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# Warm-cool color-based high-speed decolorization: an empirical approach for tone mapping applications

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**Abstract.** Grayscale images are fundamental to many image processing applications like data compression, feature extraction, printing and tone mapping. However, some image information is lost when converting from color to grayscale. In this paper, we propose a light-weight and high-speed image decolorization method based on human perception of color temperatures. Chromatic aberration results from differential refraction of light depending on its wavelength. It causes some rays corresponding to cooler colors (like blue, green) to converge before the warmer colors (like red, orange). This phenomena creates a perception of warm colors “advancing” toward the eye, while the cool colors to be “receding” away. In this proposed color to gray conversion model, we implement a weighted blending function to combine red (perceived warm) and blue (perceived cool) channel. Our main contribution is threefold: First, we implement a high-speed color processing method using exact pixel by pixel processing, and we report a  $5.7\times$  speed up when compared to other new algorithms. Second, our optimal color conversion method produces luminance in images that are comparable to other state of the art methods which we quantified using the objective metrics (E-score and C2G-SSIM) and subjective user studies (decolorization and tone mapping). Third, we demonstrate that an effective luminance distribution can be achieved using our algorithm by using global and local tone mapping applications.

**Keywords:** Warm-cool colors, chromatic aberration, decolorization, luminance, pre-processing, RGB, tonemap.

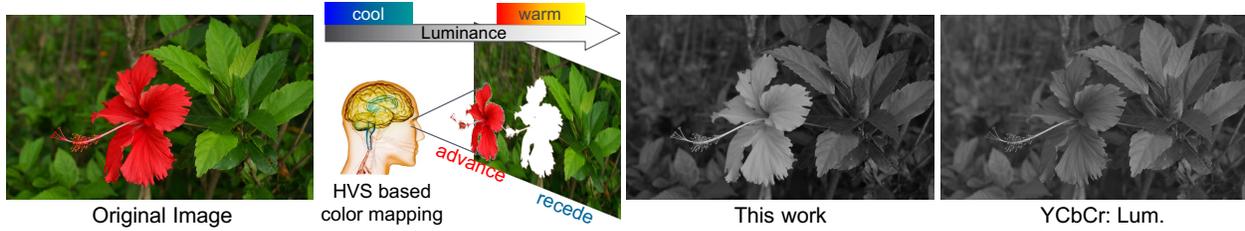
[prasoon.ak@ist.hokudai.ac.jp](mailto:prasoon.ak@ist.hokudai.ac.jp) [ou.yafei.5w@ist.hokudai.ac.jp](mailto:ou.yafei.5w@ist.hokudai.ac.jp) [ikebe@ist.hokudai.ac.jp](mailto:ikebe@ist.hokudai.ac.jp)

## 1 Introduction

Grayscale channels, which reflect image luminance, are used for various applications such as printing, tone mapping, data compression, and feature extraction. Thus, obtaining luminance along with human perception has a key role for decolorization, which converts RGB channels to high-quality gray ones. For example, High Dynamic Range (HDR) compression is ideally performed by tone mapping the luminance channel for the lower computational and memory cost. However, applying well-known luminance channels such as Y of YCbCr or V of HSV does not guarantee appropriate tone mapping, as these channels do not reflect human perceptions. Therefore, decolorization has gathered considerable attention and various sophisticated methods to achieve perceptual decolorization have recently been proposed. These methods can be classified into global and local

31 methods. Global methods can define only one conversion function for all pixels, and most of these  
32 methods use all pixels in the image to determine the function. On the other hand, local ones pro-  
33 cess the target from neighboring pixels in the same way as a spatial filter, the function is different  
34 for each pixel. However, both types of methods face the issue of calculation cost, which comes  
35 from optimization iterations or spatial filter processing.

36 We have developed a fast decolorization method that reflects the perception of warm and cool  
37 colors which is well known in psychophysics studies.<sup>1</sup> Colors are arranged according to their  
38 wavelengths on the color wheel, the ones with longest wavelengths are on the right side of the  
39 wheel and are known as warm colors, as they evoke warmth. These hues include shades of red,  
40 yellow, and orange. On the other hand, green, blue and violet which have shorter wavelengths are  
41 placed on the left side of the color wheel, and are perceived as cool colors. The color of an object  
42 in a scene affects our perception of its apparent depth and this phenomenon has been exploited  
43 by many artists. This optical illusion has been studied by psychologists, and early researchers  
44 explored color-depth relationship. One of the widely accepted theory explains this phenomenon is  
45 due to fact that shorter wavelengths of visible light are refracted more than longer wavelengths.<sup>2</sup>  
46 In other words, an equidistant source of different wavelengths cannot be focused simultaneously  
47 onto our retina. This phenomena is called as chromatic aberration and we discuss it in detail in  
48 section 2.3. In our decolorization method, we implement a weighted blending of warm and cool  
49 colors in accordance with the Helmholtz-Kohlrausch (H-K) effect.<sup>3</sup> On that account, we make two  
50 assumptions, which are: (i) warm colors (mainly including  $R$ ) are lighter than  $Y$  of YCbCr and  
51 (ii) mixed colors are darker than the  $Y$  or  $L$  of CIE with the same luminance. To satisfy these  
52 assumptions, we use a weighted blending of RGB channels and remap them to warm/cool colors  
53 on the luminance channel. Following are our main contributions:



**Fig 1** Main concept of our decolorization method: Human perception of warm and cool colors. Warm colors “advance” toward the eye, while cool colors “recede”. In this work we are able to accurately reflect the human perception of warm-cool colors, whereas this phenomenon is non-existent in conventional YCbCr color space.

- 54 • We propose a warm-cool color-based decolorization method.
- 55 • We achieve high-speed color mapping by exact pixel-by-pixel processing.
- 56 • We obtain luminance comparable to that of optimization-based methods.
- 57 • We demonstrate effective luminance distribution for pre-processing by performing objective
- 58 and subjective evaluations.

59 There are many well defined methods to convert any color image to a grayscale image. An  
 60 effortless procedure is to assign different weights to color channels, in order to have the same  
 61 luminance in the grayscale image as the original color image. For example, in the MATLAB func-  
 62 tion `rgb2gray`, it converts any RGB values to grayscale (*Gray*) values by forming a weighted  
 63 sum of the *R*, *G*, and *B* components as  $Gray = 0.2989 \times R + 0.5870 \times G + 0.1140 \times B$ . This  
 64 function operates under an assumption that human visual system is more sensitive to green color.  
 65 When operating with CIELab and YUV color spaces, one could directly obtain luminance channel  
 66 as the grayscale version of the color image as they consider the luminance and color channel to  
 67 be independent. But, such crude approaches will fail to preserve image contrast as shown in these  
 68 examples (see Fig. 1 and Fig. 2).



**Fig 2** Comparison of luminance components obtained using YCbCr, CIELAB and our proposed method. Here, we can observe that our decolorization can generate warm colors (like  $R$ ) which are lighter than  $Y$  of YCbCr, and mixed colors which are darker than the  $Y$  or  $L$  of CIE.

69 In several real-world image/video processing applications like detail enhancement, image match-  
70 ing, and segmentation under different illumination a 1-D grayscale image has to be obtained from  
71 its corresponding 3-D color image. However, mapping the 3-D color information onto a 1-D  
72 grayscale image while retaining the original contrast and fine details is a challenging problem.  
73 Additionally, implementing decolorization algorithms with a reasonable computational efficiency  
74 is pivotal for realising their real-time applications. Many studies have been carried out to develop  
75 novel decolorization methods. These mapping methods can be categorized into global<sup>4-8</sup> and local  
76 methods.<sup>9-12</sup> In local mapping methods, the same color pixel within an image could be mapped  
77 into different grayscale values depending on its spatial location. Ideally this undesirable as such  
78 output images may be perceived as unnatural. On the other hand, in global mapping methods same  
79 color pixels within an image irrespective of its spatial location are mapped to same grayscale val-  
80 ues. Thus, global methods are more likely to produce grayscale images that are perceived to appear  
81 natural.

