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ADSORPTION BEHAVIOR OF WATER-SOLUBLE PROTEINS ONTO  
BUBBLES IN CONTINUOUS FOAM SEPARATION

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## ABSTRACT

The enriching mechanism of water-soluble proteins in continuous foam separation was studied. The liquid flow rate and the protein concentration in foam phase were measured at various heights from the interphase between bulk liquid and foam layer, and the intrinsic values at the interface were estimated by the extrapolation method to determine the accurate adsorption density on bubble surface. Ovalbumin (OA) and hemoglobin (HB) were used as the soluble proteins. The solution pHs were varied from 3.5, 4.6 and 6.0 for OA and from 6.0, 6.8 and 8.0 for HB. The experimental isotherms for OA and HB were compared to the Langmuir isotherm, and the two adsorption parameters of the equilibrium constant,  $K$ , and the saturated density,  $\gamma$ , at each pH were determined. Both  $\gamma$  values obtained for OA and HB showed maxima at their isoelectric point (i.e.p., pH 4.6 for OA and pH 6.8 for HB). Assuming that OA and HB molecules are spherical in shape and they are adsorbed on bubble surface in a closed packed structure at the saturated condition, the calculated diameters for OA and HB molecules were quite similar to the literature values. The variation in  $\gamma$  for both OA and HB were discussed qualitatively relating to the net charge of protein molecule.

## INTRODUCTION

The foam separation technique has been widely used in ore flotation (1) and waste water treatment (2) and so on. Recently, it appears that the separation of proteins by this method has been studied based on interest in applicability to food and biochemical industries (3-7). For the optimal design and operation of industrial processes, it is necessary to determine the adsorption and enriching mechanism of protein onto bubble surface in this technique.

The enriching process in foam separation technique is classified into two stages; (i) adsorption of objective substance onto bubble surface in dispersed bubble bed, and (ii) enriching in foam bed due to coalescence of bubble cells and liquid drainage. The former is well characterized by the physicochemical properties of objective substance, which influence the adsorption density at bubble-liquid interface and the production rate of bubble-liquid interfacial area. Adsorption behavior of proteins on bubble surface must be clarified to apply this technique to these foam separation processes. However, there are few reports on adsorption behavior of soluble proteins in foam separation method. The latter is common in all foam separations and would be a function of liquid properties, operating conditions and liquid content in foam layer.

In previous studies about foam separation (8-14), the adsorption density,

$X$ , on bubble surface have often been determined from a relationship concerning an overhead concentration based on the mass balance of the foaming column by following relationship

$$X = (W_f / S_b)(C_f - C_b) \quad [1]$$

where  $C_b$ ,  $C_f$ ,  $W_f$  and  $S_b$  represent the bulk and collapsed foam liquid concentration in equilibrium, the volumetric flow rate of liquid in foam (collapsed foam liquid) and the bubble-liquid interfacial area generation rate in the pool, respectively. The values of all terms in the right hand side in Eq. [1] could be determined or estimated by some ways. However it should be necessary to measure the flow rate of liquid in foam and to collect the collapsed foam liquid by keeping the foam height nearly liquid-foam interface as possible, because the volumetric flow rate of liquid in foam decreases exponentially in the axial direction and this decrease is much larger in higher position of the foam within the column (15-16). This fact suggests that the amount of the adsorbate contained in foam liquid should have the distribution, moreover, the concentration of the liquid in the foam will be changed with the overflowing and the sampling position in the axial direction of the column. To determine the adsorption density on bubble surface in foam separation, the intrinsic values of volumetric flow

rate and the protein concentration in foam would have to be determined. It is, however, too difficult to determine them at liquid-foam interface directly. Such attention has not been paid in previous works. To determine the adsorption density of objective substance on bubble surface more exactly, the authors focused on the mass balance at the liquid-foam interface because the liquid-foam interface could be corresponded to the bottom of the foam bed and the top of the dispersed bubble bed. In this study, the authors performed foam separation of soluble proteins using ovalbumin and hemoglobin at various pHs and determined the liquid flow rate and the protein concentration at the liquid-foam interface by extrapolation based on axial profiles. The aim of this study is to clarify the adsorption behavior of protein onto the bubble surface and its enriching mechanism in foam separation. The applicability of Langmuir's isotherm of the present system to the adsorption of proteins on bubble surface will be discussed.

## MASS BALANCE EXPRESSION

Figure 1 shows the mass balance of continuous foam separation. Assuming that protein contained in the foam at the liquid-foam interface is originated from the adsorbed substance on bubble surface and the entrained bulk liquid, the mass balance under a steady state will be expressed by the following relation

$$W_{f0} C_{f0} = S_{f0} X + W_{f0} C_b \quad [2]$$

where  $C_b$  and  $C_{f0}$  represent the concentration of the protein in the bulk liquid and that in the foam at the interface, respectively.  $W_{f0}$  represents the volumetric flow rate of liquid in the foam at the liquid-foam interface, and  $S_{f0}$  and  $X$  denote the bubble surface area in the foam at the interface and the adsorption density on bubble surface, respectively. In the foam bed, in general,  $W_{f0}$  and  $S_{f0}$  decrease, and  $C_{f0}$  increases with the increase in foam height because of coalescence of foam cells and liquid drainage. Eq. [2] enables us to obtain  $X$ , if the values of  $W_{f0}$ ,  $C_{f0}$  and  $S_{f0}$  are given or measured. Among these variables,  $S_f$  at a definite height in the foam layer is difficult to measure, whereas the surface area of bubbles rising through the column per unit time,  $S_b$ , can be estimated from an equation related to the gas holdup and the liquid properties as described later. Assuming that,

at the liquid-foam interface,  $S_b$  is equal to  $S_{f0}$ , Eq. [2] is rewritten as

$$W_{f0} C_{f0} = S_b X + W_{f0} C_b \quad [3]$$

Eq. [3] gives the relationship between  $X$  and  $C_b$  and an experimental adsorption isotherm. In this work,  $C_{f0}$  and  $W_{f0}$  were measured indirectly by an extrapolating method described in the section below.  $S_b$  was determined from the relationship proposed by Suzuki *et al.* (17),

$$S_b = 6A\varepsilon(1-\varepsilon)^{4.65} \left\{ (4/225)(\rho_L - \rho_G)^2 g^2 / (\mu_L \rho_L) \right\}^{1/3} \quad [4]$$

where  $A$ ,  $\varepsilon$ ,  $g$ ,  $\rho_L$ ,  $\rho_G$  and  $\mu_L$  denote the cross-sectional area of the column, the gas holdup, the gravitational acceleration, the density of liquid and gas and the viscosity of the liquid, respectively. This equation was derived from the assumption that bubbles are homogeneous spheres and their terminal rising velocity can be calculated by Allen's equation (18) and Shirai's equation (19) was employed for voidage compensation.

## MATERIALS AND METHODS

### *Materials*

Ovalbumin (egg white) was purchased from Eastman Kodak Company or Difco Laboratories. Hemoglobin from bovine was purchased from Wako Pure Chemical Industries Ltd. (Japan). These were used without further purification. The ion strength and pH of their solutions were adjusted with NaCl at  $5 \times 10^{-3}$  M and with aqueous HCl or NaOH to several desired values, respectively. All experiments were carried out at room temperature and under atmospheric pressure.

