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ABSTRACT
We investigate the electronic transport property of lateral heterojunctions of semiconducting and metallic transition-metal dichalcogenide monolayers, MoSe$_2$ and NbSe$_2$, respectively. We calculate the electronic transmission probability by using a multiorbital tight-binding model based on the first-principles band structure. The transmission probability depends on the spin and valley degrees of freedom. This dependence qualitatively changes by the interface structure. The heterostructure with a zigzag interface preserves the spin and the valley of electrons in the transmission process. On the other hand, the armchair interface enables conduction electrons to transmit with changing the valley and increases the conductance in the hole-doped junctions due to the valley-flip transmission. We also discuss the spin and valley polarizations of electronic current in the heterojunctions.

I. INTRODUCTION
Transition-metal dichalcogenides (TMDCs) are layered materials of atomically thin two-dimensional crystals consisting of transition-metal and chalcogen atoms, and the monolayer has attracted much attention in condensed matter physics. In semiconducting TMDC monolayers, electrons have two discrete degrees of freedom, spin and valley, due to the band structure. Strong spin–orbit coupling (SOC) leads to spin-related physics in TMDCs, and the valley-dependent Berry curvature causes the valley Hall effect. Therefore, TMDC monolayers have been researched for applications in spintronics and valleytronics. Since the electronic spin direction is locked to the valley due to the strong SOC, the valleytronics and the spintronics can be combined, e.g., the valley can be detected as the spin.

Stable monolayers can be fabricated by cleaving from a crystal or chemical vapor deposition (CVD) on a substrate. The experimental techniques enable composing heterostructures consisting of different atomic layers. The first-designed heterostructure is a stacking of different atomic layers, the so-called van der Waals heterostructure, and it has opened several areas of research and application: optics, electric transport, and exciton physics. The lateral heterostructure is composed of two atomic layers bonded as a single layer and that of semiconducting TMDCs has been realized by CVD.

The semiconducting heterojunction has been investigated theoretically and experimentally applied to the p-n junction, valleytronics, and optoelectronics. This junction provides novel electronic properties for semiconducting TMDCs.

Metallic TMDCs have also attracted much attention in terms of condensed phases. The TMDC of the group-V transition-metal atoms, Nb and Ta, is metallic and has been discovered to show superconductivity and the charge density wave (CDW) even in the monolayer. The NbSe$_2$ monolayer, even in the normal phase, has qualitatively different properties of conduction electrons from the semiconducting monolayers. There are three Fermi pockets in the first Brillouin zone, whereas the semiconducting members have two pockets called the $K$ and $K'$ valleys. Each pocket has both the up-spin and down-spin states. Thus, the correlation between the spin and valley degrees of freedom, the key property of semiconducting monolayers for combining the spintronics and the valleytronics, is absent in the metallic monolayers. We consider the lateral heterojunction of the metallic and semiconducting TMDC monolayers and show that it induces the correlation between the spin and the three valleys.

In this paper, we report our investigation of the spin- and valley-dependent electronic transport property of the lateral heterojunction of semiconducting and metallic TMDC monolayers.
of MoSe$_2$ and NbSe$_2$ monolayers, metallic and semiconducting TMDCs, respectively. We consider two types of interface for such a junction as shown in Fig. 1. The electronic transmission is qualitatively different in two types of interface, the armchair interface in (a) and the zigzag interface in (b). We compute the spin and valley dependence of electronic conductance by using the first-principles band calculation and lattice Green’s function method, and we show the valley-spin correlated transmission effect. This result gives a fundamental knowledge for spintronics and valleytronics in lateral heterojunctions.

II. BAND STRUCTURE

The TMDC monolayer consists of three sublayers, a sublayer of transition-metal atoms sandwiched by two sublayers of chalcogen atoms. The transition-metal atoms, Nb or Mo, and chalcogen atoms, Se, are strongly bonded and form a two-dimensional hexagonal lattice as shown in Fig. 1(c).