82 In the global methods category, Gooch et al.<sup>4</sup> proposed a global decolorization algorithm  
83 that can be implemented by solving the optimization problem for all image pixels. Then, Kim et  
84 al.<sup>7</sup> aimed at high-speed processing by simplifying Gooch's method. Smith et al.<sup>6</sup> used unsharp  
85 masking and the H-K effect model of Nayatani et al.<sup>3</sup> Nayatani's model<sup>3</sup> is merely an experimental

86 model for the effect of the CIELUV chrominance component for human perception. On the other  
87 hand, the method of Lu et al.<sup>8</sup> is focused on converting a color image into a gray image with high  
88 contrast. The main advantage of these methods is transformation consistency, i.e., the same color  
89 is converted to the same grayscale. However, speed remains a problem for these methods. Most of  
90 the local methods are aimed at speeding up the method of Lu et al.<sup>8</sup> To enhance image contrast,  
91 Ancuti et al.<sup>10</sup> adopted the strategy of using a Laplacian filter and Song et al.<sup>12</sup> used a Sobel filter.  
92 Although local methods are effective in terms of contrast emphasis, they are disadvantageous in  
93 terms of tone mapping because conversion consistency is not maintained and it differs from human  
94 perception.

95 Recently, some machine learning-based techniques have also been proposed for image decol-  
96 orization.<sup>13–18</sup> Cai et al.<sup>14</sup> proposed a method, that used the perceptual loss function to pretrain  
97 VGG-Net.<sup>19</sup> However, it is difficult to control and many of their output images are far from hu-  
98 man perception additionally, the computational cost are high. Processing an image of  $256 \times 256$   
99 size it requires roughly 30 seconds on a single Nvidia GeForceGTX 1080 GPU. Zhang et al., pro-  
100 posed a CNN framework that combines local and global image features.<sup>17</sup> However, their network  
101 framework do not account for exposure features.<sup>13</sup> Lin et al.’s method<sup>16</sup> by utilizing a database  
102 of 50 images from the Corel dataset produced 50 grayscale images using the Color2Gray algo-  
103 rithm.<sup>4</sup> With these 50 input/output image pairs as training examples for their partial differential  
104 equations-based (PDE) learning system, they learn Color2Gray mapping. The proposed PDE sys-  
105 tem generated images of comparable quality to that of Gooch et al.<sup>4</sup> However, for an input image  
106 of size  $n \times n$  their PDE color mapping algorithm’s computational complexity is  $O(n^2)$ . Liu and  
107 Leung proposed a deep learning method for the multiexposure fusion problem and applied for  
108 color to gray conversion using convolutional neural network (CNN).<sup>18</sup> This paper describes the re-

109 lationship between color-to-gray transformation and multiexposure fusion (MEF) and applied the  
110 CNN to the MEF. Their method has resulted in improvements in the image fusion effects, how-  
111 ever, the cost of the processing is high and report that a  $750 \times 599$  color image computation time  
112 is reported as 27.964 seconds on CPU and 1.632 seconds on GPU.<sup>18</sup> Under these circumstances, a  
113 high-speed method for generating grayscale images that accurately captures human perception has  
114 not yet been developed. To make tone maps valid, it is necessary to develop such a method.

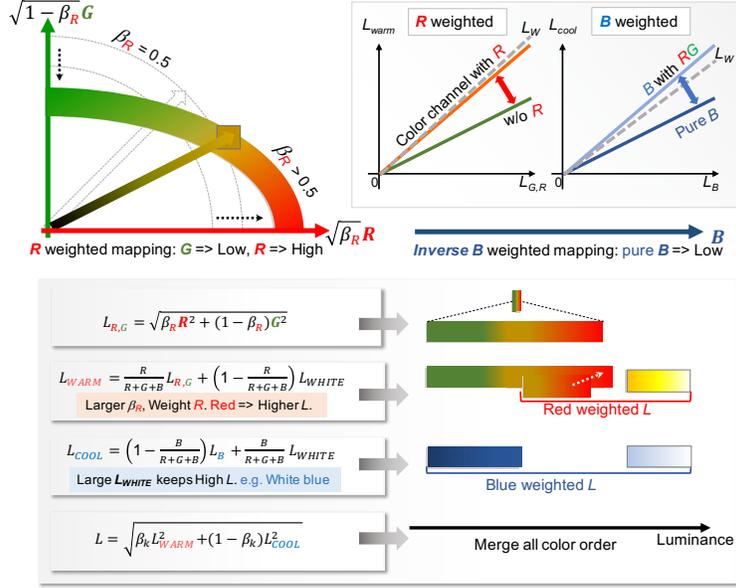
## 115 **2 Proposed Method**

### 116 *2.1 Problem Definition*

117 Luminance components such as  $Y$  of YCbCr and CIE  $L$  have been used in various image pro-  
118 cessing applications; however, they do not accurately reflect human perception (Fig.1 and Fig. 2).  
119 Figure 1 shows how the warm colored flower (red) advances towards the eye of the observer, while  
120 the background mainly green recedes. Using the luminance channel of the conventional YCbCr  
121 color space this phenomenon is absent. But, in our method we are able to capture the warmth  $R$   
122 (red) component as perceived in human perception. Figure 2 shows that the  $R$  (red) and  $B$  (blue)  
123 components do not come even close to the perception in the luminance component of CIELAB.  
124 Moreover, mixed color components such as mud yellow tend to appear dark for people. In this  
125 study, we conceived the idea that RGB weight functions for alpha blending can reproduce this  
126 phenomenon.

### 127 *2.2 Luminance mapping using red and blue weighting function*

128 We consider the idea of color mapping by performing a weighted blending of warm-colors and  
129 cool-colors in accordance with the H-K effect.<sup>3</sup> And we evaluate it using the COLOR250 dataset.<sup>20</sup>



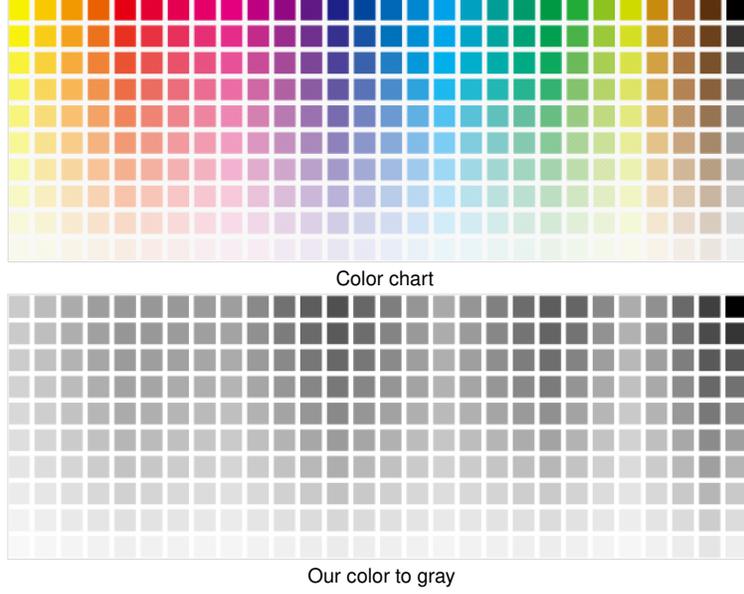
**Fig 3** Remodeling of luminance space based on our two weighting functions one each for warm and cool colors. Here, luminance is defined as the Euclidean distance of warm/cool color. The included color panels aid in intuitive understanding of the proposed method.

