



Title	Stability assessment approach for soil slopes in seasonal cold regions
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Citation	Engineering geology, 221, 154-169 <a href="https://doi.org/10.1016/j.enggeo.2017.03.008">https://doi.org/10.1016/j.enggeo.2017.03.008</a>
Issue Date	2017-04-20
Doc URL	<a href="http://hdl.handle.net/2115/73692">http://hdl.handle.net/2115/73692</a>
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# 1                    **Stability assessment approach for soil slopes in seasonal cold regions**

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## 9                    **ABSTRACT**

10                    In Hokkaido Japan, soil slope failures along some of the national highways are reported frequently in  
11                    recent years. A stability assessment method which can consider the impact of seasonal changes like  
12                    freeze-thaw action, snowmelt water infiltration etc. is of utmost importance and considered to be an  
13                    immediate requirement for geotechnical practitioners, in order to properly predict the slope stability. In  
14                    this study, a slope stability assessment approach based on two-dimensional numerical modelling is  
15                    recommended which considers the water content changes of the soil induced by the seasonal climatic  
16                    effects i.e. freeze-thaw action, snowmelt water infiltration etc. Two case studies of slope failures in  
17                    Hokkaido have been studied using the recommended approach. In order to visualise the climatic  
18                    parameters of most influence on slope stability, parametric studies have been performed through which  
19                    many useful results in view of the soil slope stability in seasonal cold regions have been obtained. It is  
20                    found that the freeze-thaw action has a considerable impact on the soil water content and slope stability.  
21                    On the other hand, the snowmelt water infiltration has a very significant impact on soil slope stability.  
22                    The recommended numerical modelling approach is found to be very useful in analysing the soil slope  
23                    stability in seasonal cold regions.

24                    **Author keywords:** Slope stability, seasonal cold regions, non-isothermal seepage, freeze-thaw action,  
25                    snowmelt water (IGC: E06/E09/E13)

26 **1. Introduction**

27 Slope failures occur in seasonal cold regions like Hokkaido during the snow melting season and rainy  
28 season. Many incidents of soil slope failure along roadways of Hokkaido are continuously being reported  
29 (Nakatsugawa et al. 2015). These slope failures involved a collapse of the man-made embankment filling  
30 constructed to support the roadway as well as failures in natural slopes and cut slopes in the vicinity of  
31 roads. Most of the failures happened particularly during the snow melting season of Hokkaido between  
32 April and May. There is an urgent need of studying the causes of soil slope failures induced in seasonal  
33 cold regions in order to prevent such disasters.

34 An enormous number of studies have been done to identify the factors that affect the soil slope  
35 stability in cold regions (McRoberts and Morgenstern 1974a, 1974b; Mackay, 1981; Goodrich, 1982;  
36 Burgess, 1993; Niu, 2005). McRoberts and Morgenstern (1974b) investigated the failure mechanism of  
37 thaw-induced landslide slope failures observed in permafrost regions of Canada. Unlike permafrost  
38 regions, seasonal cold regions like Hokkaido experience abrupt weather changes throughout the year,  
39 which in turn fluctuates the ground temperature and water content of the soil. The excess water content  
40 originating from the snowmelt water and rainfall may induce a slope failure. Since most of the slopes are  
41 unsaturated, the key factor that determines the stability of this type of slope failures is the soil water  
42 content distribution. Ishikawa et al. (2015) comprehensively summarised the distinction between slope  
43 failures in seasonal cold regions and warm temperate regions and pointed out the important factors that  
44 need to be considered in the stability assessment of unsaturated soil slopes in seasonal cold regions. To  
45 date, an applicable stability assessment approach considering all the seasonal changes of water content,  
46 for soil slopes in cold regions has not been adopted in geotechnical practice.

47 In this study, a stability assessment approach has been recommended which considers the soil water  
48 content changes of the slope influenced by seasonal changes. Two case studies of slope failures were  
49 analysed using the proposed approach. The first case is a trial physical embankment slope constructed

50 using volcanic soil studied by Matsumura (2014) and Kawamura et al. (2016). The second case study is a  
51 slope failure that occurred in a man-made embankment along a national highway in Hokkaido, Japan  
52 (Hokkaido Regional Development Bureau, 2013). Back analyses of both the slope disasters using the  
53 proposed approach have been made to investigate the causes and influencing factors of failure. A coupled  
54 numerical analysis procedure to simulate the water content of the slope considering the effects of  
55 temperature change, latent heat phase change and precipitation including snowfall and rainfall have been  
56 adopted. Using the limit equilibrium method, a stability assessment of slope has been made which uses  
57 the soil water content distribution derived from the coupled simulation. Further, in order to visualise the  
58 parameters of most influence on slope stability, parametric studies have been performed by considering  
59 and neglecting the effect of ground freezing, considering and ignoring the effect of snowfall and  
60 considering different magnitudes of snowfall and rainfall for both the case examples.

## 61 **2. Case studies of soil slope failures in Hokkaido**

### 62 **2.1 Case study of failure on embankment slope made up of volcanic soil**

63 An embankment slope was constructed using a volcanic soil at an angle of  $45^\circ$  with 5 m elevation and 7.7  
64 m length at the base. The site is located at Latitude  $42^\circ 57' 13''$  North and Longitude  $141^\circ 21' 46''$  East in  
65 Hokkaido, Japan. As shown in Fig. 1(a) thermometers, tensiometers, moisture content sensors, rainfall  
66 gauges and a snow gauge were installed in the slope to monitor the ground temperature, pore water  
67 pressure, soil water content, rainfall and snowfall respectively. To avoid disturbance to the surface soil of  
68 the slope, monitoring instruments were installed in three different cross sections namely Left (L), Centre  
69 (C) and Right (R) as viewed from the bottom of the slope. The monitoring instruments installed in cross  
70 sections are shown in Fig. 1 (b) in a two-dimensional view. In order to prevent the mutual water exchange  
71 between the physical embankment and ground surface, the embankment slope was covered by  
72 impermeable sheets made up of thin waterproof plastic materials at the bottom and side portions. A

73 geomembrane liner is not used in this case, as it was understood that the water flow through the slope  
74 might not reach the slope bottom due to the soil's low permeability, and the purpose of impermeable  
75 sheets are to avoid some possible flow of water from the foundation soil. The foundation was also made  
76 up of the same volcanic soil material. In this case, no consideration was given to the interface friction that  
77 may occur between the impermeable sheets and soil layers. After placing the sheets at the bottom and  
78 back side, the soil is compacted layer by layer with a constant depth of 0.25 m per layer up to 5 m height,  
79 using a hand-guided roller compactor. A prescribed volume of water (approximately 1 m<sup>3</sup>/day) was  
80 supplied to the slope using water supply pipes at constant intervals through different cross sections. The  
81 amount of the water supplied is determined based on the storage of water supply tanks. The intervals at  
82 which water was supplied through Left (L) section are 27-07-2013 to 06-08-2013 (10 to 11 days) and  
83 11-10-2013 to 17-10-2013 (6 to 7 days). The construction and setting up of monitoring instruments were  
84 finalised and monitoring starting on November 9, 2012 (09-11-2012). The monitoring continued until the  
85 day of slope failure on October 17, 2013 (17-10-2013). Total monitoring time was around 343 days.  
86 Further details about the slope monitoring program can be found from Matsumura, (2014) and Kawamura  
87 et al. (2016).