We plot the band structure of the pristine monolayer of NbSe$_2$ and MoSe$_2$ in Figs. 2(a) and 2(b), respectively. These bands are calculated by using quantum-ESPRESSO, a first-principles calculation code. Here, we adopt a projector augmented wave (PAW) method with a generalized gradient approximation (GGA) functional including SOC, the cut-off energy of the plane wave basis 50 Ry, and the conversion criterion 10$^{-8}$ Ry. The lattice parameters are also calculated by the lattice-relaxation code of quantum-ESPRESSO as $d_{\text{Mo-Mo}} = 3.319$ Å and $d_{\text{Se-Se}} = 3.343$ Å in MoSe$_2$, where $a_M$ ($d_X$) is the horizontal (vertical) distance between nearest neighbor transition-metal (chalcogen) atoms.

The MoSe$_2$ monolayer is a semiconductor and has a direct gap at the $K$ and $K'$ points in the Brillouin zone. At the band edge, the electronic states split into two spin states due to SOC (see Fig. 2), where the spin-split in the valence band is much larger than that in the conduction band. Here, the spin axis is restricted in the out-of-plane direction due to the crystal symmetry. We show the Fermi surface of electron-doped and hole-doped monolayers with the charge density $n = -3 \times 10^{13}$ cm$^{-2}$ and $3 \times 10^{13}$ cm$^{-2}$.

![FIG. 1. The schematics of the atomic heterostructure of MoSe$_2$ and NbSe$_2$ with an armchair interface (a) and a zigzag interface (b). The unit cell of this junction is indicated by a square frame in (a) and (b). The crystal structure and the primitive unit cell of TMDC monolayer in (c) and (d), respectively. The two arrows indicate the lattice vectors.](image)

![FIG. 2. Band structure of monolayer NbSe$_2$ in (a) and MoSe$_2$ in (b). The horizontal line implies the Fermi energy. The dashed lines indicate the bands computed by a multiorbital tight-binding model (see Sec. III).](image)
respectively, in Fig. 3. Here, the Fermi energy $E_F$ is computed under the condition of a charge density $n$ as

$$n = n_0 - \frac{dFk}{2\pi^2} \theta(E_{\alpha k} - E_F),$$

where $n_0$ is the charge density of nuclei and $E_{\alpha k}$ is the energy dispersion in Fig. 2. The Fermi pockets appear around the $K$ and $K'$ points, and each pocket is so-called a valley. In the hole-doped monolayer, the spin is fully polarized in each valley up to $|n| \sim 6 \times 10^{13}$ cm$^{-2}$, the experimentally feasible charge density by using electrostatic gating. In the case of the fully polarized spin, the spin polarization direction is opposite in two valleys due to the time-reversal symmetry, and total spin polarization is absent. Under the condition of $0 < \delta n < L$, on the other hand, both the spin states are present in each valley. The electrons in MoSe$_2$ can be characterized by spin and valley indexes at any charge density.

In the NbSe$_2$ monolayer, the band is quite similar to that of MoSe$_2$ due to the crystal structure as shown in Fig. 2, but the band is partially filled even at the charge neutral point because the atomic number of Nb is one less than Mo. We show the Fermi surface of the pristine NbSe$_2$ monolayer in Fig. 4. The Fermi pockets appear around three high-symmetry points, the $K$, $K'$, and $\Gamma$ points. We represent the pockets as the $K$, $K'$, and $\Gamma$ valleys in what follows. In every valley, both the two spin states are present. The spin polarization is nonzero and opposite to each other in the $K$ and $K'$ valleys, but the populations of two spins are equal to each other in the $\Gamma$ valley. Every Fermi pocket is strongly trigonal warping due to the threefold symmetry of the crystal structure.

