<table>
<thead>
<tr>
<th>Title</th>
<th>Interior thermal state of Enceladus inferred from the viscoelastic state of the ice shell</th>
</tr>
</thead>
<tbody>
<tr>
<td>Author(s)</td>
<td>Kamata, Shunichi; Nimmo, Francis</td>
</tr>
<tr>
<td>Citation</td>
<td>Icarus, 284, 387-393</td>
</tr>
<tr>
<td>DOI</td>
<td><a href="https://doi.org/10.1016/j.icarus.2016.11.034">https://doi.org/10.1016/j.icarus.2016.11.034</a></td>
</tr>
<tr>
<td>Issue Date</td>
<td>2017-03-01</td>
</tr>
<tr>
<td>Doc URL</td>
<td><a href="http://hdl.handle.net/2115/72823">http://hdl.handle.net/2115/72823</a></td>
</tr>
<tr>
<td>Rights</td>
<td>(C) 2016 Elsevier Inc. All rights reserved. Licensed under the Creative Commons Attribution-NonCommercial-NoDerivatives 4.0 International <a href="http://creativecommons.org/licenses/by-nc-nd/4.0/">http://creativecommons.org/licenses/by-nc-nd/4.0/</a></td>
</tr>
<tr>
<td>Rights(URL)</td>
<td><a href="http://creativecommons.org/licenses/by-nc-nd/4.0/">http://creativecommons.org/licenses/by-nc-nd/4.0/</a></td>
</tr>
<tr>
<td>Type</td>
<td>article (author version)</td>
</tr>
<tr>
<td>File Information</td>
<td>Kamata_and_Nimmo_2017_Icarus_final_draft.pdf</td>
</tr>
</tbody>
</table>
Interior thermal state of Enceladus inferred from the viscoelastic state of the ice shell

Shunichi Kamata\textsuperscript{a,}\textsuperscript{*}, Francis Nimmo\textsuperscript{b}

\textsuperscript{a}Creative Research Institution, Hokkaido University, Sapporo, Hokkaido 001-0021, Japan.
\textsuperscript{b}Department of Earth and Planetary Sciences, University of California, Santa Cruz, Santa Cruz, CA 95064, USA.

Abstract

Recent geodetic measurements for Enceladus suggest a global subsurface ocean that is thicker beneath the south pole. In order to maintain such an ocean, viscous relaxation of topography at the base of the ice shell and melting of ice need to be balanced. In this study, we investigate the interior thermal state that can lead to the relaxation timescale being comparable to the melting timescale. Our results indicate that a basal heat flux about ten times higher than that due to radiogenic heating, or an ice shell tidal heating rate about ten times higher than the conventional estimate of 1.1 GW is necessary if the ice shell is in thermal equilibrium. These requirements are concordant with recent astrometric studies.

\textit{Keywords:} Enceladus; Planetary dynamics, Interiors

1. Introduction

Multiple flybys of the Cassini spacecraft revealed that the South Polar region of the Saturnian satellite Enceladus is one of the most geologically active regions among icy worlds (e.g., Spencer \& Nimmo 2013). One striking result is that Enceladus is currently producing plumes of gases and solid particles, strongly suggesting the presence of a subsurface ocean in Enceladus (e.g., Porco \textit{et al.} 2006, Postberg \textit{et al.} 2009, Waite \textit{et al.} 2009). This result is surprising because
such a small satellite (i.e., \( \sim 250 \) km in radius) is expected to undergo ocean freezing on a timescale of order \( 10^7 - 10^8 \) yr (Roberts & Nimmo, 2008). Data from the infrared spectrometer onboard Cassini also revealed a hot south pole; the power output across this region is \( \sim 5 - 15 \) GW (e.g., Spencer et al., 2006; Howett et al., 2011). This amount of heat is much larger than the equilibrium value conventionally estimated considering tidal heating and radiogenic heating in the core (Meyer & Wisdom, 2007; Roberts & Nimmo, 2008). Despite a number of studies since the discovery of plumes emanating from this region (e.g., Roberts & Nimmo, 2008; Tyler, 2008; O’Neill & Nimmo, 2010; Shoji et al., 2014; Travis & Schubert, 2015; Roberts, 2015), the heat production mechanism that can account for this anomalously large amount of heat is still unclear. For a better understanding of Enceladus’ heat budget, we investigate the current interior thermal state assuming an equilibrium condition as a starting point.