## 88 **2.2 Case study of slope failure occurring along national highway route 230**

89 On April 7, 2013, at 11:20 A.M., a slope failure happened along the national highway route No.230 near  
90 42° 54' 52" North Latitude and 141° 07' 22" East Longitude in Hokkaido, Japan. The national highway  
91 connects Sapporo city with Setana, a town in the Hiyama subprefecture of Hokkaido. Hereafter, the slope  
92 failure will be referred as highway slope failure in this paper. The slope failure occurred in the  
93 embankment along the roadway. The size of the slope failure was around 40 m wide along the road and  
94 19 m in vertical depth along the failure plane. Approximately 11000 m<sup>3</sup> of sediment, containing

95 embankment filling material and accumulated snow above the soil ground together flowed out downward  
96 to the slope foot up to 40 to 50 m length, as shown in Fig. 2 (a) and (b).

97 The slope failure was induced by the combined action of heavy rainfall and snowmelt water  
98 (Hokkaido Regional Development Bureau, 2013). The cumulative daily rainfall that occurred on the day  
99 of slope failure was 92 mm and the cumulative snowmelt was 31 mm, as recorded in a nearby  
100 meteorological telemetry, maintained by Ministry of Land, Infrastructure, Transport and Tourism,  
101 Hokkaido Regional Development Bureau (MLIT) shown in Fig. 2 (c). The maximum hourly rainfall  
102 recorded on 07-04-2013 was 12 mm. The rainfall was continuous from 07-04-2013 00:00 to 07-04-2013  
103 11:00. The cumulative daily rainfall along with the cumulative snowmelt water caused the failure of the  
104 slope. The cumulative daily rainfall and snowmelt water, which together amounted to 123 mm, is a  
105 considerable intensity to make the slope fail.

### 106 **3. Recommended slope stability assessment approach**

107 In geotechnical design practice, for the long-term stability assessment of soil slopes i.e. embankment  
108 slopes and cut slopes along highways, the factors such as freeze-thaw action and snowmelt water  
109 infiltration are not considered. As found by previous research, for the design of soil slopes in seasonal  
110 cold regions the above-mentioned factors are significant (Ishikawa et al. 2015 and Siva Subramanian et al.  
111 2015). Unlike geotechnical problems like frost heave, the instabilities of soil slopes in Hokkaido are  
112 driven by the abrupt changes in soil water content distribution (Nakatsugawa et al. 2015). For the analysis  
113 of frozen soil behaviour, many complex thermo-hydro-mechanical models (THM) were developed  
114 (Selvadurai et al. 1999; Li et al. 2000, 2002, 2008; Nishimura et al. 2009; Ishikawa et al. 2016).  
115 Selvadurai et al. (1999) developed a novel computational approach to study the discontinuous frost heave  
116 within a frozen soil region. Li et al. (2000) introduced a coupled heat-moisture-mechanical model for  
117 frozen soil and demonstrated the applicability for a foundation problem. Later, Nishimura et al. (2009)

118 proposed a fully coupled THM model using finite element (FE) framework and developed a new  
119 critical-state elasto-plastic soil constitutive model to consider problems involving water-saturated frozen  
120 and unfrozen soils. Recently, Ishikawa et al. (2016) developed a coupled thermo-hydro-mechanical FE  
121 analysis method to analyse freeze-thaw of unsaturated soils. The robustness of the THM models discussed  
122 above is well proven for the prediction of soil behaviour influenced by frost-heave.

123 Generally, THM models consider the phase mechanics of ice, soil solid and pore water relationships in  
124 a sophisticated manner. For slope instability problems in seasonal cold regions, the effects of  
125 ground-atmosphere interactions i.e. freeze-thaw action and snowmelt water infiltration are more  
126 significant because of the direct impacts of these factors on soil water content distribution. Computational  
127 difficulties may arise if the ground-atmosphere interactions are modelled using a THM model. Chen et al.  
128 (2013) pointed out the difficulties in performing a fully coupled THM analysis for frozen soil slope  
129 stability problems. Simultaneous numerical solutions of coupled unsaturated seepage, thermal and stress  
130 relationships including the ground-atmosphere interactions are very hard to achieve and computational  
131 methods for this purpose are not common in geotechnical engineering practice. Performing a stress based  
132 numerical simulation for a duration of one year including the time-dependent changes in soil water  
133 content, changes in temperature and including the atmospheric effects are extremely cumbersome. In  
134 addition, the dominant factor that influences the unsaturated soil slope stability in seasonal cold regions is  
135 the change in soil water content due to freeze-thaw action and snowmelt water infiltration (Ishikawa et al.  
136 2015; Kawamura and Miura, 2013). Since the soil water content distribution inside the slope is the major  
137 factor determining the stability, it should be properly estimated for a precise stability assessment. For this  
138 purpose, a coupled thermo-hydro (TH) analysis would be appropriate, followed by a pseudo coupled  
139 mechanical analysis.

140 In view of these contexts, an approach to simulate the soil water content distribution subjected to  
141 freeze-thaw action and snowmelt water infiltration is recommended in this study. The approach is based

142 on two-dimensional plane strain numerical modelling considering non-isothermal seepage simulation  
143 followed by a slope stability assessment as explained in the flow chart shown in Fig. 3. There are three  
144 parts i.e. initial analysis, soil water content simulation and slope stability analysis. The first part is the  
145 initial analysis to configure the initial equilibrium of the soil slope in terms of soil water content  
146 distribution and temperature. The second part is the method used to estimate the water content  
147 distribution of the soil slope subjected to freeze-thaw action and snowmelt water infiltration.  
148 Non-isothermal seepage flow has been used to simulate the soil water flow in frozen and unfrozen soil.  
149 The interactions between the atmosphere and ground surface are modelled using a sophisticated  
150 numerical method which considers the climatic effects i.e. precipitation (rainfall and snowfall),  
151 evaporation effects and ground temperature estimations, using various governing equations as briefly  
152 explained in the following sections. The outcome of the soil water content simulation is the water content  
153 distribution inside the soil slope on a day to day basis. In the slope stability analysis, a traditional limit  
154 equilibrium technique based on the Morgenstern and Price (1965) method is used to calculate the factor  
155 of safety (FOS). The unsaturated shear strength of soil is also considered, as discussed below. The  
156 proposed numerical simulations were performed in a code GeoStudio using Vadose/W (Krahn, 2012a)  
157 and Slope/W (Krahn, 2012b) modules. As of author's knowledge, this study is the first attempt of this  
158 kind to investigate the effects of extreme climate conditions on non-frost susceptible soil slope stability in  
159 seasonal cold regions. The application of the recommended numerical approach is expected to contribute  
160 to the pre-design studies of soil slopes.

### 161 **3.1 Governing equations for non-isothermal seepage flow**

162 The governing equation for two-dimensional seepage flow is as given by Richards, (1931) and Childs and  
163 Collins-George, (1950),

$$164 \quad \frac{I}{\rho_w} \frac{\partial}{\partial x} \left( D_v \frac{\partial P_v}{\partial x} \right) + \frac{I}{\rho_w} \frac{\partial}{\partial y} \left( D_v \frac{\partial P_v}{\partial y} \right) + \frac{\partial}{\partial x} \left( k_x \frac{\partial \left( \frac{P}{\rho_w g} \right) + y}{\partial x} \right) + \frac{\partial}{\partial y} \left( k_y \frac{\partial \left( \frac{P}{\rho_w g} \right) + y}{\partial y} \right) + Q = m_w \frac{\partial P}{\partial t} \quad (1)$$

165 where,  $\rho_w$  = density of water (kg/m<sup>3</sup>),  $P$  = pressure (kPa),  $P_v$  = vapor pressure of soil moisture (kPa),  $k_x$  =  
166 hydraulic conductivity in the x direction (m/s),  $k_y$  = hydraulic conductivity in the y direction (m/s),  $Q$  =  
167 seepage boundary flux applied over a unit length (m/s),  $D_v$  = diffusion coefficient of water vapor through  
168 soil ((kg·m)/(kN·s)),  $y$  = elevation head (m),  $g$  = acceleration due to gravity (9.81 m/s<sup>2</sup>),  $m_w$  = slope of the  
169 soil water characteristic curve SWCC (1/kPa),  $\gamma_w$  = unit weight of water (kN/m<sup>3</sup>) and  $t$  = time (unit  
170 according to the numerical time step).

