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Multi-Objective Topology Optimization of Rotating Machines Using Deep Learning

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Abstract—This paper presents fast topology optimization methods for rotating machines based on deep learning. The cross-sectional image of electric motors and their performances obtained during a multi-objective topology optimization based on the finite element method (FEM) and genetic algorithm (GA) are used for training of convolutional neural network (CNN). Two different approaches are proposed: (i) CNN trained by preliminary optimization with small population for GA is used for main optimization with large population, (ii) CNN is used for screening of torque performances in the optimization with respect to the motor efficiency.

Index Terms—Deep learning, Genetic algorithm, IPM motor, Multi-objective optimization, Topology optimization.

I. INTRODUCTION

Recently, the effective design method for electric motors especially for electric vehicles has been strongly required. In optimization of electric motors, it is necessary to consider many properties such as average torque, torque ripple, iron loss, radial force and so on. The multi-objective optimization based on stochastic algorithm, e.g., genetic algorithm (GA), allows us to obtain Pareto solutions with respect to multiple motor properties. By increasing the population and children sizes of GA, one would obtain the sufficiently populated Pareto solutions. The optimization based on GA with rich population, however, needs large computational cost due to a number of field computations with e.g. finite element method (FEM). Thus, solution of such multi-objective problems would lead to unallowable computational cost.

Deep learning (DL) based on convolutional neural network (CNN) has been shown effective for fast evaluation of the performance of an electric motor [1] and also acceleration of the topology optimization [1]. In order to reduce the number of evaluations by FEM in the multi-objective optimizations, we propose here an optimization method based on DL. In this method, the cross-sectional images of electric motors and their performance obtained by a topology optimization is used for training of CNN. Then, CNN is used as the surrogate method of FEM for acceleration of the multi-objective topology optimization. Two different approaches are proposed here: (i) CNN trained by a preliminary optimization with small population of GA is used for main optimization with large population, (ii) CNN trained by an optimization with respect to torque performances is used for screening of the torque performances in another optimization with respect to the motor efficiency. The first approach is effective to obtain a sufficiently populated Pareto solution using GA with rich population. The second approach can be generalized as follows:

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CNN is trained through data obtained by solving problem A, then the trained CNN is extendedly used for fast optimization of problems B, C... with different cost functions or constraints. These approaches will be verified by numerical examples.

II. MULTI-OBJECTIVE TOPOLOGY OPTIMIZATION WITH CNN

A. Why deep learning

In this work, the data composed of the cross-sectional images of electric motors and their performance obtained during the topology optimization process are used for training of CNN, which is then used to reduce the field computing cost of optimization with other cost functions, constraints and models. There exist several approximate computing methods for optimization that are used for evaluation of fitness instead of time-consuming field computations using, e.g. FEM. They include the response surfaces [3][4], kriging method[5], artificial neural network (ANN) [6]. Although the former two methods are effective when degree of freedoms (DoFs) is less than, say, ten, DoFs in the pixel image of an electric motor is far larger. ANN can treat the images, while the image features for accurate classification have to be extracted by the user. However, it would be hard to extract such features from diverse images generated through the topology optimization. In contrast, CNN can automatically extract such features from the training images. For these reasons, we employ CNN for the surrogate model in this work.

B. Classifier using CNN

In the learning phase, we construct the classifiers of the average torque T_{ave} and torque ripple $T_{rip} = (T_{max} - T_{min})/T_{ave}$ using CNN with 22 layers, for which GoogLeNet is employed [7]. The structure of CNN is schematically shown in Fig. 1. The input data for CNN is a bitmap image representing the cross-sectional shape of an inner permanent magnet (IPM) motor. The output data is the corresponding values of T_{ave} or T_{rip} . The classes provided by CNN are summarized in TABLE I, TABLE II where $T_{ave}^{FEM}, T_{rip}^{FEM}$ denote the average torque and torque ripple computed with FEM, while $T_{ave}^{CNN}, T_{rip}^{CNN}$ denote the classes output from CNN. The training data is obtained by a

