



<b>Title</b>	Estimation of hybrid jig separation efficiency using a modified concentration criterion based on apparent densities of plastic particles with attached bubbles
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1 **Estimation of hybrid jig separation efficiency using a modified concentration criterion based on**  
2 **apparent densities of plastic particles with attached bubbles**

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18

19 **Abstract**

20 The hybrid jig which combines the principles of jig separation and flotation was recently developed to  
21 separate mixed-plastics with similar specific gravities (SG) effectively. In this type of jig, air bubbles are  
22 introduced during water pulsation to modify the apparent SG ( $SG_{\text{apparent}}$ ) of plastics by the attachment of air  
23 bubbles to the particles so that the hybrid jig can separate materials having identical SGs if their surface  
24 wettabilities are different. Because the change in  $SG_{\text{apparent}}$ , which is determined by the volume of attached  
25 bubbles on the particle surface, is critical for efficient separation in hybrid jigs, a method to estimate this  
26 parameter should be developed.

27 In this study, a laser-assisted measurement apparatus was developed to quantify the attached-  
28 bubble volume on plastics during water pulsation. Hybrid jig separation was also conducted using three  
29 mixtures containing plastics of almost identical SGs: (i) polyvinyl chloride (PVC)/polyethylene  
30 terephthalate (PET), (ii) polypropylene with glass fiber (PPGF)/high-impact polystyrene (HIPS), and (iii)  
31 cross-linked polyethylene (XLPE)/polyethylene (PE). Finally, to estimate the separation efficiency of  
32 hybrid jig, a new index called the apparent concentration criterion ( $CC_{\text{apparent}}$ ) is proposed. The results  
33 showed that  $SG_{\text{apparent}}$  and  $CC_{\text{apparent}}$  calculated using proposed methods could be used to estimate the hybrid  
34 jig separation efficiency.

35 **Keywords:** Recycling, jig, hybrid jig, plastic separation, attached-bubble volume

36

37 **Introduction**

38 The generation of plastic-dominated wastes has exploded globally in recent years primarily because of the  
39 wide availability and the unique properties of plastic-based materials that make them superior to traditional  
40 materials like wood and metals. Jambeck et al. [1] estimated that 275 million metric tons of plastic-  
41 dominated waste was generated in 192 coastal countries in 2010, with 4.8 to 12.7 million metric tons  
42 entering the ocean. Without proper disposal, majority of these wastes pose high risks of contaminating the  
43 environment because they contain numerous environmentally regulated contaminants like organic  
44 molecules, hazardous heavy metals, and toxic metalloids [2-5].

45 One of the most important approach to address these concerns is recycling because it not only  
46 lessens our dependence on natural mineral resources but also reduces the volume of wastes for disposal. In  
47 Japan, recycling laws were first enacted in 1998 for home appliances like air conditioners, televisions,  
48 refrigerators and washing machines, which were later extended to automobiles (2002) and small home  
49 appliances (2012) that included personal computers, mobile phones, digital cameras and clocks, game  
50 consoles, music players, and hair dryers [6]. For example, the amounts of automobile shredded residues  
51 (ASR) generated during the recycling of end-of-life vehicles (ELV) in the EU and Japan accounted for  
52 about 12–32% and 17% of the total weight of ELVs, respectively [7, 8]. In the EU, ASR is typically disposed  
53 of in landfills, which was similar to what was previously done in Japan before the enactment of the recycling  
54 law for automobiles. After the recycling law’s enforcement, material separation of secondary resources (i.e.,

55 various types of wastes including ASR), collection of slags from melting furnaces, and thermal recovery  
56 have become commonplace. As a result, Sakai et al. [8] reported that only 1–2% of the total weight of ELVs  
57 end-up in landfills because an additional 15–16% of components and materials were recovered. Recently,  
58 the Japanese government is planning to increase the material recycling ratio for combustible wastes  
59 especially mixed-plastics and reduce the amounts that end up for thermal recovery. For example, the  
60 Ministry of Environment of Japan has been supporting studies to improve material recycling including  
61 plastic-plastic separation from ASR [9].

62 Potentially effective techniques for the separation of various types of plastics in mixed-plastic  
63 wastes is the use of separation techniques from mineral processing [10]. For examples, gravity separation  
64 (e.g., sink–float separation [11], jig [12-15], cyclone [16]), magnetic separation (e.g., magnetic levitation  
65 (MagLev) [17], magnetic projection [18]), electrical separation (e.g., triboelectrostatic [19-21]), and  
66 flotation [22, 23]. Among these various separation techniques, wet separation methods are more widely  
67 used in mineral processing because they have higher efficiency as well as products are cleaner due to the  
68 washing process than dry-type separation techniques [24, 25].

69 Flotation is a common and very efficient wet separation methods in mineral processing for fine  
70 fraction ( $-75\ \mu\text{m}$ ) because fine grinding is typically required for the liberation of target minerals from its  
71 ores prior to flotation [2, 5]. Since, most minerals have hydrophilic surfaces, so a collector (e.g., xanthate  
72 and aerofloats [25]) is usually added to selectively change their surface wettability and enhance the

73 separation efficiency. In contrast, plastic flotation is usually carried out with wetting agents (e.g., AOT,  
74 NaLS, CaLS, TA, and PVA [22, 23]) since most plastics have inherently hydrophobic surfaces. Plastic  
75 flotation is also very challenging because in resources recycling, especially plastics, sufficient liberation is  
76 already achieved at relatively coarse particle sizes (mm–cm) [14]. Moreover, additional size reduction (i.e.,  
77 crushing and grinding) is required for flotation that requires more energy and incurs higher costs and energy  
78 [25].