### *Experimental setup*

The experimental setup used in this study is shown in Fig. 2. The column was constructed of a transparent acrylic resin tube of  $4.4 \times 10^{-2}$  m in inside diameter. The main part of this column was 0.65 m in height and was connected to 0.3 m pipes with a flange in order to vary the column height up to 1.25 m. A column of 0.95 m was normally employed, but the columns of 0.65 and 1.25 m were also used, when necessary. A sintered glass filter with an average pore size ranging from  $10\text{-}15 \times 10^{-6}$  m was installed as a gas distributor at the bottom of the column. Nitrogen gas was supplied to the column through the distributor. In the experiments, a foam

collector was equipped at the top of the column to entrap foam generated from the liquid surface. The collector was also made of an acrylic resin cylinder of  $4.8 \times 10^{-2}$  m in height and  $5.0 \times 10^{-2}$  m in inside diameter, which corresponded to the outside diameter of the column with a steel mesh at the bottom end. The collector filled with a certain amount of polyester fiber wool was placed at the column top. Pressure taps for measuring gas holdup in the column were installed at intervals of 0.25 m along the wall.

#### *Experimental procedure for continuous foam separation*

Egg ovalbumin (OA) and hemoglobin from bovine (HB) were used as typical water-soluble proteins. The protein solution prepared at a desired concentration was stored in a storage tank. The solution was charged into the column from a feed tap by a pump. The volumetric flow rate of feed liquid was  $5.0 \times 10^{-7}$  m<sup>3</sup>/s. After the column was filled with the solution, nitrogen gas was supplied and was dispersed as bubbles by the distributor. The foam height,  $H_f$ , within the column, that is, the distance between the liquid-foam interface and the column top was adjusted by control of the volumetric flow rate of the drain liquid using a rotameter. The bulk liquid in the column was regarded as completely mixed because the axial distribution of the bulk concentration was not observed. Thus, it was sampled at the bottom of the column. After a steady state condition was

attained after about 2 hours, the samplings of the foam liquid for measuring the volumetric flow rates and the concentrations were started. The concentrations of the proteins were measured by the Lowry method. The pH of the bulk liquid in the column was measured with a pH meter (ORION Model SA 520). The gas holdup was determined from the difference in static pressure between the clear and aerated liquids using a differential pressure transducer. Voltage signals were recorded by a personal computer (NEC PC-9801VM) via A/D convertor (CONTEC).

*Procedure for measurement of axial profiles of volumetric flow rate of liquid in foam*

The volumetric flow rate of liquid in the foam was measured as follows. The collector was attached on the top of the column and was exposed to the upward flow of foam generated from the liquid surface. After ca. 15 seconds, the collector was detached from the column and was weighted on a balance. This procedure was repeated five times using five collectors (for ca. 6 minutes). The volumetric flow rate,  $W_f$ , of liquid in the foam was determined from the change in the sum of the weight of the collectors and the exposure time, assuming that the density of the liquid in the foam was nearly equal to that of water. After changing the height,  $H_f$ , between the bottom of the foam collector and the liquid-foam interface, the experiments

were repeated.

## RESULTS AND DISCUSSION

### *Measurement of volumetric flow rate of liquid in foam*

Typical results of the liquid flow rate in foam layer measured at various  $H_f$  are shown in Fig. 3.  $M$  in the y-axis denotes the value of the cumulative liquid weight in the foam captured by five foam collectors. The relationship between  $M$  and the sampling time showed linearity. Therefore, the volumetric flow rate,  $W_f$ , of liquid in the foam at  $H_f$  can be determined from the slope of the plot of  $M$  versus sampling time. Other experimental results with different experimental conditions were also same results as Fig. 3. The solid lines in Fig. 3 are determined by the least squares regression.

### *Axial profiles of $W_f$ and $C_f$ in foam bed*

Thus,  $W_f$  and  $C_f$  at each sampling  $H_f$  were obtained from the manner described above and Lowry method, respectively. Figures 4 and 5 show typical examples of the axial profiles of the volumetric flow rate,  $W_f$ , and the protein concentration,  $C_f$ , of liquid in the foam bed for both OA and HB in semi-log plots.  $W_f$  was determined from the slope of the plot of  $M$  vs. sampling time. When  $H_f$  increased,  $W_f$  decreased and  $C_f$  increased exponentially, respectively due to the liquid drainage. The results obtained under different conditions were also similar to these figures.  $W_f$  decreased

exponentially, on the other hand,  $C_f$  increased exponentially with  $H_f$  for both OA and HB. Plots of logarithm of  $W_f$  and  $C_f$  versus  $H_f$  yielded straight lines with slopes of negative and positive values, respectively. The intrinsic values of volumetric flow rate,  $W_{f0}$ , and protein concentration,  $C_{f0}$ , at the liquid-foam interface were determined by an extrapolation method (intercepts of the ordinates both  $W_f$  and  $C_f$ ) as same as the method reported previously for nonfoaming adsorptive bubble separation (18).

#### *Axial profile of mass flux of proteins in foam bed*

Figure 6 shows the axial profile of the mass flux,  $n_{OA}$  and  $n_{HB}$ , of both (a) OA and (b) HB, respectively, as a typical example. Figure 6 depicts the axial distribution of the mass flux of proteins present in the foam. Most of the mass flux in Fig. 6 decreased with increasing  $H_f$ . This shows that the liquid drainage occurred due to gravitational acceleration. From a comparison with the results of the axial profiles of  $W_f$  and  $C_f$  (Figures 4 and 5), it seemed that the mass flux was significantly influenced more by  $W_f$  than by  $C_f$ . No remarkable coalescence of bubbles within the foam was visually observed under the present experimental conditions along with the foam height. Especially in the case of  $C_b = 3.30 \times 10^{-2} \text{ kg/m}^3$  for OA, a significant distribution was not observed although the plot shows some scattering. Under this condition, the more “dry” and “cellular” foam was

made and the liquid drainage and the collapse of foam cells might be much less for  $C_b > 3.30 \times 10^{-2} \text{ kg/m}^3$  for OA. The change in the mass flux was influenced by the foam stability as a function of the liquid properties and the operating variables. We will not discuss these influences in any more further detail. These axial distributions support the validity of the proposed method for the determination of  $W_{f0}$  and  $C_{f0}$ . Coalescence of the foam cells would affect the present extrapolation method for the determination of  $W_{f0}$  and  $C_{f0}$ . If a more significant coalescences occurred in the foam bed, the profile of  $n$  values should decrease with increasing foam height. This resulted underestimation of the values of  $W_{f0}$  and  $C_{f0}$ . The extrapolation method could be applied to the lower foam height region within the column to avoid underestimation because there was little coalescence in the lower foam height.