130 Psychophysical studies find that, warm and cool colors impact our visual perception of the objects  
 131 that we see. For example, the red color associated with fire/sun advances toward the eye, creates  
 132 an illusion of heat and therefore perceived as warmth and comforting. On the other hand, cool  
 133 colors have reverse effects of warm colors. Receding from the eye of the observer, cool colors  
 134 reminds of the earthy objects, like meadows and oceans. These hues often are perceived as cool  
 135 and refreshing<sup>1,21</sup> In our decolorization method, we developed two weighting functions as shown  
 136 in Fig 3. One function for remapping warm colors and the other for remapping cool colors. In our  
 137 method, actual luminance is defined as the Euclidean distance of weighted warm/cool luminance  
 138 including the  $W$  (white) channel. Essential luminance is given by

$$L_{WHITE} = \sqrt{\frac{R^2 + G^2 + B^2}{3}} \quad (1)$$

139

$$L_B = B \quad (2)$$



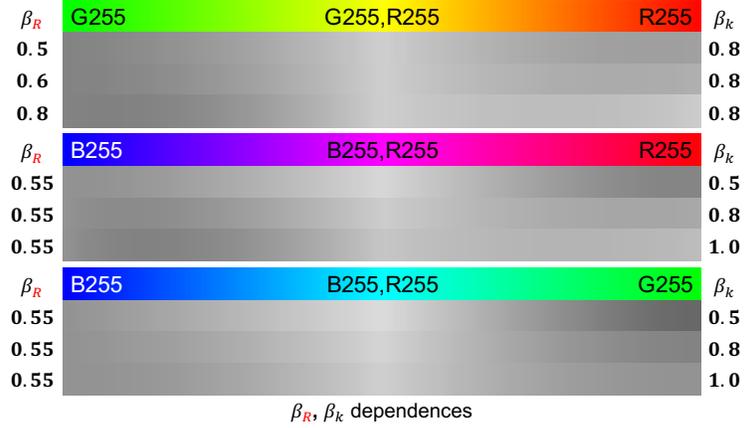
**Fig 4** Decolorization of a color chart illustrating our method’s effectiveness in generating brighter shades of gray for warm colors.

140

$$L_{R,G} = \sqrt{\beta_R R^2 + (1 - \beta_R) G^2}, \quad (0.5 < \beta_R < 1) \quad (3)$$

141

142 As we know,  $L_{WHITE} : W$  (in Eq. 1) is the Euclidean distance of  $RGB$  channels;  $L_B$  (in Eq.  
 143 2) is the  $B$  (blue) channel as it is. The component of warm color function  $L_{R,G}$  which includes red,  
 144 orange and yellow is also defined as the Euclidean distance by  $\beta_R$  weighted  $R$  (red) and  $G$  (green)  
 145 vectors (in Eq. 3). When  $\beta_R = 0.5$ , the vector length of each color is same. Here, we focus on the  
 146 relationship between red and green as in H-K effect; green has less brightness than red with same  
 147 luminance. Thus, we apply a weight  $\beta_R > 0.5$  as a bias for the  $R$  component; when  $\beta_R$  increases,  
 148 more  $R$  components than  $G$  components are rated. In actual H-K effect, color brightness order is  
 149 yellow, green and red (Y,G,R).<sup>3</sup> However, since yellow is generated by mixing of red and green, if  
 150 we manually place yellow as darker shade than green, the vector length of yellow color becomes  
 151 similar to the length of green vector. Thus, we keep the color brightness order as green, yellow  
 152 and red (G,Y,R). The remappings made by the blending function using the  $R$  and  $B$  ratio of  $RGB$



**Fig 5** Impact of  $\beta_R$  and  $\beta_k$  on output luminance value. (top)  $\beta_k$  set to 0.8 and for changing  $\beta_R$  we move from  $G_{max}$  to  $R_{max}$ . (middle)  $\beta_R$  set to 0.55 and for changing  $\beta_k$  we move from  $B_{max}$  to  $R_{max}$ . (bottom)  $\beta_R$  set to 0.55 and for changing  $\beta_k$  we move from  $B_{max}$  to  $G_{max}$

153 values are given by

$$L_{WARM} = \frac{R}{R+G+B} \cdot L_{G,R} + \left(1 - \frac{R}{R+G+B}\right) \cdot L_{WHITE} \quad (4)$$

154

$$L_{COOL} = \left(1 - \frac{B}{R+G+B}\right) \cdot L_B + \frac{B}{R+G+B} \cdot L_{WHITE} \quad (5)$$

155 Here,  $L_{WARM}$  is obtained by blending red weighted  $L_{R,G}$  with white as shown in Fig. 3 and Eq. 4.

156 The blending ratio determines the relationship of warm color components and the colors which are

157 closer to white. When the color includes large red components (e.g. pure red), this color has large

158 brightness approaching white. In inverse  $B$  weighting, pure  $B$  components are assigned to low

159 luminance in the  $L_{COOL}$ . Since both functions are blended with  $L_{WHITE}$ , bright orange/yellow

160 and sky blue, which include high white components, are mapped to higher luminance. Finally, we

161 obtain the luminance channel  $L$ , which is given by

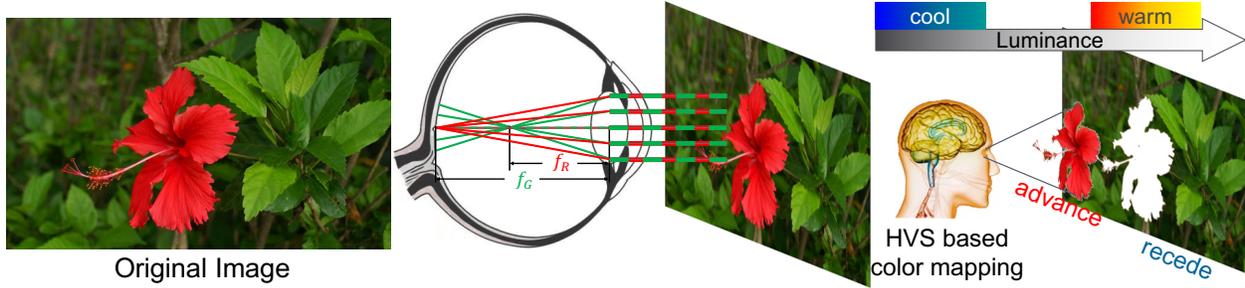
$$L = \sqrt{\beta_k L_{WARM}^2 + (1 - \beta_k) L_{COOL}^2} \quad (0.5 < \beta_k < 1) \quad (6)$$

162 In this study, we mainly used warm-color weighting luminance in experiments and set the  $\beta_k$

163 higher. We set two parameters relating to color component emphasis as follows: ( $\beta_R = 0.55$ ;  $\beta_k =$   
164  $0.8$ ), and from Fig 5 it can be easily understood how  $\beta_R$  and  $\beta_k$  can bias the resulting luminance  
165 values. Figure 4 presents a color reference chart and the corresponding grayscale conversion in-  
166 tended for visual comparisons and measurements. This chart illustrates our method’s effectiveness  
167 in generating brighter shades of gray for warm colors.

