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Temperature dependence of a Raman CO₂ densimeter from 23 to 200°C and 7.2 to 248.7 MPa: Evaluation of density underestimation by laser heating

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Abstract

Unintended local temperature enhancement by excitation laser might change Raman spectral features and potentially lead to misinterpretation of the data. To evaluate robustness of Raman CO₂ densimeters in the presence of laser heating, we investigate the relation between temperature \( (T, \, ^\circ C) \), density \( (\rho, \, g/cm^3) \), and Fermi diad split \( (\Delta, \, \text{cm}^{-1}) \) using a high-pressure optical cell at 23–200°C and 7.2–248.7 MPa. Results indicate that \( \Delta \) decreases concomitantly with increasing temperature for a constant density in all density regions investigated. This result suggests that the density estimated based on \( \Delta \) might be underestimated if the fluid is heated locally by the laser. Combining results of earlier studies with those of the present study indicates that the temperature dependence of \( \Delta \left( |(\partial \Delta/\partial T)_{\rho}| \right) \) has a maximum value around 0.6–0.7 g/cm³. Consequently, at very high densities such as 1.1–1.2 g/cm³, \( |(\partial \Delta/\partial T)_{\rho}| \) is small. Thus, \( \Delta \) at such densities is less affected by laser heating. However, at densities below approximately 0.7 g/cm³, although \( |(\partial \Delta/\partial T)_{\rho}| \) becomes smaller at lower densities, the relative density decrease becomes larger even for a small density decrease because the density itself becomes smaller. Therefore, at such densities, a density decrease of more than 10% was observed for some fluid inclusions, even at typical laser powers for inclusion analysis. Finally, to accurately estimate the density even in the presence of laser heating, we show that it is
effective to estimate the intercept Δ from the correlation between Δ and laser power,
and substitute it into Δ–ρ relations.

Keywords

Carbon dioxide, Densimeter, Fermi resonance, Fluid inclusions, Laser heating
1. INTRODUCTION

Fluid inclusions with compositions approximated as CO$_2$-rich systems are common in many geologic environments, including hydrothermal ore deposits,$^{[1–3]}$ medium-grade to high-grade metamorphic rocks,$^{[1,4–7]}$ and mantle xenoliths$^{[1,8,9]}$. In many geological settings, the density of those fluid inclusions has been studied to track volcanic plumbing systems,$^{[10–13]}$ to ascertain the depth provenance of mantle xenoliths,$^{[14–18]}$ and to identify the pre-eruptive volatile contents of magmas$^{[19–24]}$. Although microthermometry is the principal method for estimating the density of CO$_2$-rich inclusions, this method is effective only when inclusion is sufficiently large to measure the CO$_2$ homogenization temperature accurately because change in the fluid phase is determined using an optical microscope. This size limitation is generally approximately 5 µm.$^{[25]}$ Furthermore, if the host mineral has a large absorption coefficient of visible light, then measuring the homogenization temperature might be difficult, even for inclusions larger than 5 µm. Additionally, because the accuracy decreases at low and extremely high densities, microthermometry is applicable only when the density of CO$_2$ inclusions is 0.65–1.18 g/cm$^3$.$^{[26]}$ Raman spectroscopy is used as an alternative or complementary technique to estimate CO$_2$ fluid density when estimating fluid density by microthermometry is
difficult. The method is applicable to a wide density range of 0.001–1.24 g/cm³ and to small inclusions down to sub-micrometer size and to inclusions in colored minerals, where the homogenization temperature is difficult to measure, as long as Raman scattering photons with a sufficient number for quantitative analysis reach the detector. \cite{27-29} Raman-based CO₂ densimetry uses the relation between CO₂ fluid density (ρ) and Fermi diad splitting (Δ = ν⁺\text{F.D} - ν⁻\text{F.D}). \cite{18,25,27-42} Although Raman CO₂ densimeter is useful, some caution is necessary for application of this method to density measurements of natural fluid inclusions: 1) Effect of intermolecular interactions between CO₂ and trace molecules other than CO₂ on the spectral properties of CO₂, \cite{28,32-37,43-46} 2) discrepancy in the Δ–ρ relations derived in earlier studies, \cite{27,37,47} and 3) apparent density reduction because of the local temperature rise caused by excitation lasers \cite{48}. Regarding the first problem, this method has been improved vigorously to quantify the fluid pressure in inclusions with various P–V–T–x properties. Its applicability is now expanding to include the CO₂±N₂±CH₄ \cite{28,34,36,45,46,49} and CO₂–H₂O±NaCl systems \cite{28,32,35,37,44}. The second difficulty can be resolved by adding a correction term δ to the measured Δ. This correction term can be found by optimizing the residual sum of squares between the density estimated by any Δ–ρ relation from the Δ values of several standard fluid inclusions and the known density to the minimum.\cite{37}
Alternatively, in the region where the $\Delta-\rho$ relation can be approximated linearly, it is also effective to derive an original $\Delta-\rho$ relation applicable to the Raman system to be used, using two standard fluid inclusions with known density.\cite{27} For the third one, because $\left(\frac{\partial \Delta}{\partial T}\right)_\rho$ is always negative, at least in the density range investigated by earlier studies,\cite{35,36} the density estimated from the measured $\Delta$ might be underestimated if the excitation laser causes unintended heating. Nevertheless, few examples exist to verify the conditions and the extent to which it affects the measurement accuracy.\cite{48}

To assess the uncertainty that laser heating imposes on density estimation, one must ascertain the amount of change in $\Delta$ when the temperature of a fluid inclusion with a certain density $\rho$ is increased unintentionally by $T^\circ$C because of laser heating, i.e., $\left|\left(\frac{\partial \Delta}{\partial T}\right)_\rho\right|$. The value of $\left|\left(\frac{\partial \Delta}{\partial T}\right)_\rho\right|$ can be obtained directly from the $\Delta-\rho-T$ relation.