The thermal state inside an ice shell can be inferred from its viscoelastic state (e.g., White et al., 2013; Kamata & Nimmo, 2014); warmer ice has a lower viscosity, leading to more rapid relaxation, and vice versa. Geodetic data of Enceladus obtained by the Cassini spacecraft suggest that the ice shell has a mean thickness of \( \sim 25 \) km and is thinner around the South Polar Terrain (SPT) (Iess et al., 2014; McKinnon, 2015; Thomas et al., 2016; Van Hoolst et al., 2016; Cadek et al., 2016; Beuthe et al., 2016); the ice shell thus has large-scale topography not only at the surface (Nimmo et al., 2011) but also at its base. Since the basal temperature of the ice shell is the melting point, the basal viscosity of the shell would be low, and thus the timescale of viscous relaxation should be short. Lateral flow in the deep part of the ice shell should therefore efficiently remove basal topography, but this is apparently not consistent with the geodetic observations. A likely mechanism to maintain basal topography is melting of the shell near the SPT; the timescale of melting and that of topography relaxation would need to be comparable.

Collins & Goodman (2007) compare these two timescales assuming a regional subsurface ocean and find that such an ocean can be maintained. This result, however, is based on calculations assuming extremely large heat fluxes from the...
core; several GW of thermal emission are assumed at the base of the regional ocean. Although this assumption is consistent with observations at the surface, it is about ten times larger than radiogenic heat from the core. If the heat from the core is only due to radiogenic sources, is it possible to maintain a regionally thick subsurface ocean? If not, how large an amount of heat is necessary to maintain such an ocean? These questions remain uncertain.

In this study, we compare timescales for melting and relaxation under a wide variety of thermal conditions at the base of the ice shell. We assume that the ice shell is in a thermal equilibrium and is overlying a global subsurface ocean, which is suggested from a recent study of Enceladus’ librations (Thomas et al., 2016). Section 2 describes our interior structure model for Enceladus. Section 3 and 4 describe methods and results for the timescale for melting and that for relaxation, respectively. Section 5 compares these timescales and discusses implications for Enceladus’ heat budget.

2. Interior model

We adopt a three-layer incompressible Enceladus model consisting of an ice shell, a global subsurface ocean, and a rocky core. The layers are assumed to be a Maxwellian viscoelastic material, an inviscid fluid, and a purely elastic material, respectively. Table 1 lists the model parameters adopted. The background thickness of the ice shell ($D_{sh}$) is a free parameter and is less than 60 km; otherwise the ice shell contacts the core. An increase in $D_{sh}$ requires an increase in the radius of the rocky core in order to lead to the same surface gravitational acceleration for a given satellite radius and given densities for each layer. Although these changes slightly affect the moment of inertia, our model gives a normalized moment of inertia of $\sim$0.33, which is consistent with geodetic observations (Iess et al., 2014; McKinnon, 2015).

We assume that the ice shell is completely (Airy) isostatically compensated. Topography at the base of the shell ($h_b$) is then given by

$$h_b = \frac{\rho_i}{\rho_i - \rho_o} \frac{g_s R_s^2}{g_b (R_s - D_{sh})^2} h_s,$$  \hspace{1cm} (1)
where \( h_s \) is surface topography, \( \rho_o \) is density of ocean, \( g_s \) is gravitational acceleration at the surface, \( g_b \) is that at the base of the shell, and \( R_s \) is the radius of Enceladus, respectively. The second factor represents the correction factor for the finite curvature. Note that our model considers the balance of vertical stresses only; this is different from a new isostatic model that minimizes deviatoric stresses (Beuthe et al. 2016). This difference, however, does not change the crustal structure significantly. We use the zonal components of surface topography given by Nimmo et al. (2011).

Figure 1 shows results for \( D_{sh} = 20 \) km. The location where the base of the shell becomes the deepest gives the extent of the thickened portion of the subsurface ocean. The volume of this portion \( (V) \) ranges between \( \sim 4.2 \times 10^5 \) km\(^3\) (for \( D_{sh} \sim 60 \) km) and \( \sim 4.8 \times 10^5 \) km\(^3\) (for \( D_{sh} \sim 10 \) km). We note that \( D_{sh} > 9.5 \) km is necessary in order for the minimum shell thickness to exceed zero and \( D_{sh} < 55.6 \) km to avoid contact between the shell and the silicate core. Consequently, the range of \( D_{sh} \) we explore is between 9.5 km and 55.6 km.