171 The governing equation for two-dimensional thermal flow is given by the concept based on Harlan and  
172 Nixon (1978).

$$173 \quad L_w \frac{\partial}{\partial x} \left( D_v \frac{\partial P_v}{\partial x} \right) + L_w \frac{\partial}{\partial y} \left( D_v \frac{\partial P_v}{\partial y} \right) + \frac{\partial}{\partial x} \left( k_{tx} \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left( k_{ty} \frac{\partial T}{\partial y} \right) + Q_t + \zeta V_x \frac{\partial T}{\partial x} + \zeta V_y \frac{\partial T}{\partial y} = \left( \zeta + L_w \frac{\partial \theta_u}{\partial T} \right) \frac{\partial T}{\partial t}$$

174 (2)

175 where,  $T$  = temperature (°C),  $\zeta$  = volumetric heat capacity of soil (kJ/m<sup>3</sup>-°C),  $k_{tx}$  = thermal conductivity in  
176 the x-direction (kJ/(s·m·°C)),  $k_{ty}$  = thermal conductivity in the y-direction (kJ/(s·m·°C)),  $V_x$  = the Darcy  
177 water velocity in x-direction (m/s),  $V_y$  = Darcy water velocity in y-direction (m/s),  $Q_t$  = thermal boundary  
178 flux applied over a unit length (kJ/(sec·m<sup>3</sup>)) and  $L_w$  = latent heat of water during phase change either  
179 liquid to gas (vaporisation) or liquid to solid (fusion as ice) (kJ/kg) and  $\theta_u$  = unfrozen volumetric water  
180 content determined by the slope of soil freezing characteristic curve (SFCC) (m<sup>3</sup>/m<sup>3</sup>).

181 The seepage flow Eq. 1 and thermal flow Eq. 2 are linked by the relationships given by Edlefsen and  
182 Anderson (1943) and Joshi (1993),

$$183 \quad P_v = P_{vs} \left( e^{\frac{-P_w}{\rho_w R T}} \right) = P_{vs} h_{rair} \quad (3)$$

184 where,  $P_{vs}$  = saturated vapor pressure of pure free water (kPa),  $\rho$  = density of water vapor or ice (kg/m<sup>3</sup>),  
 185  $w$  = molecular mass of water vapor (kg/kmol),  $R$  = universal gas constant (kJ/kmol·°C),  $T$  = temperature  
 186 (°C) and  $h_{air}$  = relative humidity of air (%).

### 187 **3.2 Modelling atmosphere-ground interactions**

188 To consider the freeze-thaw action, snowfall during winter and other climatic effects, a seepage flux  
 189 boundary used in conventional seepage analysis may not be sufficient since the surface flux resulting  
 190 from snowmelt and outgoing flux resulting from evaporation are needed to be properly considered in  
 191 order to estimate the ground surface temperature, surface infiltration and soil water content etc. During  
 192 the winter season, the precipitation occurs as snowfall in seasonal cold regions. The snow will accumulate  
 193 above the soil ground until the air temperature is below 0 °C. Once the temperature rises high enough to  
 194 melt the accumulated snow (> 0 °C), the snow will start to melt and will release water to the soil surface.  
 195 The snow water equivalent is the water that is stored in the snowpack. The snow water equivalent is  
 196 determined based on the following equation.

$$197 \quad SWE_t = SWE_{t-1} + SF - SM \quad (4)$$

198 where,  $SWE_t$  = snow water equivalent at the present numerical time step (mm/day),  $SWE_{t-1}$  = snow water  
 199 equivalent at the previous numerical time step (mm/day),  $SF$  = snowfall precipitation rate (mm/day),  $SM$   
 200 = snowmelt rate (mm/day).

201 The snowfall precipitation is calculated based on the amount of precipitation and air temperature  
 202 according to the following relationships.

$$203 \quad SF = Q_p \times P \quad (5)$$

204 where,  $Q_p$  = thermal factor,  $P$  = precipitation (mm/day). The thermal factor  $Q_p$  varies according to the  
 205 average daily air temperature as,

$$206 \quad Q_p = 0 \text{ (if } T_a > T_f \text{) and } Q_p = 1 \text{ (if } T_a < T_f \text{)} \quad (6)$$

207 where,  $T_a$  = average daily air temperature ( $^{\circ}\text{C}$ ) and  $T_f$  = freezing point temperature ( $0^{\circ}\text{C}$ ). The snowmelt  
 208 rate ( $SM$ ) is determined based on an energy balance approach used by Bras (1990), Liang et al. (1994),  
 209 Flerchinger and Saxton (1989). For the estimation of snow precipitation, precipitation data (including  
 210 rainfall and snowfall) and air temperature data are required.

211 To calculate the snow depth and density of snow the following relationships are used.

$$212 \quad D_{sn} = \frac{\rho_w}{\rho_{sn}} SWE_{t-1}; \rho_{sn} = \frac{SWE_{t-1}}{D_{sn}} + \beta(0.55 - \rho_{sn(t-1)}) \text{ and } \beta = \begin{cases} 0.002 & \text{if } T_a < 1.0 \\ 0.002 \times T_a & \text{if } T_a \geq 1.0 \end{cases} \quad (7)$$

213 where,  $D_{sn}$  = snow depth (mm),  $\rho_{sn}$  = density of snow,  $\rho_{sn(t-1)}$  = density of snow on the previous time step  
 214 ( $\text{kg}/\text{m}^3$ ),  $SWE_{t-1}$  = snow water equivalent on the previous time step (mm),  $\beta$  = snow consolidation  
 215 parameter and  $T_a$  = average daily air temperature ( $^{\circ}\text{C}$ ).

216 The ground surface temperature when there is snow cover in the ground is estimated using the following  
 217 relationship given by Bras (1990),

$$218 \quad T_g = T_{sn} - \frac{D_{sn}}{\lambda_{sn}} q_{Tg} \quad (8)$$

219 where,  $T_g$  = ground surface temperature ( $^{\circ}\text{C}$ ),  $T_{sn}$  = temperature of snow surface considered equal to the  
 220 air temperature ( $^{\circ}\text{C}$ ),  $D_{sn}$  = snow depth (mm),  $\lambda_{sn}$  = thermal conductivity of snow ( $\text{kJ}/(\text{s}\cdot\text{m}\cdot^{\circ}\text{C})$ ) and  $q_{Tg}$  =  
 221 energy flux at the ground surface ( $\text{kJ}/(\text{sec}\cdot\text{m}^2)$ ).