III. CALCULATION METHOD

To calculate the electronic transmission probability, we adopt a tight-binding model defined on the basis of Wannier functions, where the hopping integrals are computed from the first-principles band structure in Sec. II. The maximally localized Wannier functions and spin-dependent hopping integrals are computed by using Wannier90. Here, we adopt three $d$-orbitals $|M, d_{xy} \rangle$, $|M, d_{yx} \rangle$, and $|M, d_{z^2} \rangle$ of the transition-metal atom $M$ and three superpositions of $p$-orbitals of the top selenium Se$^i$ and the bottom one Se$^i$ as $|\text{Se}^i, p_x \rangle$, $|\text{Se}^i, p_y \rangle$, and $|\text{Se}^i, p_z \rangle$ with $|\text{Se}^\pm, p_i \rangle = (|\text{Se}^i, p_i \rangle \pm |\text{Se}^i, p_i \rangle) / \sqrt{2}$. These orbitals have even parity under mirror operation in the $z$ axis, and they are independent of odd parity orbitals in the electronic structure. We show the band structure calculated by the tight-binding model in Fig. 2. It well reproduces the first-principles bands.

We simulate the electronic transmission in lateral heterostructures by using the multiorbital tight-binding model including the interface between MoSe$_2$ and NbSe$_2$ monolayers. We assume a commensurate interface, where two atomic layers are bonded without dangling and misalignment as shown in Fig. 1 and a periodic boundary condition in the parallel direction to the interface. The incident electronic wave with $k_x$ in MoSe$_2$ transmits to NbSe$_2$ as a wave with $k_x' = (\text{Se}_{\text{Mo-Mo}} / \text{Se}_{\text{Nb-Nb}}) k_x$ and thus, the transmission coefficient is defined at each $k_x$. In what follows, we represent both the wave numbers, $k_x$ and $k_x'$, by $k_x$. Despite the mismatch of lattice parameters, such a commensurate heterostructure has been fabricated experimentally. To use the lattice Green’s function method, we consider a unit cell including four transition-metal atoms and eight Se as shown in Fig. 1. The choice of the unit cell transforms the tight-binding Hamiltonian into a suitable form for the recursive Green’s function method, where it includes only hopping integrals between nearest neighbor cells. Here, we adopt the hopping matrix in NbSe$_2$ as that between MoSe$_2$ and NbSe$_2$ because the outer shell of Mo and Nb atoms is the same as $4d$-orbitals, and the hopping integral is similar to each other in the two monolayers.

We show the charge distribution around the interface of the lateral heterojunction for $n = -3 \times 10^{13}$ cm$^{-2}$ and $n = 3 \times 10^{13}$ cm$^{-2}$ in Fig. 5. They are obtained by using the tight-binding model under...
Fig. 5. The charge distribution around the interface for \( n = -3 \times 10^{13} \text{ cm}^{-2} \) and \( n = 3 \times 10^{13} \text{ cm}^{-2} \). Here, \( x \) indicates the position in the unit of half the unit cell and the interface is placed at \( x = 0 \). The vertical axis indicates the summation of wave amplitude over all the occupied states in the tight-binding model. The schematic of the lattice structure represents the atomic positions.

A periodic boundary condition with 20 unit cells aligned in the \( x \) axis. The vertical axis indicates the wave amplitude of adopted orbitals, which is included in the tight-binding model, for the occupied states, and the horizontal axis exhibits the position in the \( x \) axis with the interface at \( x = 0 \). The wave amplitude is nearly \( |\psi_n|^2 = 5 \) at Se atoms in both the regions, and in the transition-metal atoms, the wave amplitude changes between two regions due to the difference of atomic numbers for Mo and Nb. Around the interface \( x = 0 \), the charge distribution varies from that far from the interface \( 2 \leq |x| \). In the electron-doped junction (circle symbols in Fig. 5), the charge transfer arises between two regions, and it induces the drastic fluctuation of the charge density at the vicinity of the interface. In the hole-doped junction (triangle symbols in Fig. 5), on the other hand, the charge distribution slightly fluctuates even in the vicinity of the interface. The difference between the electron-doped and hole-doped cases is discussed in Sec. V.