The viscosity profile of the ice shell is calculated from its temperature profile. In this study, we assume that the ice shell is in thermal equilibrium: heat from the core and heat production due to tides in the shell are balanced with heat transport due to thermal conduction. The temperature profile is given by

\[
0 = \frac{1}{r^2} \frac{d}{dr} \left( k r^2 \frac{dT}{dr} \right) + H(r),
\]

where \( T \) is temperature, \( k \) is thermal conductivity (taken to be constant), \( r \) is radial distance from the center of Enceladus, and \( H \) is heat production rate, respectively. The heat production rate \( H \) for a Maxwell body is given by

\[
H(r) = \frac{2\mu \dot{\varepsilon}^2}{\omega} \left( \frac{\omega \eta(r)/\mu}{1 + (\omega \eta(r)/\mu)^2} \right),
\]

where \( \mu \) is rigidity, \( \eta \) is viscosity, \( \omega \) is orbital frequency, and \( \dot{\varepsilon} \) is strain rate, respectively (Ojakangas & Stevenson 1989). See Table 1 for values we used. Temperature at the base of the shell \( (T_b) \) and strain rate \( (\dot{\varepsilon}) \) are free parameters, and we adopt 180–270 K and \( 2 \times 10^{-10}–5 \times 10^{-10} \) s\(^{-1}\), respectively. Such values of strain rate give temperature profiles similar to those inferred from a numerical
study coupling tidal heating and thermal convection at the SPT (Běhouňková et al. 2013).

We apply the rheology of pure water ice (Goldsby & Kohlstedt 2001) to this thermal profile and calculate the Newtonian viscosity as a function of depth:

$$\eta(r) = \eta_{\text{ref}} \exp \left( \frac{E_a}{R_g} \left( \frac{1}{T(r)} - \frac{1}{T_{\text{ref}}} \right) \right),$$

where $\eta_{\text{ref}}$ is reference viscosity of ice, $T_{\text{ref}}$ is reference temperature, $E_a$ is activation energy, and $R_g$ is the gas constant, respectively. Because the reference viscosity for the ice shell of Enceladus is uncertain, we consider a wide range of reference viscosities: $10^{12} - 10^{17}$ Pa s.

Although the interior structure adopted in this study is simple, particularly below the ice shell, the timescale of viscoelastic relaxation at the base of the shell depends only weakly on the deep interior structure. Thus, the use of a more realistic deep interior structure model would not change our conclusions.

It is noted that we assume a purely conductive ice shell. The actual ice shell of Enceladus, however, may be convective, at least locally (e.g., Běhouňková et al. 2013, 2015). If this is the case, the thickness of warm ice would be larger than in the conductive model. This would lead to a smaller relaxation timescale. The consequence of this effect will be discussed in Section 5.

3. $\tau_{\text{melt}}$: Timescale of melting

The timescale of melting ($\tau_{\text{melt}}$) can be estimated analytically:

$$\tau_{\text{melt}} = \frac{\rho_i LV}{P_{\text{melt}}},$$

where $\rho_i$ is density of ice, $L$ is latent heat of ice, $V$ is the volume of ice to be melted, and $P_{\text{melt}}$ is power used for melting, respectively. Results are shown in Figure 2 assuming that $V$ is the volume of the thickened portion of the ocean obtained in Section 2. The upper and lower bound is given by the largest and smallest $V$ (i.e., the smallest and largest $D_{\text{sh}}$), respectively; the use of different values of $D_{\text{sh}}$ has little effect on $\tau_{\text{melt}}$. For example, if $P_{\text{melt}} = 1.1$ GW, which is
the conventional long-term limit of tidal heating rate (Meyer & Wisdom 2007), \( \tau_{\text{melt}} \) is \( \sim 4 \) Myr.

4. \( \tau_{\text{rel}} \): Timescale of viscoelastic relaxation

4.1. Method

In contrast to the timescale of melting, that of viscoelastic relaxation (\( \tau_{\text{rel}} \)) needs to be estimated numerically. We calculate the time evolution of topography at the base of the ice shell using a semi-analytical code (e.g., Kamata & Nimmo 2014). In the following, we briefly summarize the calculation method. The governing equation system consists of three equations: the linearized equation of momentum conservation,

\[
0 = \nabla_j \cdot (\sigma_{ji} - P \delta_{ji}) + \rho \nabla_i \phi,
\]  

the Poisson’s equation for the gravitational field,

\[
\nabla^2 \phi = -4\pi G \rho,
\]  