### 168 *2.3 Warm-cool color and chromatic aberration*

169 From Snell’s law we know that the refraction of light is dependent on its wavelength. As the  
170 frequency of light increases, its refractive index becomes larger, causing more refraction of the  
171 shorter wavelengths. Therefore, when an image is captured through a lens, all colors do not focus  
172 at the same distance, and these imperfections are known as chromatic aberration. In cameras  
173 this imperfection is removed by using a combination of second achromatic lens which is made of  
174 different material(glass) than the first lens. This second lens would reverse the color dispersion  
175 caused by the first lens. The human eye, also employs a lens and does exhibit this phenomena as  
176 shown in Fig. 6. From this figure we can observe that red light forms the image farthest from the  
177 lens as it has the smallest refractive index. Colors with higher index of refraction would ideally  
178 bend more thereby forming images closer to the lens. Therefore, it would be impossible to focus on  
179 all colors simultaneously, resulting in “somewhat fuzzy” images that are not in focus. Colors that  
180 are closer to red end of the electromagnetic spectrum are said to be warm colors and are perceived  
181 as closer to the observer.<sup>22,23</sup> Colors that are around the blue end are said to be cooler colors and  
182 are perceived to be receding away from the observer. This phenomenon has been exploited by  
183 traditional artists to add depth information in artwork,<sup>24</sup> display devices,<sup>25</sup> and 3D imagery.<sup>26</sup>



**Fig 6** Chromatic aberration which results from differential refraction of light depending on its wavelength, it causes some rays (green) to converge before other (red). This results in a perception of red “advancing” toward the eye, while green to be “receding”.

#### 184 2.4 Limitation of our method

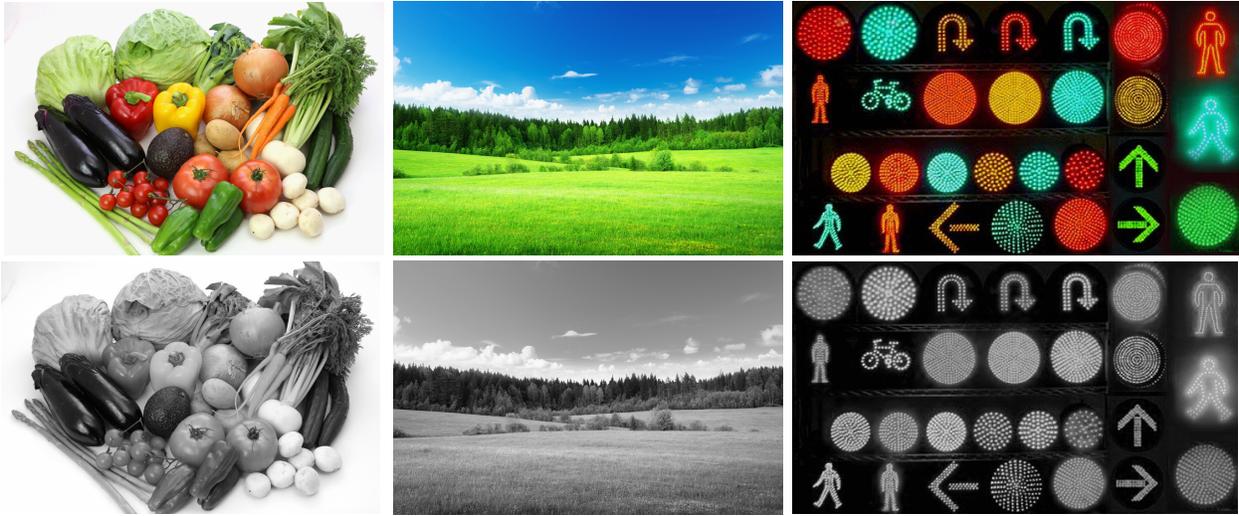
185 In our decolorization method, pure green is likely to be mapped to a dark luminance value. Light  
 186 green will also be mapped to a lesser dark luminance part as shown in Fig. 5. Therefore, certain  
 187 scenes are likely to be perceived as unnatural. For example: (a) Vegetables (e.g. leafy greens like  
 188 cabbage) (b) Green meadows under bright sky. (c) Bright green neon lights. However, in Fig. 7 we  
 189 perceive them as natural. We postulate the following as the possible reasons: (i) There are rarely  
 190 any pure bright green (like G255) scene in nature. (ii) In our color space, green color with white  
 191 components follow Eq.(1) by weighting function. Therefore, the color keeps a balance among  
 192 other color channels. (iii) Vegetation scenery with dark green are well perceived as healthy plants.

### 193 3 Experimental Results

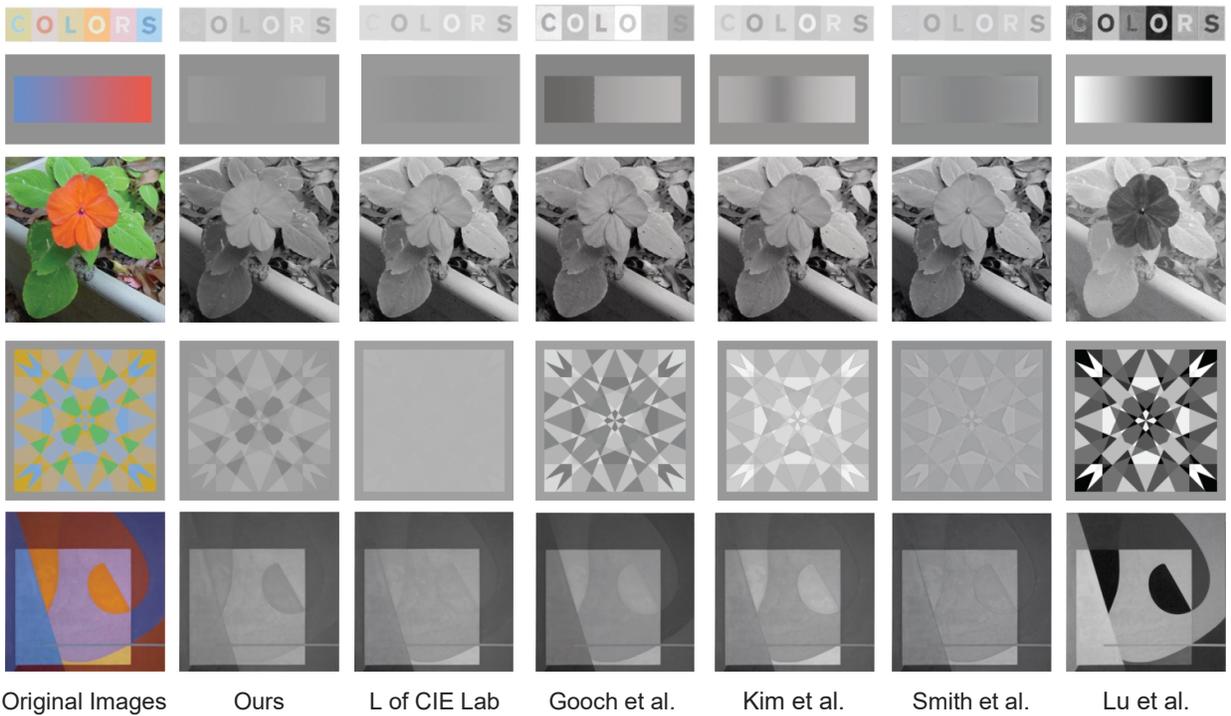
#### 194 3.1 Comparison with related decolorization methods

195 When evaluating our method, we focused on the following points:

- 196 • Objective and subjective image quality assessment.
- 197 • Compare their processing speeds.



**Fig 7** Examples to demonstrate limitation of our decolorization method when mapping bright green/neon color.



**Fig 8** Color to gray conversion comparison with other decolorization methods.

198 The evaluations demonstrated that our method does reflect human perception better than or equal  
 199 to other optimized methods (refer sections 3.2 and 4.3). It delivers high-speed processing, and  
 200 is a useful tool for many image processing applications. Figure 8 shows a comparison between  
 201 our proposed method and other decolorization methods, and a detailed subjective evaluation is

202 presented in section 3.3. For this comparison we have used images from Cadik’s dataset.<sup>27</sup> In Fig.  
203 8 first and second columns from the left are original images and images obtained with our method  
204 respectively. The images in the third column from the left were obtained with the  $L$  component of  
205 the CIELAB color space, which is a reversible model reflecting human visual characteristics. The  
206 images in columns four, five and six were obtained from global decolorization methods, which  
207 means only one conversion function is applied to each pixel. For example, in these methods,  
208 optimization techniques referring to whole pixels are applied to luminance conversion without  
209 regard to the brightness perceived by human perception. The images in the far right column were  
210 obtained with a local method that refers to pixel values in the local patch of the image for contrast  
211 enhancement.