*Determination of adsorption equilibrium constant and saturated adsorption density*

Using Eqs. [3] and [4] and the extrapolated data of  $W_{f0}$  and  $C_{f0}$  as previously determined in each run, the adsorption isotherms for OA and HB were obtained as shown in Fig. 5, respectively. Langmuir's adsorption isotherm, which is well-known, can be expressed as

$$X = K\gamma C_b / (1 + KC_b) \quad [5]$$

where  $K$  and  $\gamma$  denote the equilibrium constant and the saturated surface density on the bubble surface, respectively. The elimination of  $X$  from Eqs. [3] and [5] gives

$$W_{f0} (C_{f0} - C_b) = S_b K \gamma C_b / (1 + KC_b) \quad [6]$$

The reciprocal of Eq. [6] is written as

$$S_b / \{ W_{f0} (C_{f0} - C_b) \} = (1/K\gamma)(1/C_b) + 1/\gamma \quad [7]$$

Eq. [7] is a modified form of the Langmuir adsorption isotherm for the present system. The slope and the intercept of the straight line give the values of  $K$  and  $\gamma$ , respectively.  $S_b$ ,  $W_{f0}$  and  $C_{f0}$  have already been estimated, therefore, we can now plot Eq. [7] for both OA and HB as shown in Fig. 7. The straight lines were obtained using the least squares method. Judging from the fact that the data for both OA and HB are in good accordance with Eq. [7], the adsorption behavior of OA and HB on the bubble surface in a continuous foam separation system should be expressed by Langmuir's isotherm. From the intercept and the slope of each line, the equilibrium

constant,  $K$ , and the saturated surface density,  $\gamma$ , were obtained for OA and HB as listed in Table 1. The variation in  $K$  and  $\gamma$  with pH is shown in (a) and (b) of Fig. 7, respectively. The  $\gamma$  values for both OA and HB showed maxima at their respective isoelectric points (i.e.p., pH 4.6 for OA and pH 6.8 for HB) and decreased in the more acidic and alkaline pH regions. On the other hand,  $K$  showed a different tendency between OA and HB as is seen in Fig. 7 (b).  $K$  should be strongly influenced by some physicochemical properties such as the hydrophobic characteristics of the protein molecules; thus, the physical meaning of  $K$  is more complicated than that of  $\gamma$ . In the following part, some discussion will be given only for  $\gamma$ .

*Calculation of occupied area for OA and HB on bubble surface in saturated state*

Assuming that the cross section of the OA and HB molecules is circular and that they adsorb on the bubble surface in a closest-packing structure (packing fraction = 0.907) in the saturated state, the diameter,  $D$ , of the molecules can be calculated from  $\gamma$  as

$$D = 2 \{0.907M_w/(\pi L\gamma)\}^{0.5} \quad [8]$$

where  $L$  and  $M_w$  represent Avogadro's number and the molecular weight of the protein, respectively. The  $D$  values of OA and HB were calculated using 45,000 and 65,000 as the  $M_w$  for OA and HB, respectively. The diameters obtained at several pHs are listed in Table 2. On the other hand, it is reported that a native OA molecule in an aqueous system is almost spherical with a diameter of ca. 50 nm based on small angle X-ray scattering (SAXS) measurement (21). Stein *et al.* (22) reported ovalbumin whose crystal-structure dimensions are 70×45×50 nm. A vertebrate hemoglobin was said to be a globular protein with dimensions of about 64×55×50 nm (23). It was reported that the dimensions of a hydrated molecule of horse hemoglobin as revealed from its crystal structure analysis was about 70×55×55 nm (24). Thus, it should be considered that the OA and HB molecules had a closest packed structure in the saturated state. From a comparison of the  $D$  values calculated in this study and the literature data, although  $D$  of HB is slightly larger than the literature values, the values for both OA and HB were quite similar to the literature values. This result supports the validity of the proposed method for the determination of the adsorption density in this study.

An electrostatic repulsive force and the van der Waals attractive force act between proteins adsorbed on the air-liquid interface (25-26). The van der Waals attractive force includes the Hamaker constant, which is a

complicated factor. To simplify the discussion, we now focus on the electrostatic repulsive force. The protein molecule is a well-known amphometric macromolecule. The surface charge of the protein molecule originates from the dissociation of the amino acid residues. Tanford *et al.* (27) and Scatchard *et al.* (28) developed the charge model and evaluated the net charge on BSA from the model. we applied the simplified model to both OA and HB. Assuming that the dominant amino acid residues are the carboxyl, amino, imidasol, phenolic hydroxyl, guanidine and thiol, these dissociation equilibrium constants between these functional groups and a proton are given by

$$K_c = [\text{P-COO}^-]_s [\text{H}^+]_s / [\text{P-COOH}]_s \quad [9]$$

$$K_p = [\text{P-O}^-]_s [\text{H}^+]_s / [\text{P-OH}]_s \quad [10]$$

$$K_t = [\text{P-S}^-]_s [\text{H}^+]_s / [\text{P-SH}]_s \quad [11]$$

$$K_a = [\text{P-NH}_2]_s [\text{H}^+]_s / [\text{P-NH}_3^+]_s \quad [12]$$

$$K_g = [\text{P-NH}]_s [\text{H}^+]_s / [\text{P-NH}_2^+]_s \quad [13]$$

$$K_i = [\text{P-N}]_s [\text{H}^+]_s / [\text{P-NH}^+]_s \quad [14]$$

where  $[\text{H}^+]_s$  denotes the surface hydrogen ion concentration. Subscripts "c", "p", "t", "a", "g" and "i" express the carboxyl, phenolic hydroxyl, thiol, animo, guanidine and imidasol, respectively. The dissociation degree of

each amino acid residue,  $\alpha$ , can be written as follows from Eqs. [9]-[14].

$$\alpha_c = K_c / (K_c + [H^+]_s) \quad [15]$$

$$\alpha_p = K_p / (K_p + [H^+]_s) \quad [16]$$

$$\alpha_t = K_t / (K_t + [H^+]_s) \quad [17]$$

$$\alpha_a = K_a / (K_a + [H^+]_s) \quad [18]$$

$$\alpha_g = K_g / (K_g + [H^+]_s) \quad [19]$$

$$\alpha_i = K_i / (K_i + [H^+]_s) \quad [20]$$

The net charge per a protein molecule,  $z$ , can be calculated using the following equation.

$$z = (1 - \alpha_a) N_a + (1 - \alpha_g) N_g + (1 - \alpha_c) N_c - \alpha_t N_t - \alpha_p N_p - \alpha_i N_i \quad [21]$$

In Eq. [21],  $N$  denotes the number of each amino acid residue. Figure 10 shows the variation in  $z$  with the pH value for both OA and HB. The number of each amino acid residue and the dissociation constants using the calculation of  $z$  are summarized in Table 3. In this calculation, the surface concentration of the proton is approximated by its bulk concentration for the simplification. The calculated  $z$  values for both OA and HB varies from positive to negative with increasing pH and become zero near each i.e.p..

This curves for both OA and HB suggest that the electrostatic repulsion is weakest at the i.e.p. and becomes stronger with varying pH from the i.e.p. to the more acidic or alkaline regions. Because the lateral electrostatic repulsion between protein molecules adsorbed on the bubble surface is considered to be the weakest at the i.e.p., therefore negligible, then the proteins are expected to be adsorbed more compactly on the bubble surface and the  $\gamma$  values for both OA and HB show a maximum value at the i.e.p.. In the acidic or alkaline pH region, proteins would not be able to be attracted to each other due to the stronger lateral electrostatic repulsion.

## CONCLUSIONS

The enriching mechanism of proteins in a continuous foam separation was studied. The experiments were conducted with a bubble column using ovalbumin (OA) and hemoglobin (HB) in various pH ranges as typical water-soluble proteins. Using foam collectors, the volumetric flow rate,  $W_f$  and the protein concentration,  $C_f$  in the foam layer at various heights were measured. The data were processed with the extrapolation method to yield the intrinsic values of  $W_{f0}$  and  $C_{f0}$  at the interface between the liquid pool and the foam layer. Using the intrinsic values, the adsorption density was determined from the mass balance of protein at the liquid-foam interface. Thus obtained adsorption isotherms of both OA and HB were in good accordance with the Langmuir's equation. The two adsorption parameters, the equilibrium constant,  $K$ , and the saturated surface density on the bubble surface,  $\gamma$ , were determined from the Langmuir's plots modified for the present system.  $\gamma$  for each protein had a maximum value at the i.e.p., on the other hand,  $K$  for OA and HB showed a maximum and a minimum at each i.e.p. The sphere equivalent diameters of OA and HB at several pHs were calculated from the  $\gamma$  values, based on the assumption that proteins at the saturated adsorption state take a two-dimensional closest packing structure on bubble surface. The obtained diameters for OA and HB were in good

accordance with the literature values. This results support the validity of the proposed extrapolating method. The reason of the maximum value of  $\gamma$  and the minimum value of occupied area of both OA and HB at each i.e.p. was considered qualitatively relating to lateral electrostatic repulsion based on the variation of the net charge of protein molecule with pH calculated from the simplified net charge model.