and the constitutive equation for a Maxwell medium,

\[
\frac{d\sigma_{ji}}{dt} + \frac{\mu}{\eta} (\sigma_{ji} - \frac{\sigma_{kk}}{3} \delta_{ji}) = \left( \kappa - \frac{2\mu}{3} \right) \frac{de_{kk}}{dt} \delta_{ji} + 2\mu \frac{de_{ji}}{dt},
\]

where \( \nabla_i \) is a spatial differentiation in direction of \( i (= x, y, z) \), \( t \) is time, \( \sigma \) is stress tensor, \( e \) is strain tensor, \( \phi \) is gravitational potential, \( P \) is hydrostatic pressure, \( \kappa \) is bulk modulus, \( \mu \) is shear modulus, \( \delta \) is the Kronecker delta, and \( G \) is the gravitational constant, respectively. Applications of a finite difference to the time differentials in the constitutive equation and of a spherical harmonic expansion to the three equations leads to a six-component, time-dependent, inhomogeneous first-order ordinary differential equation system. We then carry out time-marching calculations and obtain the time evolution of the amplitude of topographic undulation for each harmonic degree. The time evolution of topography can be calculated by superposing spherical harmonics with time-dependent coefficients. See Kamata et al. (2012) for further details of the formulation. In this study, we consider spherical harmonic degrees \( n = 1–10 \).
It should be noted that we assume a spherically symmetric interior model (see Section 2) and use a one-dimensional calculation code. Nevertheless, the rate of viscoelastic relaxation beneath the SPT should mainly be controlled by the thermal state around this region. Thus, the thermal state we adopt should be considered as that relevant to the SPT and its immediate surroundings, not the shell as a whole.

4.2. Results

Figure 3 shows the time evolution of topographic amplitudes at the base of the ice shell under a given set of shell conditions: \(D_{sh} = 20\) km, \(\eta_{ref} = 10^{14}\) Pa s, \(T_b = 270\) K, and \(\dot{\varepsilon} = 4 \times 10^{-10}\) s\(^{-1}\). The amplitude is normalized by the amount of load. Except for spherical harmonic degree \(n = 1\), the normalized amplitude starts from \(\approx 1\), decreases with time, and approaches 0, because of viscous relaxation. The deformation timescale of basal topography is longer for a lower harmonic degree (i.e., longer wavelength), and this result is consistent with previous studies (e.g., McKenzie et al. 2000; Kamata et al. 2015b). The case of \(n = 1\) has an initial normalized amplitude of \(\sim 0.93\). Since the center of mass does not change with time, the potential perturbation for \(n = 1\) needs to be zero at all times. Such a different boundary condition at the surface leads to a non-negligible instant response only for \(n = 1\) (Kamata & Nimmo 2014).

Using these results, we calculate the time evolution of topography at the base of the ice shell as well as that of the volume of the regionally thickened portion of the ocean. We define the timescale of relaxation (\(\tau_{rel}\)) as the time when this volume becomes \(1/e\) of the initial condition. Figure 4 summarizes \(\tau_{rel}\) as a function of shell thickness (\(D_{sh}\)) and of reference viscosity (\(\eta_{ref}\)) for a given basal temperature (\(T_b = 270\) K) and a given strain rate (\(\dot{\varepsilon} = 4 \times 10^{-10}\) s\(^{-1}\)). A higher \(\eta_{ref}\) leads to a longer \(\tau_{rel}\), as expected; a factor of 10 increase in \(\eta_{ref}\) leads to a factor of \(\sim 10\) increase in \(\tau_{rel}\). A lower \(T_b\) also leads to a longer \(\tau_{rel}\) because this leads to an increase in the viscosity at the base of the shell. Consequently, a decrease in \(T_b\) has an effect on \(\tau_{rel}\) similar to that by an increase in \(\eta_{ref}\). Specifically, a factor of 10 increase in \(\tau_{rel}\) can be achieved by a decrease in \(T_b\) of
∼10−20 K, depending on other parameters. In addition, a smaller $D_{sh}$ also leads to a longer $\tau_{rel}$; $\tau_{rel}$ is almost proportional to $D_{sh}^{-3}$, and this result is consistent with previous studies (e.g., McKenzie et al. [2000] [Kamata et al. 2015b]).