79 One potentially effective technique for the separation of coarse plastics from mixed-plastic wastes  
80 is through the use of jigs. Jigs are gravity concentrators, machines that separate different kinds of materials  
81 with coarse size fractions (+ 0.5 mm) based on differences in their densities or specific gravities (SG), are  
82 well known in mineral processing especially for coal cleaning due to its simple operation, low cost, and  
83 high efficiency [24, 25]. Because traditional jigs are designed for ores, however, their direct application to  
84 mixed plastic wastes having lower SGs caused unpredictable fluidization behavior during separation  
85 resulting in very low separation efficiency [26], To address this serious drawback of conventional jigs,  
86 Tsunekawa et al. [12] developed the RETAC jig (R&E, Co., Ltd., Japan), a modified BATAAC jig, for plastic-  
87 plastic separation. The RETAC jig works by taking advantage of the very small SG differences between  
88 plastics through precision control of the wave form during jig separation [12, 13]. This advanced jig has  
89 been successfully applied to separate various plastics (e.g., polystyrene (PS), acrylonitrile butadiene styrene  
90 (ABS), and polyethylene terephthalate (PET)) from discarded copy machines [12]. A schematic illustration

91 of a desktop-type batch-wise RETAC jig is shown in Fig. 1(a). The reverse jig is a modified RETAC jig  
92 that could separate particles that are lighter than water by adding a screen on top of the separation chamber.  
93 Similar to the RETAC jig, the reverse jig separates particles by stratification based on differences in SGs.  
94 In the separation chamber, particles move up and down underneath the top screen and stratification occurs  
95 because of the differences in levitation velocities of particles. The reverse jig has been successfully applied  
96 to separate polypropylene (PP) and high-density polyethylene (HDPE) from waste containers [26].

97 Another challenging problem in the recycling of plastic-dominated waste streams is the separation  
98 of mixed-plastic wastes with almost identical SGs. Hori et al. [27] found a workaround to this dilemma by  
99 combining the principles of gravity separation and flotation to develop a density/surface-based technique  
100 called the hybrid jig (Fig. 1(b)). The hybrid jig can separate materials having identical SGs so long as their  
101 surface wettabilities are different. The hybrid jig is a more reasonable method for resources recycling  
102 compared with only surface-based technique like flotation because it operates at a coarser liberation size.

103 In flotation, attachment of many bubbles is required to float the particle up to the water surface,  
104 but in a hybrid jig, only a small amount of bubbles are needed to change the “apparent” specific gravity  
105 ( $SG_{\text{apparent}}$ ) of particle, so it is ideal for the separation of coarse plastics even with similar SG. In hybrid jig  
106 separation (Fig. 1(b)), an aeration tube is installed under the screen (particle bed) to generate air bubbles  
107 inside the separation chamber. When bubbles attach to particles, their apparent SG becomes lower than  
108 those particles without or less attached bubbles, so particles with extremely small identical SGs difference

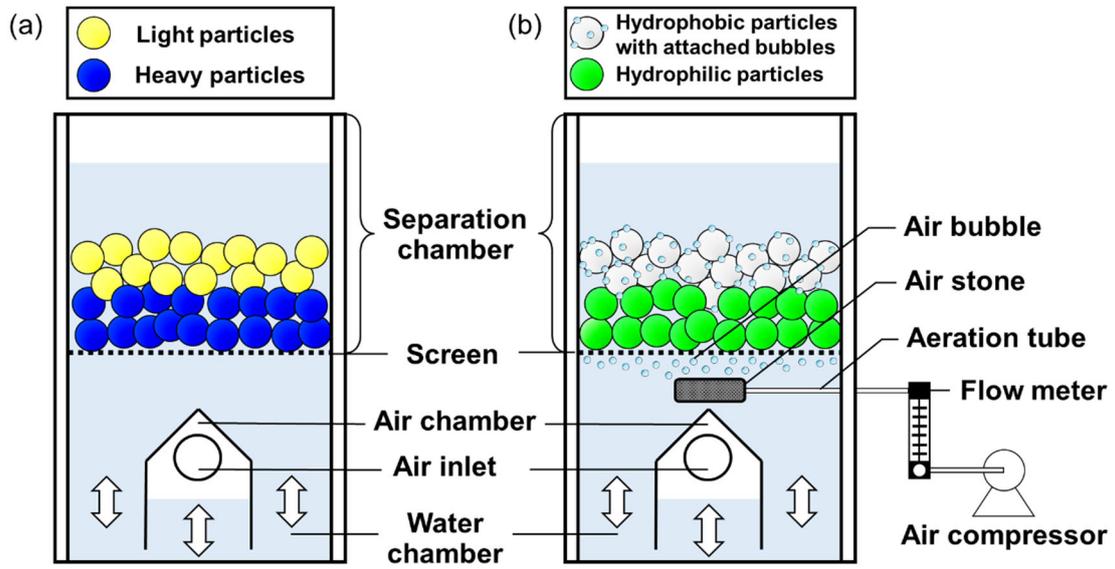
109 could be successfully separated due to jiggling stratification [27-29].

110           The authors recently reported dramatic improvement on the hybrid jig separation efficiency by  
111 adding wetting agents (e.g., Aerosol OT (AOT), sodium lignin sulfonate (NaLS), tannic acid (TA) to control  
112 the surface wettability of plastics [29]. The authors also showed that the volume of bubbles attached on  
113 plastic particles, which is directly related to  $SG_{\text{apparent}}$ , is an important parameter for hybrid jig separation.  
114 Bubble attachment is also a crucial parameter in flotation, which is generally determined by the hallimond  
115 tube test and contact angle measurements to optimize the process [29-31]. Unfortunately, the hallimond tube  
116 test and contact angle measurement cannot estimate volume of bubble attached on plastic and the motion  
117 of the particle with attached bubbles during hybrid jig separation and flotation are different (i.e., hybrid jig  
118 has pulsing motion (upward and downward motion) while flotation has levitation motion (only upward  
119 motion). Thus, hybrid jig needs standard testing methods to determine the volume of bubbles attached on  
120 plastics during water pulsation because the change in  $SG_{\text{apparent}}$ , which is determined by the volume of  
121 attached bubbles on the particle surface, is critical for efficient separation in hybrid jigs.