212 In the  $L$  component of the CIELAB color space, the base luminance is  $Y$  in the YCbCr color  
213 space; the luminance is also mapped along with the color order of  $Y$ . In the image (third column,  
214 fourth row), since the luminance of all colors are the same in  $Y$ , output values are also the same  
215 in the CIELAB color space. However, we can perceive the contrast in this image. Thus, an  
216 appropriate conversion is required; our method can generate the perceived contrast in this image.  
217 Gooch et al.<sup>4</sup> obtained the highest average C2G-SSIM score but clearly a step artifact occurs in  
218 the gradation image (fourth column, second row). Kim et al.<sup>7</sup> proposed an improved version of  
219 Gooch’s method that achieves high-speed optimization and reflects the H-K effect.<sup>3</sup> In this method,  
220 since a weighting function is applied for expanding luminance distribution of whole pixel colors  
221 in the image along with chrominance, its conversion becomes different in each image. Thus, over-  
222 enhancement is observed in the images (fifth column, first row) and (fifth column, fourth row).  
223 The output images of our method are similar to those of Smith et al.<sup>6</sup> Their method uses the H-K  
224 effect, but it also requires a lot of processing time for post-unsharp-mask filtering. In Lu et al.,<sup>8</sup>

**Table 1** Run-time comparison table with other decolorization algorithms.

Algorithm	Processing time	Image size W×H	CPU Clock Speed	Optimization	Process	Normalized Time*
Gooch et al. <sup>4</sup>	25.7s	200×200	-GPU-	✓	Global	N/A
Kim et al. <sup>7</sup>	102ms	320×240	2.66GHz	✓	Global	1.30μs
Smith et al. <sup>6</sup>	6.7s	570×593	3.0GHz	×	Global+Local	22.02μs
Lu et al. <sup>8</sup>	800ms	600×600	3.80GHz	✓	Global Contrast	3.12μs
Song et al. <sup>12</sup>	40ms	320×240	N/A	×	Local Contrast	N/A
Ancuti et al. <sup>10</sup>	100ms	800×600	2.5GHz	×	Local Contrast	0.19μs
L of CIE Lab	25.57ms	800×600	2.7GHz	×	Global	0.053μs
Ours low res	<b>16.71ms</b>	800×600	2.7GHz	×	Global	<b>0.034μs</b>
Ours high res	<b>202.05ms</b>	3008×2008	2.7GHz	×	Global	<b>0.033μs</b>

\* Normalized time is the processing time normalized by frequency (2.7 GHz) and divided by the number of pixels. It indicates the effective processing time per pixel.

225 their method does not reflect human perception; they try generating high contrast images for mask  
 226 images that are input to an edge-preserving filter such as a guided filter.

227 Table 1 lists the processing speed of various methods, our proposed implementation and the  
 228 CIELAB were implemented in C++; these codes were executed on an Intel Core i5-5257U (2.70GHz)  
 229 CPU without any multicore, multithread or SIMD operations. The results confirmed that our  
 230 method had the fastest run-time among the methods compared. It is worth noticing that it ex-  
 231 ceeded CIELAB in runtime; this indicates it also has advantages in total calculation cost including  
 232 post-processing. Its computational complexity is only  $O(1)$  because it performs exact pixel by  
 233 pixel processing, referring only to the RGB value at each pixel. Among other methods, the one de-  
 234 veloped by Gooch et al. was reported to have  $O(n^4)$  computational complexity. Using  $O(1)$  spatial  
 235 filtering it is possible to develop  $O(1)$  local methods,<sup>10,12</sup> but the filter calculations required would  
 236 degrade their run-time in comparison to our decolorization method. The proposed color to gray  
 237 technique has demonstrated faster run-time than local methods by maintaining global coherence,  
 238 which means the conversions were the same in all pixels.

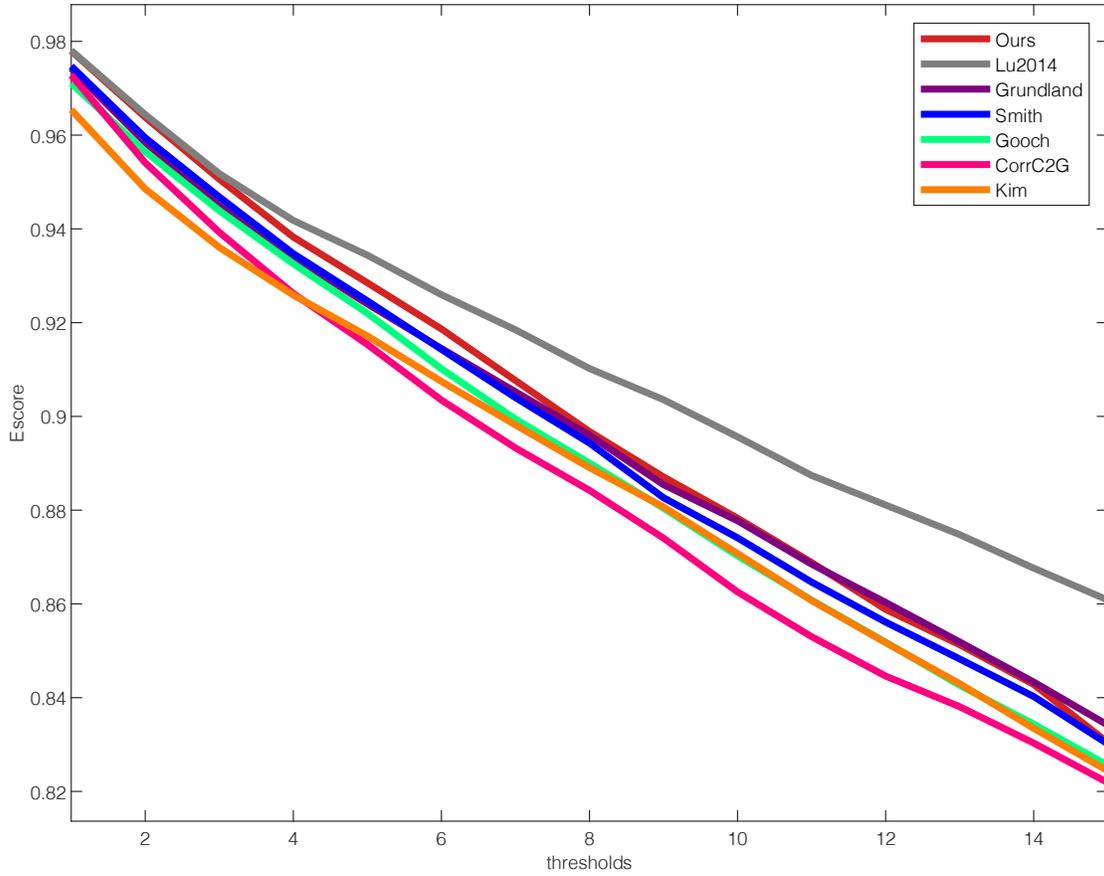
**Table 2** Comparison of seven color to gray methods based on average objective metrics for 250 images.