It is found that a change in $\dot{\varepsilon}$ has only a minor contribution. In our model, an increase in $\dot{\varepsilon}$ increases the amount of heat produced in the shell (see equation (3)). However, this heat becomes important only when the shell is soft; a low $\eta_{ref}$, a high $T_b$, and a large $D_{sh}$ are needed. Under such a condition, an increase in $\dot{\varepsilon}$ results in a shorter $\tau_{rel}$, though the effect is not significant.

It is noted that a low reference viscosity (i.e., $\eta_{ref} \sim 10^{13}$ Pa s) requires a thin shell (i.e., $D_{sh} < \sim 20$ km). This is because such a reference viscosity leads to a large tidal heating rate, and temperature significantly increases with depth. However, since the basal temperature is assumed to be the melting point, a thick ice shell is not allowed. The largest heat production rate is given when $\omega \eta/\mu = 1$ (see equation (3)); for our model, $\eta \sim 6 \times 10^{13}$ Pa s gives the largest heat production rate.

5. Comparison of timescales and discussion

Figure 5 summarizes the relation of the timescale of melting ($\tau_{melt}$) and that of relaxation ($\tau_{rel}$) under different thermal states at the base of the ice shell for a given power ($P_{tot}$). Figure 5 (a) assumes that $P_{tot}$ is the sum of radiogenic heat (0.3 GW) and tidal heat (1.1 GW), both conventional estimates [Roberts & Nimmo 2008 Meyer & Wisdom 2007]. Note that not all the power can be used to melt the ice; a part of heat is used to warm the shell (i.e., $H$ in equation (2)). See the Appendix for the method to calculate the amount of heat used for warming the shell. We subtract this power from $P_{tot}$ and calculate $\tau_{melt}$ using equation (5). We found parameter conditions that can lead to $\tau_{rel} = \tau_{melt}$ only if the basal heat flux ($q_b$) is higher than 5 mW m$^{-2}$ (the green shaded area in Figure 5); below this basal heat flux, relaxation is faster than melting, leading to rapid removal of basal topography. The radiogenic heat from the core of 0.3 GW produces a heat flux of only 0.4–0.6 mW m$^{-2}$ at the base of
the ice shell, depending on $D_{sh}$. Consequently, if the basal heat is only due to radiogenic sources, the basal topography would relax, and a regionally thick subsurface ocean cannot be maintained over the long term.

As noted above, our model assumes a purely conductive model, and a convective shell would lead to a shorter relaxation timescale. This indicates that the red shaded area in Figure 5 increases if we assume a convective ice shell; a minimum basal heat flux larger than our model would be necessary to maintain basal topography. Consequently, the occurrence of convection in the shell does not affect the above conclusion that a regionally thick subsurface ocean requires a heat source other than radiogenic. Furthermore, recent studies suggest that the present-day ice shell is thin (i.e., $\sim$20 km) (e.g., Thomas et al., 2016; Van Hoolst et al., 2016; Čadek et al., 2016; Beuthe et al., 2016). Although mobile lid convection may be possible even for such a thin shell if the near-surface ice is sufficiently damaged (Barr, 2008), thermal convection for the entire ice shell is unlikely to operate; the ice shell is likely to be conductive.

Although we adopt an activation energy for pure water ice, an inclusion of other compounds may affect the “effective” activation energy for the actual ice on Enceladus. Hydrate salts have higher activation energies (Durham et al., 2005), leading to a larger increase in viscosity as decreasing temperature. However, such an effect becomes apparent only if the volume fraction of salts is $\geq$20% (Durham et al., 2005), which is unlikely to be the case for Enceladus. Consequently, our model (i.e., a pure water ice model) should give a good estimate of the relaxation timescale for the Enceladus’ ice shell.

The inclusion of volatiles, such as ammonia, in ice also affects the physical properties of ice and ocean. When ammonia water freezes, ammonia molecules concentrate in the liquid. Consequently, melting and freezing leads to ammonia-poor ice and an ammonia-rich ocean. An increase in ammonia content in the ocean leads to a decrease in the melting point (i.e., the basal temperature). Note that our calculation conditions cover basal temperatures down to 180 K, which is close to the lowest melting point (e.g., Fortes & Choukroun, 2010). Consequently, this effect does not affect our main conclusion that a regionally
thick subsurface ocean requires a heat source other than radiogenic.