Several attempts have been undertaken to characterize high $P-T$ CO$_2$ Raman spectra.\cite{28,35,36,42,44,50} The temperature dependence of $\Delta$ at a given density ($\left|\left(\frac{\partial \Delta}{\partial T}\right)_\rho\right|$) below 0.7 g/cm$^3$ was found to be smaller for lower densities.\cite{35,36} However, regarding the density dependence of $\left|\left(\frac{\partial \Delta}{\partial T}\right)_\rho\right|$ at $> 0.7$ g/cm$^3$, several studies have yielded somewhat different conclusions.\cite{28,35,36} According to the $\Delta-\rho-T$ relation for pure CO$_2$ derived by Wang et al.\cite{35} using a high-pressure optical cell (HPOC), $\left|\left(\frac{\partial \Delta}{\partial T}\right)_\rho\right|$ becomes smaller at higher densities, greater than 0.7 g/cm$^3$. However, when using the relation...
derived by Sublett et al.\textsuperscript{36}, \(|(\partial \Delta/\partial T)_\rho|\) becomes larger at higher densities above 0.7 g/cm\(^3\), which is inconsistent with results reported by Wang et al.\textsuperscript{35}. Therefore, some disagreement exists with results of earlier studies of density dependence of \(|(\partial \Delta/\partial T)_\rho|\) conducted at densities higher than 0.7 g/cm\(^3\).

The density dependence of \(|(\partial \Delta/\partial T)_\rho|\) is consistent at low densities but inconsistent at high densities in earlier studies perhaps because few data have been reported for earlier studies undertaken in conditions above ambient temperature and at densities higher than 1.0 g/cm\(^3\) (Figure 1). For this study, we extended the pressure range of investigation markedly beyond that of earlier studies. We examined the \(\Delta–\rho–T\) relation at 23–200°C and 7.2–248.7 MPa using a HPOC filled with pure CO\(_2\) having density of 0.694–1.203 g/cm\(^3\). Based on the results, we acquired calibration curves to estimate density at various temperatures. Then we compared the curves with those obtained from published data. Finally, to elucidate how the fluid density and physical properties of the host minerals affect the amount of fluid density underestimation by laser heating in the analysis of fluid inclusions, the value of \(\Delta\) of CO\(_2\)-rich fluid inclusions with various densities in Cr-spinel and orthopyroxene was measured at various laser powers. The goals of this study are 1) to clarify the discrepancy between previous studies on the density dependence of \(|(\partial \Delta/\partial T)_\rho|\) at high densities, 2) to show
the extent to which laser heating introduces uncertainties in the density estimation of
natural fluid inclusions depending on the host mineral species and fluid density, and 3)
to propose an analytical procedure to accurately estimate the density even in the
presence of laser heating.

2. EXPERIMENTAL

2.1 High-pressure and high-temperature optical cell

We used a high-temperature and high-pressure cell (PC-400 ms; Syn Corp.) to
investigate the temperature-dependence of $\Delta - \rho$ relations. The high-pressure cell can
create a fluid with respective maximum pressure and temperature of 400 MPa and
200°C, but because the pressure resistance of the high-pressure generator is 200 MPa,
the uppermost pressure is limited by the pressure resistance of the high-pressure
generator. To measure the fluid at higher pressure than the resistance of the high-
pressure generator, high-pressure fluid was generated using two pressurization methods.
One is isothermal compression, by which pressure is applied with a hydraulic jack while
maintaining the cell temperature constant. Using this method, measurements were
performed from 23°C to 200°C in approximately 20°C increments under 10 temperature
conditions. Under the experimental conditions, CO$_2$ was single-phase. In addition,
spectra were acquired up to 153.8 MPa under each temperature condition. We
pressurized the CO₂ fluid gradually while maintaining the temperature constant.
Furthermore, we measured the Raman spectra twice under each $P\text{-}T$ condition. The $P\text{-}T$ conditions measured using this method are shown by filled red squares on $P\text{-}T$
injection of the CO₂ phase diagram calculated according to the explanation by Pitzer
and Sterner⁵¹ EOS (Figure 1). Regarding the other method, the pressure was increased
at first to 153.8 MPa while maintaining the high-pressure cell at a low temperature
(approx. −10°C) using a cryogen. Subsequently, we closed valve-1 (shown in Figure 2)
between the cell and the high-pressure generator. We raised the cell temperature to the
target. Using the latter method, we were able to generate fluid with pressures of 153.5–
248.7 MPa, which is higher than the pressure resistance of the high-pressure generator.
Using this method, after reaching the target temperature, the Raman spectrum was
measured while gradually reducing the pressure by loosening valve-1 (Figure 2). The
measurements were repeated more than three times at each $P\text{-}T$ condition. The
measurements are taken at temperatures from 60°C to 200°C in 20°C increments under
eight temperature conditions. The $P\text{-}T$ conditions measured using the latter method are
shown by the open blue squares in Figure 1 together with $P\text{-}T$ conditions measured in
earlier studies using HPOC and fused silica capillary capsules (FSCC).²⁸,³¹,³³–³⁶,⁵⁰
Detailed $P-T$ measurement conditions are presented in Tables S1 and S2. Hereinafter, we designate the former and latter experiments respectively as “isothermal pressurization experiments” and “near isochoric heating experiments.”

Figure 2 is a schematic drawing of the HPOC and its attached components. To remove air from the high-pressure system, the high-pressure line was flushed with CO$_2$ (99.99% purity; Sun Chemical Corp.) for about 30 s before pressurizing the fluid. The temperature was measured using a K-type thermocouple placed in direct contact with the fluid. The fluid temperature during analysis of isothermal pressurization experiments and near isochoric heating experiments were, respectively, kept to uncertainty below ± 0.1°C and ± 0.5°C through PID control of the cartridge heater (Tables S1 and S2). The room temperature was 22.1–23.6°C throughout the analysis.

We measured pressures using a PG-2TH digital pressure transducer with a manometer (WGA-650A; Kyowa Electronic Instruments Co., Ltd.). The overall accuracy of the pressure transducer was ± 0.2% of the reading. The accuracy compensation temperature of the pressure gauge was −10 to 70°C. The pressure changes during analyses of isothermal pressurization experiments and near isochoric heating experiments were, respectively, less than ± 0.1 MPa and ± 1.1 MPa. In the case of the near isochoric heating experiments, the pressure change during the analysis was large because of the large
pressure difference between the high-pressure cell and generator.