122           In this study, a laser-assisted measurement apparatus was developed to quantify the attached-  
123 bubble volume on plastics during water pulsation. Hybrid jig separation was also conducted using three  
124 mixtures containing plastics of almost identical SGs: (i) polyvinyl chloride (PVC)/polyethylene  
125 terephthalate (PET), (ii) polypropylene with glass fiber (PPGF)/high-impact polystyrene (HIPS), and (iii)  
126 cross-linked polyethylene (XLPE)/polyethylene (PE). Finally, a new index called the apparent

127 concentration criterion ( $CC_{\text{apparent}}$ ) is proposed to estimate the separation efficiency of hybrid jig separation.

128



129

130 **Fig. 1** A schematic illustration of (a) RETAC jig, and (b) Hybrid jig.

131

132 **Materials and methods**

133 **Samples**

134 Three mixtures, each having two types of plastic with almost identical SGs, size, and shape [14]: (i) virgin  
135 plastics of PVC and PET (+2.8–4.0 mm size fraction, pellets with 4x4x2 mm dimension), (ii) crushed  
136 plastics of PPGF and HIPS obtained from a recycling facility of home appliances in Japan (+2.8–5.6 mm  
137 size fraction with  $D_{50} = 4.59$  and 4.56 mm, respectively), and (iii) crushed plastics of XLPE and PE obtained  
138 from an eco-electrical wire recycling plant in Japan (+6.7–8.0 mm size fraction), were used for the hybrid  
139 jig separation tests and the measurement of attached-bubble volume using the laser-assisted measurement  
140 setup (Table 1).

141

142 **Table 1** Specific gravities of plastic samples

Plastic samples	Specific gravity (SG)
Polyvinyl chloride (PVC)	1.31
Polyethylene terephthalate (PET)	1.31
Polypropylene with glass fiber (PPGF)	1.043
High impact polystyrene (HIPS)	1.038
Cross-linked polyethylene (XLPE)	0.93
Polyethylene (PE)	0.92

143 **Hybrid jig separation tests**

144 Hybrid jig separation tests were carried out using a batch-type hybrid jig with a separation chamber 145  
145 mm long, 155 mm wide, and 320 mm high. Each separation test was carried out in 18 L distilled water  
146 containing 20 ppm of methyl isobutyl carbinol (MIBC, Wako Pure Chemical Industries Ltd., Japan), a  
147 reagent widely used in flotation to stabilize bubble formation in solution.

148 Hybrid jig separation experiments were conducted under the following conditions: displacement  
149 of 20 mm, frequency of water pulsation equal to 30 cycles/min, and separation time of 3 min. The amounts  
150 of samples, particle size, air flow rate, and type as well as of wetting agents used for each plastic mixture  
151 that were selected based on preliminary experiment according to Ito et al. [29] are summarized in Table 2.  
152 After the hybrid jig separation, products were divided into six layers from the top and collected using a  
153 vacuum sampling system. Particles in the layers were separated by hand to determine the purity of each  
154 layer.

155

156 **Table 2** Conditions of hybrid jig separation tests

Plastic mixture	Amount of sample [g]	Particle size [mm]	Air rate [mL/min]	Wetting agent*
PVC/PET	500	+2.8–4.0	1000	NaLS** (50 ppm)
PPGF/HIPS	500	+2.8–5.6	1500	TA*** (350 ppm)
XLPE/PE	300	+6.7–8.0	1000	TA*** (50 ppm)

157 \*The amount and type of wetting agent were selected based on preliminary experiment according to Ito et

158 al. [29].

159 \*\*Sodium Lignin Sulfonate (Tokyo chemical industry Co., Ltd., Japan),

160 \*\*\*Tannic acid (Wako Pure Chemical Industries Ltd., Japan)

161

162 **Attached-bubble volume determination under water pulsation using the laser-assisted measurement**

163 **setup**

164 To estimate the hybrid jig separation efficiency using a modified concentration criterion based on apparent  
165 densities of plastic particles with attached bubbles, a special laser-assisted apparatus using a small scale  
166 batch-type hybrid jig with a separation chamber 60 mm long, 60 mm wide, and 150 mm high to measure  
167 the volume of attached bubbles on plastic particles was proposed (Fig. 2). In this setup, air bubbles are  
168 introduced by a pump under the particle bed, then attach to the particles and rise the water level in the water  
169 chamber. This water level rise is accurately measured and recorded by the laser-based level sensor system  
170 (IL-S100, Keyence Corporation, Japan), and the attached-bubble volume can then be calculated from  
171 changes in water level inside the separation chamber before and after bubble introduction. Measurements  
172 of attached-bubble volume were carried out under static and pulsed water conditions.

173 For the attached-bubble volume measurements, water was first put into the water chamber of a  
174 small scale batch-type hybrid jig where an inner column was set with a bottom screen to hold the plastic  
175 samples. A space between the water chamber and inner column (air chamber) was sealed with a flange  
176 connected to the top of the inner column. A tube with an air stone as a bubble generator is set in the air  
177 chamber through the hole of the flange. Air bubbles from an air pump are introduced from the bottom of  
178 the inner column. The water level was measured by a laser-based level sensor using a floating reflector on  
179 top of the water surface. A hand pump was connected to the air chamber through the hole in the flange to