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## APPENDIX 1

### NOTATION

$A$	= a cross sectional area of bubble column	$[\text{cm}^2]$
$C_b$	= protein concentrations of the liquids in bulk phase	$[\text{kg}/\text{m}^3]$
$C_f$	= concentrations of the liquids in foam	$[\text{kg}/\text{m}^3]$
$C_{f0}$	= the intrinsic concentration of liquid in foam at the liquid-foam interface	$[\text{kg}/\text{m}^3]$
$C_i$	= concentrations of the feed liquid	$[\text{kg}/\text{m}^3]$
$D$	= sphere equivalent diameters calculated from Eq. [7]	$[\text{m}]$
$g$	= gravitational acceleration	$[\text{kg m}/\text{s}^2]$
$H_f$	= foam height within column	$[\text{m}]$
$K$	= equilibrium constant	$[\text{m}^3/\text{kg}]$
$L$	= Avogadro's number	$[-]$
$M$	= the value of the cumulative weight of the liquid in foam	$[\text{kg}]$
$M_w$	= molecular weight	$[\text{kg}/\text{mol}]$
$n$	= mass flux in foam bed	$[\text{kg}/(\text{cm}^2 \text{ s})]$
$N$	= number of amino acid residue	$[\text{/molecule}]$
$S_b$	= production rate of bubble surface area	$[\text{m}^2/\text{s}]$
$S_f$	= bubble surface area in foam at $H_f$	$[\text{m}^2/\text{s}]$
$S_{f0}$	= bubble surface area in foam at the liquid-foam interface	$[\text{m}^2/\text{s}]$

$U_g$	= superficial gas velocity	[m/s]
$W_f$	= volumetric flow rate of liquid in foam at $H_f$	[m <sup>3</sup> /s]
$W_{f0}$	= intrinsic volumetric flow rate at the liquid-foam interface	[m <sup>3</sup> /s]
$W_i$	= volumetric flow rate of feed liquid	[m <sup>3</sup> /s]
$X$	= adsorption density on bubble surface	[kg/m <sup>2</sup> ]
$z$	= net charge per protein molecule	[/molecule]

*Greek letter*

$\alpha$	= degree of dissociation	[-]
$\varepsilon$	= gas holdup	[-]
$\gamma$	= saturated surface density on bubble surface	[kg/m <sup>2</sup> ]
$\mu$	= viscosity	[kg/(m s)]
$\rho$	= density	[kg/m <sup>3</sup> ]

*subscript*

$G$	= gas phase
$L$	= liquid phase
$a$	= amino
$c$	= carboxyl
$g$	= guanidine
$i$	= imidasol
$p$	= phenolic hydroxyl

*s* = surface

*t* = thiol

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## FIGURE CAPTIONS

**FIG. 1.** Schematic diagram of mass balance between the bubble dispersed and the foam bed in the column.

**FIG. 2.** Schematic drawing of experimental setup for continuous foam separation.

**FIG. 3.** Typical results of determination of volumetric flow rate,  $W_f$ , of liquid in foam at  $H_f$ .

**FIG. 4.** Axial profiles of the volumetric flow rate of liquid in foam for various bulk concentrations of ovalbumin at pH 4.6 (a) and hemoglobin at pH 6.8 (b). Experiments were conducted with a superficial gas velocity,  $U_g = 5.37 \times 10^{-4}$  m/s.

**FIG. 5.** Axial profiles of the protein concentration in liquid in foam for various bulk concentrations of ovalbumin at pH 4.6 (a) and hemoglobin at pH 6.8 (b). Experiments were conducted with a superficial gas velocity,  $U_g = 5.37 \times 10^{-4}$  m/s.

**FIG. 6.** Axial profiles of the mass flux,  $n$ , of proteins for both (a)

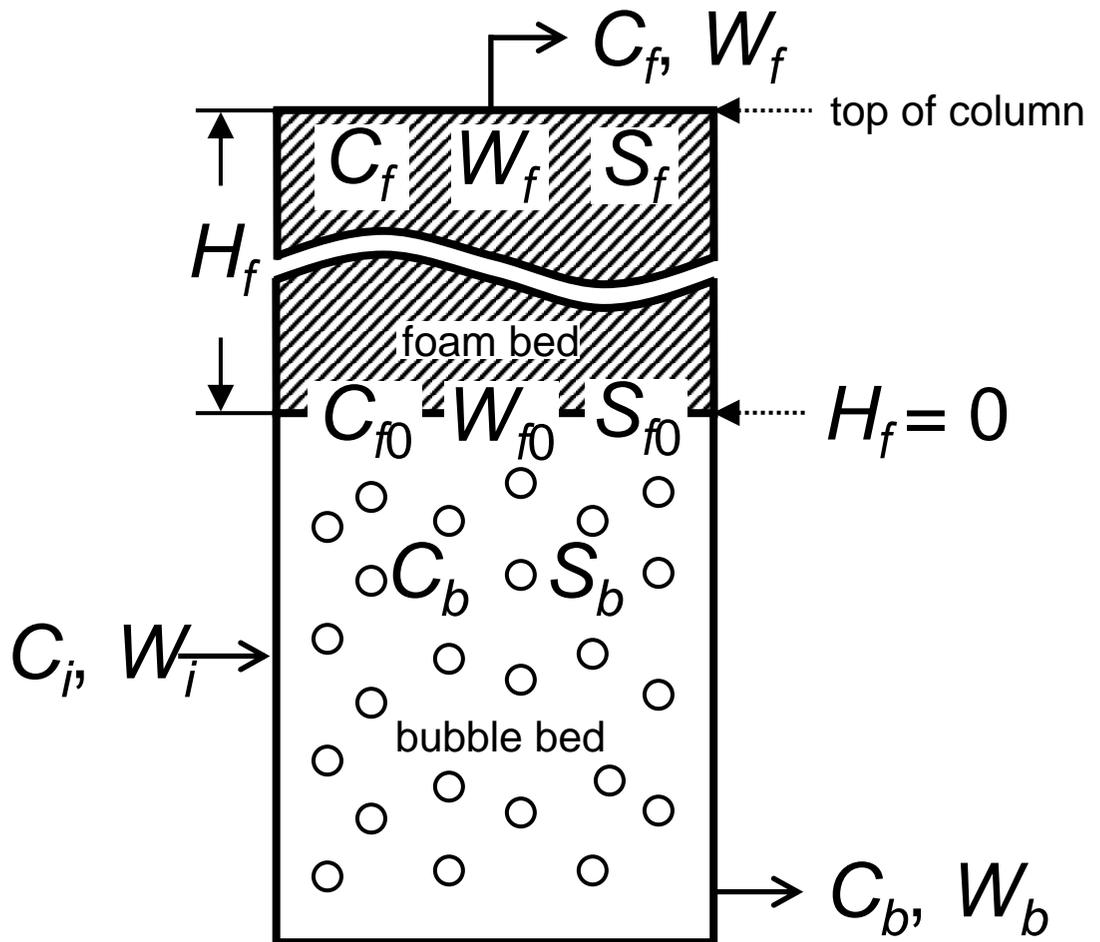
ovalbumin and (b) hemoglobin in the foam bed. Experiments were conducted with a superficial gas velocity,  $U_g = 5.37 \times 10^{-4}$  m/s.