2.2 Measurement of Raman spectra of CO$_2$ in a HPOC at constant laser power

Raman spectra of the CO$_2$ fluid were obtained using a micro-Raman spectrum analysis system set up at the Hokkaido University Museum. Raman spectra were acquired during excitation by a diode-pumped solid-state laser (532 nm, Gem 532; Laser Quantum), and were acquired using a spectrometer with 75 cm focal length (Acton SP-2750; Princeton Instruments, Inc.) and a CCD camera (1650 × 200 pixels, 16 µm width, iVac; Andor Technology). A 50-µm core diameter multimode fiber served as the pinhole for confocality and as the entrance slit to the spectrometer. The laser power ($P_{\text{ill}}$) was 13.2 mW at the sapphire window surface. The excitation laser was focused through a super long working distance 10× objective (T Plan SLWD; Nikon Corp.; N.A. = 0.2). The wavenumber dispersion for each pixel of the present Raman system when using a grating of 1800 lines/mm was 0.28 cm$^{-1}$/pixel at 1400 cm$^{-1}$. The accuracy in identification of peak position was enhanced further by application of a curve-fitting technique.$^{[52]}$ Earlier studies demonstrated that least-squares fitting improves precision by approx. 30 times compared to the value based on the detector pixel resolution.$^{[52,53]}$ Each CO$_2$ band was fitted to a Gaussian and Lorentzian mixing
Spectra were collected in a single window ranging from 1007.53 to 1485.58 cm\(^{-1}\), which covers the main peaks of the Fermi diad of CO\(_2\) and two well-established reference peaks of neon occurring at 1221.73 and 1449.19 cm\(^{-1}\). Data were collected using two accumulations of 50 s or 100 s.

This study did not specifically examine the absolute value of the peak position, but instead emphasized investigation of the difference in the peak position of Fermi diad, which is not susceptible to the nonlinearity of the optical system. Nevertheless, to reduce mechanical errors in the optical system induced by changes in the measurement environment, the measured values were corrected using the atomic emission spectrum of the Ne lamp fixed to the optical system. Although Lamadrid et al.\(^{[27]}\) calibrated \(\Delta\) using the two Ne lines appearing at 1031 and 1458 cm\(^{-1}\) surrounding the Fermi diad, the \(\Delta\) was calibrated using the following equation because the wavelengths of the excitation lasers used for this study differ from the wavelengths used for theirs.

\[
\Delta_{\text{Ne calib}} = \Delta_{\text{raw}} \times \left(\frac{227.46}{\Delta_{\text{mes}}^{\text{Ne}}}\right)
\]

(1)

In that equation, \(\Delta_{\text{Ne calib}}\) denotes the corrected splitting of the Fermi diad, \(\Delta_{\text{mes}}^{\text{Ne}}\) represents the measured separation between 1449.19 and 1221.73 cm\(^{-1}\) Ne emission lines. \(\Delta_{\text{raw}}\) stands for the measured splitting of \(\Delta\) in the CO\(_2\) Raman spectrum. Tables S1 and S2 show the wavenumber difference of corrected \(\Delta\) (\(\Delta_{\text{Ne calib}}\)) together with the \(P-T\)
conditions of the fluid.

2.3 Measurement of CO₂ Raman spectra as a function of laser power

2.3.1 HPOC experiments

To assess the temperature-dependence of Δ–ρ relations accurately, the local heating caused by the focused laser must also be considered because it might affect the Raman spectrum in a similar fashion to that by which the cartridge heater heats the HPOC and the fluids.

The temperature measurement can be performed using two peaks with much lower intensity next to the Fermi diad (1264.8 and 1409.0 cm⁻¹; \(ν_{\text{H.B.}}\) and \(ν_{\text{H.B.}}^+\)), designated as hot bands.[54] Hot bands putatively arise from transitions that originate from excited vibrational states that are higher in energy than the ground vibrational state and which are attributable to the thermal energy of the molecules. The hot bands are also attributable to Fermi resonance between \(ν_1 + ν_2\) and \(3ν_2\).[55] Earlier studies have assessed CO₂ hot band availability for use as a thermometer.[25,48,56–58] These thermometers use the hot band to Fermi diad intensity ratio \(\left(\frac{I_{\text{H.B.}}^+ + I_{\text{H.B.}}^-}{I_{\text{F.D.}}^+ + I_{\text{F.D.}}^-}\right)\). Peak heights of \(ν_{\text{F.D.}}^+\), \(ν_{\text{F.D.}}^−\), \(ν_{\text{H.B.}}^+\), and \(ν_{\text{H.B.}}^-\) are represented respectively as \(I_{\text{F.D.}}^+\), \(I_{\text{F.D.}}^−\), \(I_{\text{H.B.}}^+\), and \(I_{\text{H.B.}}^−\). In the studied \(P–T\) region, temperature enhancement of about \(>4^\circ\text{C}\) can be detected using a
hot-band thermometer. Therefore, to investigate the influence of the local laser heating, we monitored the change of $\Delta$ and hot band to Fermi diad intensity ratio while changing $P_{\text{ill}}$ at two pressure conditions: 7.2 and 153.8 MPa.

We measured $\Delta$ and the hot band to Fermi diad intensity ratio using the same 10× objective (T Plan SLWD, N.A. = 0.2; Nikon Corp.) and excitation laser (532 nm) as those used for the HPOC experiments. Measurements were made while changing $P_{\text{ill}}$ at the sample surface from 1.7 to 16.7 mW. The $P_{\text{ill}}$ during the experiments were measured using a laser power meter (PD300-ROHS; Ophir Optronics Ltd.). The uncertainty of the measured $P_{\text{ill}}$ was ±3%. The fluid pressures were 7.2 MPa and 153.8 MPa at 23°C, respectively corresponding to 0.783 g/cm³ and 1.204 g/cm³. The spectrum was measured five times at each $P_{\text{ill}}$. Table 1 presents the results.

2.3.2 Natural fluid inclusions

We selected a total of seven CO₂-rich fluid inclusions hosted in mineral separates of orthopyroxene and Cr-spinel, which are derived from a mantle xenolith designated as “En2A” from Ennokentiev, Sikhote-Alin, Far Eastern Russia. Petrological descriptions were presented by Yamamoto et al. The fluid inclusion compositions were investigated using Raman spectroscopic analysis. Volatile species other than CO₂ are
not detected from the seven inclusions. Although no H$_2$O liquid phase was visible under microscopic observation, trace amounts of H$_2$O might be wetting the wall of inclusions.[6,59] For the fluid inclusions in orthopyroxene, the partial homogenization temperatures of the carbonate phase to liquid were measured using a heating–cooling stage (THMS600; Linkam Scientific Instruments Ltd.) at Hokkaido University. Homogenization temperature was not reported for Cr-spinel because of its high absorption coefficient, which made observation of the phase transition difficult, but the density estimated from the measured $\Delta$ value is presented in Table 2. The instrument was calibrated using the melting points of H$_2$O (0.0 °C) in synthetic pure H$_2$O fluid inclusions. Homogenization was recorded at the heating rate of 0.1 °C/min. Fluid densities are calculated as described by Span and Wagner[60].