We calculate the transmission probability \( t_{\mu\nu}(k_y) \) by using the lattice Green’s function method for the multiorbital tight-binding model, where \( \nu \) and \( \mu \) represent the incoming and outgoing waves in MoSe\(_2\) and NbSe\(_2\), respectively. At the zero temperature, the conductance per unit width is given by

\[
G(E_F) = \frac{e^2}{\pi \hbar} \int \frac{dk_y}{2\pi} \sum_{\mu,\nu} \sqrt{\langle \psi_{\nu} \mid \psi_{\mu} \rangle}^2.
\]

Here, \( \psi_{\nu} \) and \( \psi_{\mu} \) are the velocity along the \( x \) axis for the outgoing wave in NbSe\(_2\) and the incoming wave in MoSe\(_2\), respectively. The NbSe\(_2\) monolayer shows the phase transition, CDW and superconductivity, at low temperature, but we consider normal states of NbSe\(_2\) for investigating the fundamental transport property of the metallic NbSe\(_2\) monolayer. We define the positive direction in the \( x \) axis as the transmission direction. Thus, the electronic waves \( \mu \) and \( \nu \) have the positive velocity in the \( x \) axis. The wave functions are represented by the periodic part \( c_{\mu} \), wave amplitudes of Wannier functions, in a unit cell and the phase shift \( \lambda = e^{-i\theta} \) in the transmission process between adjacent cells. The coefficients are the eigenfunction and eigenvalue of the following equation for each \( k_y \) in pristine MoSe\(_2\) and NbSe\(_2\) monolayers as

\[
\hat{\lambda} \begin{pmatrix} c_j \\ c_{j-1} \end{pmatrix} = \begin{pmatrix} \hat{h}_1^{-1}(k_y) & -\hat{h}_1^{-1}(k_y) \\ 1 & 0 \end{pmatrix} \begin{pmatrix} c_j \\ c_{j-1} \end{pmatrix},
\]

with the on-site potential \( \hat{h}_0(k_y) \) and the right-going and left-going hopping matrix \( \hat{h}_1 \) and \( \hat{h}_{-1} \), respectively. The velocity in the \( x \) axis is calculated by \( \nu_x = \left( c_j, c_{j-1} \right) \hat{v}_x \left( c_j, c_{j-1} \right) \) with the velocity operator defined by

\[
\hat{v}_x = -\frac{\alpha_x}{\hbar} \begin{pmatrix} 0 & \hat{h}_{-1}(k_y) \\ \hat{h}_1(k_y) & 0 \end{pmatrix},
\]

where \( \alpha_x \) is the length of the square unit cell in Fig. 1 along \( x \). The relation between the Fermi energy and the charge density is represented in Eq. (1). We consider the charge induction by using a top or back gate being homogeneous in the \( xy \) plane. By gating, opposite charges are induced in the substrate and homogeneously distributed in the \( xy \) plane. Thus, we can assume that the induced charges in the heterojunction are distributed homogeneously, i.e., \( n = \text{const} \), in the \( xy \) plane due to the local charge neutrality. Then, the Fermi energy is also applied to the MoSe\(_2\) and NbSe\(_2\) regions in the lateral heterojunction. In a realistic interface, the charge distribution is more complicated, but we adopt the approximation for analyzing an ideal transmission case and for simplicity. We also calculate \( k_s \) of incoming and outgoing waves by using \( \phi = k_x c_x \), and thus, we can characterize these waves by the valley degree of freedom \( \tau \) by referring to the Fermi surface in Figs. 3 and 4. Therefore, the wave index, \( \mu \) and \( \nu \), is given by the valley index \( \tau \) and the spin index \( s \). By picking up a spin...
and a valley, it is possible to calculate the conductance of spin-polarized electrons transferring between two valleys.