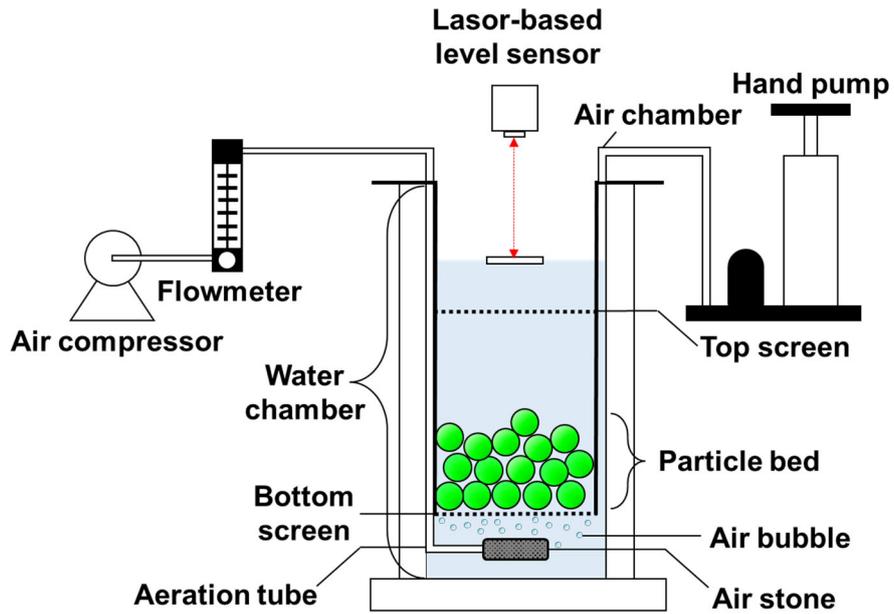
180 facilitate water pulsation. When air bubbles are introduced from the bottom of the water chamber, they rise  
181 through the particle bed and attach to plastic particles, changing the water level in proportion to the volume  
182 of attached air bubbles. The volume of attached bubbles was calculated using a calibration curve (Fig. 3  
183 and Eq. 1).

$$184 \qquad \qquad \qquad \Delta V = 7.55 \times \Delta H \qquad \qquad \qquad (1)$$

185 where  $\Delta V$  and  $\Delta H$  are the additional water volume [mL] and change of water level [mm] due to the volume  
186 of attached bubble, respectively.

187 Fig. 4 shows a schematic diagram of attached-bubble volume measurement procedure. Each kind  
188 of plastic sample was placed in 1 L of distilled water containing 20 ppm of MIBC, which was added to  
189 stabilize bubble formation. Aeration (100 mL/min) and water pulsation (displacement: 20 mm and  
190 frequency: 30 cycles/min) was applied for 3 min and the change in water level after 3 min was measured  
191 (Fig. 4(a) and (b)). Then, one water pulsation to remove trapped bubbles in voids within the particle bed,  
192 as will be further described later, was given and the water level was measured (Fig. 4(c)). This procedure  
193 was repeated a total of 4 times to remove trapped and unattached bubbles. A brief summary of conditions  
194 of the attached-bubble volume experiments are listed in Table 3.

195

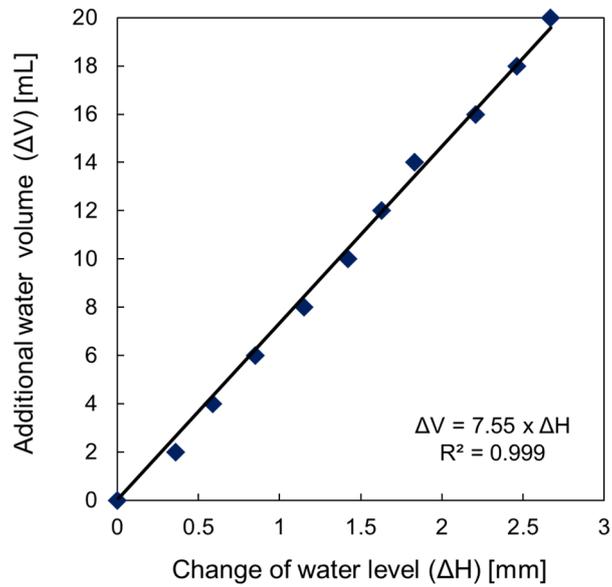


196

197 **Fig. 2** A schematic diagram of the laser-assisted measurement setup for the determination of attached-

198 bubble volume.

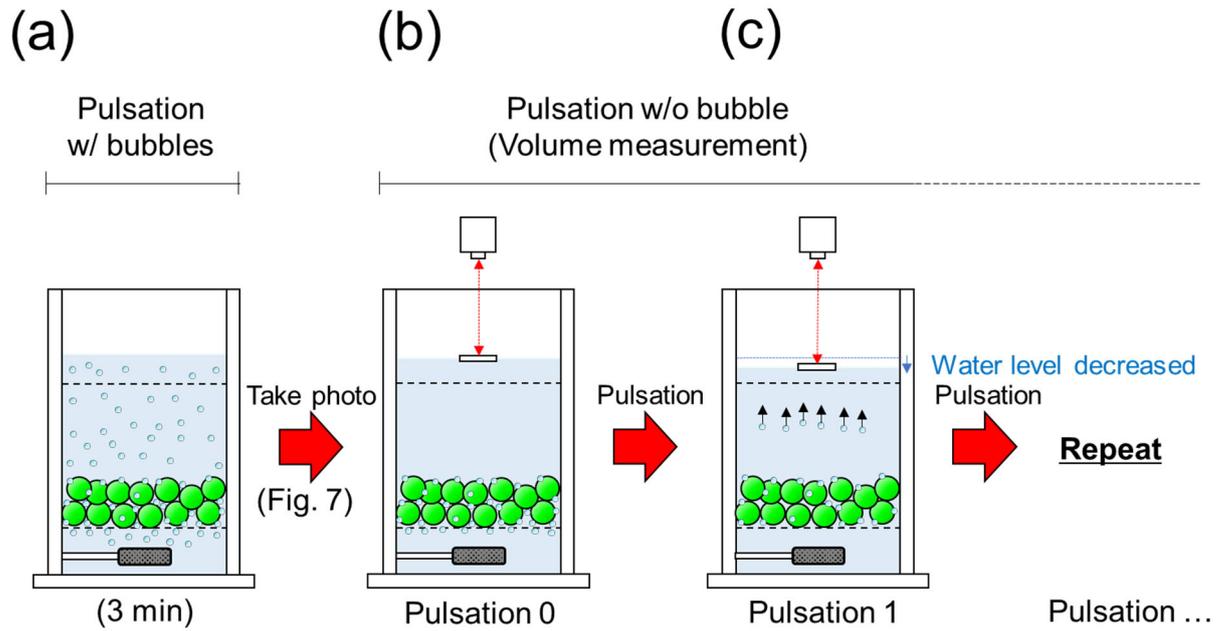
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200

201 **Fig. 3** Relationship between volume increase and water level rise in water chamber after bubble

202 introduction.