The individual inclusions were measured in the order of 4.7, 11.6, 7.9, and 14.4 mW using almost identical Raman apparatus to that described section 2.2. The only difference from the configuration explained above is the objective lens: a 50× objective lens (LU Plan, N.A. = 0.8; Nikon Corp.) was used. The sample was placed on a glass slide. During the measurement, room temperature was maintained at 20.5±1.0°C. Considering that the temperature increases of inclusions per unit laser power in Cr-spinel and orthopyroxene were, respectively, approx. 6°C/mW and approx. 1°C/mW,[48] this
variation in room temperature is sufficiently smaller than the expected temperature increases of inclusions during analysis. Given the same temperature increase of inclusions per unit of laser power, the CO$_2$-rich phase of all inclusions is homogenized into a single supercritical fluid, liquid, or gas phase during the analysis. Measurements were taken five times at each $P_{\text{ill}}$. Table 2 presents the average $\Delta$ value of five measurements and their standard deviation ($1\sigma$) at each $P_{\text{ill}}$. The duration of every Raman analysis is three accumulations of 100 s for inclusion in Cr-spinel and two accumulations of 100 s for those in orthopyroxene. This is because, in the case of Cr-spinel, both incident laser and Raman scattering light are more absorbed by the host mineral because of its high absorption coefficient, resulting in a low number of CO$_2$ Raman scattering photons detected per unit time.

The measured $\Delta$ ($\Delta^{\text{raw}}$) values are first calibrated using measured and known distances between the Ne lines according to the explanation presented by Lamadrid et al.$^{[27]}$ ($\Delta_{\text{Ne calib}}$ in Table S3). Subsequently, discrepancies in the calibration curves between laboratories were corrected by adding the correction term $\delta_{\text{Eq.2}}$ to $\Delta_{\text{Ne calib}}$. Finally, corrected $\Delta$ ($\Delta_{\text{calib}}$) are defined as $\Delta_{\text{calib}} = \Delta_{\text{Ne calib}} + \delta_{\text{Eq.2}}$. According to Hagiwara et al.$^{[37]}$, $\delta_{\text{Eq.2}}$ was calculated using Equation (2), Equation (10) of Hagiwara et al.$^{[37]}$, and the 2 $\Delta_{\text{Ne calib}}$ obtained from the standard fluid inclusions with known density (0.786 and 1.167
g/cm³). Using the correction procedures described above, the differences between known density of standard fluid inclusions and density calculated by substituting Δ_{calib} into Equation (2) were found to be less than 0.2%. The values of δ_{Eq.2} are shown in the footnote of Table S3.

3. RESULTS

3.1 Temperature-dependence of Δ – ρ relations

We investigated the P–T dependence of Δ at temperatures of 23–200°C and pressures of 7.2–248.7 MPa using HPOC. In this study, the density corresponding to the P–T conditions of every analysis was calculated using the method described by Span and Wagner[60] EOS for CO2. In all, total of 151 Δ values obtained from 23 to 200°C are portrayed in Figure 3a. In agreement with results reported from earlier studies, all Δ values shift systematically to higher values with increasing density at constant temperature.[18,25,27–32,34–36,42] In addition, the (∂ρ/∂Δ)_T rates obtained from our data decrease gradually with increasing density, especially at high density. This tendency was also observed from earlier studies conducted at high density (Figure 3b).[29,31,37,42] The (∂Δ/∂T)_ρ rate was found to be negative in all density regions studied, from 0.7 to 1.2 g/cm³, which is consistent with results obtained from earlier studies for 0.0 to 1.0
The main findings obtained from HPOC experiments are that the temperature derivative of $\Delta$ at constant density ($((\partial \Delta/\partial T)_\rho)$ depends strongly on the density and that the $((\partial \Delta/\partial T)_\rho)$ rates are always negative, even at high density (Figure 3a). Although the temperature dependence of the $\Delta-\rho$ relations exists throughout the entire density range that was analyzed (0.7–1.2 g/cm$^3$), $|((\partial \Delta/\partial T)_\rho)|$ rates are maximum at approx. 0.7 g/cm$^3$; they decrease as density increases from 0.7 g/cm$^3$ (Figure 4c).

### 3.2 Regression analysis and error analysis

The respective $P-T$ changes during analysis of the isothermal pressurization experiments were less than $\pm 0.1$ MPa and $\pm 0.1^\circ$C. The $P-T$ condition shown in Table S2 is an average value obtained during analysis of the near isochoric heating experiments. The $P-T$ variation during the analysis was less than $\pm 1.1$ MPa and $\pm 0.5^\circ$C (Table S2). Density uncertainty caused by $P-T$ fluctuation during Raman analysis was lower than $\pm 0.0028$ g/cm$^3$ (Tables S1 and S2). Measurements of 153.8 MPa at 120, 140, 160, and 180$^\circ$C were taken in both the isothermal pressurization experiments (increasing pressure cycle) and near isochoric heating experiments (decreasing pressure cycle) to evaluate the effects of differences in the pressurization method. The
differences of $\Delta$ of the four pairs were $-0.018$, $-0.029$, $+0.029$, and $+0.024$ cm$^{-1}$, respectively, at 120, 140, 160, and 180°C. No systematic error resulted from the difference in the pressure generation method.

To estimate the fluid density from the sample temperature and measured $\Delta$, we conducted regression analysis. The density of CO$_2$ fluid inclusions at elevated temperatures can be found using the following polynomial equation.

$$\rho = a + bT^2 + cT^3 + d\Delta + e\Delta^2 + f\Delta^3 + g\Delta T + h\Delta^2 T + i\Delta T^2 + j\exp(\Delta)$$  \hspace{1cm} (2)

Therein, $a$ through $j$ represent fitting parameters. These parameters and associated errors are given in Table 3. In that equation, $\rho$ (g/cm$^3$), $T$ (°C), and $\Delta$ (cm$^{-1}$), respectively represent the fluid density, temperature, and Fermi diad splits of CO$_2$. It is noteworthy that “$T$” is not included in the explanatory variables in Equation (2) because we selected them so that the $p$-values of all explanatory variables are less than 0.05. Instead, $\exp(\Delta)$ was added as an explanatory variable, which is particularly useful in reflecting the characteristic that $(\partial \rho / \partial \Delta)_T$ becomes smaller at higher densities. Because the $p$-values of all explanatory variables are less than 0.008, they are influential factors for the objective variable. Equation (2) has a coefficient of determination ($R^2$) of 0.999. Equation (2) is valid in the experimentally calibrated regime of 23°C ≤ $T$ ≤ 200°C and 0.7 g/cm$^3$ ≤ $\rho$ ≤ 1.2 g/cm$^3$ (Figure 1). The half of the difference between the upper and lower bounds of
the prediction interval at 1σ of the Equation (2) was lower than ± 0.0057 g/cm³. Finally, the uncertainty in the density estimation based on Equation (2), which takes into account both the uncertainty in the model and the density variation during the analysis, is ± \sqrt{0.0028^2 + 0.0057^2} ≈ 0.006 g/cm³.