We also consider the conductance at nonzero temperatures. The temperature does not change the transmission probability at the interface because the width of the scattering region, the interface, is always shorter than the coherent length. The incident electrons, on the other hand, are distributed in the energy around the Fermi level due to the temperature $T$ and described by the Fermi distribution function $f_{\text{F}}(E, T) = \frac{1}{1 + \exp[(E - E_F)/k_B T]}$ with the Boltzmann constant $k_B$. At nonzero temperature, the conductance can be calculated by using the Landauer formula at the finite temperature,

$$
  g_e(E_F, T) = \frac{e^2}{h} \int_{-\infty}^{\infty} dE \left( \frac{\partial f_{\text{F}}(E, T)}{\partial E} \right) g_s(E).
$$

Here, the derivative of the Fermi distribution function becomes the Dirac delta function $\delta(E - E_F)$ at zero temperature, and thus, the formula reproduces the conductance in Eq. (2) at the zero temperature. In Fig. 6, we show the conductance at 50 K and 150 K, where both the temperatures are above the phase transition temperature to CDW $T_{\text{CDW}} = 33$ K–45 K on the bilayer graphene substrate and 145 K on the sapphire substrate.

**IV. NUMERICAL RESULTS**

First, we show the charge density-dependence of electric conductance $g_e$ in Fig. 7. The conductance drops around $n = 0$ in both the two types of heterostructures with an armchair-type interface and a zigzag-type interface in Figs. 1(a) and 1(b), respectively, and it monotonically increases with $|n|$. This is because the Fermi level is in the insulating gap under $n = 0$, and the conducting channels increase with $|n|$ in MoSe$_2$. At every nonzero charge densities, the heterostructure with the armchair-type interface gives a larger $g_e$ than that with the zigzag-type interface in the hole-doped junctions. The armchair interface allows electrons transferring between different valleys, e.g., $K$ and $\Gamma$, in MoSe$_2$ and NbSe$_2$ as discussed below, and thus, it enhances the total transmission probability. In the transmission process, the electronic spin is conserved due to the mirror symmetry in the $z$ axis, the out-of-plane direction. Thus, the conductance $g_e$ is separated into that of up-spin electrons $g_{\uparrow}$ and down-spin electrons $g_{\downarrow}$. In TMDC monolayers, the spin relaxation is suppressed even in the presence of the nonmagnetic impurity due to the mirror symmetry.$^{44-46}$ The two spin components are

![FIG. 6. Temperature dependence of electric conductance in the lateral heterostructure with the armchair interface (a) and the zigzag interface (b).](image)

![FIG. 7. The charge density-dependence of electric conductance per unit width (solid line) in the heterojunction with an armchair-type interface (a) and a zigzag-type interface (b). The dashed lines indicate the conductivity for each spin state.](image)
balanced due to the equal population of two spins in the presence of the time-reversal symmetry.

Next, we show the valley-dependent conductance in the two types of heterostructures in Figs. 8 and 9. The heterostructure with a zigzag interface preserves the mirror symmetry in the $y$ axis. Thus, the transmission probability is equivalent in both the valleys as shown in Fig. 8. When passing through the zigzag interface, electrons preserve the valley degree of freedom due to conservation of wave number $k_y$ parallel to the interface. Here, $k_y$ is parallel to the $M-K$ direction in Figs. 3 and 4, and the transmission of the electron with $k_y$ is nonzero as long as electronic states are present in the Fermi surface of both MoSe$_2$ and NbSe$_2$. Since the spin is fully polarized in the $K$ and $K'$ valleys on the condition of $0 < n$ in MoSe$_2$, the spin and valley are locked to each other in the transmission process. In $n < 0$, on the other hand, the up-spin and down-spin electrons flow above $n = 3 \times 10^{13}$ cm$^{-2}$ in both the two valleys.