203

204 **Fig. 4** A schematic diagram of attached-bubble volume measurement procedure; (a) water pulsation with

205 bubble generation for 3 min, (b) measurement of water level after step (a), and (c) measurement of water

206 level after one pulsation of water without bubble generation to remove trapped bubbles in voids with in

207 particle bed.

208

209

210 **Table 3** Conditions for attached-bubble volume measurements.

Plastic mixture	Amount of sample [g]	Particle size [mm]	Air flow rate [mL/min]	Wetting agent
PVC/PET	50	+2.8 -4.0	100	NaLS (50 ppm)
PPGF/HIPS	50	+2.8 -8.0	100	Tannic acid (100 ppm)
XLPE/PE	30	+6.7 -8.0	100	Tannic acid (50 ppm)

211

212

213 **Results and Discussion**

214

215 **Hybrid jig separation tests**

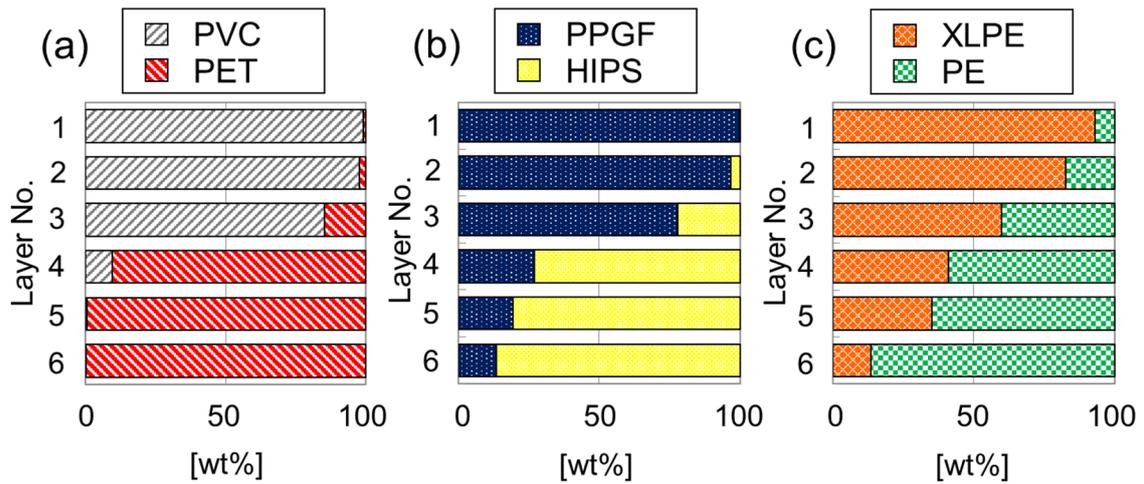
216 Fig. 5 shows the results of hybrid jig separation tests of the three plastic mixtures. In the PVC/PET mixture,  
217 PVC was concentrated in the top layers while PET was concentrated in bottom layers (Fig. 5(a)). Separation  
218 occurred even though these two plastics have identical SGs because PVC's  $SG_{\text{apparent}}$  (i.e., SG of particles  
219 with attached bubbles) became smaller than that of PET as a result of the preferential attachment of bubbles  
220 on the hydrophobic surface of PVC. Preferential bubble attachment occurred because PET became more  
221 hydrophilic due to the adsorption of wetting agent (50 ppm NaLS). Wetting agents could change the surface  
222 tension of solutions by changing the water–air surface properties and the surface wettability (contact angle)  
223 of plastics by surface adsorption, both of which lowered the bubble attachment probability [29]. In the case  
224 of wetting agents used in this study (i.e., NaLS and TA), according to the study of Ito et al. [29], the changes  
225 in surface tension were negligible and so, the selective attachment of bubbles on the one kind of plastic was  
226 occurred by the change of contact angle on plastic surfaces, so high separation efficiency could be obtained.

227 The results confirmed that plastics having identical SGs could be separated using the hybrid jig  
228 with wetting agent. For PPGF/HIPS and XLPE/PE mixtures, separation was also successfully done using  
229 the hybrid jig with wetting agents (Figs. 5(b) and (c)), however, purities of the top and bottom layers in  
230 PPGF/HIPS and XLPE/PE mixtures were lower than those obtained in the PVC/PET mixture, indicating

231 that an evaluation method is required to determine the attached-bubble volume on plastic surfaces for the

232 understanding and improvement of hybrid jig separation efficiency.

233



234

235 **Fig. 5** The proportion of plastics in each layer after hybrid jig separation of (a) PVC/PET with 50 ppm of

236 NaLS, (b) PPGF/HIPS with 350 ppm of TA, and (c) XLPE/PE with 50 ppm of TA.

237

238 **A novel method to estimate attached-bubble volume during water pulsation**

239 The separation efficiency of conventional jigs is typically estimated using the concentration criterion (CC),  
240 which is calculated using the following equation [25]:

$$241 \quad CC = \frac{SG_h - SG_f}{SG_l - SG_f} \quad (2)$$

242 where  $SG_h$  and  $SG_l$  are the SG of heavy and light materials, respectively while  $SG_f$  is the SG of fluid.

243 The CC is a parameter that estimates the degree of ease by which materials could be separated  
244 by gravity-based separation techniques like jigs. In other words, when the value of CC is high, separation  
245 via gravity separation would be relatively easy. This parameter could also be applied to estimate the  
246 efficiency of hybrid jig separation, but because  $SG_{\text{apparent}}$  is more important in this process than the inherent  
247 SGs of plastics, an estimation method for this value is required. To estimate the  $SG_{\text{apparent}}$  of particles, a  
248 laser-assisted measurement apparatus to quantify the volume of attached bubbles on particles was  
249 developed.

