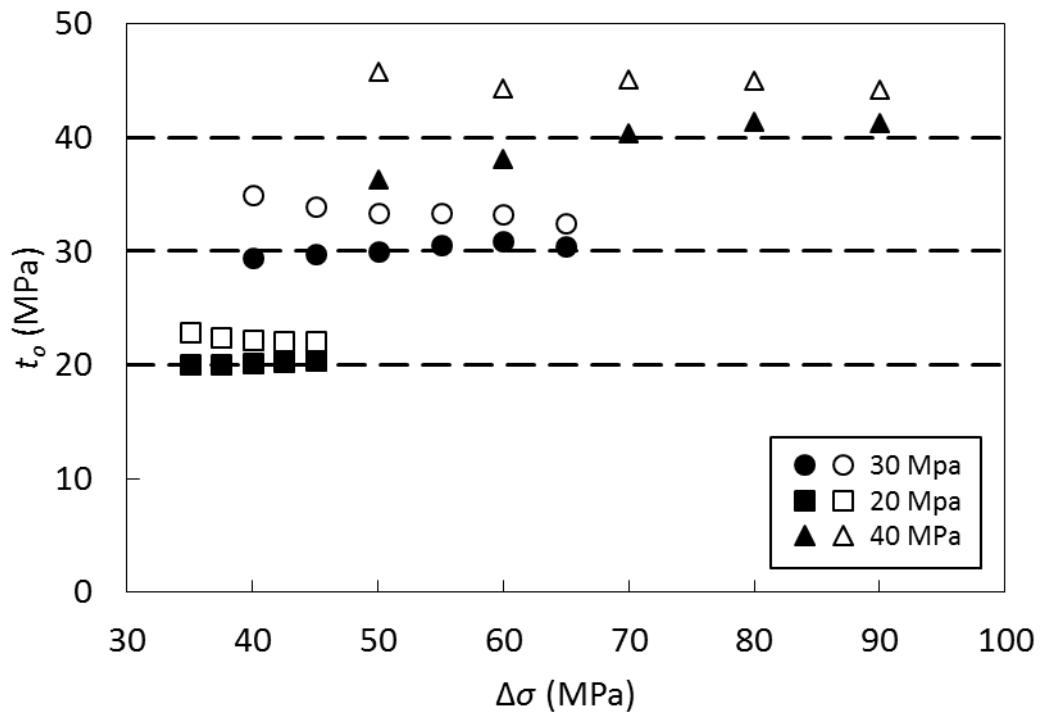


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392 Fig. 4. FEA result for carbon fiber-hard epoxy composite with case-1 interfacial
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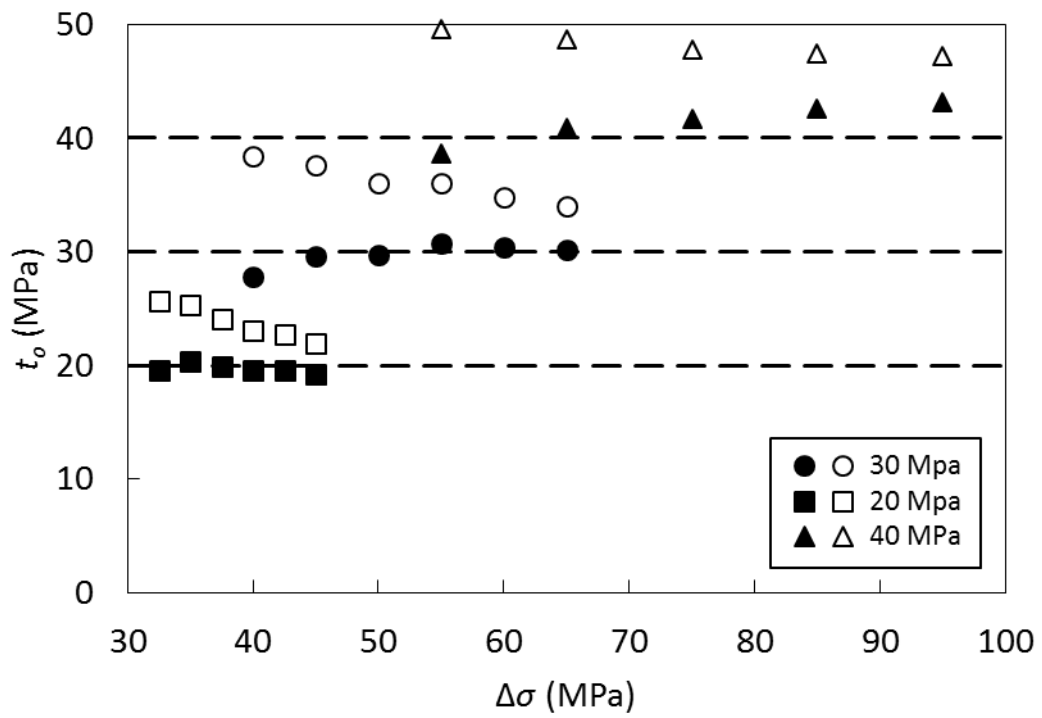