In Fig. 9, we show the spin and valley dependence of conductance of the heterojunction with an armchair-type interface. Valley-conserving transmission probability is similar to that in the zigzag interface. Moreover, electrons in MoSe$_2$ are able to switch with switching the valley to $\Gamma$ as shown in (b) and (e), but the valley-switch between the $K$ and $K'$ valleys is highly suppressed even in this heterostructure as shown in (c) and (d). The electronic flow in the $\Gamma$ valley carries the spin current in $0 < n$. The spin flow is attributed to the difference of the transmission coefficient for incoming electronic waves in the $K$ and $K'$ valleys of MoSe$_2$. Here, the transmission coefficient is defined as $\mathcal{S}_{\mu\nu} = \sqrt{\nu_\mu/\nu_\nu}$, which is the integrand in Eq. (2), and it depends on the ratio of the Fermi velocity $\nu_\mu/\nu_\nu$ in the pristine NbSe$_2$ and MoSe$_2$. We show the Fermi velocity in MoSe$_2$ and NbSe$_2$ in Fig. 10, where the electronic states having the right-going velocity and being inside of dashed lines correspond to the wave vector holding conducting channels. The Fermi velocity of right-going states with down-spin is much smaller than that with up-spin in NbSe$_2$. The spin current in the $\Gamma$ valley is caused by this anisotropy of the Fermi velocity. The armchair interface allows us to obtain not only the spin-polarized electronic current in the $\Gamma$ valleys but also the valley polarized current between the $K$ and $K'$ valleys, which can be observed by the valley Hall effect due to the opposite Berry curvature in the two valleys.\cite{1,2,3,47}
In Sec. IV, we consider the heterojunction with a charge density induced by electrostatic gating. In this section, we discuss the effect of chemical doping in the lateral heterojunction. The dopants form impurity levels inside the gap of the semiconductor and pin the Fermi energy at a level without gating. Around the interface, the charge density is modulated due to the difference of the work function between MoSe$_2$ and NbSe$_2$. We calculate the electrostatic potential for electrons as a function of $z$, the out-of-plane coordinate, using quantum-ESPRESSO and plot it referring to the Fermi level in Fig. 11. Here, we set the origin of $z$ at the transition-metal atoms and adopt the potential at $z/d_{Se- Se} = 2$ as the vacuum level. The work function is defined by the vacuum level with respect to the Fermi energy. We compute the work function $W_{MoSe_2} = 5.217$ eV and $W_{NbSe_2} = 5.447$ eV, where $W_{MoSe_2}$ is similar to a previous work and obtain the difference $W_{MoSe_2} - W_{NbSe_2} = -0.230$ eV. Since the semiconducting TMDC, MoSe$_2$, has a smaller work function than the metallic TMDC, NbSe$_2$, a Schottky barrier is formed in the junction of electron-doped MoSe$_2$ due to the modulation of the doped carrier density. In the hole-doped heterostructure, on the other hand, the junction has a Ohmic contact.

Around the interface of realistic materials, charges transfer between two TMDCs due to the difference of work functions as shown in Fig. 5. The charge transfer modifies the Fermi energy near the interface, and it can be treated as a contact resistance. It reduces the transmission probability, but the spin and valley polarization is unchanged qualitatively because time-reversal and mirror symmetries are preserved. Furthermore, the control of contact resistance for atomic layered materials has been developing, e.g., the graphene-metal junction. In our calculation, we assume the uniform Fermi energy over each TMDC for analyzing an ideal transmission case.

Finally, we discuss the experimental observation associated with the spin and valley-dependent transmission in the lateral heterojunction. We show that the spin of conduction electrons is not...
polarized at a single heterojunction as shown in Fig. 7. By combining the armchair and zigzag interfaces, on the other hand, the two-interface heterojunction induces the spin and valley polarized current. In Fig. 12, the left interface changes the transmission probability between K and K', and the right interface allows the equal transmission for the two valleys. Then, the spin and valley polarization induced by the left interface remains in the right MoSe₂ region. Therefore, the spin- and valley-dependent transmission can be shown in the two-interface heterojunction experimentally.

VI. CONCLUSION

We have investigated the electronic transport property of lateral heterojunctions of the metallic NbSe₂ monolayer and the semiconducting MoSe₂ monolayer and have shown that the spin and valley dependence of conductance changes with the interface structure. The zigzag-type interface conserves the spin and valley conduction electrons in the K and K' valleys, and the conductance is independent of the valley and spin. This means that NbSe₂ can be applied to the lead in spintronic or valleytronic devices made by only atomic layers.

REFERENCES