3.3 Laser heating effects during HPOC experiments

Absorption of excitation laser light by the optical window of the HPOC or CO₂ fluid itself might cause unintentional local temperature enhancement. In that case, Δ can be expected to decrease concomitantly with increasing \( P_{\text{ill}} \) because Δ decreases concomitantly with increasing temperature at constant density (Figure 3). However, all Δ values are within the range of error (Figures 5a and 5b). No systematic decrease was observed to occur along with the increase of \( P_{\text{ill}} \) (Figures 5a and 5b). Similarly, hot bands to the Fermi diad intensity ratio can increase with \( P_{\text{ill}} \) because it increases concomitantly with increasing temperature at constant density.\[^{25,48,56–58}\] Although a temperature change of about > 4°C can be detected from the hot bands to the Fermi diad intensity ratio, the intensity ratio does not change systematically with \( P_{\text{ill}} \) (Figures 5c and 5d).\[^{58}\] Therefore, results demonstrate that the influence of laser heating is lower than 4°C, at least under the present analytical conditions. Nevertheless, to avoid
possible heating effects, measurements are taken at the sample surface with $P_{\text{ill}}$ of 13.2 mW. Therefore, the maximum laser heating during the HPOC experiment, if any, is about 3°C (approx. $4 \times \frac{13.2}{16.7} \circ C$). This temperature enhancement is sufficiently lower than the experimental temperature range of 23–200°C. Therefore, we can ignore laser heating effects in the HPOC experiments.

3.4 Laser heating effects during natural fluid inclusion analysis

Because $\Delta$ decreases monotonically with laser power (Table 2), the intercept of the linear fitting between $\Delta_{\text{calib}}$ and $P_{\text{ill}}$ ($\Delta_{\text{intercept}}$) can be regarded as $\Delta$ without laser heating. For estimating the best fit straight line to data, we applied bivariate least-squares fitting method (York method) using OriginPro9.0 software (OriginLab Corporation, Northampton, US). Figure 6 presents the relation between “$\Delta_{\text{intercept}}-\Delta_{\text{calib}}$” and laser power. For all fluid inclusions, $\Delta$ tends to decrease with laser power. The slope of the relation between $\Delta$ and laser power ($\partial \Delta/\partial P_{\text{ill}}$) is, invariably, significant and negative (Table 2). Details underlying the reason for this negative slope are explained in Section 4.2, but it is not attributable to the monotonic drift of the Raman system because the measurements were performed in the order of 4.7, 11.9, 7.9, and 14.4 mW without monotonically increasing (or decreasing) $P_{\text{ill}}$. 
Figure 6a presents data for fluid inclusions with densities of 1.201, 0.919, 0.737, and 0.377 g/cm³ in Cr-spinel. For inclusions with density higher than 0.7 g/cm³, densities are calculated by substituting $\Delta_{\text{intercept}}$ into Equation (2). For inclusions with density lower than 0.7 g/cm³, $\Delta_{\text{calib}}$ was defined as $\Delta_{\text{Ne calib}} + \delta_{\text{Kawakami03}}$, where $\delta_{\text{Kawakami03}}$ was calculated from the $\Delta-\rho$ relation of Kawakami et al.[42], Equation (10) of Hagiwara et al.[37], and $\Delta_{\text{calib}}$ for two standard fluid inclusions (Table S3). Then, the density was calculated by substituting $\Delta_{\text{intercept}}$ into the $\Delta-\rho$ relation presented by Kawakami et al.[42]. For the three inclusions with densities greater than 0.7 g/cm³, $|\frac{\partial \Delta}{\partial P_{\text{ill}}} \rho|$ is shown to become smaller for higher densities (Figure 6a). A similar trend was obtained for fluid inclusions with densities of 1.167, 0.914, and 0.704 g/cm³ in orthopyroxene. However, the $|\frac{\partial \Delta}{\partial T}\rho|$ of fluid inclusions with density of 0.377 g/cm³ in Cr-spinel is 0.0075±0.0033 cm⁻¹/mW, which is clearly lower than that of 0.737 g/cm³ (0.0143±0.0020 cm⁻¹/mW). This is consistent with results of earlier studies, which show that below approx. 0.7 g/cm³, $|\frac{\partial \Delta}{\partial T}\rho|$ becomes a smaller value at lower densities. [35,36]

4. DISCUSSION

4.1 Effects of density on $\partial \Delta/\partial T$: Comparison with results of earlier studies

Many earlier studies have clarified details of the temperature dependence of
the relation between $\Delta$ and density.$^{[28,31,32,34–36,42,44,50]}$ To raise the accuracy of discussion related to the temperature dependence of $\Delta$, the differences of measurement conditions among earlier studies such as spectral resolution, pressure measurement accuracy, temperature range, and fluid composition must be clarified. After reviewing earlier studies, we eventually chose to compare the results reported by Sublett et al.$^{[36]}$, Wang et al.$^{[35]}$, and Wang et al.$^{[28]}$ with those of the present study. Details of the process of selecting the earlier studies to be used for comparison with this study are presented in Supporting Information.