222 The maximum rate of evaporation from a pure water surface/saturated soil pore under given climatic  
 223 conditions is defined as the potential rate of evaporation (PE). If the surface soil becomes unsaturated, the  
 224 amount of water inside the soil pore will become limited and the rate of evaporation begins to decline.  
 225 This phenomenon is defined as the actual rate of evaporation (AE). Actual evaporation is the actual rate  
 226 of evaporative flux from a partially saturated soil pore. The actual evaporation from an unsaturated soil is  
 227 modelled adopting the approach given by Wilson et al. (1994),

228 
$$AE = \frac{\Gamma Q_n + \eta E_a}{\Gamma + \frac{\eta}{h_s}} \quad (9)$$

229 where,  $AE$  = actual vertical evaporative flux (mm/day),  $\Gamma$  = slope of the saturation vapor pressure versus  
 230 temperature curve at the mean temperature of the air (kPa/°C),  $Q_n$  = net radiant energy flux available at  
 231 the water surface (mm/day),  $\eta$  = psychrometric constant,  $E_a$  = flux associated with vapor pressure mixing  
 232 (mm/day) and  $h_s$  = relative humidity at the soil surface (%). For the estimation of actual evaporation from  
 233 unsaturated soil, relative humidity of air and soil, wind speed and net radiation are required. To model the  
 234 soil surface evaporation reasonably, Wilson et al. (1994) equation is appropriate.

235 The infiltration, runoff and actual evaporation are considered based on the following relationship.

236 
$$I = P - AE - R \quad (10)$$

237 where,  $I$  = infiltration (mm/day),  $P$  = precipitation (mm/day),  $AE$  = actual evaporation (mm/day) and  $R$  =  
 238 runoff (mm/day). The runoff  $R$  is defined as the amount of water that cannot infiltrate into the soil ground.  
 239 The runoff is determined by the amount of precipitation, actual evaporation and infiltration. If the  
 240 precipitation is less than the anticipated actual evaporation, then the applied surface flux boundary  
 241 condition will be equal to the precipitation value minus the actual evaporation and a negative flux will be  
 242 applied to the node. If the precipitation minus actual evaporation is a positive value, then a positive  
 243 infiltrative surface flux will be applied as a boundary condition. The amount of total surface water flux  
 244 near the ground surface is determined by the length of the sloping ground (length of the surface nodes  
 245 along the slope surface). The slope angle will change the length of the slope surface which in turn affects  
 246 the total surface flux. The total flux near the ground surface can be expressed simply using the following  
 247 relationship,

248 
$$Q_{surface} = P \times \sum L_n \quad (11)$$

249 where,  $Q_{surface}$  = amount of total surface flux ( $m^3/day$ ),  $P$  = precipitation ( $mm/day$ ) and  $\sum L_n$  = summation  
 250 of length between nodes along the entire slope surface (m). The length of the slope surface is indirectly  
 251 proportional to the slope angle as given by,

$$252 \quad \sum L_n \propto \frac{1}{S_{angle}} \quad (12)$$

253 where,  $\sum L_n$  = summation of length between nodes along the entire slope surface (m) and  $S_{angle}$  = slope  
 254 angle ( $^\circ$ ).

255 The amount of surface flux that is applied at the boundary strongly depends on the slope angle and the  
 256 length of sloping ground. The assumption, by neglecting the slope angle effect in runoff calculations, is  
 257 not valid in terms of surface water flow simulations and runoff through a mountain valley etc. Surface  
 258 water flow and runoff caused by flooding cannot be simulated using these assumptions. The adopted  
 259 numerical simulations do not track the route of surface water and flow speed etc. The infiltration  
 260 boundary condition for the model is defined by Gitirana (2005). If the surface soil is saturated, the pore  
 261 spaces will get filled with water and no more water can get into the soil element. Conceptually, this effect  
 262 is modelled considering the rate of applied surface flux ( $q$ ) and saturated hydraulic conductivity of the  
 263 soil ( $k_s$ ). If the soil surface is a flat ground, there is a possibility of surface ponding. If conditions for  
 264 infiltration met later, the ponded water from the flat surface will infiltrate into the soil ground. To  
 265 incorporate these conditions, the method given by Gitirana (2005) is useful. By this way, the effect of  
 266 slope angle on surface infiltration is considered in the analysis.

### 267 **3.3 Shear strength of soil under unsaturated conditions**

268 The shear strength of an unsaturated is expressed based on Bishop's effective stress principle by Vanapalli  
 269 et al. (1996) as given by,

$$270 \quad \tau = c' + \left( \sigma_n - u_a \right) \tan \phi' + \left( u_a - u_w \right) [\chi \tan \phi'] \quad (13)$$

271 where,  $\tau$  = shear strength of soil (kPa),  $\sigma_n$  = net total stress (kPa),  $u_a$  = pore air pressure (kPa),  $u_w$  = pore

272 water pressure (kPa),  $c'$  = effective cohesion (kPa),  $\phi'$  = effective angle of internal friction ( $^\circ$ ) and  $\chi$  =  
 273 parameter related to the degree of saturation. According to Vanapalli et al. (1996) the magnitude of  
 274 parameter  $\chi$  can be expressed in terms of volumetric water content as,

$$275 \quad \chi = \frac{\theta_w - \theta_r}{\theta_s - \theta_r} \quad (14)$$

276 where,  $\theta_w$  = volumetric water content ( $\text{m}^3/\text{m}^3$ ),  $\theta_s$  = saturated volumetric water content ( $\text{m}^3/\text{m}^3$ ) and  $\theta_r$  =  
 277 residual volumetric water content ( $\text{m}^3/\text{m}^3$ ).

### 278 **3.4 Factor of safety estimation for slope stability analysis**

279 Slope stability has been analysed using limit equilibrium technique based on the method given by  
 280 Morgenstern and Price (1965). The Morgenstern and Price method is a widely used slope stability method  
 281 in general geotechnical engineering practice. The factor of safety equations with respect to moment  
 282 equilibrium ( $F_m$ ) and force equilibrium ( $F_f$ ) considering the unsaturated shear strength of soil are given in  
 283 Eq. 15 and Eq. 16 respectively. The unsaturated soil shear strength in the factor of safety is considered  
 284 based on the nonlinear relationship given by Vanapalli et al. (1996) as explained in Eq. 13 and Eq. 14.

$$285 \quad F_m = \frac{\sum [c'lR + \{N - u_w l \chi - u_a l (1 - \chi)\} R \tan \phi']}{\sum Wx - \sum Nf \pm \sum Dd \pm \sum Aa} \quad (15)$$

$$286 \quad F_f = \frac{\sum [c'l \cos \alpha + \{N - u_w l \chi - u_a l (1 - \chi)\} \tan \phi' \cos \alpha]}{\sum N \sin \alpha - \sum D \cos \omega \pm \sum A} \quad (16)$$

287 where,  $W$  = the total weight of a slice of width  $b$  and height  $h$  ( $\text{kN}/\text{m}^2$ ),  $N$  = the total normal force on the  
 288 base of the slice (kN),  $D$  = an external point load (kN).  $R$  = the radius of a circular slip surface (m),  $x$  =  
 289 the horizontal distance from the centerline of each slice to the center of rotation or to the center of  
 290 moments (m),  $d$  = the perpendicular distance from a point load to the center of rotation or to the center of  
 291 moments (m),  $f$  = the perpendicular offset of the normal force from the center of rotation or from the  
 292 center of moments (m),  $a$  = the perpendicular distance from the resultant external water force to the center

293 of rotation or to the center of moments (m),  $A$  = the resultant external water forces (kN),  $\omega$  = the angle of  
294 the point load from the horizontal ( $^{\circ}$ ),  $\alpha$  = the angle between the tangent to the center of the base of each  
295 slice and the horizontal ( $^{\circ}$ ) and  $l$  = the base length of each slice (m).