**FIG. 7.** Adsorption isotherms of (a) ovalbumin and (b) hemoglobin at various pHs. Solid lines in this figure are calculated using  $K$  and  $\gamma$  determined from Eq. [7].

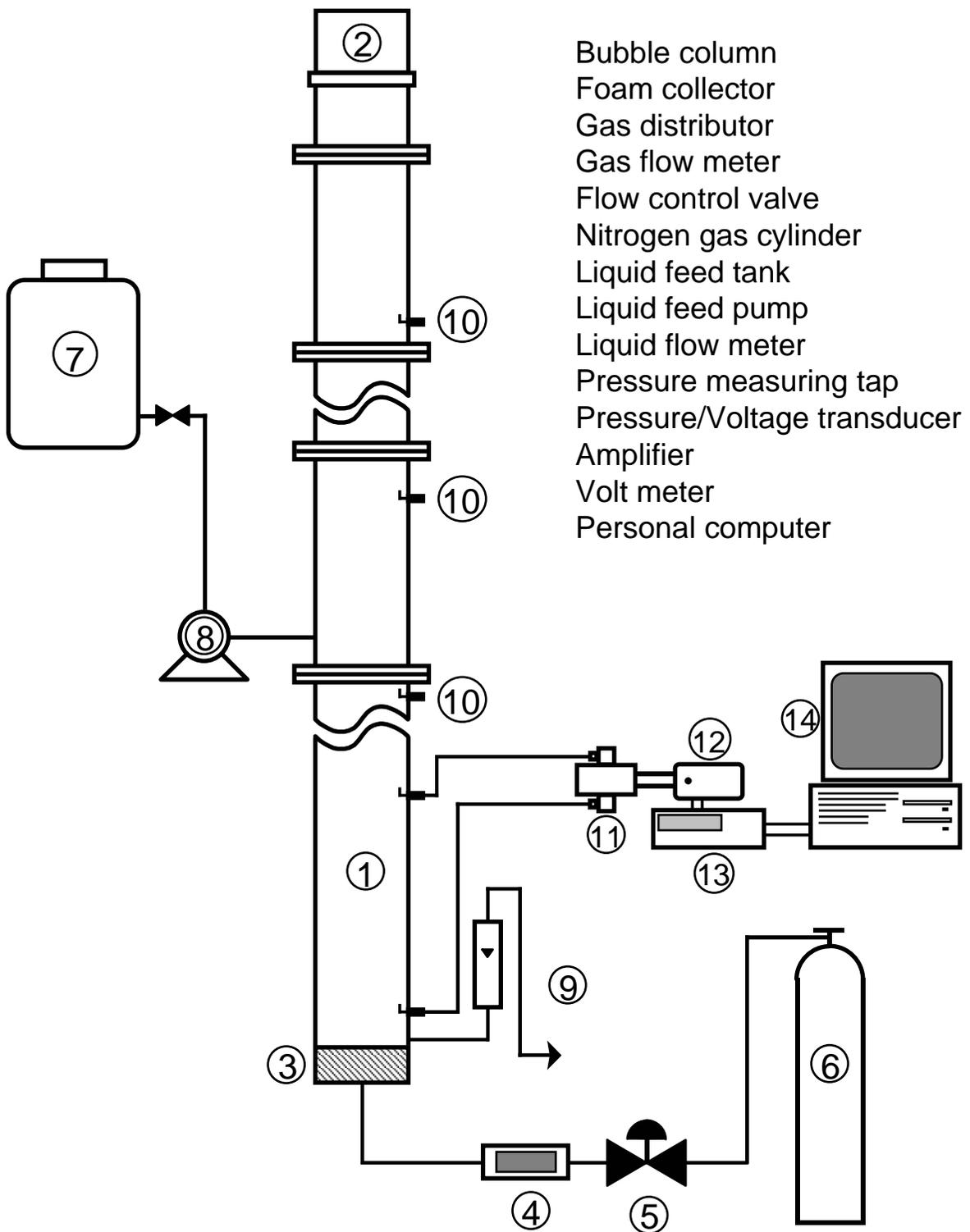
**FIG. 8.** Estimation of the equilibrium constant and the saturated surface density of (a) ovalbumin and (b) hemoglobin at various pHs by fitting of data to Eq.[7]. Symbols are the same as FIG. 7.

**FIG. 9.** pH dependence of (a) the saturated surface density,  $\gamma$ , and (b) the equilibrium constant,  $K$ , for ovalbumin ( ) and hemoglobin ( ).

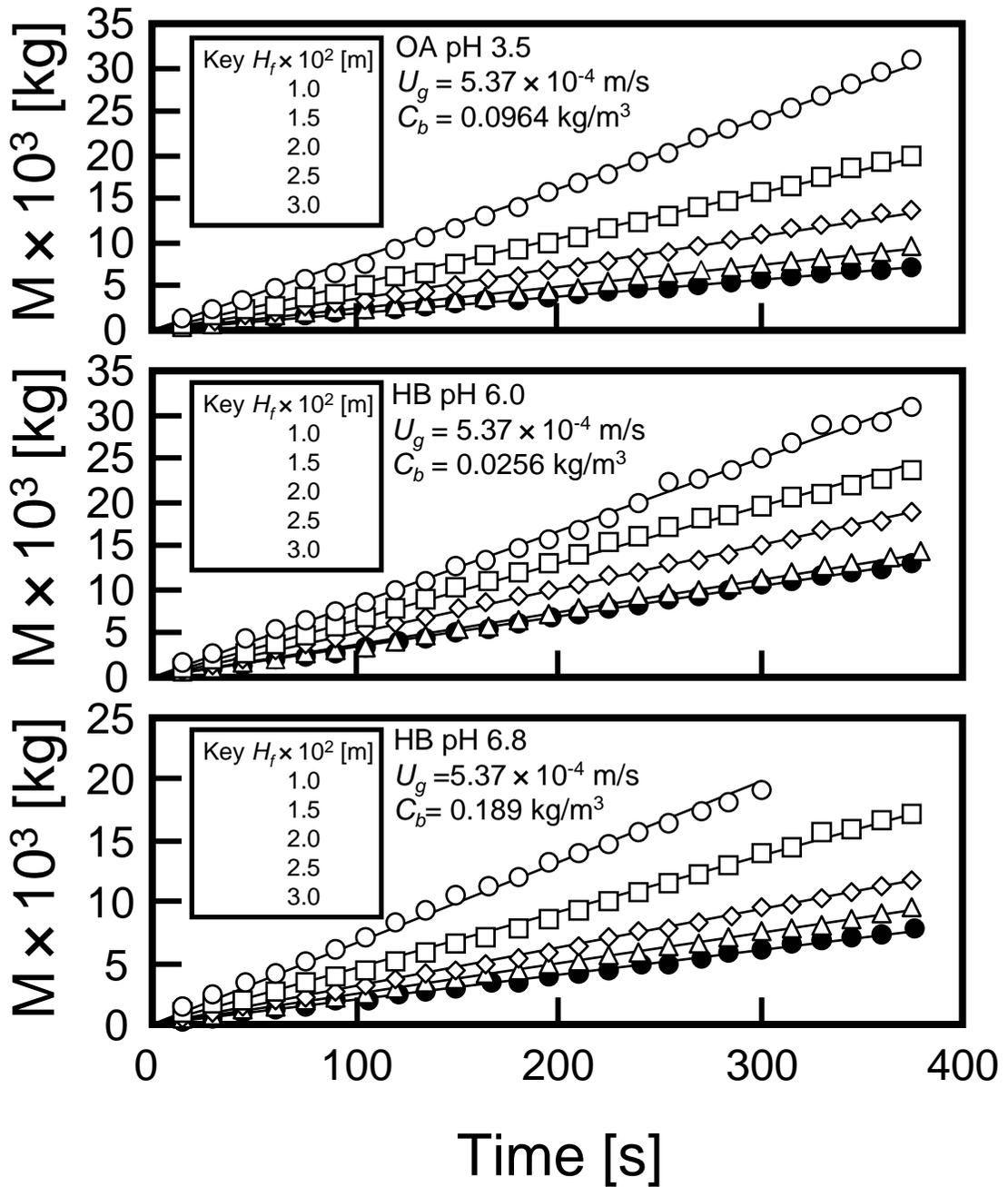
**FIG. 10.** Variation in the net charge of protein molecule with pH for both ovalbumin (OA) and hemoglobin (HB) calculated by Eq. [21]. Solid and dotted lines correspond to OA and HB, respectively.