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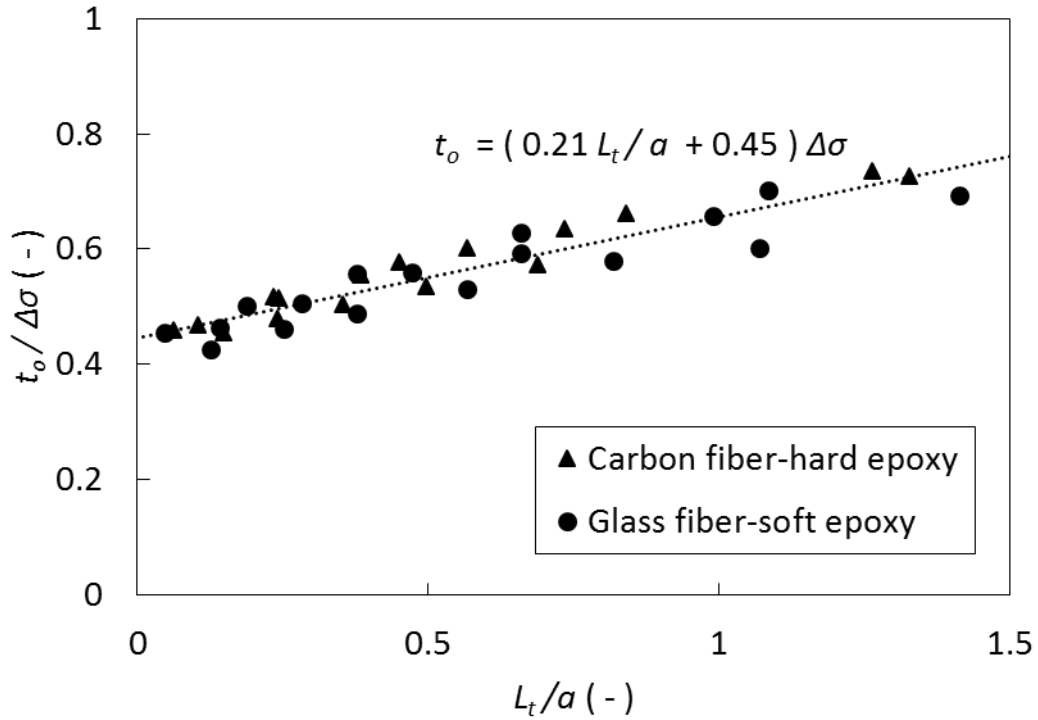
397 Fig. 5. Measurement of t_o for carbon fiber-hard epoxy composite. The black and white

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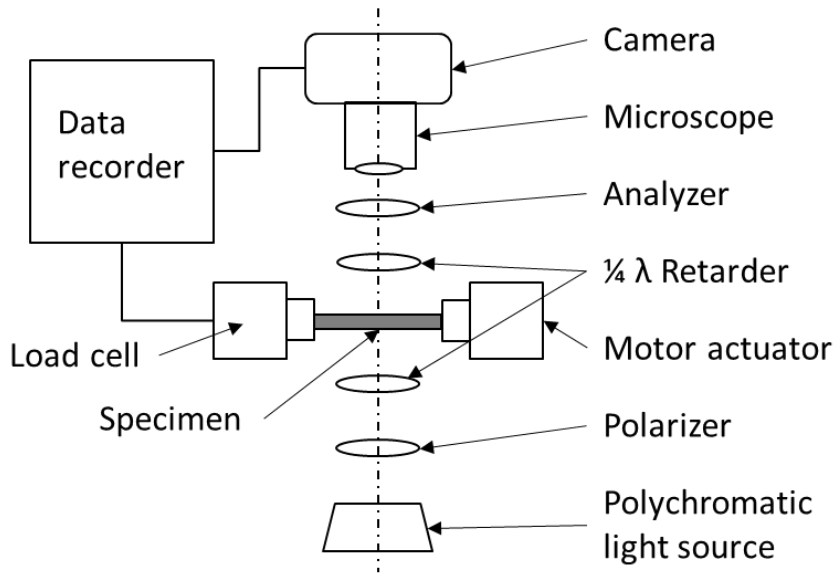