#### 296 **4. Study of embankment slope failure using the recommended approach**

297 The case example of failure on embankment slope constructed using Shikotsu Komaoka volcanic soil is  
298 analysed using the recommended approach.

#### 299 **4.1 Numerical model, soil properties and analytical conditions**

300 The two-dimensional numerical finite element mesh with the slope geometry adopted for the embankment  
301 slope is given in Fig. 4. Shikotsu Komaoka volcanic soil has been used as the slope material in the  
302 embankment slope. The soil parameters used for the numerical simulation of embankment slope are  
303 summarised in Table 1. The parameters i.e. dry density ( $\rho_d$ ), hydraulic conductivity of saturated soil ( $k_s$ ),  
304 effective cohesion ( $c'$ ) and effective angle of internal friction ( $\phi'$ ) have been obtained from laboratory  
305 element tests (Matsumura et al. 2015). The parameters for which no laboratory measurements are  
306 available, i.e. thermal conductivity ( $\lambda$ ), volumetric heat capacity ( $\zeta$ ) and volumetric water content of soil  
307 at  $0^{\circ}\text{C}$  ( $\theta_{w,0}$ ), have been estimated using equations given by Kersten (1949), Jame (1977) and Black and  
308 Tice (1989), respectively. The soil-water characteristic curve (SWCC) was obtained from laboratory  
309 element tests by Matsumura et al. (2014). The coefficient of permeability under unsaturated conditions is  
310 estimated using the SWCC (van Genuchten, 1980). The initial distribution of the volumetric water  
311 content and temperature of the slope has been configured based on the soil water content and temperature  
312 data recorded during day 1 (09-11-2012). To derive an equilibrium of volumetric water content  
313 distribution corresponding to day 1 (09-11-2012), the average volumetric water content recorded at  
314 locations SML0, SML1, SML2 and SML3 (as shown in Fig. 1 and Fig. 4) are specified exactly at the  
315 corresponding locations in the numerical model. For the temperature distribution on the initial day

316 (09-11-2012), the measured temperature has been specified at the depths of 0 m to 1 m. For the climatic  
317 boundary conditions used in the transient non-isothermal seepage model, climate data i.e. maximum and  
318 minimum air temperature, average daily rainfall, maximum and minimum relative humidity, average daily  
319 wind speed and average daily net radiation are required. During the monitoring of the volcanic soil  
320 embankment slope, the temperature and rainfall were monitored. Additional required climatic data were  
321 obtained from the AMeDAS (Automated Meteorological Data Acquisition System) data provided by the  
322 Japanese Meteorological Agency (JMA) and as given in Fig. 5.

## 323 **4.2 Results and discussions**

324 From the numerical simulations, the magnitude of the various influencing factors i.e. precipitation,  
325 accumulated snow depth, snowmelt water, ground temperature, net surface infiltration etc. was analysed  
326 and finally the factor of safety of the slope was estimated. The numerical results are compared with the  
327 measured data.

328 A comparison of volumetric water content has been made from the numerical results and monitoring data  
329 as given in Fig. 6(a) showing the comparison between numerical estimation and measurement of the  
330 average volumetric water content of the soil water content sensors at SML0, SML1, SML2 and SML3  
331 installed at depths 0.2 m to 1.5 m. The ground temperature estimated from the numerical simulation is  
332 compared with the measured data as given in Fig. 6(b). The numerically estimated snow depth and  
333 measured snow depth is compared and given in Fig. 6(c). A close similarity between the numerical  
334 estimation and measured data has been found. Slope failure will occur if the soil is saturated near the  
335 slope surface and the failure may trigger along the slip surface. In such circumstances, the reason for  
336 failure could be judged by estimating the average volumetric water content. The average volumetric water  
337 content is compared here in order to visualise the saturation of the slope. It may be seen that the average  
338 volumetric water content at locations SML1, SML2 and SML3 reaches to a range of  $0.52 \text{ m}^3/\text{m}^3$  to  $0.56$

339  $\text{m}^3/\text{m}^3$ . The saturated volumetric water content of the soil is  $0.63 \text{ m}^3/\text{m}^3$  as given in Table 1. From this  
340 observation, it could be said that during the day of the slope failure the degree of saturation ( $S_r$ ) was up to  
341 85 % on the slip surface. The numerical simulation results match well with the trend of the measured data.  
342 The maximum difference found between the numerically estimated volumetric water content and  
343 measured volumetric water content is 0.02. The stability of the soil slope starting from the day of slope  
344 construction until the failure is expressed as a factor of safety and has been plotted in Fig. 6(d). The factor  
345 of safety during the day of slope failure is 0.954. The slip surface estimated using the limit equilibrium  
346 method is compared with the field slope failure data, as shown in Fig. 7 (a) and (b) respectively.  
347 In field conditions, the failure surface was about 3 m in height and 0.6 m to 0.8 m in depth. From the  
348 numerical simulation, the failure surface is estimated as 4.5 m in height and 0.6 m to 0.9 m in depth. The  
349 numerical simulation demonstrated close similarity in estimating the influencing parameters i.e. net  
350 surface infiltration, snow depth, snowmelt water and ground temperature etc. and could predict the soil  
351 water content distribution of the slope appropriately. The numerically estimated data closely matches with  
352 the measured data almost in all circumstances. Through these observations, it could be claimed that the  
353 adopted approach is reliable to predict the soil slope stability in seasonal cold regions.

## 354 **5. Study of the highway slope failure using the recommended approach**

355 The slope failure that occurred along the national highway route 230 (highway slope failure), is analysed  
356 using the recommended approach. The two-dimensional numerical model, boundary conditions and  
357 material properties were considered to be similar to the embankment slope failure model and are  
358 discussed in the following section.

### 359 **5.1 Numerical model, soil properties and analytical conditions**

360 The two-dimensional numerical model for the highway slope failure is designed using the geological  
361 cross-sectional data. The two-dimensional numerical model with the soil/rock stratigraphy and surveyed

362 ground water table are given in Fig. 8. The slope stratigraphy has three soil/rock types, namely  
363 embankment filling, talus slope materials and the bedrock (Andesite). The surveyed ground water table is  
364 at an average depth of 8 m from the ground surface. The soil material properties used for the numerical  
365 simulation of the highway slope model are given in Table 2. The parameters i.e. dry density ( $\rho_d$ ),  
366 hydraulic conductivity of saturated soil ( $k_s$ ), and undrained shear strength ( $q_u$ ) have been obtained from  
367 laboratory measurements (Hokkaido Regional Development Bureau, 2013). The parameters for which no  
368 laboratory measurements are available, i.e. thermal conductivity ( $\lambda$ ), volumetric heat capacity ( $\zeta$ ),  
369 volumetric water content of soil at 0°C ( $\theta_{wp}$ ), effective cohesion ( $c'$ ) and effective angle of internal friction  
370 ( $\phi'$ ) have been estimated using methods given by Kersten (1949), Jame (1977), Black and Tice (1989) and  
371 Hoek and Brown (1977), respectively. The SWCC of the embankment filling material and Talus  
372 sediments were estimated from the grain size distribution curve based on the method given by Fredlund et  
373 al. (2002). For the embankment filling and talus material, the unsaturated shear strength data is not  
374 available so that the available undrained shear strength is considered for the embankment filling and  
375 saturated shear strength is estimated for the talus slope material. The bedrock is modelled as a low  
376 permeability material.