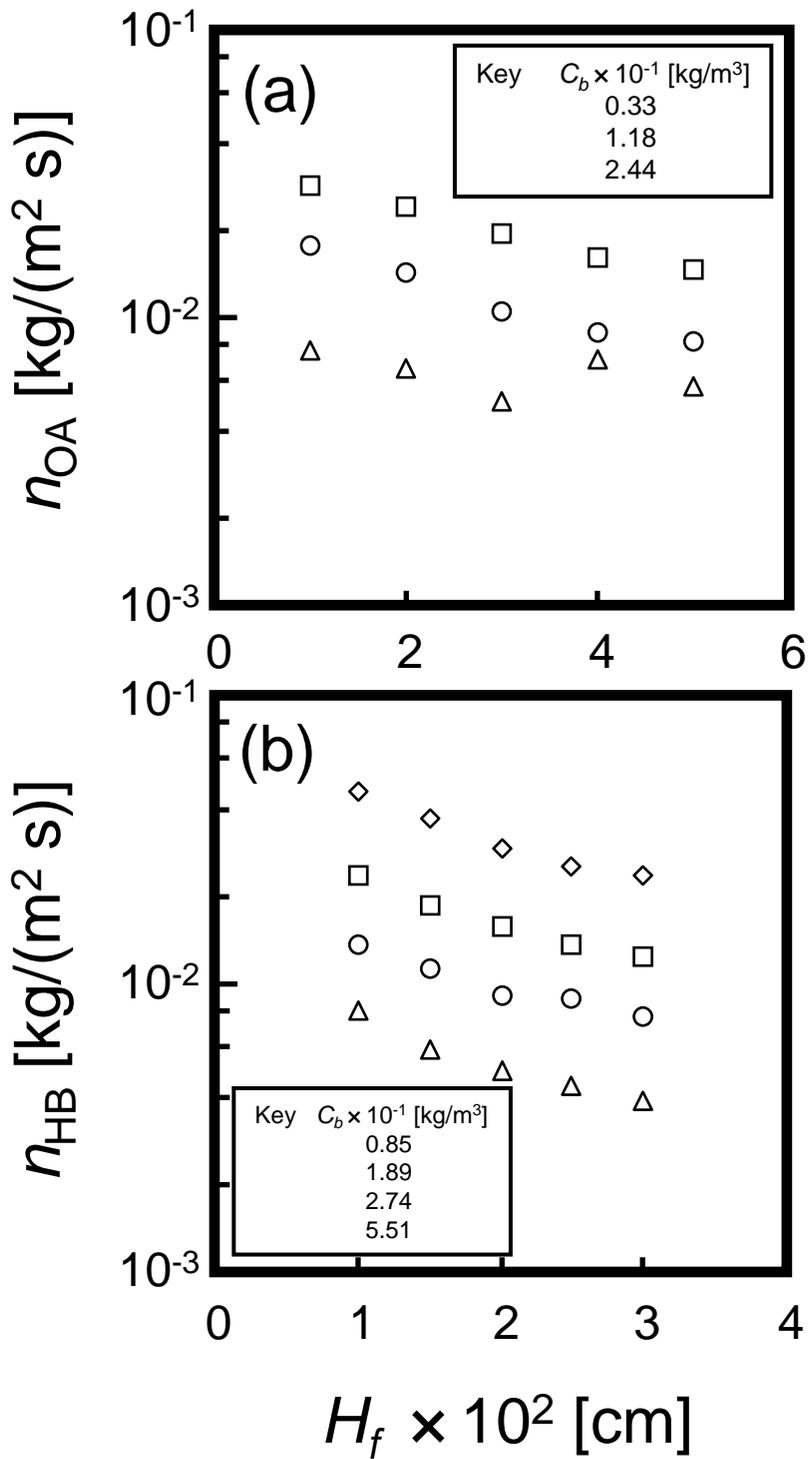
**FIG. 1.** Schematic diagram of mass balance between the bubble dispersed and the foam bed in the column.



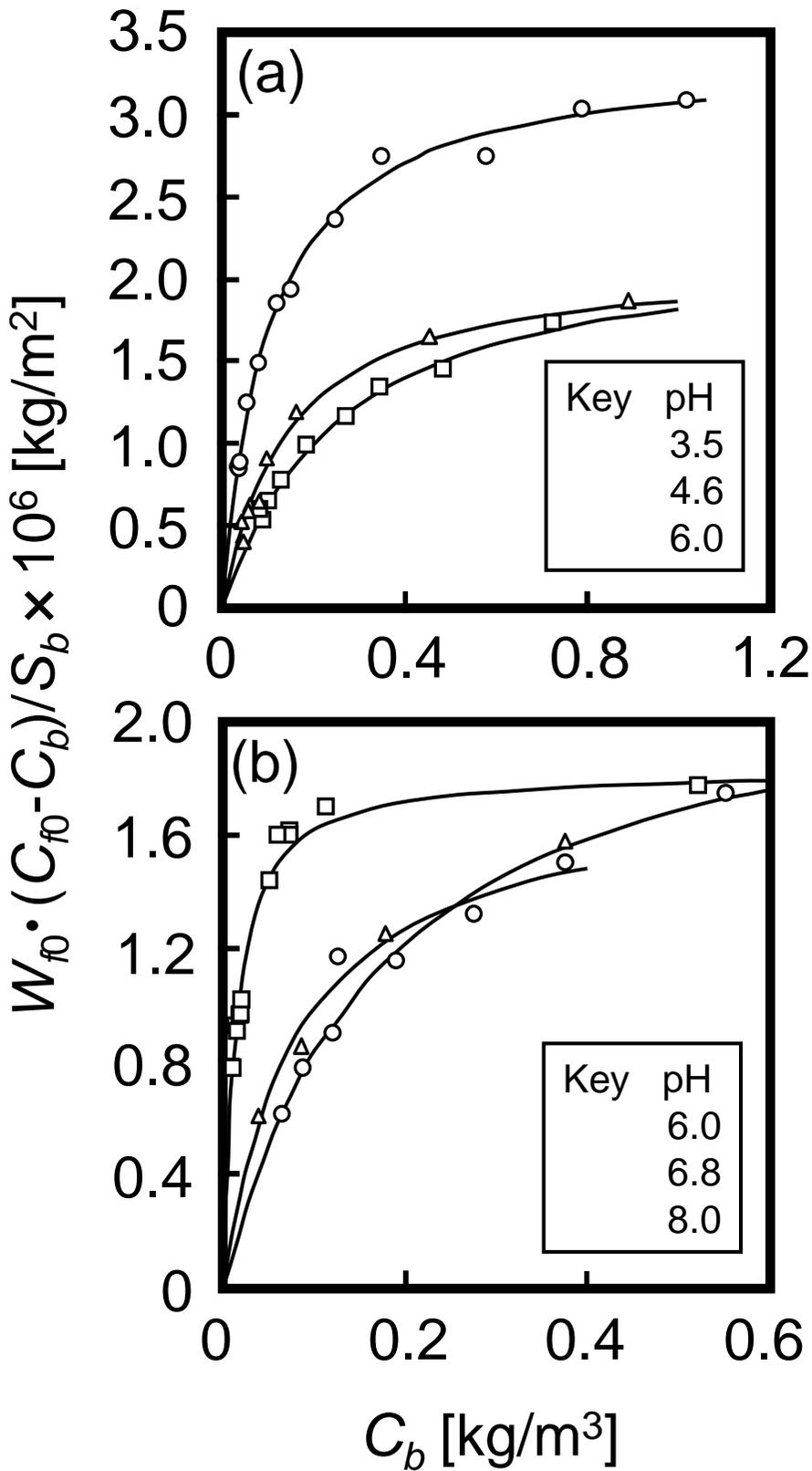
**FIG. 2.** Schematic drawing of experimental setup for continuous foam separation.