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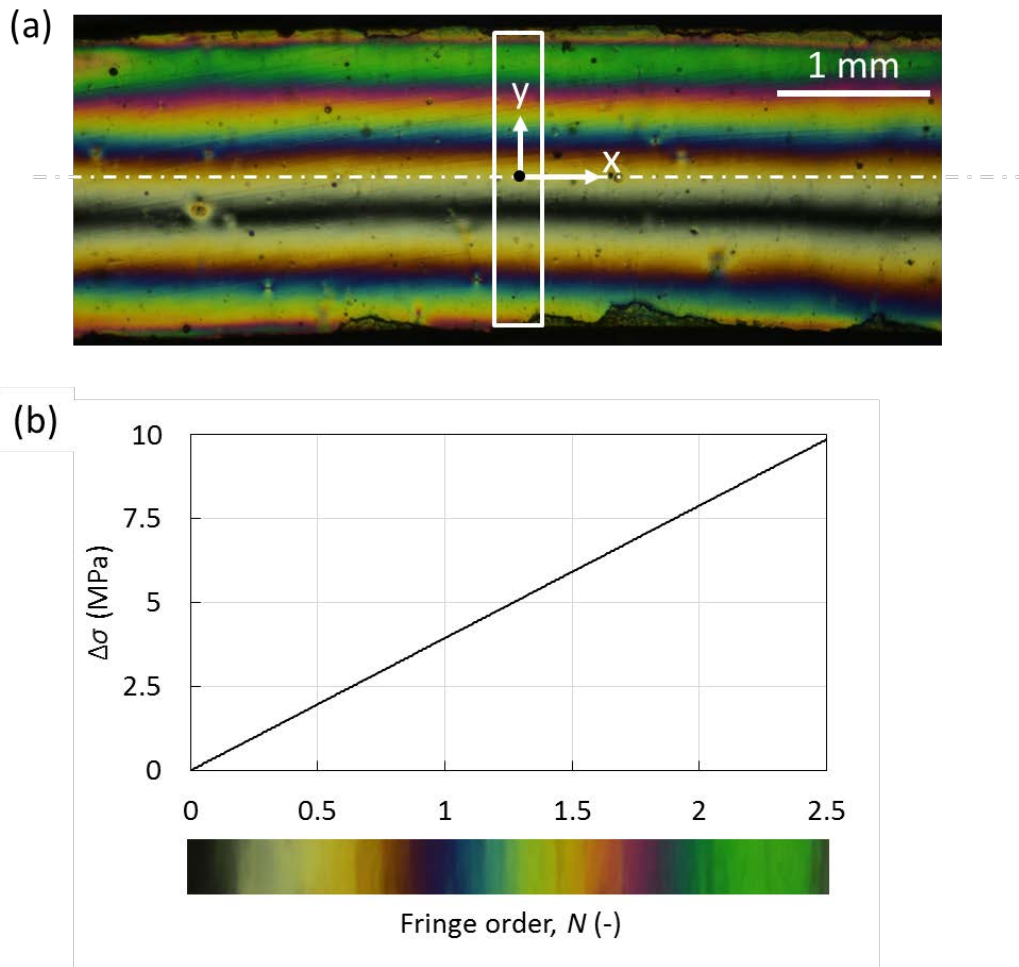
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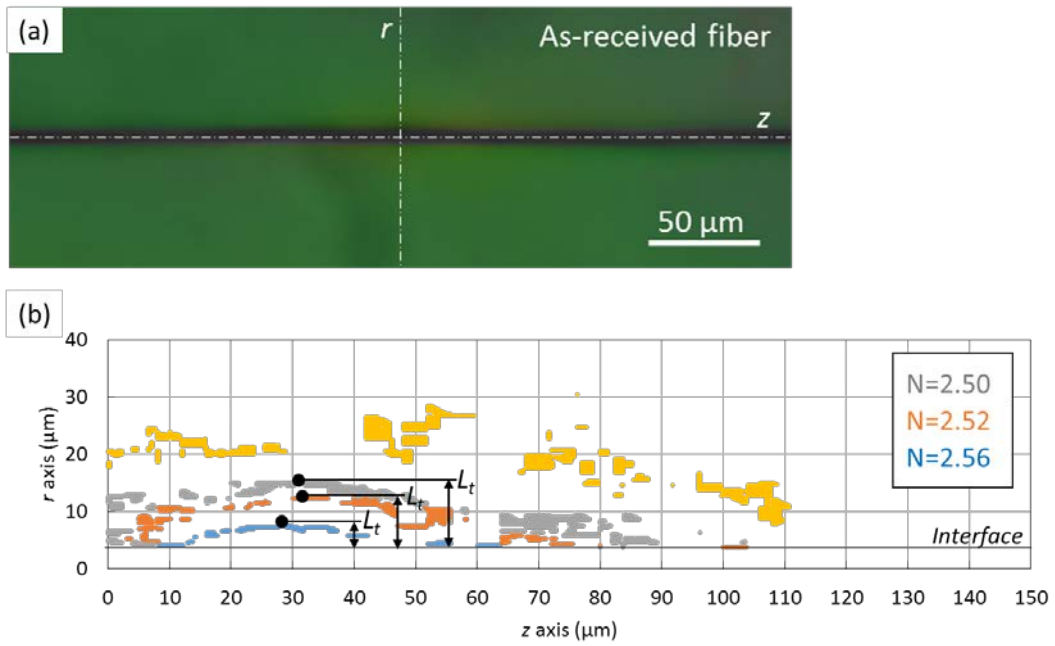
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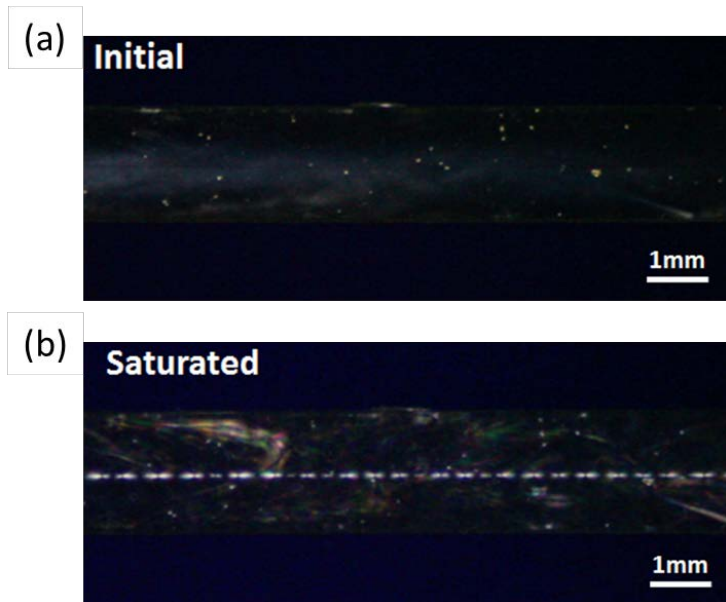