377 For the long-term slope stability analysis, drained shear strength parameters are needed. The effective  
378 cohesion ( $c'$ ) and effective angle of internal friction ( $\phi'$ ) for the embankment filling material were derived  
379 using rigorous back calculation methods given by Duncan and Stark (1992), Okui et al. (1997) and Zhang  
380 et al. (2013). Several values of cohesion and angle of internal friction are given initially. By setting the  
381 FOS = 1 and using the reference ground water table derived from the non-isothermal seepage simulation  
382 and using the pre-known dimensions of the slope failure, several iterations of calculations have been  
383 made from which different cohesion and angle of internal friction values are obtained. In consideration to  
384 the height of the failure surface, the effective cohesion and effective angle of internal friction for the  
385 embankment soil were derived as shown in Fig. 9 (a) and (b). Back-calculation of shear strength

386 parameters may have some limitations concerning with the precision of the estimated shear strength  
387 (Tang et al. 1999; Duncan and Wright, 2005; Deschamps and Yankey, 2006). Since the major objective of  
388 this study is to examine the influencing parameters of slope failure, the problems with the precision of the  
389 estimated shear strength may be negligible and these values can be used as a basis for a parametric study.  
390 The shear strength of the Talus materials was intentionally kept larger so that the steep portions of the  
391 mountain slope located far away from the embankment does not influence the factor of safety calculations.  
392 Prior to the transient non-isothermal coupled seepage analysis, an initial equilibrium condition in terms of  
393 pore water pressure and the ground temperature is necessary. The ground water table has been measured  
394 from the geological survey performed after the slope failure. The ground water table line from the  
395 geological survey is kept as a reference and an average of 10-year climate data recorded between years  
396 2002 to 2012 obtained from a meteorological telemetry at Mui Ne, Hokkaido, Japan maintained by the  
397 Ministry of Land, Infrastructure, Transport and Tourism, Hokkaido Regional Development Bureau  
398 (MLIT) has been used and to derive the initial equilibrium. The climate data used for the numerical  
399 simulation is also obtained from the meteorological telemetry at Mui Ne which is closest to the disaster  
400 site. The climate data is given in Fig. 10. The air temperature on the day 1 (01-04-2012) is just close to  
401 0°C and it increases during the thawing period. The maximum rainfall of 92 mm/day occurred during the  
402 day of slope failure 07-04-2013.

## 403 **5.2 Results and discussions**

404 To study the changes in pore water pressure and volumetric water content of the embankment, histories  
405 were given at particular locations 1 to 6 in the numerical model, as shown in Fig. 8. The variation in  
406 volumetric water content and pore water pressure are given in Fig. 11 (a) and Fig. 11 (b) respectively.  
407 From Fig. 11, it could be seen that there is a higher fluctuation of soil water at locations 1 and 2. During  
408 the day of slope failure, the volumetric water content and pore water pressure at all locations of the

409 embankment reaches  $0.47 \text{ m}^3/\text{m}^3$  and  $0 \text{ kPa}$  respectively, as shown in Fig. 11 (a) and (b). The saturated  
410 volumetric water content of the slope is  $0.47$ .

411 The ground temperature and accumulated snow depth measured at locations 1 to 6 are given in Fig. 11(c)  
412 and (d). The ground temperature rises above  $0^\circ$  after March 12, 2013. The maximum accumulated snow  
413 depth is  $3708 \text{ mm}$  at location 1 ( $x=-7$  and  $y=490$ ). A comparison of snowmelt with the measured data  
414 could not be obtained in this case because the snow depth varies with location. The accumulated snow  
415 started to melt from March 12, 2013. During this period, the stability may get reduced due to the  
416 snowmelt water. The factor of safety estimated from the simulation is plotted in Fig. 12(a).

417 During initial days from 01-04-2012, the stability of the slope reduced rapidly due to continuous  
418 precipitation until early May 2012. During the month of June 2012, there is not much precipitation  
419 observed and hence an increasing trend in safety factor is estimated. Further, the factor of safety reduces  
420 whenever there is continuous precipitation. During the month of October to November 2012, the stability  
421 reduces rapidly due to continuous precipitation. A similar trend continues until December 2012. The  
422 ground temperature reduces below  $0^\circ \text{ C}$  during January 2013 and the soil surface remains frozen until  
423 March 12, 2013. During this period, an increase in the factor of safety is observed and later the factor of  
424 safety value keeps nearly constant. The reduction in the factor of safety commences once the ground  
425 temperature increases above  $0^\circ \text{ C}$ , exactly on March 12, 2013. The reduction continues markedly, and on  
426 the day, April 07, 2013, the factor of safety reaches a value  $0.992$  which denotes the slope failure. The  
427 surveyed failure surface and the numerically estimated failure surface with the factor of safety on April 07,  
428 2013 is given in Fig. 12(b). The height of the numerically estimated slip surface is  $19$  to  $20 \text{ m}$  and  $30$  to  
429  $35 \text{ m}$  in length. From the geological survey, the length of the failure is around  $40 \text{ m}$  with a height of  $20 \text{ m}$ .

430 The minimum safety factor  $0.992$  has been found for the critical slip surface passes through the  
431 embankment portion.

432 **6. Parametric studies**

433 The effects of the factors i.e. freeze-thaw action, snowmelt water infiltration and the weight of the  
434 accumulated snow need to be known for the precise assessment of the long-term stability of soil slopes i.e.  
435 embankment and cut slopes along the highways. Based on this purpose, in this study, a series of  
436 parametric studies using the recommended numerical simulation method has been performed using the  
437 embankment slope model and highway slope model with the analytical conditions as given in Table 3.

438 **6.1 Effect of increased magnitudes of rainfall on slope stability**

439 The amount of rainfall has been increased twice and thrice in order to see the effect on slope stability  
440 using the embankment slope model. The twice and thrice considered rainfall magnitude significantly  
441 reduces the stability as given in Fig. 13 (a).

442 **6.2 Effect of increased magnitudes of snowfall on soil slope stability**

443 To clearly visualise the effect of snowmelt on slope failure, the snowfall precipitation has been configured  
444 in different magnitudes, like twice and thrice for the embankment slope model. The stability of the slope  
445 abruptly reduces during March-April-May months due to snowmelt and surface infiltration. It could be  
446 seen that as the depth of accumulated snow increases, the duration took to melt the snow also increases  
447 and finally it results in a reduction in safety factor as shown in Fig. 13 (b). The failure-inducing factor is  
448 not only the rainfall or not the snowmelt water alone. The rainfall along with snowmelt water induces  
449 such a reduction in slope stability. Through the parametric studies, it is found that the accumulated snow  
450 depth increase may result in an excess amount of snowmelt water which may eventually reduce the soil  
451 slope stability.