Under what conditions can basal topography be maintained? One possibility is that the heat production rate below the ice shell is at least about one order of magnitude larger than that due to radiogenic heating: \( q_b > 5 \text{ mW m}^{-2} \) or \( >3 \text{ GW} \). One potential heat production mechanism below the ice is tidal dissipation in the ocean. Recent studies have considered such production mechanisms and find that tides and dissipation can be large only if the ocean is very thin (i.e., \(<1 \text{ km}\) \cite{Tyler2011, Matsuyama2014, Kamata2015}). Since such a thin ocean is not supported by recent estimates based on geodetic data (e.g., \cite{Cadek2016}), tidal dissipation in the ocean is unlikely to play a major role in heating the base of the ice shell.

Another possibility is a large heat production rate in the core. The 2-D numerical work by \cite{Collins2007} adopts this condition and concludes that a regional subsurface ocean can be maintained. Consequently, their 2-D results and our 1-D results agree with each other. A possible additional heat production mechanism in the core is chemical reaction, such as serpentinization. However, it is unlikely that it can produce sufficiently large amount of heat \cite{Malamud2013, Travis2015}. Another possible mechanism is tidal heating in the core. Although the amount of energy dissipated in a fragmented, fluffy core is larger than that in a rigid core, it is \(<2 \text{ GW}\) if a Maxwellian rheology is adopted \cite{Roberts2015}. A different rheological behavior (i.e., stress-dependent rheology) or tidally-driven water flow in the core may lead to a larger amount of heat; a future study investigating such effects is necessary to quantify the (maximum) amount of heat from the core.

Another possibility is that the tidal dissipation in the ice shell that can be used for melting \((P_{\text{melt}})\) is much larger than 1 GW. This leads to a decrease in \( \tau_{\text{melt}} \) and to a decrease in the minimum basal heat flux that gives \( \tau_{\text{rel}} = \tau_{\text{melt}} \).

Results for different values of \( P_{\text{tot}} \) are also shown in Figure 5. These results indicate that \( q_b \) can be as low as that expected from radiogenic heating if \( P_{\text{tot}} \geq 10 \text{ GW} \). Thus, if the tidal heating rate in the shell is \( \geq10 \text{ GW} \), a regionally thick ocean can be maintained without invoking anomalously large heat production.
in the core. Shoji et al. (2014) show that episodically increased tidal heating due to the coupling of the thermal and orbital evolution could be plausible, though the amount of additional heat is only $\sim\!0.5$ GW. In addition, their study finds that an episodic heating cycle requires a basal temperature of $\sim\!175$ K. Such a low melting point requires a large amount of ammonia (i.e., $>30$ wt%) (e.g., Fortes & Choukroun 2010). However, this is difficult to reconcile with the chemical composition of the plumes (e.g., Waite et al. 2009; Marion et al. 2012). Roberts (2015) also points out that an increase in the amount of ammonia leads to a decrease in the density of water and that the NH$_3$ content should be less than $\sim\!15\%$; otherwise ice I is not buoyant. Consequently, increased tidal heating due to coupled thermal-orbital evolution is unlikely to be the major factor that maintains a regionally thick subsurface ocean. It is noted that the model by Travis & Schubert (2015) assumes an episodic increase of $\sim\!10$ GW. While this may be consistent with observations, the mechanism leading such a large increase in tidal heating rate is not clear.

A tidal heating rate much larger than the conventional estimate (i.e., $\sim\!1$ GW) does not necessarily require an episodic heating cycle. This conventional equilibrium estimate by Meyer & Wisdom (2007) is based on the assumption that the dissipation factor $Q$ of Saturn is $>18,000$. This lower bound on $Q$ (assumed constant) is based on the present-day position and assumed primordial age of Mimas (e.g., Gavrilov & Zharkov 1977; Dermott et al. 1988). A smaller $Q$ (more dissipative Saturn) would imply a greater equilibrium heating rate. A recent interpretation of astrometric data suggests a $Q$ for Saturn about one order of magnitude smaller than the conventional estimate, which leads to a tidal heating rate of $\sim\!15$ GW (Lainey et al. 2012). If this is the case, the maintenance of a regionally thick subsurface ocean can be explained. The problem is, however, a change in the $Q$ of Saturn affects not only the orbital evolution of Enceladus but also those of other satellites. In particular, such a low $Q$ is usually taken to require an extremely young age for inner satellites such as Mimas. However, this argument assumes that $Q$ is constant. Recent work has suggested both that the $Q$ of Saturn is highly frequency-dependent, and that the timescale of satel-
lite orbital evolution may depend on the evolution timescale of Saturn itself, owing to resonance locking between satellites and internal oscillation modes of Saturn [Fuller et al. 2016]. As a result, high rates of present-day dissipation in Enceladus do not necessarily require that Mimas be very young. Furthermore, such high dissipation rates can readily sustain a global ocean for as long as the Enceladus-Dione resonance has operated [Nimmo et al. submitted].