	Decolorization	CCFR	CCPR	E-score	C2G-SSIM
(a)	Lu et al. <sup>20</sup>	0.9922	0.9645	0.9781	0.8900
(b)	Nafchi et al. <sup>30</sup>	0.9880	0.9555	0.9710	0.8900
(c)	Grundland et al. <sup>5</sup>	0.9811	0.9584	0.9747	0.8749
(d)	Smith et al. <sup>6</sup>	0.9880	0.9555	0.9710	0.8935
(e)	Gooch et al. <sup>4</sup>	0.9839	0.9545	0.9714	0.9062
(f)	Kim et al. <sup>7</sup>	0.9682	0.9310	0.9047	0.8569
(g)	Ours	0.9890	0.9576	0.9728	0.9018

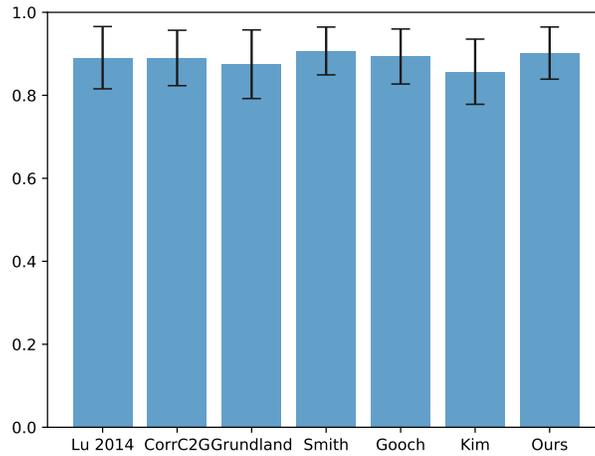
### 239 3.2 Objective Image Quality Assessment

240 In our experiments, we utilized the color250 dataset which comprises of 250 natural and synthetic  
241 color images.<sup>20</sup> To quantitatively evaluate our decolorization algorithm we choose two objective  
242 metrics: E-score and C2G-SSIM by Ma et al.<sup>28</sup> E-score is a joint measure proposed by Lu et  
243 al., a harmonic mean which is computed by combining two metrics: Color Contrast Preserving  
244 Ratio (CCPR), and Color Content Fidelity Ratio (CCFR).<sup>20</sup> The CCPR is useful in maintaining  
245 the color contrast in decolorization images which is perceivable to humans. Specifically, when  
246 the color difference is smaller than a certain threshold value, it becomes undetectable to humans.  
247 Furthermore, CCFR estimates if the decolorization image is accurate in terms of structures when  
248 compared to the original color image. C2G-SSIM is new color to gray objective evaluation metric  
249 based on the Structural Similarity (SSIM) index quality metric.<sup>29</sup> The C2G-SSIM generates quality  
250 map and has good correlation with HVS subjective preference. Table 2 presents the average E-  
251 score and C2G-SSIM for the color 250 dataset in comparison with other decolorization methods.

252 In our experiment we computed the average CCPR for the 250 images in the dataset by varying  
253  $\tau$  from 1 to 15.<sup>20</sup> As can be seen from Fig .9, our algorithm’s performance is reasonable and  
254 practicable when compared to other color to gray algorithms. Figure 10 shows the average C2G-  
255 SSIM score for the seven decolorization methods. According to the plot in Fig .9, Lu et al.’s  
256 method shows best performance based on the E-score, however, our method delivers high average

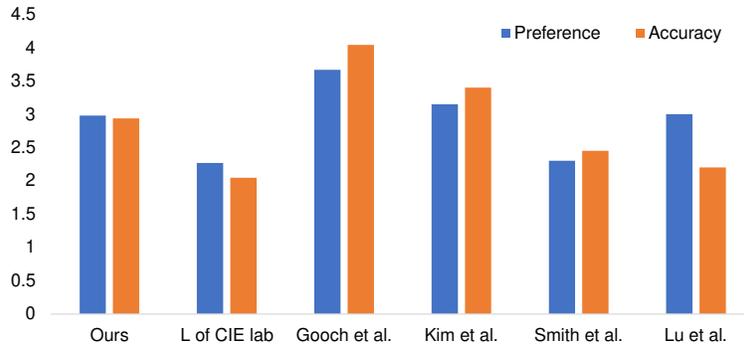


**Fig 9** Comparison of seven color to gray methods based on the E-score.



**Fig 10** Comparison of seven color to gray methods based on the C2G-SSIM score.

257 C2G-SSIM measure which is better correlated to human perception.<sup>30</sup>



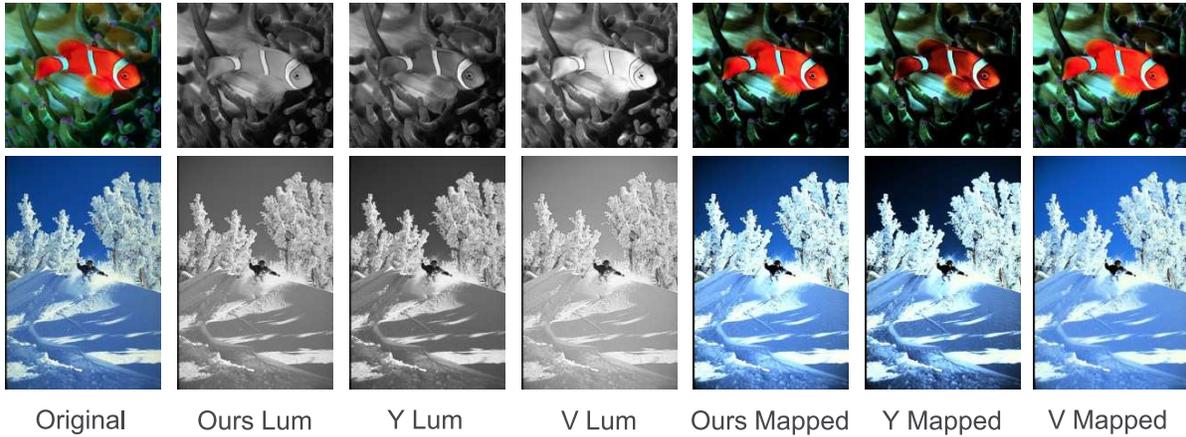
**Fig 11** Subjective visual test survey and mean opinion score.

### 258 3.3 Subjective Image Quality Assessment

259 The main objective of our perceptual evaluation is to determine the accuracy and preference<sup>20,27</sup>  
 260 of our decolorization method. Our study group of 15 students (9 males, 6 females, average age =  
 261 23) were shown five sets of images (refer Fig. 8) from Cadik’s dataset.<sup>27</sup> The group was asked  
 262 to evaluate the images and assign points to them on a scale of 1 (low) to 5 (high) for accuracy  
 263 and preference. For the first task, that is to measure the accuracy they compared the original  
 264 color images to their decolorized output image. For the preference measurements, the user group  
 265 compared the decolorized images only, i.e., without referring to the corresponding color image.