### 452 **6.3 Effect of freeze-thaw action on soil slope stability**

453 Two different numerical simulations, one considering the freeze-thaw process and the second without  
454 considering the freeze-thaw process were performed using embankment slope model and highway slope  
455 model. When there is no freeze-thaw action considered, the effects of soil water freezing, the effect of the  
456 latent heat phase change and the temperature flow are neglected. The calculation of all other variables i.e.  
457 precipitation (rainfall and snowfall), air temperature, relative humidity etc. are kept same for both the  
458 analysis and the shear strength of frozen soil is not considered for this parametric study. For the  
459 simulation considering freeze-thaw action, the soil water content distribution is estimated using  
460 non-isothermal seepage flow and for the simulation without freeze-thaw action, the soil water content  
461 distribution is estimated using isothermal seepage flow. These analyses were performed for both the  
462 embankment slope model and highway slope model. The factor of safety for both the simulations was  
463 analysed and compared as given in Fig. 14(a) and (b). A stability difference could be seen between  
464 analysis considering freeze-thaw action and analysis without freeze-thaw action during the period when  
465 the ground surface temperature is below zero for both the cases. In the case example of embankment  
466 slope, the freeze-thaw action has very small impact on soil water content and factor of safety. Whereas,  
467 for the highway slope, a major difference in the factor of safety between analysis considering freeze-thaw  
468 action and analysis without considering freeze-thaw action is observed. On the day of slope failure, the  
469 factor of safety estimated by the analysis considering freeze-thaw action is 0.992 and the factor of safety  
470 estimated by the analysis without considering freeze-thaw action is 1.003. From this observation, it could  
471 be said that the freeze-thaw action has a considerable effect on soil water content fluctuation which in  
472 turn affects the slope stability and for the proper assessment of the stability of soil slopes in seasonal cold  
473 regions, the freeze-thaw action must be considered in estimating the soil water content distribution.

474 **6.4 Effect of snowfall/snowmelt water infiltration on soil slope stability**

475 The snowfall accumulated above the slope during the winter season will start to melt once the air  
476 temperature increases above the phase change temperature ( $0^{\circ}\text{C}$ ). During this snow melting period, the  
477 snowmelt water will infiltrate into the soil or runoff above the slope based on the ground surface  
478 temperature. From Fig. 14(c) and (d), it can be seen that the factor of safety does not get reduced during  
479 the months of March, April and May for the analysis without considering snowmelt water. The reason is  
480 due to the lack of snowmelt water. Whereas when snowfall is considered, the factor of safety abruptly  
481 reduces during the snow melting season. The contribution of snowmelt water in the net surface infiltration  
482 is high during the thawing season which abruptly reduces the slope stability. One more important  
483 observation made from the embankment slope model is that when there is no snow on the ground the  
484 safety factor starts deviating from the early February 2013 itself. The reason behind this phenomenon is,  
485 if there is no snow accumulated on the soil ground, the soil temperature may be much lower than it would  
486 be under the accumulated snow. There would not be a heat flux variation in this case. Due to this fact, the  
487 ground will freeze up to a certain depth more than it will freeze under the accumulated snow. If the  
488 ground is frozen over greater depth, it will become impermeable and there will not be any surface  
489 infiltration. The factor of safety will be high during the winter period if there is no snow accumulated on  
490 the soil ground. Due to the absence of snowmelt water, during snowmelt period, there will not be any  
491 reduction in stability. Similar behaviour has been observed from the highway slope model as well. It is  
492 very interesting to note that for the highway slope if the snowmelt water infiltration is ignored, the factor  
493 of safety and stability of the slope is considerably higher throughout the year from 01-04-2012 to  
494 07-04-2013. On the day of slope failure, the factor of safety of slope when the snowmelt water is ignored  
495 is 1.224 which emphasises considerable stability. In the case of simulation, in which the snowmelt water  
496 is included in the calculation of soil water content, the factor of safety on the day of slope failure is 0.992  
497 which clearly denotes the slope failure. Based on this observation, it could be said that for the case of

498 highway slope failure, the 92 mm cumulative rainfall alone would not have induced the slope failure. The  
499 water originating from the snowmelt that infiltrated into the soil ground together with the cumulative  
500 rainfall should have induced the disaster.

501 One more interesting observation found for the highway slope model is that the difference in the  
502 factor of safety during the month of December 2012 between analysis considering snowfall and analysis  
503 neglecting snowfall, as shown in Fig. 14(d). The air temperature fluctuates below and above 0°C during  
504 the starting of the freezing season, November and December 2012. In this situation, there is a possibility  
505 of rainfall and snowfall together. If there is accumulated snow above the soil ground originating from the  
506 previous day snowfall, on the next day if the air temperature is above 0°C and there will be precipitation  
507 in terms of rainfall. The factor of safety reduces to 1.137 on December 25, 2012, when the effect of  
508 snowmelt water is considered in the analysis. Whereas, for the analysis without the effect of snowmelt  
509 water, the factor of safety is 1.507 on December 25, 2012. Based on this observation it could be said that  
510 the snowfall that occurs during the initial stages of freezing (November and December months) will also  
511 influence the slope stability considerably.

512 From these parametric studies, it is very clear that snowmelt water infiltration seriously affects the soil  
513 slope stability and it should be considered in long-term slope stability analysis of embankment structures  
514 and cut slopes along the highways in seasonal cold regions.

## 515 **6.5 Effect of weight of snow on soil slope stability**

516 The snow accumulated on top of the slope surface has its own weight. In such cases, it may induce a  
517 reduction in slope stability. To analyse this effect, the weight of the snow is considered as a surcharge  
518 load. The snow load is estimated using the snow density ( $\rho_{sn}$ ) and accumulated snow depth. As the  
519 accumulated snow depth increases, the snow load starts to build up. The maximum snow load calculated  
520 for 1689 mm snow depth is 7 kN/m<sup>2</sup>. To see whether this snow load will affect the slope stability or not,

521 the load is considered as a surcharge pressure in the slope stability analysis. Since it is not possible to  
522 consider the increasing snow load day by day in a safety factor calculation, a 25 days averaging has been  
523 adopted, as given in Fig. 15(a). The safety factor seems to be affected much by the accumulated snow  
524 weight, as given in Fig. 15(b).

525 In Fig. 15, the factor of safety obtained with and without snow load both considers the effect of snowmelt  
526 water. It seems the weight of snow combined with the snowmelt water may affect the slope stability to a  
527 considerable amount during the freezing and snow melting seasons, respectively. The maximum  
528 difference in safety factor is observed during the month of March 2013 when the snow load reaches its  
529 maximum. Once the snow starts melting, the load of the snow will decrease and diminish when all the  
530 accumulated snow is converted into water.

## 531 **6.6 Effect of slope angle on soil slope stability**

532 Kawamura and Miura (2013) performed experiments with small scale model soil slopes made up of  
533 volcanic soil material under different slope angles considering a slope angle range from  $45^\circ$  to  $65^\circ$ . For  
534 the design of embankment slopes and cut slopes along the express highways in Japan, the NEXCO  
535 (Central Nippon Expressway Company Limited) has set some guidelines (Yasuda and Fujioka, 2012). For  
536 the design of embankment slopes in express highways, the standard slope would be 1:1.8 that is  $29^\circ$  and  
537 for highways other than the national expressways in Japan, a standard slope angle ratio of 1:1.5 to 1:1.8 $^\circ$   
538 is adopted depending on the soil/rock material type underlying the embankment. Further, for natural cut  
539 slopes along the highways, the slope may range up to a slope angle of  $60^\circ$  if the base of the soil is rock. In  
540 view of all these considerations, a study to evaluate the effect of slope angle is performed by making  
541 numerical slope models with different slope angles. The slope angles are considered to be  $30^\circ$ ,  $35^\circ$ ,  $40^\circ$ ,  
542  $45^\circ$ ,  $50^\circ$ ,  $55^\circ$  and  $60^\circ$ , though the physical embankment model considered in this study was built at an  
543 angle of  $45^\circ$ . In order to study the effect of slope angle,  $30^\circ$ ,  $35^\circ$ ,  $40^\circ$ ,  $45^\circ$ ,  $50^\circ$ ,  $55^\circ$  and  $60^\circ$  numerical

544 slope models are made and simulated with the recorded climatic measurements. It may be seen from Fig.  
545 15(c) that the safety factor of the slope varies with different slope angles. During the slope failure day,  
546 October 17, 2013, the safety factor for slope angles 45° to 60° are lesser than slope angles 30°, 35° and 40°.  
547 For shallow slopes, 30°, 35° and 40°, the factor of safety is more than 1. Interestingly, the reduction in  
548 safety factor during the snow melting season is more for the shallow slopes 30°, 35°, 40° than 45°, 50°,  
549 55° and 60° slopes. The variation in the factor of safety between different slope angles is governed by the  
550 infiltration and runoff which will vary significantly according to the slope angle.