250 Fig. 6 shows the attached-bubble volume measured after 3 mins of aeration and pulsation while  
251 Figs. 7(a) and (b) are photographs of the samples after aeration illustrating bubbles attached to plastic  
252 particles and the bottom screen as well as those trapped in “voids” within the particle bed. The photographs  
253 shown in Fig. 7 indicate that the increase in volume immediately after stopping aeration was the sum of the  
254 volume of bubbles attached to plastics, trapped in “voids”, and those clinging on the bottom screen. To  
255 remove this “trapped” bubbles and facilitate the measurement of attached-bubble volume on particles, water

256 pulsation without further aeration was repeated a total of 4 times (Fig. 4). The total volume within the water  
257 chamber decreased after each succeeding water pulsation and visual inspection showed that “trapped”  
258 bubbles were removed by simply doing repetitive water pulsations. It is also interesting to note that the bulk  
259 of “trapped” bubbles were removed after the first water pulsation, and volume reduction after the 2<sup>nd</sup>, 3<sup>rd</sup>,  
260 and 4<sup>th</sup> pulsations could be attributed to the detachment of bubbles not firmly attached to plastic particles.  
261 These results suggest that in addition to “trapped” bubbles, there are two types of bubbles on plastic  
262 particles: (i) bubbles that are only loosely attached (“trapped” by “voids” not directly attach on the particle  
263 surface and could be detached by water pulsation), and (ii) bubbles that are firmly adhered to particles  
264 (could not be detached by water pulsation) (Fig. 7(c)). To estimate the volume of these two kinds of bubbles,  
265 Eq. (3) were formulated.

$$266 \qquad \qquad \qquad V_S = V_0^*(1 - P_D)^n \qquad \qquad \qquad (3)$$

267 where  $P_D$  is the probability of detachment of bubbles attached to particles (an empirical parameter obtained  
268 from the experiments), ‘n’ is the number of water pulsations, and  $V_0^*$  is the estimated value of attached-  
269 bubble volume immediately after aeration and water pulsation. Eq. (3) shows the volume of bubbles  
270 remaining after water pulsation ( $V_S$ ), which corresponded to bubbles that are firmly adhered to particles.

271  $V_0^*$  can be calculated by the least-square method from the data shown in Fig. 6 ( $V_0^*$  is the value  
272 extrapolated to  $x = 0$ ). The plots at 0 ( $V_0$  was an experimentally determined value at time = 0, without extra  
273 pulsations in Fig. 6) was excluded from the calculations because at this point, both “trapped” and attached

274 bubbles were present in the water chamber.

275 Fig. 8 shows the estimated attached-bubble volume on each type of plastic ( $V_0^*$ ) during water  
276 pulsation and  $V_0^*$  of PVC was observed to be larger than that of PET. Because the conditions during  
277 hybrid jig separation are very similar to those used to obtain  $V_0^*$ , this parameter could be used to estimate  
278 the apparent specific gravity ( $SG_{\text{apparent}}$ ) of plastics using Eq. (4).

$$279 \quad SG_{\text{apparent}} = \frac{SG_p}{1+V_0^*} \quad (4)$$

280 where  $SG_p$  is the inherent specific gravity of particles.

281 From Eq. (2) – (4), the modified concentration criterion based on  $SG_{\text{apparent}}$  of plastic particles  
282 with attached bubbles or “apparent concentration criterion ( $CC_{\text{apparent}}$ )” was proposed as Eq. (5) to determine  
283 the suitability of hybrid jig separation.

$$284 \quad CC = \frac{SG_{\text{apparent},h} - SG_f}{SG_{\text{apparent},l} - SG_f} \quad (5)$$

285 where  $SG_{\text{apparent},h}$  and  $SG_{\text{apparent},l}$  are the  $SG_{\text{apparent}}$  of heavy and light materials, respectively.

286 Table 4 summarizes the apparent specific gravities ( $SG_{\text{apparent}}$ ) of each sample and the values  
287 calculated for PVC and PET were 1.05 and 1.18, respectively, which are both lower than the inherent SGs  
288 of these plastics (1.31). Using the values of  $SG_{\text{apparent}}$ , the apparent concentration criterion ( $CC_{\text{apparent}}$ ),  
289 concentration criterion based on the apparent specific gravity ( $SG_{\text{apparent}}$ ), could be calculated and the results  
290 are summarized in Table 5.

291 Fig. 9 illustrates the purity distribution curves as a function of height (distance from the bottom

292 screen, H) of the hybrid jig separation (Fig. 5). The vertical axis is the purity of plastics concentrated in the  
 293 bottom layer while the horizontal axis refers to the distance between the middle of particle bed and screen  
 294 (H).

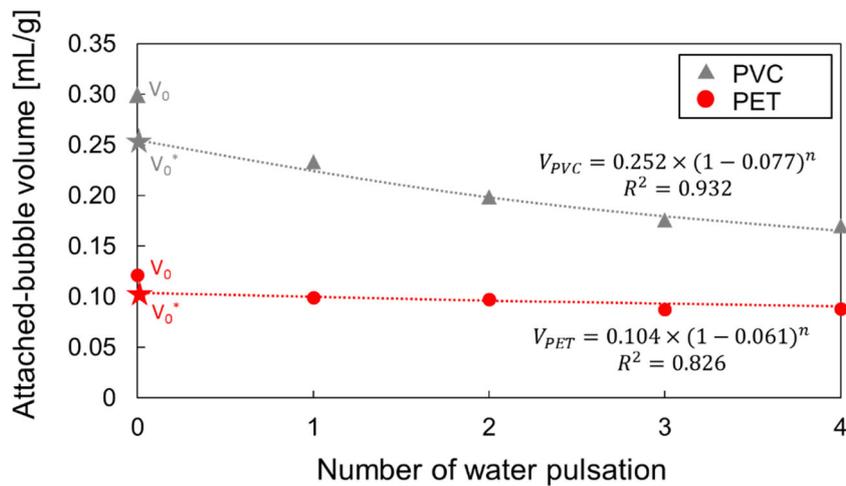
295 The sharpness index of separation (SI) could be calculated from Fig. 9 by following Eq. (6) [32],  
 296 and the values of SI for the three mixtures of plastics are listed in Table 6.

$$297 \quad SI = \frac{H_{84.13} - H_{50}}{H_{50}} \quad (6)$$

298 where  $H_{50}$  and  $H_{84.13}$  are the heights when purities are 50 and 84.13%, respectively [32].