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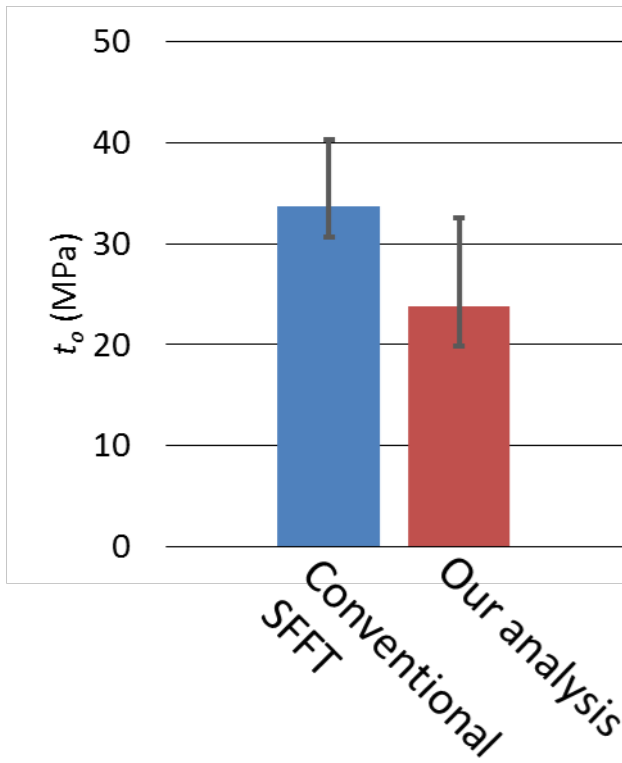
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418

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420 analysis.

421 **Table 1.** Mechanical properties of fibers and epoxy used in simulations.

Parameter	Elastic modulus (E)	Poisson ratio (ν)
Carbon fiber ^a	240 GPa	0.2
Glass fiber ^b	80 GPa	0.22
Hard epoxy ^c	2 GPa	0.4
Soft epoxy ^c	1 GPa	0.4

422 ^aToho Tenax's Datasheet, ^bASM handbook vol 21: Composites, ^cassumption

423

424 **Table 2.** Model parameters used in simulation.

Parameter	Value
Fiber radius (a)	3.5 μm
Matrix radius (b)	70 μm
Model length (L)	1 mm
Fiber element	10500 els. (7 \times 1500)
Matrix element	82500 els. (55 \times 1500)

425

426

427 **Table 3.** Interfacial properties of sample cases examined via simulation.

Interfacial properties	Case 1	Case 2	Case 3
Interfacial stiffness (K_o)	2×10^4 MPa/mm	2×10^4 MPa/mm	2×10^4 MPa/mm
Interfacial strength (t_o)	30 MPa	20 MPa	40 MPa
Interfacial fracture toughness (G_c)	0.04 mJ/mm ²	0.03 mJ/mm ²	0.05 mJ/mm ²

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