Earlier studies have examined the density dependence of $|\frac{\partial \Delta}{\partial T}|$. Reports have described that $|\frac{\partial \Delta}{\partial T}|$ becomes smaller at lower densities (Figure S1).$^{[35,36]}$ By contrast, regarding density dependence of $|\frac{\partial \Delta}{\partial T}|$ at $>0.7$ g/cm$^3$, several studies have yielded somewhat different conclusions.$^{[28,35,36]}$ According to the $\Delta$–$T$–$\rho$ relation for pure CO$_2$ derived by Wang et al.$^{[35]}$ using HPOC, $|\frac{\partial \Delta}{\partial T}|$ becomes smaller at densities higher than 0.7 g/cm$^3$ (Figure 4a). This is supported by the fact that their data obtained using FSCC shows that $|\frac{\partial \Delta}{\partial T}|$ is larger at 0.743 g/cm$^3$ than at 0.807 g/cm$^3$. However, using the relation derived by Sublett et al.$^{[36]}$, $|\frac{\partial \Delta}{\partial T}|$ becomes larger at densities higher than 0.7 g/cm$^3$, which is inconsistent with the results reported by Wang et al.$^{[35]}$ (Figure 4b). Furthermore, Wang et al.$^{[28]}$ investigated the temperature dependence of $\Delta$
at 35–200°C and 40–200°C, respectively using natural and synthetic fluid inclusions in quartz with densities of 0.7074 and 0.4676 g/cm³. Results respectively portray that Δ decreased concomitantly with increasing temperature up to 200°C by 0.19 cm⁻¹ and 0.24 cm⁻¹ (Figure 4a). Comparing the results obtained from the two fluid inclusions by Wang et al. [28], there appears to be little density dependence of |(∂Δ/∂T)_ρ|. Therefore, disagreement exists between earlier studies of the density dependence of |(∂Δ/∂T)_ρ| at densities higher than 0.7 g/cm³.

Our results demonstrate that |(∂Δ/∂T)_ρ| decreases concomitantly with increasing density for densities higher than 0.7 g/cm³ (Figure 4c), which is consistent with results reported by Wang et al. [35]. Our results support the results reported by Wang et al. [35] more than those of Sublett et al. [36], probably because Wang et al. [35] obtained more data at high densities than Sublett et al. [36] did. Therefore, this study, which specifically examined high-density data, yielded results that are rather consistent with those reported by Wang et al. [35] for densities higher than 0.7 g/cm³. The fluid inclusions of Wang et al. [28] at 0.7074 and 0.4676 g/cm³ had similar |(∂Δ/∂T)_ρ|, perhaps because the density was 0.7074–0.4676 g/cm³ at which the sign of d|(∂Δ/∂T)_ρ|/dρ is reversed. Consequently, the two fluid inclusions used by Wang et al. [28] might have coincidentally had densities for which |(∂Δ/∂T)_ρ| is comparable mutually. Strictly speaking, however, the effect of
the amount of H$_2$O in the CO$_2$-rich inclusions should also be considered, as described by Wang et al.\cite{35}, but because the amount of H$_2$O is unknown, we do not discuss it further.

In summary, the combination of our $\Delta$–$T$–$\rho$ relation in the high-density region and that in the low-density region investigated in results of earlier studies suggests that density at which the sign of $\partial |(\partial \Delta/\partial T)_{\rho}|/\partial \rho$ is reversed exists around 0.6–0.7 g/cm$^3$.

Therefore, when the density of CO$_2$ fluid inclusions is measured using a Raman CO$_2$ densimeter, fluid inclusions with densities of approximately 0.6–0.7 g/cm$^3$ are the most susceptible to $\Delta$ change because of laser heating.

4.2 Apparent density reduction caused by laser heating

4.2.1 Causes of variation in $(\partial \Delta/\partial P_{\text{ill}})_{\rho}$

The values of $\Delta$ obtained from the fluid inclusions clearly decrease concomitantly with increasing $P_{\text{ill}}$. The decrease shows density dependence (Figure 6).

These features can be explained well by the $\Delta$–$T$–$\rho$ relation (i.e., $(\partial \Delta/\partial T)_{\rho}$ is always negative and $|(\partial \Delta/\partial T)_{\rho}|$ reaches its maximum at 0.6–0.7 g/cm$^3$) and the monotonic temperature increase of the inclusion with increasing $P_{\text{ill}}$, but other factors that can engender variations in $(\partial \Delta/\partial P_{\text{ill}})_{\rho}$ must also be examined carefully.
Another mechanism that causes a reduction in $\Delta$ with increasing $P_{ill}$ is the difference in the temperature increase of individual inclusions during analysis. In other words, the inclusions with density of 0.737 g/cm$^3$ of Cr-spinel and 0.704 g/cm$^3$ of orthopyroxene have the highest $|(\partial \Delta / \partial P_{ill})_\rho|$ in their respective host minerals, probably because those inclusions were the hottest during analysis. Because Hagiwara et al.$^{[48]}$ have demonstrated that the size and depth from the sample surface of the selected inclusions have little effect on laser heating, they will be excluded as factors in the difference in the magnitude of $|(\partial \Delta / \partial P_{ill})_\rho|$. Regarding size effect, the minimum and maximum inclusion radius in orthopyroxene are 4.9 µm and 9.3 µm, respectively, and the ratio of the laser heating coefficient ($B_{9.3\mu m}/B_{4.9\mu m}$) calculated by Figure 6b of Hagiwara et al.$^{[48]}$ is 0.95. Therefore, the difference in temperature increase due to the inclusion size difference is only 5%. The maximum temperature rise expected for inclusions in orthopyroxene is about $1^\circ$C/mW × 15 mW = 15$^\circ$C, thus the temperature difference at that time is $15 \times 0.05 = 0.75^\circ$C, and the change in $\Delta$ caused by this slight temperature difference would be negligible. In fact, no systematic correlation exists between the size and depth of inclusions and $|(\partial \Delta / \partial P_{ill})_\rho|$ (Tables 2 and S3). Furthermore, according to earlier studies, the temperature increase per unit of laser power in the same host mineral is almost identical for different inclusions.$^{[48]}$ Therefore, the difference in heating rates can be
excluded as a reason for the difference in $|\partial \Delta / \partial P_{\text{ill}}|_\rho$ between inclusions.

If one assumes that the temperature increase per unit laser power is nearly constant for inclusions in the same host mineral, then $|\partial \Delta / \partial T|_\rho = |\partial \Delta / \partial P_{\text{ill}}|/(dT/dP_{\text{ill}}) \propto |\partial \Delta / \partial P_{\text{ill}}|_\rho$. Therefore, similarly to the density dependence of $|\partial \Delta / \partial T|_\rho$ predicted by the HPOC experiment, $|\partial \Delta / \partial P_{\text{ill}}|_\rho$ also can be expected to have a maximum value of around 0.6–0.7 g/cm$^3$, and $|\partial \Delta / \partial P_{\text{ill}}|_\rho$ can be expected to decrease as the density increases at >0.7 g/cm$^3$. In fact, inclusions with densities closest to 0.6–0.7 g/cm$^3$ have the largest $|\partial \Delta / \partial P_{\text{ill}}|_\rho$ in each host mineral. In addition, for inclusions in both orthopyroxene and Cr-spinel, for densities higher than 0.7 g/cm$^3$, the higher the density, the smaller the $|\partial \Delta / \partial P_{\text{ill}}|_\rho$, which is consistent with the trend expected from HPOC experiments. Therefore, one can infer that the combination of laser heating and the temperature dependence of the $\Delta-\rho$ relations is responsible for the observed features of $|\partial \Delta / \partial P_{\text{ill}}|_\rho$, such as $(\partial \Delta / \partial P_{\text{ill}})_\rho$ always being negative and $|\partial \Delta / \partial P_{\text{ill}}|_\rho$ being largest for inclusions with densities closest to 0.6–0.7 g/cm$^3$.