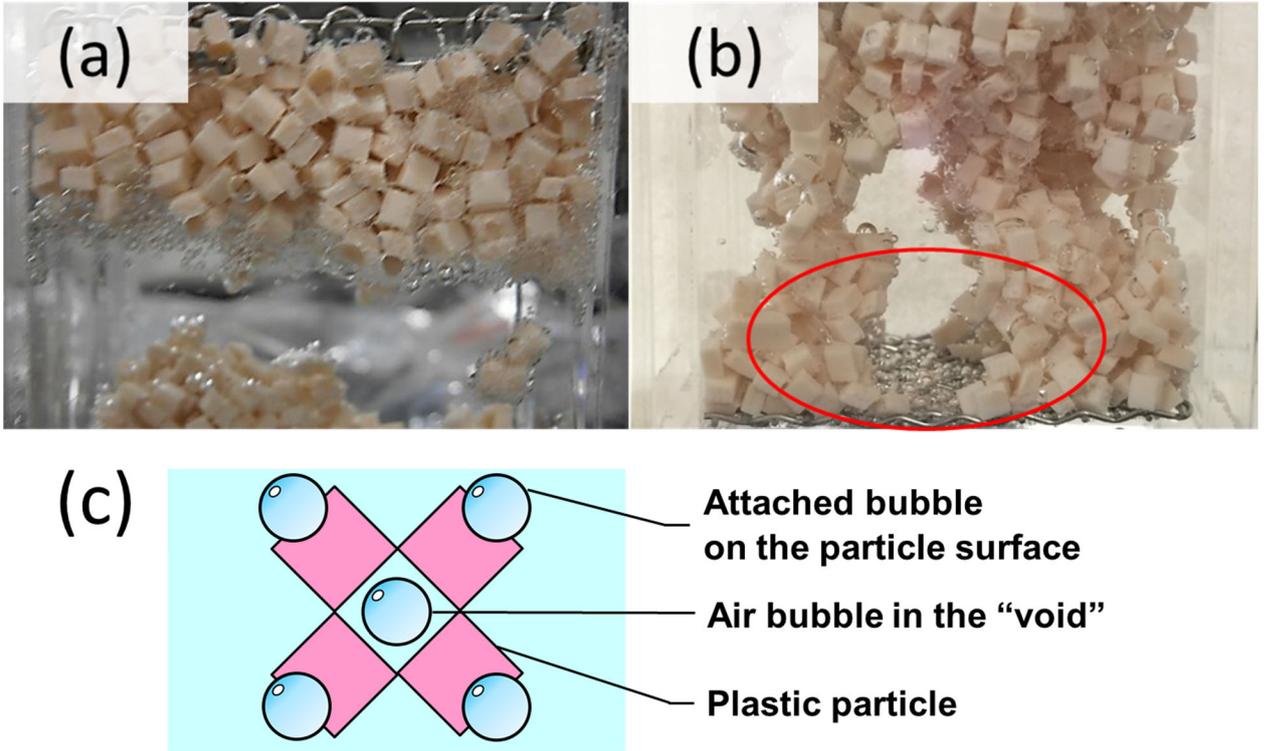
299 The relationship between the  $CC_{\text{apparent}}$  (Table 4) and SI (Table 5) is shown in Fig. 10. The values  
 300 of SI were low when the separation efficiency was high, suggesting that values of  $CC_{\text{apparent}}$  obtained with  
 301 the attached-bubble volume measurement apparatus was useful in the estimation of SI values for hybrid jig  
 302 separation.

303



304

305 **Fig. 6** Attached-bubble volume on PVC and PET as a function of water pulsation without air introduction.

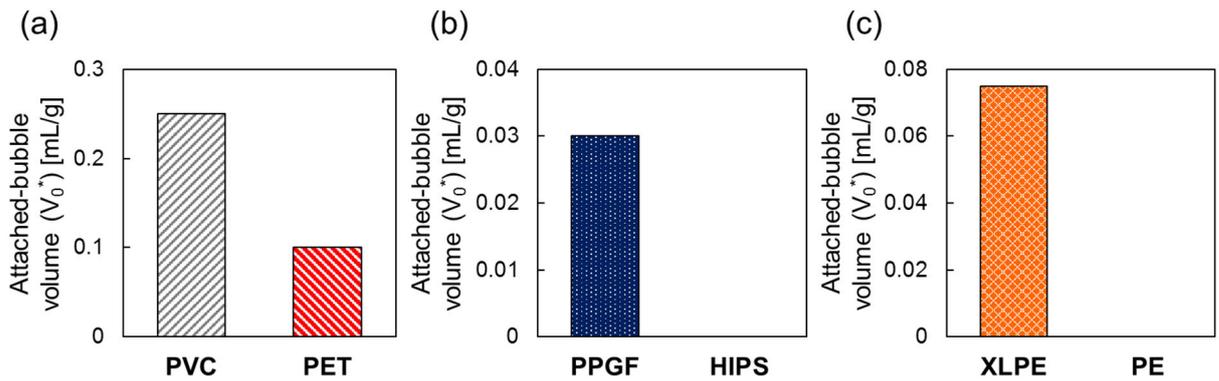


306

307 **Fig. 7** Photographs of (a) bubbles in the "void" and (b) bubbles attached on the bottom screen, and (c) a

308 schematic diagram of air bubble in the void and on the particle surface.