## 266 4 Tone mapping application

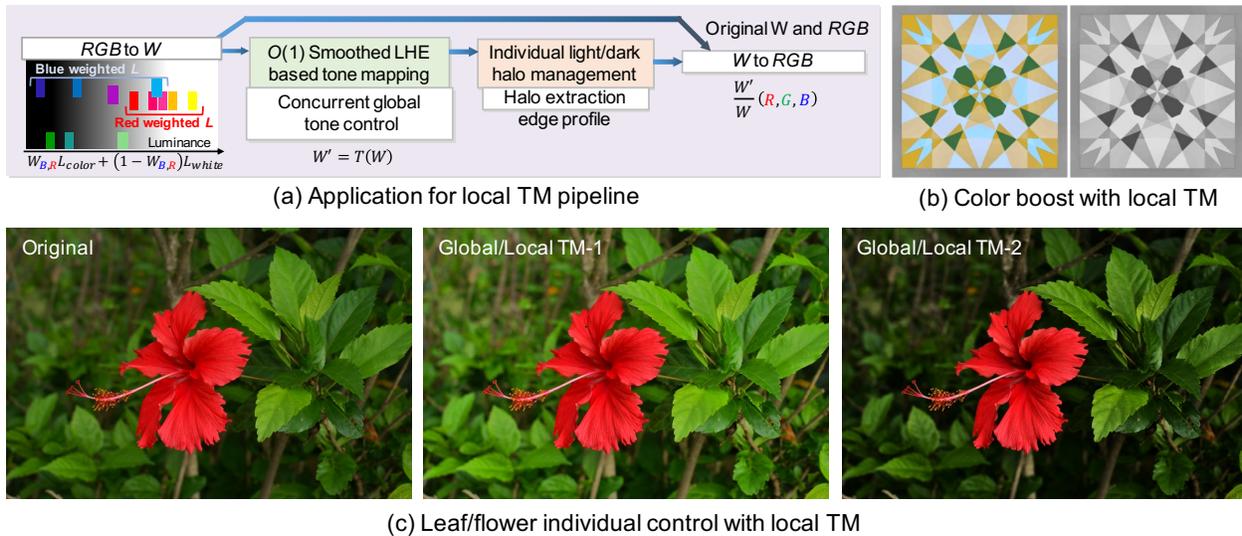
267 The color to grayscale conversion is a dimensionality reduction problem whose significance has  
 268 been underestimated. Usually the tone mapping is performed on the grayscale image because of  
 269 the lower computational and memory requirements, when compared to tone mapping on the RGB  
 270 channels. In this section we will discuss global and local tone mapping application using the  
 271 proposed decolorization algorithm and demonstrate its effectiveness.



**Fig 12** Global tone mapping performed in three different luminance spaces: Ours,  $Y$  of YCbCr and  $V$  of HSV

#### 272 4.1 Global tone mapping

273 We discuss our decolorization method’s applicability for post-processing tasks such as tone map-  
 274 ping. Conventional methods have not shown such applicability because of their long run-time;  
 275 thus, the use of  $Y$  of YCbCr or  $V$  of HSV for tone mapping is popular today. We evaluated our  
 276 method’s output of global tone mapping because it has the ability to adequately remap colors to  
 277  $1 - D$  luminance. Thus, even using global tone mapping confirms the effectiveness of our method.  
 278 Figure 12 shows tone mapped results using  $Y$ ,  $V$ , or our luminance channel. In the fish image,  
 279 using  $Y$ , the fish color became the same as the background and could not be controlled separately,  
 280 because the weight of  $R$  is small in the YCbCr color channel. Our method was able to separate  
 281 fish color from background in the same way as human perception and directly mapped the color  
 282 of the background to dark. In the sky and snow scene, the global tone curve for contrast enhance-  
 283 ment is a centered sigmoid curve, in which highlight/shadow clippings occur naturally. Since HSV  
 284 color space treats primary colors and whites the same way, colors of sky and snow were mapped  
 285 to luminance that was too light. Thus, the sigmoid function degraded the contrast of the outputted  
 286 image. YCbCr treats  $B$  as too low luminance; the sky became too dark. We confirmed that our



**Fig 13** Application: (a) Ideal image processing pipeline (tone mapping) (b) Color boosted by local tone mapping and corresponding grayscale image. (c) Demonstration example for easy control features using our decolorization algorithm. TM1: background boost TM2: background suppression

287 method generates well-balanced images maintaining the contrast and the colors.

## 288 4.2 Local tone mapping

289 Local histogram equalization based local tone mapping converts target pixels by using tone curves  
 290 constructed from local cumulative histograms. Smoothed local histogram equalization (LHE) are  
 291 also used as a smoothed LH filter.<sup>31</sup> The Apical's (ARM<sup>®</sup>) Iridix algorithm,<sup>32</sup> which is based on  
 292 smoothed LHE are used by a range of camera makers, including Nikon, Olympus and Sony. For  
 293 our local tonemap application we selected smoothed LHE-based function as they are very suitable  
 294 for practical real-time applications, in Fig. 13(a) we show an ideal pipeline for such a system.  
 295 We implemented the local tonemap application similar to one presented by Ambalathankandy et  
 296 al.,<sup>33</sup> as their implementation has a linear  $O(1)$  computational complexity and produces output  
 297 images with fine quality as shown in Fig. 13(b, c). The total computational time including our  
 298 proposed decolorization and the local tonemap operation was only  $14.7\mu s$  per pixel (normalized  
 299 time @2.7GHz CPU). This time utilization is  $20\times$  less than Lu et al.'s work.<sup>8</sup> Additionally, using

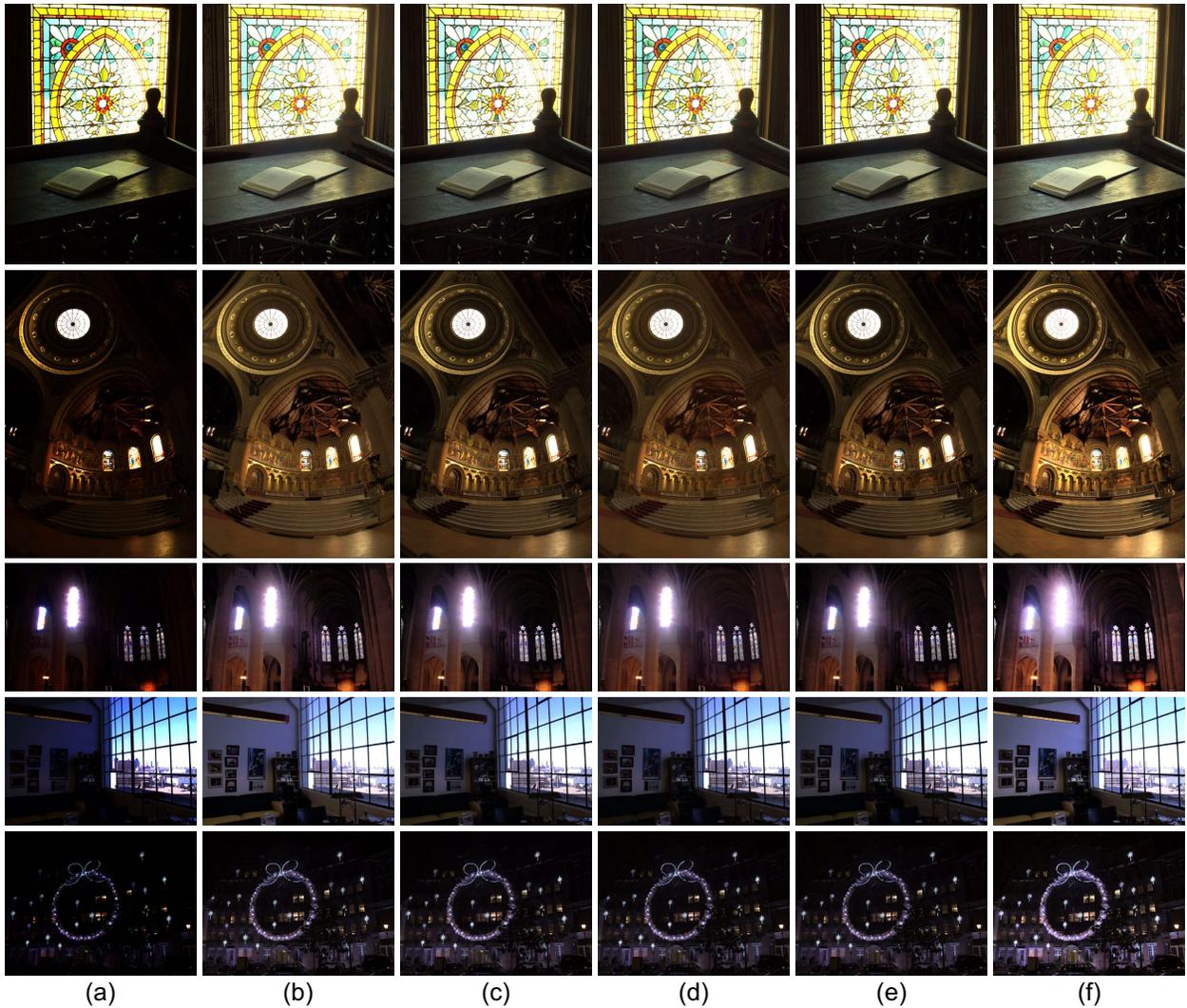
300 our decolorization method has an advantage, which is to individually control the back/foreground  
301 as shown in Fig. 13(c).