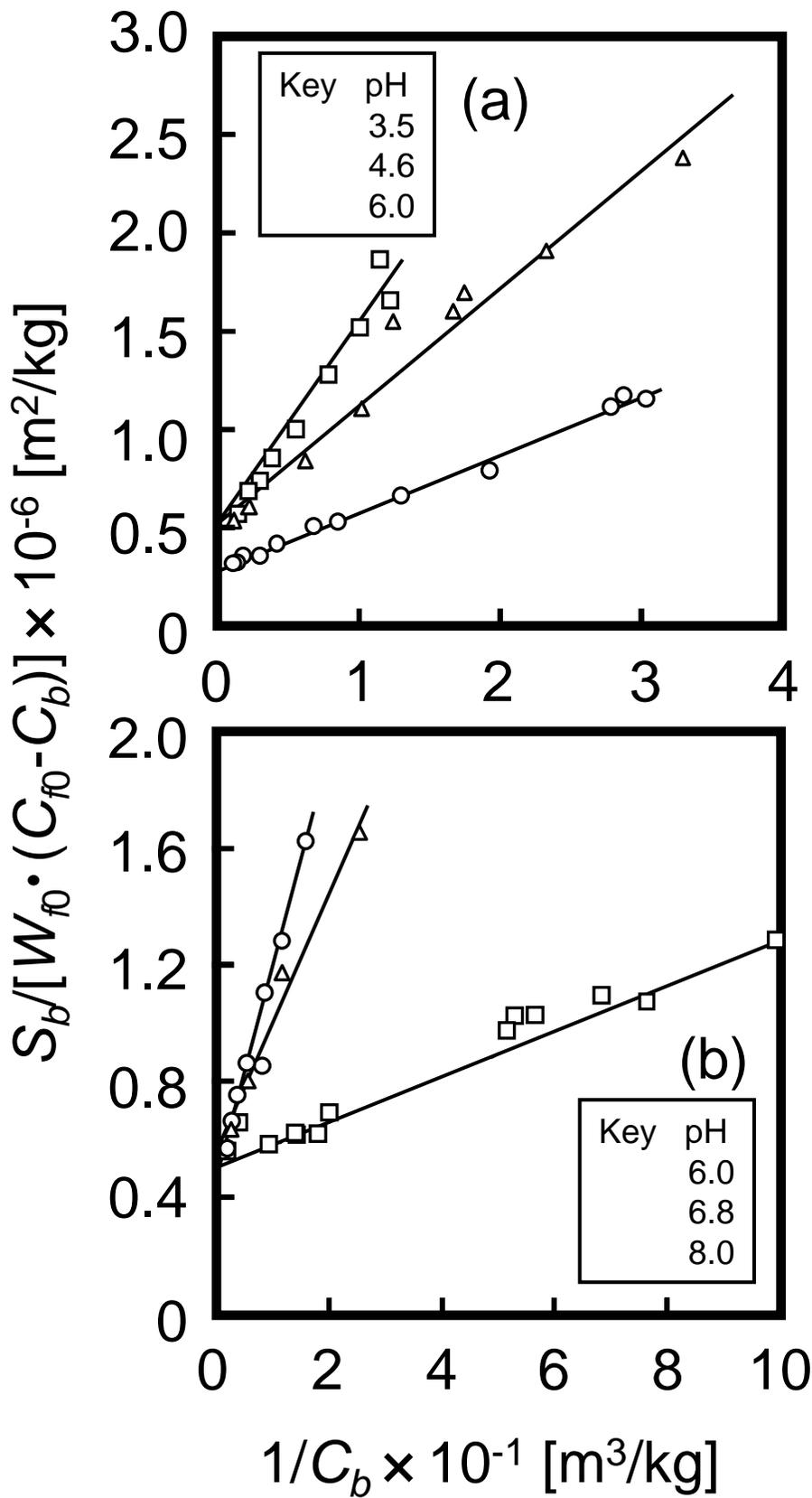
**FIG. 3.** Typical results of determination of volumetric flow rate,  $W_f$ , of liquid in foam at  $H_f$ .