preliminary multi-objective topology optimization of the IPM motor shown in Fig. 2 with relatively small populations in GA. In the topology optimization, the element state S_e is determined from the shape function $\varphi(\mathbf{x}) = \sum_i^n w_i G_i(\mathbf{x})$ where G_i and w_i denote the normalized Gaussian function and weighting coefficient such that $S_e = \text{iron (air)}$ if $\varphi \geq 0$ (< 0) [8]. The optimization problem is defined as follows:

$$\max T_{\text{ave}}(\mathbf{w}), \min T_{\text{rip}}(\mathbf{w}) \quad (1a), (1b)$$

where $\mathbf{w}$ denotes the vector composed of $w_i, i = 1, 2, \dots, n$. Note that the material distribution and thus machine performance depend on $\mathbf{w}$. The population sizes are summarized in the left column of TABLE III. Fig. 3 shows the distribution of $T_{\text{ave}}^{\text{CNN}}$ in the initial population whose individuals are randomly generated. As shown in Fig. 3, many individuals belong to the classes with low average torques. Such individuals could be approximately evaluated only by CNN because these have little influence on the evolution. On the other hand, individuals in classes with higher torques should be accurately evaluated by FEM. Namely, the trained CNN can be effectively used for screening of the torque performances.

We use 6000 data obtained during the multi-objective optimization of the IPM motor with respect to $T_{\text{ave}}, T_{\text{rip}}$ using GA with the size parameters in the left column of Table III for the training of CNN. The 700 data that are not used for the training are used for test of CNN. TABLE IV, TABLE V summarizes the classification results. It is found that there are small number of off-diagonal samples. The reason why the classification accuracy in T_{rip} is lower than that in T_{ave} is due to the relatively weak correlation between the material distribution and torque ripple.

Fig. 1 Structure of CNN

Fig. 2. IPM motor obtained by preliminary optimization

C. Optimization Method (i)

We use the CNN trained for the data obtained through the

preliminary optimization process mentioned above for the acceleration of the main multi-objective topology optimization with larger population size, which is summarized in the center column of TABLE III.

In the main multi-objective optimization process after the learning phase, the values $T_{\text{ave}}^{\text{CNN}}, T_{\text{rip}}^{\text{CNN}}$ are evaluated by the trained CNN to make fast evaluation of the rank $F_i^{\text{CNN}} \in \mathbb{Z}$ of individual i using non-dominated sorting by NSGA-II [9]. Since there would be errors in the ranking, the correction is made by performing finite element (FE) analysis with probability P_i given by

$$P_i = \left(\frac{F_{\text{worst}}^{\text{CNN}} - F_i^{\text{CNN}}}{F_{\text{worst}}^{\text{CNN}} - 1} \right)^2 \quad (2)$$

where P_i is evaluated over the whole population in the first generation and over the children in other generations. We design P_i so that it increases as the score provided by CNN becomes better. In Fig. 5, P_i is plotted against F_i^{CNN} . In the first steps of GA, a limited number of individuals would be analyzed by FEM because the majority of population tends to

TABLE I AVERAGE TORQUE		TABLE II TORQUE RIPPLE	
$T_{\text{ave}}^{\text{FEM}} [\text{Nm}]$	$T_{\text{ave}}^{\text{CNN}} [\text{Nm}]$	$T_{\text{rip}}^{\text{FEM}} [-]$	$T_{\text{rip}}^{\text{CNN}} [-]$
~0.5	0.25	2.0~	2.0
0.5~1.0	0.75	1.0~2.0	1.5
1.0~1.5	1.25	0.8~1.0	0.9
1.5~1.7	1.60	0.6~0.8	0.7
1.7~1.9	1.80	0.4~0.6	0.5
1.9~2.1	2.00	0.2~0.4	0.3
2.1~2.3	2.20	0.0~0.2	0.1