It should be noted that our model assumes that the current ice shell of Enceladus is in thermal equilibrium. The actual ice shell of Enceladus, however, may not be in such a state. O’Neill & Nimmo (2010) show that occasional catastrophic overturns of a convective ice shell could lead to an extremely large amount of heat release during these overturns. Such ice shell dynamics, which are not modeled in this study, may contribute not only to the observed high surface heat fluxes but also to the presence of a regionally thick, global subsurface ocean.

It is also noted that mechanisms that remove basal topography other than viscous relaxation are not considered in this study. One such mechanism is ice pumping due to the pressure-dependent melting point of ice (e.g., Lewis & Perkin 1986). When a water parcel at the base of a thick shell moves to the base of a thin shell, it will freeze; a thin ice shell thickens. If the timescale of ice pumping is shorter than that of viscous relaxation, one should compare the former timescale with that for melting. However, such a comparison is beyond the scope of this study and is left for future studies.

6. Conclusion

The presence of a regionally thick, global subsurface ocean in Enceladus is inferred based on geodetic measurements by Cassini. This requires a balance between melting of ice and viscous relaxation of basal topography. We investigate the interior thermal state of Enceladus by comparing the timescale of melting of ice and that of viscoelastic relaxation at the base of the ice shell. Our results indicate that a heat flux $>5$ mW m$^{-2}$ (3 GW) at the base of the ice
shell is necessary in order to maintain basal topography if we assume conventional estimates for radiogenic and tidal heating rates. This condition, however, is unlikely to be satisfied by Enceladus. Alternatively, we find that a tidal heating rate of $\sim 10$ GW in the ice shell is sufficient to maintain basal topography if the basal heat flux is due only to radiogenic heat from the core. Although we cannot rule out the possibility of episodic heat release, our results assuming thermal equilibrium are concordant with a large tidal heating rate supported by recent astrometric studies.

Appendix: $P_{sh}$: Power used to heat the ice shell

For a given shell thickness ($D_{sh}$), reference viscosity ($\eta_{ref}$), basal temperature ($T_b$), and strain rate ($\dot{\varepsilon}$), we can calculate the temperature profile using equations (2) and (3). The power used to heat the ice shell ($P_{sh}$) is given as the integral of the tidal heating rate in the shell ($H$) and can be expressed as

$$P_{sh} = \Omega \left(q_s R_s^2 - q_b R_b^2\right),$$

where $\Omega$ is solid angle of the heated region, $q_s$ is heat flux at the surface, $q_b$ is that at the base of the shell, $R_s$ is the radius of Enceladus, and $R_b = R_s - D_{sh}$ is the radial distance of the base of the shell from the center of Enceladus, respectively. Values except $\Omega$ can be determined from the temperature profile.

The solid angle of the tidally heated region ($\Omega$) is unclear. In this study, we use three different values for $\Omega$: from the south pole to $75^\circ$S, to $60^\circ$S, and to $45^\circ$S. Note that $P_{sh}$ is large only if $H$ can be large. Such a case is found only for $\eta_{ref} \sim 10^{13}$ Pa s and $D_{sh} \sim 20$ km (see Figure 6). Most other conditions lead to small $P_{sh}$ independent of $\Omega$. Consequently, the use of different values for $\Omega$ does not change our results significantly.

Acknowledgments

We thank two anonymous reviewers for constructive comments improving the manuscript. Any requests for data produced in this study should be sent to
Shunichi Kamata at kamata@mail.sci.hokudai.ac.jp. This work was supported by JSPS KAKENHI grant 16K17787.

References


Figure 1: Cross section of the upper part of our Enceladus model. \( V \) represents the volume of the thickened portion of the ocean.

Figure 2: Timescale of melting as a function of power. A conventional estimate on the tidal heating rate (i.e., 1.1 GW) leads to a relaxation timescale of \( \sim 4 \) Myr.
Figure 3: Time evolution of basal topography for different spherical harmonic degrees. Calculation conditions are shown. A higher degree results in a faster relaxation. Only degree-1 topography exhibits a non-negligible instant response because its boundary condition differs from those for other degrees.