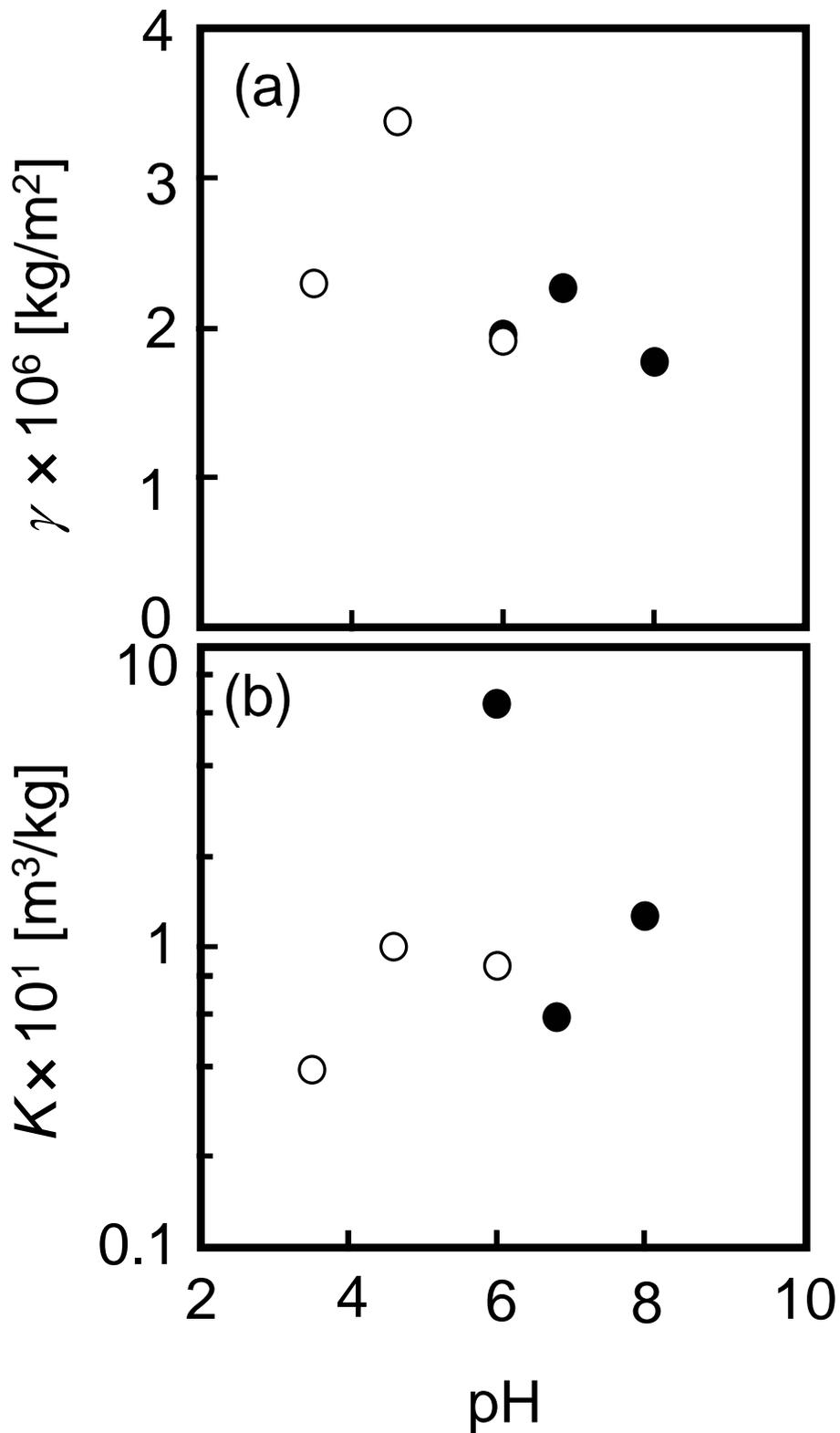
**FIG. 4.** Axial profiles of the mass flux,  $n$ , of proteins for both (a) ovalbumin and (b) hemoglobin in the foam bed. Experiments were conducted with a superficial gas velocity,  $U_g = 5.37 \times 10^{-4}$  m/s.



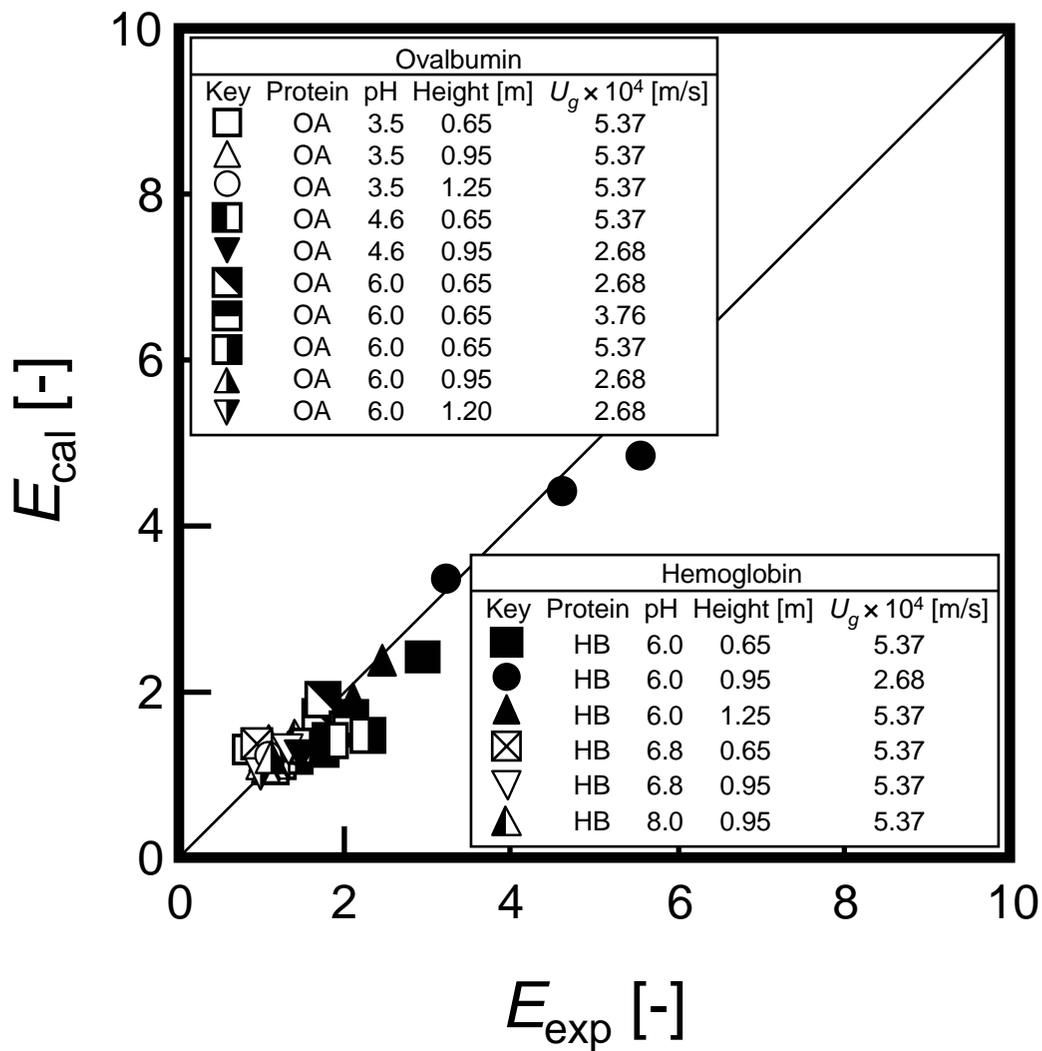
**FIG. 5.** Adsorption isotherms of (a) ovalbumin and (b) hemoglobin at various pHs. Solid lines in this figure are calculated using  $K$  and  $\gamma$  determined from Eq. [7].



**FIG. 6.** Estimation of the equilibrium constant and the saturated surface density of (a) ovalbumin and (b) hemoglobin at various pHs by fitting of data to Eq. [7]. Symbols are the same as Fig. 5.



**FIG. 7.** pH dependence of (a) the saturated surface density,  $\gamma$ , and (b) the equilibrium constant,  $K$ , for ovalbumin (  $\circ$  ) and hemoglobin (  $\bullet$  ).



**FIG. 8.** Comparison of the experimental values of enriching ratio,  $E$ , between the calculated ones from Eq. [9] for ovalbumin and hemoglobin.

**TABLE 1      Adsorption parameters for ovalbumin and hemoglobin at various values of pH.**

	pH	$\gamma \times 10^6$ [kg/m <sup>2</sup> ]	$K \times 10^2$ [m <sup>3</sup> /kg]
OA	3.5	2.30	3.94
	4.6	3.39	10.1
	6.0	1.92	8.72
HB	6.0	1.96	65.2
	6.8	2.27	5.88
	8.0	1.78	12.7

**TABLE 2** Sphere equivalent diameters for ovalbumin and hemoglobin at saturated state.

	pH	$D$ [ $\mu$ ]
OA	3.5	61.2
	4.6	50.4
	6.0	67.0
HB	6.0	81.6
	6.8	75.8
	8.0	83.6