TABLE III PARAMETERS FOR GA			
	Preliminary	Problem (i)	Problem (ii)
Number of genes	28	28	35
Population size N_{pop}	192	1920	400
Number of children N_c	64	192	40
Number of parents N_p	30	30	36
Number of generations	100	100	300

Fig. 3. Distribution of $T_{\text{ave}}^{\text{CNN}}$ in the initial population

TABLE IV CLASSIFIER OF AVERAGE TORQUE		TABLE V CLASSIFIER OF TORQUE RIPPLE	
Accuracy	CNN	Accuracy	CNN
92%	0.25 0.75 1.25 1.6 1.8 2 2.2	81%	0.1 0.3 0.5 0.7 0.9 1.5 2
0.25	53 2 0 0 0 0 0	0.1	82 5 0 0 0 0 0
0.75	0 83 8 0 0 0 0	0.3	9 71 8 4 0 0 0
1.25	0 4 87 5 0 0 0	0.5	0 14 78 9 1 0 0
1.6	0 0 6 108 5 0 0	0.7	0 0 8 94 5 1 0
1.8	0 0 0 7 102 5 0	0.9	0 3 1 15 84 13 1
2	0 0 0 0 6 117 3	1.5	0 2 1 1 15 82 7
2.2	0 0 0 0 0 2 97	2	0 0 0 0 0 8 78

have low values of F_i^{CNN} . The algorithm of the main multi-objective optimization is shown in Fig. 6.

D. Optimization Method (ii)

We consider here the optimization to reduce the iron loss of the IPM motor keeping the torque performance better than a threshold. The optimization model is shown in Fig. 4. To make the computing cost smaller, CNN trained for the preliminary optimization is used for screening of the torque performances. The optimization problem is defined by

$$\min W_{\text{iron}}, \quad \text{sub. to } T_{\text{ave}} > 2.0 \text{ AND } T_{\text{rip}} < 0.2 \quad (3)$$

where W_{iron} denotes the iron loss, which is here evaluated by the Steinmetz formula

$$W_{\text{iron}} = k_h f \left(\frac{B_a}{B_0} \right)^2 + k_e f^2 \left(\frac{B_a}{B_0} \right)^2 \quad (4)$$

where B_a and f denotes the maximum amplitude and frequency of the magnetic flux density, and the constants are set as follows: $B_0 = 1$, $k_h = 7.5 \times 10^{-2} \text{J}$, $k_e = 6.0 \times 10^{-4} \text{Js}$.

In this optimization, we evaluate T_{ave} , T_{rip} using the trained CNN, and if they satisfy the prescribed condition

Fig. 4. Optimization model

Fig. 5. Probability P_i for execution of FE analysis

```

1  for max generation
2  if initial generation
3      generate initial population with random genes
4      evaluate  $T_{\text{ave}}$  and  $T_{\text{rip}}$  of population by classifiers
5      rank population by NSGA-II
6      for each individuals of population
7          compute probability  $P_i$  for FE analysis
8          if  $P_i \geq \text{Seed}[0,1]$ 
9              evaluate  $T_{\text{ave}}$  and  $T_{\text{rip}}$  by FEM
10         end if
11     end for
12 else
13     select parents
14     generate children
15     evaluate  $T_{\text{ave}}$  and  $T_{\text{rip}}$  of children by classifiers
16     rank children by NSGA-II
17     for each individuals of children
18         compute probability  $P_i$  for FE analysis
19         if  $P_i \geq \text{Seed}[0,1]$ 
20             evaluate  $T_{\text{ave}}$  and  $T_{\text{rip}}$  by FEM
21         end if
22     end for
23     rank individuals of population + children by NSGA-II
24     choose next population
25 end if
26 end for

```

Fig. 6. Pseudocode of main multi-objective optimization

$$T_{\text{ave}} \geq 1.7 \text{ AND } T_{\text{rip}} \leq 0.4 \quad (5)$$

these torque properties as well as iron loss are evaluated by FEM. The region satisfying this condition is shown in Fig. 7.