### 4.2.2 Accurate density estimation in the presence of laser heating

As expected from the results of HPOC experiments, the greatest decrease in $\Delta$ for fluid inclusions in the 0–14.4 mW range was observed for the fluid inclusions in Cr-
spinel with density closest to 0.6–0.7 g/cm³. For this inclusion (spinel03 fi146), the
density estimated by substituting the $\Delta_{\text{calib}}$ measured at 14.4 mW without considering
the effects of laser heating into Equation (2) is 0.655 g/cm³, whereas the density
obtained by substituting the $\Delta_{\text{intercept}}$ corrected for the effect of laser heating into
Equation (2) is 0.737 g/cm³. In this case, the density is underestimated by 0.082 g/cm³
(approx. 12%). In addition, for the fluid inclusion of 0.373 g/cm³ (spinel03 fi154),
where $|(\partial \Delta / \partial P_{\text{ill}})_{\rho}|$ is smaller than that of the inclusion of 0.737 g/cm³, the decrease in
density itself is 0.052 g/cm³, which is smaller than that of the inclusion of 0.737 g/cm³.
However, in percent notation, the density underestimation is 15%, which is severer than
that of 0.737 g/cm³. Therefore, even though $|(\partial \Delta / \partial P_{\text{ill}})_{\rho}|$ is small at densities lower than
0.6–0.7 g/cm³, the relative underestimation of density because of laser heating might be
rather more severe than for inclusions at 0.6–0.7 g/cm³. Therefore, for inclusions in host
minerals such as Cr-spinel, which have a large absorption coefficient and which are
affected strongly by laser heating, the density might be underestimated by about >10%,
even at typical laser power of 15 mW. For such inclusions, some correction is necessary
to estimate the density accurately. Underestimation of the density of fluid inclusions in
orthopyroxene (0.704 g/cm³, opx06 fi005), which has almost identical density to that of
spinel03 fi146, is 3.4% according to the calculation presented above, which is one-
fourth that of Cr-spinel. The reason for this difference in density underestimation might be that the temperature increase of the inclusions in Cr-spinel is greater than that in orthopyroxene because the absorption coefficient of Cr-spinel (approx. 20 cm$^{-1}$)\cite{61} is larger than that of orthopyroxene (approx. 9 cm$^{-1}$)\cite{62}. For an inclusion with density of 1.201 g/cm$^3$ in Cr-spinel, the underestimation is only 0.9% (= 0.010 g/cm$^3$) under the conditions described above. Therefore, for densities of approx. 1.1–1.2 g/cm$^3$, where $|\partial \Delta/\partial T|\rho$ is small, the underestimation of density because of laser heating is small, even in host minerals that are extremely sensitive to laser heating, such as Cr-spinel. Therefore, at such very high densities, the effect of laser heating can be neglected in many cases.

The following is an explanation of how to estimate the density accurately even in the presence of laser heating, based on data of opx06 fi005, which had the largest $|\partial \Delta/\partial P_{\text{ill}}|\rho$ among inclusions with known density. The densities obtained by substituting $\Delta_{\text{calib}}$ into Equation (2) without correcting for the effect of laser heating ($\rho_{\Delta_{\text{calib}}}$) are 0.699 ± 0.005 g/cm$^3$ at 4.7 mW, 0.692 ± 0.003 g/cm$^3$ at 7.9 mW, 0.682 ± 0.005 g/cm$^3$ at 11.9 mW, and 0.681 ± 0.003 g/cm$^3$ at 14.4 mW, respectively, which become lower than the known density of 0.704 g/cm$^3$ as the laser power increases (Table 2). In the case of inclusions in orthopyroxene, at laser powers below 4.7 mW, the
deviation between $\rho_{T_h}$ and $\rho_{\Delta\text{calib}}$ is less than 0.005 g/cm$^3$ (= 0.7%). The effect of laser heating on density estimation is almost equivalent to the density uncertainty in the calibration curve itself. Thereby, the effect of laser heating can be ignored. However, at 14.4 mW, the deviation between $\rho_{T_h}$ and $\rho_{\Delta\text{calib}}$ is 0.023 g/cm$^3$ (= 3.4%), which is clearly an underestimation of the true value. In this way, when the effect of heating cannot be neglected, substituting $\Delta\text{intercept}$, corrected for the effect of laser heating, into the $\Delta$–$\rho$ relation yields a value of 0.707 ± 0.005 g/cm$^3$, which is consistent with the true value (0.704 g/cm$^3$) within the error (Table 2).

In light of the points raised above, one must ascertain whether correlation exists between the $\Delta$ value and laser power in the laser power region bracketing the laser power to be used for the measurement when measuring a sample for which the effect of laser heating on $\Delta$ is unknown. If a significant positive value of $|(\partial \Delta / \partial P_{\text{lai}})_{\rho}|$ is obtained, as observed in the natural fluid inclusions of this study, then that value indicates that $\Delta$ is reduced by the laser heating and indicates that the density is somewhat underestimated if not corrected for that effect. However, if $|(\partial \Delta / \partial P_{\text{lai}})_{\rho}|$ is not significantly positive, as observed for HPOC in this study and for colorless quartz in earlier studies$^{[48]}$, then one can infer that the effect of laser heating is negligible, at least in that laser power region. If the effect of laser heating is found to be present, then the correction method described
in the paragraph above is useful to estimate the density more accurately, whether or not a correction is applied depends on the quality of the data desired by the researchers. However, at least when comparing and interpreting $\Delta$ obtained from different mineral species, the presence or absence of laser heating effects should be noted. If laser heating effects on the measurements are not negligible, then we recommend some report of how the ideal measurement conditions were reached and what corrections were made to the raw data to interpret them.