309

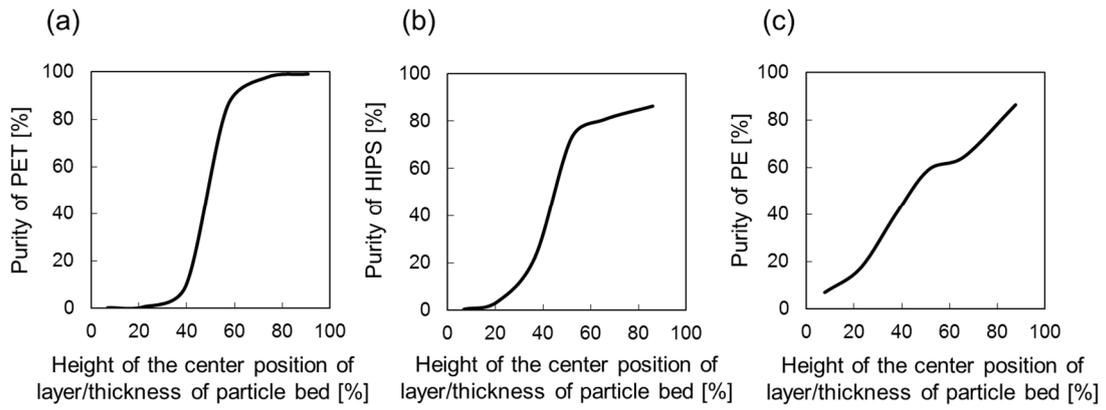


310

311 **Fig. 8** Estimated volume of attached bubble on (a) PVC/PET in NaLS 50 ppm solution, (b) PPGF/HIPS in

312 TA 100 ppm solution, and (c) XLPE/PE in TA 50 ppm solution.

313

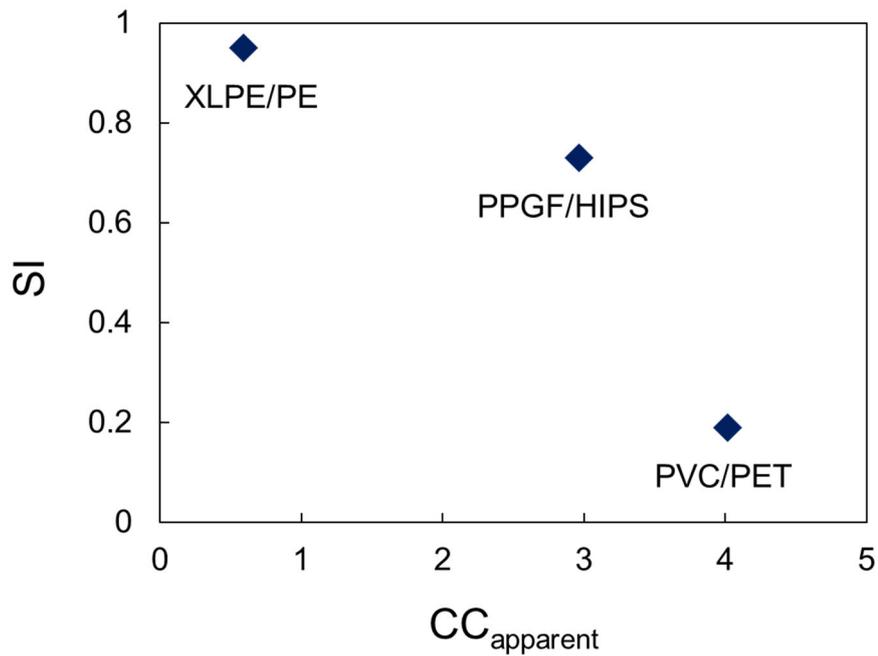


314

315 **Fig. 9** Purity distribution curves as a function of height of hybrid jig separation of (a) PVC/PET with 50

316 ppm of NaLS, (b) PPGF/HIPS with 350 ppm of TA, and (c) XLPE/PE with 50 ppm of TA.

317



318

319 **Fig. 10** Relationship between sharpness index (SI) and concentration criterion using apparent specific

320 gravity ( $CC_{\text{apparent}}$ ).

321

322 **Table 4** Apparent specific gravity of each sample

Sample	Specific gravity (SG)	Apparent specific gravity ( $SG_{\text{apparent}}$ )
PVC	1.31	1.05
PET	1.31	1.18
PPGF	1.043	1.013
HIPS	1.038	1.038
PE	0.93	0.86
XLPE	0.92	0.92

331

332 **Table 5** Apparent concentration criterion based on the apparent specific gravity in each separation test.

Separation test	Apparent concentration criterion ( $CC_{\text{apparent}}$ )
PVC/PET	4.0
PPGF/HIPS	3.0
XLPE/PE	0.59

333

334

335

336 **Table 6** Sharpness index of each separation test

Separation test	Sharpness index (SI)
PVC/PET	0.19
PPGF/HIPS	0.73
XLPE/PE	0.95

337

### 338 **Conclusions**

339 The extent of bubble attachment during hybrid jig separation strongly influences the separation efficiency  
340 of the technique and wetting agents can be used to modify the surface wettability of plastic to improve the  
341 separation. In this study, a laser-assisted apparatus was developed to measure bubble attachment during  
342 water pulsation and a novel method to estimate attached-bubble volume ( $V_0^*$ ) on plastic particles is  
343 proposed.  $SG_{\text{apparent}}$  and  $CC_{\text{apparent}}$  were calculated based on the measured  $V_0^*$  and a clear and distinct  
344 relationship between  $CC_{\text{apparent}}$  and SI was obtained. This means that the new techniques developed in this  
345 study are useful to optimize the conditions during hybrid jig separation.

346

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