Figure 4: Relaxation timescale ($\tau_{\text{rel}}$) as a function of ice shell thickness ($D_{\text{sh}}$) and reference viscosity of ice ($\eta_{\text{ref}}$). Results for a basal temperature ($T_b$) of 270 K and a strain rate ($\dot{\varepsilon}$) of $4 \times 10^{-10} \text{ s}^{-1}$ are shown. The shaded areas in gray violate our assumptions that the ice shell is isostatically fully compensated. No solution for a large $D_{\text{sh}}$ and a low $\eta_{\text{ref}}$ is found.
Figure 5: Comparison of the timescale of relaxation ($\tau_{\text{rel}}$) and that of melting ($\tau_{\text{melt}}$). Results under all calculation conditions are used to produce this figure. Each panel shows results for different powers ($P_{\text{tot}} = 1.4–15$ GW). Parameter conditions that can lead to $\tau_{\text{rel}} = \tau_{\text{melt}}$ can be found only in the green area (upper right in each panel). The black band at $\sim0.5$ mW m$^{-2}$ indicates the heat flux due to radiogenic heating in the core of 0.3 GW. No solution is found for a low basal temperature and a low basal heat flux. A basal heat flux due to radiogenic heating in the core can be sufficient for maintaining basal topography only if $P_{\text{tot}} \geq 10$ GW.
Figure 6: Power used for heating the ice shell ($P_{sh}$) as a function of ice shell thickness ($D_{sh}$) and reference viscosity of ice ($\eta_{ref}$). Results for a basal temperature ($T_b$) of 270 K and a strain rate ($\dot{\varepsilon}$) of $4 \times 10^{-10}$ s$^{-1}$ are shown. The shaded areas in gray violate our assumptions that the ice shell is isostatically fully compensated.
Table 1: Model parameters.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Quantity</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_s$</td>
<td>Radius of Enceladus</td>
<td>252.1</td>
<td>km</td>
</tr>
<tr>
<td>$D_{sh}$</td>
<td>Thickness of the ice shell</td>
<td>10–56</td>
<td>km</td>
</tr>
<tr>
<td>$g_s$</td>
<td>Surface gravity</td>
<td>0.11345</td>
<td>m s$^{-2}$</td>
</tr>
<tr>
<td>$\rho_i$</td>
<td>Density of the ice shell</td>
<td>920</td>
<td>kg m$^{-3}$</td>
</tr>
<tr>
<td>$\rho_o$</td>
<td>Density of the ocean</td>
<td>1000</td>
<td>kg m$^{-3}$</td>
</tr>
<tr>
<td>$\rho_m$</td>
<td>Density of the mantle</td>
<td>2470</td>
<td>kg m$^{-3}$</td>
</tr>
<tr>
<td>$\mu_i$</td>
<td>Rigidity of the ice shell</td>
<td>3.3</td>
<td>GPa</td>
</tr>
<tr>
<td>$\mu_m$</td>
<td>Rigidity of the mantle</td>
<td>10</td>
<td>GPa</td>
</tr>
<tr>
<td>$k$</td>
<td>Thermal conductivity of ice</td>
<td>2.3</td>
<td>W m$^{-1}$ K$^{-1}$</td>
</tr>
<tr>
<td>$L$</td>
<td>Latent heat of ice</td>
<td>330</td>
<td>kJ kg$^{-1}$</td>
</tr>
<tr>
<td>$2\pi/\omega$</td>
<td>Orbital period</td>
<td>1.37</td>
<td>days</td>
</tr>
<tr>
<td>$T_s$</td>
<td>Surface temperature</td>
<td>75</td>
<td>K</td>
</tr>
<tr>
<td>$T_{ref}$</td>
<td>Reference temperature</td>
<td>273</td>
<td>K</td>
</tr>
<tr>
<td>$T_b$</td>
<td>Basal temperature</td>
<td>180–270</td>
<td>K</td>
</tr>
<tr>
<td>$E_a$</td>
<td>Activation energy</td>
<td>60</td>
<td>kJ mol$^{-1}$</td>
</tr>
<tr>
<td>$\eta_{ref}$</td>
<td>Reference viscosity of ice</td>
<td>10$^{12}$–10$^{17}$</td>
<td>Pa s</td>
</tr>
<tr>
<td>$\dot{\varepsilon}$</td>
<td>Strain rate</td>
<td>2 $\times$ 10$^{-10}$–5 $\times$ 10$^{-10}$</td>
<td>s$^{-1}$</td>
</tr>
</tbody>
</table>