### 302 4.3 HDR tone mapping subjective user study

303 In this user study we collected response from an online survey of 50 volunteers (31 males, 19  
304 females, average age = 29). They evaluated five sets of HDR tone mapped images which are  
305 shown in Fig. 14. The main objective of this second user study is to judge the overall quality  
306 of the tone mapped images using different decolorized images which are obtained using simple  
307 histogram equalization method. Volunteers were asked to evaluate the tone mapped images for  
308 their overall perceptual quality, they rated 5 for images that were perceived as best with minimal  
309 artifacts on a scale 1 to 5. The compiled response of the user study group are presented in Fig. 15.

## 310 5 Conclusion

311 In this paper, we present warm-cool color-based RGB to gray conversion model by taking in to  
312 account the chromatic aberration phenomena. This anomaly results from differential refraction  
313 of light depending on its wavelength, it causes some of the rays (cool colors) to converge before  
314 others (warm colors). This results in a perception of warmer colors “advancing” towards the eye,  
315 while the cooler ones to be “receding”. Essentially, since decolorization is expected to have a  
316 key role in the pre-processing of tone mapping or edge preserving filters, low calculation cost and  
317 fast operation for the processing are required. To address this requirement, we have developed  
318 a high-speed  $O(1)$  decolorization method that is based on warm-cool color-based perception. It  
319 refers to RGB values in one pixel and performs weighted blending of the Euclidean distances of  
320 warm/cool color vectors. This simple conversion outputs a gray channel that is comparable to the

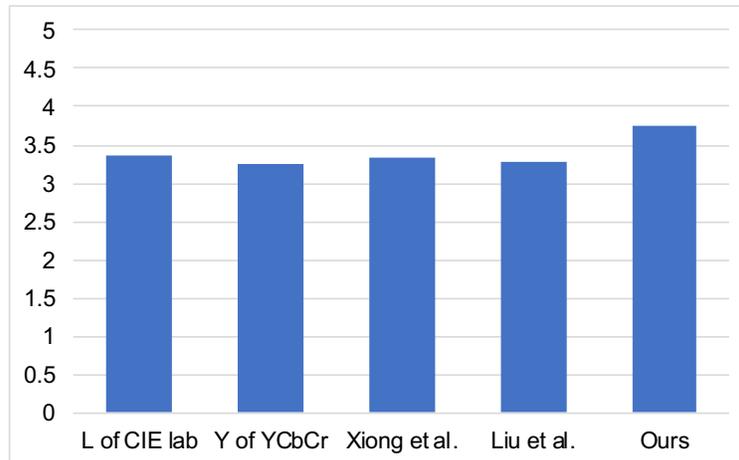


**Fig 14** Effect of different decolorization on HDR tone mapping using simple histogram equalization. (a) HDR test image. (b) CIELab (c) YCbCr (d) Xiong et al.<sup>34</sup> (e) Liu et al.<sup>35</sup> (f) Ours

321 conventional optimization methods using iterations. When our method is applied to tone mapping,  
 322 it achieves better results than one could be obtained with YCbCr/HSV color space.

### 323 5.1 Acknowledgments

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 325 other authors for sharing their source codes.



**Fig 15** Mean opinion score from the tone mapping subjective user study.

## 326 5.2 Biographies

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342 ing systems.

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## Appendix

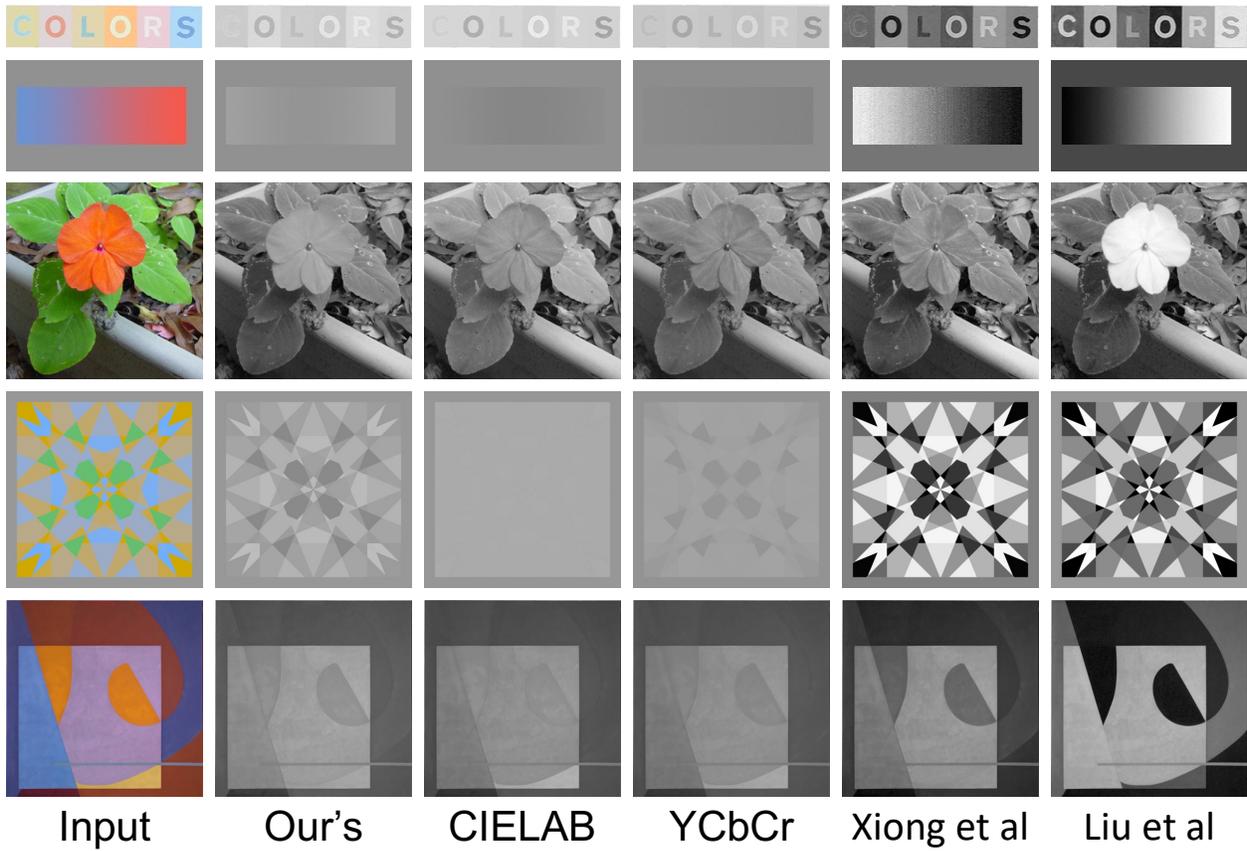
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The effectiveness of our decolorization algorithm for tone mapping application was evaluated in Sec. 4.3 with a subjective user study. Our proposed algorithm is compared with newer decolorization methods, whose color to gray performance was not included in Fig. 8 for brevity and clarity which is presented in Fig. 16.



**Fig 16** Color to gray conversion comparison using five images from Cadik's dataset.<sup>27</sup> Decolorization methods: Ours, CIELAB, YCbCr, Xiong et al.,<sup>34</sup> and Liu et al.<sup>35</sup>