We impose this *weakened* condition for FE analysis because the original constraint in (3) is too strict to have sufficiently large number of population that evolves toward the optimal solution. In the first steps of the GA process, the majority of population does not satisfy (5). Thus, the number of FE analysis is strongly suppressed. The GA setting is summarized in the right column of TABLE III.

III. OPTIMIZATION RESULTS

A. Result Obtained by Method (i)

Fig. 8 shows the Pareto solutions at the 100th generation of GA obtained by the preliminary and main multi-objective optimizations. Using the proposed method, the Pareto solutions can be refined with reduced computational cost. The number of FE analysis, normalized by the total number of ranking evaluation, is plotted against the GA generations in Fig. 9. Because the individuals with higher ranking increase with the generation, the number of FE evaluations increases. In the entire optimization process, FE analysis is performed for 49.5% of the individuals.

The shapes of the IPM motors on the Pareto front, marked by A and B in Fig. 8, are shown in Figs 10. and 11, where solution A has the largest average torque but large torque ripple, while B has a good balance in these two torque performances. The rotor of solution A has large notches which would yield large reluctance torque as well as large torque ripple. On the other hand, the rotor of solution B has a smooth surface, hence has a lower torque ripple and average torque.

Fig. 7. Domain for execution of FE analysis

Fig. 8. Comparison of Pareto solutions obtained by method (i)

Fig. 9. Rate of FEM evaluations

Fig. 10. Shape of motor A in the pareto front shown in Fig.8
 $T_{ave} = 2.21\text{Nm}$, $T_{rip} = 0.700$ Fig. 11. Shape of motor B in the pareto front shown in Fig.8
 $T_{ave} = 2.02\text{ Nm}$, $T_{rip} = 0.074$ Fig. 12. Optimization result obtained by method (ii).
 $W_{iron} = 1.75 \times 10^{-3}$,
 $T_{ave} = 2.00\text{Nm}$, $T_{rip} = 0.191$

Fig. 13. Radial component of flux density along the midline of the air-gap

B. Result Obtained by Method (ii)

Fig. 12 shows the optimization result, which is found to meet the constraints. The flux distribution in the air gap is plotted in Fig.13. The iron loss, average torque and torque ripple of the best individual are plotted against the generation of GA in Fig. 14(a)-(c). The iron loss is not plotted until 21th generation because no individuals are analyzed by FEM. The torque ripple goes up and down because the optimization seeks for a ground for compromise between the average torque and torque ripple which have a reciprocal relationship.

The number of FE analysis, normalized by the total number of ranking evaluation, is plotted against the generation of GA in Fig. 14(d). In the early stage of optimization, the number of FE analysis is suppressed, as expected, because only small number of population satisfies condition (5). As evolution progresses, the execution rate of the FE analysis grows because individuals satisfying (5) increase. As a result, the number of FE analysis is reduced to approximately 30%. This rate depends on the condition for the FE analysis. If we make (5) stricter, then the number of FE analysis would be further suppressed. However, the evolution would not be successful when the condition is made too strict because the number of individuals satisfying such condition is limited.

Fig. 14. Evolution of the best values and change of the analysis rate

IV. CONCLUSION

In this paper, we have proposed new methods based on DL to accelerate the multi-objective topology optimization. In method (i), the CNN trained through the preliminary optimization with small population is used to make a fast evaluation of fitness in the main optimization with large population. In method (ii), the CNN trained through the preliminary optimization with respect to the torque performances is used for fast evaluation of constraints in the optimization with respect to iron loss. The FE computations are reduced to about 50% and 30%, respectively, by (i) and (ii).

We plan to study methods for adequate design of the probability function and the condition for the FE analysis. We will also study adequate modification of the shape obtained by the topology optimization for industrial realization.

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