### 551 **6.7 Effect of shear strength of frozen soil**

552 Chen et al. (2013) analysed the effect of shear strength of frozen soil on soil slope stability conceptually.  
553 When the soil is frozen, it will gain additional shear strength depending on the ice content. In the case  
554 study of volcanic soil embankment, during the freezing months, a maximum freezing depth of 0.2 m is  
555 observed from the embankment monitoring (Matsumura, 2014). The region where the soil water is frozen  
556 would have gained additional shear strength which could result in an increase in stability. In any case, in  
557 this study so far this phenomenon is not considered due to the following reasons,

- 558 1. The additional shear strength will only increase the stability which will eventually increase the  
559 factor of safety.
- 560 2. Once the frozen water content of the soil melts, the additional shear strength will diminish.
- 561 3. Since the freezing depth in the present study is only 0.2 m (20 cm) it would not have strongly  
562 influenced the overall stability of 5 m tall slope.

563 In order to check the generality of the above-mentioned statements, a slope stability analysis considering  
564 additional shear strength in terms of effective cohesion and effective angle of internal friction is  
565 performed. Due to non-availability of frozen shear strength data, basic empirical equations as referred  
566 from the literature is adopted to calculate the frozen soil shear strength parameters. The frozen soil shear

567 strength is estimated as given by Arenson and Springman (2005) and Chen et al. (2013), assuming that  
 568 the effective angle of internal friction  $\phi'$  is independent of temperature and strain rate, and the effective  
 569 cohesion  $c'$  is independent of strain rate.

$$570 \quad \phi_f = \phi' - \phi' (\theta_i)^{2.6} \quad (17)$$

571  $\phi_f$  = angle of internal friction of frozen soil ( $^\circ$ ),  $\phi'$  = effective angle of internal friction ( $^\circ$ ),  $\theta_i$  = volumetric  
 572 ice content ( $\text{m}^3/\text{m}^3$ ). For the estimation of frozen shear strength, two variables viz. unfrozen water content  
 573 and unfrozen ice content of the soil are needed. The unfrozen water content of the soil is estimated using  
 574 the relationships given by Black and Tice, (1989).

575 A simple empirical estimation for cohesion of frozen soils is given by Chen et al. (2013),

$$576 \quad C = \begin{cases} c_f(T, \theta_{uw}) = (\beta_1 T + \chi_1)(\beta_2 \theta_{uw} + \chi_2), & T_g < 0^\circ\text{C} \\ c', & T_g \geq 0^\circ\text{C} \end{cases} \quad (18)$$

577  $C$  = cohesion (kPa),  $c'$  = effective cohesion at unfrozen state (kPa),  $C_f$  = cohesion at frozen state (kPa),  $T$   
 578 = Temperature ( $^\circ\text{C}$ ),  $\theta_{uw}$  = unfrozen volumetric water content ( $\text{m}^3/\text{m}^3$ ),  $\beta_1 = 0.074$ ,  $\beta_2 = -5.14$ ,  $\chi_1 = -0.015$ ,  
 579  $\chi_2 = -1.23$  fitting parameters for the cohesion function for coarse grained soils.

580 Since the motivation of considering the estimation equation in this study is to only see the effect of frozen  
 581 shear strength on slope stability, the maximum cohesion value and minimum angle of internal friction are  
 582 specified to the frozen soil zone up to 0.2 m depth and a slope stability analysis has been performed.

583 The increment in safety factor due to frozen shear strength seems to be very minimal and it has very little  
 584 impact on the safety factor for the analysis performed, as shown in Fig. 15(d). There could be two  
 585 possible reasons behind this behaviour. The increased frozen shear strength is too low (only 0.67 kPa) and  
 586 the freezing depth is very small (0.2 m) comparing with the overall slope geometry. However, if the  
 587 frozen soil occupies an adequate amount of the slope slip surface, the frozen shear strength should be  
 588 properly considered for the estimation of slope stability.

589 **7. Conclusions**

590 A slope stability assessment approach applicable to analyse the long-term stability of soil slopes i.e.  
591 embankment slopes, and natural cut slopes along highways in seasonal cold regions is recommended in  
592 this study. The validity of the proposed approach has been studied by applying the method for two soil  
593 slope failure case examples that occurred in a seasonal cold region in Hokkaido, Japan. Based on the  
594 detailed studies performed, it has been found that the adopted slope stability assessment approach can be  
595 used for the design of slope structures along highways through performing pre-assessment of stability  
596 against anticipated climatic influences. Through the various parametric studies performed, the following  
597 conclusions can be drawn.

- 598 — The freeze-thaw action has a considerable effect on soil water content distribution which in  
599 turn influences the stability of soil slope. It is important to consider the freeze-thaw action in  
600 estimating the soil water content distribution for the proper pre-judgement of slope stability.
- 601 — The soil water content distribution inside the soil slope is seriously affected by the snowmelt  
602 water infiltration. Ignoring the amount of water derived from the snowmelt may not predict  
603 the soil water content distribution of the slope precisely.
- 604 — The weight of snow accumulated above the soil ground may reduce the slope stability  
605 considerably. The consideration of snow weight in the estimation of the factor of safety is  
606 essential if the snow during accumulation is not removed manually.
- 607 — The frozen shear strength of the soil should be properly considered to analyse the stability  
608 during freezing seasons if it is expected that the soil ground will freeze for a considerable  
609 depth.
- 610 — The freeze-thaw action and snowmelt water infiltration have a substantial impact on soil  
611 slope stability regardless of the slope angle considered.

612 In geotechnical engineering practice, the factors such as freeze-thaw action, snowmelt water infiltration  
613 are generally not considered for the design and analysis of slope structures, especially for cold regions  
614 like Hokkaido. It is evident that these factors seriously affect the soil slope stability. The stability  
615 assessment approach adopted in this study is found to be very useful in analysing the slope stability  
616 against anticipated climatic factors i.e. freeze-thaw action and snowmelt water infiltration. Based on the  
617 studies performed, it is strongly recommended that an assessment of the long-term stability of soil slopes  
618 considering the climatic effects will be helpful for the prevention and mitigation of such disasters.

### 619 **Acknowledgements**

620 We gratefully acknowledge the Sapporo Road Office, Bureau of Hokkaido Development and Docon Co.,  
621 Ltd for their surveyed data and comments. This research was supported in part by Grant-in-Aids for  
622 Scientific Research (A) (16H02360) from Japan Society for the Promotion of Science (JSPS) KAKENHI.  
623 The financial support provided by the MEXT (Ministry of Education, Culture, Sports, Science and  
624 Technology in Japan) scholarship is also gratefully acknowledged.

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