5. CONCLUSIONS

Raman spectra of CO$_2$ were measured at 23–200$^\circ$C and 7.2–248.7 MPa using a high-pressure optical cell. Fermi diad splits ($\Delta$) decreased concomitantly with increasing temperature at constant density. In addition, the $|(\partial \Delta / \partial T)_{\rho}|$ is maximum at approx. 0.7 g/cm$^3$; it decreases as the density increases from approx. 0.7 g/cm$^3$. In combination with the results of the earlier study, we conclude that $|(\partial \Delta / \partial T)_{\rho}|$ increases gradually from 0.0 g/cm$^3$ to 0.6–0.7 g/cm$^3$; it then decreases as the density increases to 1.2 g/cm$^3$. Therefore, if the inclusion temperature is increased by a certain temperature by laser heating, the largest decrease in $\Delta$ will be observed for inclusions with density of 0.6–0.7 g/cm$^3$. In
contrast, fluid inclusions with very high densities of 1.1–1.2 g/cm³ are less affected by laser heating.

To confirm that the density dependence of $|(\partial \Delta/\partial T)_\rho|$ predicted by HPOC experiments is also valid for natural fluid inclusions, we measured $\Delta$ for fluid inclusions with densities ranging from approx. 0.3–1.2 g/cm³ in Cr-spinel and orthopyroxene at varying laser powers ($P_{\text{ill}}$). We found that, above 0.7 g/cm³, $|(\partial \Delta/\partial P_{\text{ill}})_\rho|$ decreased concomitantly with increasing density. Below 0.7 g/cm³, it decreased concomitantly with decreasing density. Furthermore, even though $|(\partial \Delta/\partial P_{\text{ill}})_\rho|$ become smaller at lower densities below 0.6–0.7 g/cm³, the relative underestimation of density because of laser heating might be rather more severe than for inclusions at 0.6–0.7 g/cm³. The key finding is that for host minerals with large absorption coefficients at the excitation laser wavelength, laser heating can underestimate the CO₂ density by more than 10%, even at typical laser powers used for inclusion analysis. If the decrease in $\Delta$ because of laser heating is not negligible, then a more accurate fluid density is obtainable by estimating the intercept $\Delta$ ($\Delta_{\text{intercept}}$, i.e. $\Delta$ at 0 mW) from the correlation between $\Delta$ and laser power, and substituting it into the $\Delta$–$\rho$ relation.

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Figure 1 $P$–$T$ projection of the CO$_2$ phase diagram showing locations of all data measured for this study. Filled red squares show $P$–$T$ conditions at which measurements are made using isothermal pressurization experiments. Open blue squares denote $P$–$T$ conditions at which measurements are made using near isochoric heating experiments. The black symbols give $P$–$T$ conditions under which measurements were made in earlier studies using a high-pressure optical cell and fused silica capillary capsule.$^{[28,31,33,34,43,50]}$ Black solid lines are phase coexistence curves. Grey ones are isochore calculated using Pitzer and Sterner$^{[51]}$ EOS. Contours are labeled according to fluid density (g/cm$^3$). The data shown are those presented in Tables S1 and S2.
Figure 2 (a) Schematic diagram of experimental apparatus used for high-$P$–$T$ Raman spectroscopic investigation. CO$_2$ is loaded into the HPOC from the right side through stainless steel tubing with outer diameter of 1/16 inch. During the near isochoric heating experiments, the fluid pressure in the cell was adjusted by gradually loosening valve-1. The excitation laser (532 nm) was focused on the CO$_2$ fluid through a 10× objective lens. The laser power was 13.2 mW at the surface of optical window. (b) Cross-sections of the HPOC. It is equipped with a 2.5-mm-thick sapphire optical window that is transparent to visible light.
Figure 3 (a) Relation of CO$_2$ density and Fermi diad (Δ) as a function of temperature. Raman spectra of CO$_2$ are measured at temperatures of 23–200°C and pressures of 7.2–248.7 MPa using HPOC. For this study, the density corresponding to the temperature and pressure condition of every analysis was calculated according to Span and Wagner$^{[60]}$ EOS for CO$_2$. The data shown are those from Tables S1 and S2. (b) Comparison of published Δ–ρ relations. All densimeters shown are within the density region in which calibration measurements were made and effective at near room temperature.$^{[28–31,35,37,42,43]}$
Figure 4 Δ change relative to initial Δ obtained at approx. 24°C as a function of temperature. Colored solid lines show the temperature dependence of Δ at constant density calculated using (a) Equation (3) of Wang et al.[35], (b) Equation (8) of Sublett et al.[43], and (c) Equation (2) of this study. The dotted line shows the extrapolation of the Δ–T–ρ relation derived in each study to the P–T region where no experimental calibration has been performed. (a, b) Colored solid lines are isochores at 0.7, 0.8, and 0.9 g/cm³. (a) Black solid lines with open symbols are data obtained from the FSCCs with densities of 0.807 and 0.743 g/cm³ by Wang et al.[35]. Dashed–dotted lines show data obtained from the fluid inclusions with densities of 0.707 and 0.468 g/cm³ by Wang et al.[28]. (c) Colored solid lines are isochores at 0.7, 0.8, 0.9, 1.0, 1.1, 1.15, and 1.2 g/cm³.
Figure 5 Fermi diad split (Δ) (a, b) and hot band to the Fermi diad intensity ratio (c, d) of CO₂ with pressures of 153.8 MPa (a, c) and 7.2 MPa (b, d) as a function of the laser power at the sapphire window surface. Red bars represent the expected Δ change attributable to the temperature change of 4°C under measured P–T conditions calculated using Equation (2). The blue bar represents the expected \( \frac{I_{H,B}}{I_{F,D}} + \frac{I_{H,B}}{I_{F,D}} \) change attributable to temperature change of 4°C under measured P–T conditions calculated using Equation (5) of Hagiwara et al.\(^{[48]} \). Measurements were made five times at each laser power. Error bars represent 1σ. Data shown are from Table 1.
Figure 6 Δ change of CO₂-rich fluid inclusions hosted in Cr-spinel and orthopyroxene versus laser power. The vertical axis shows deviation of the measured Δ (Δ_{calib}) from the Δ value at 0 mW (Δ_{intercept}) estimated from the intercept of the linear fit of the measured Δ and laser power. Error bars for Δ show the standard deviation (n = 5). Those for laser power are 3%. Dashed lines show linear fit (York method) to four data points. (a) Red, green, yellow, and blue symbols respectively represent fluid inclusions with densities of 1.201, 0.919, 0.737, and 0.377 g/cm³ in Cr-spinel. (b) Red, green and yellow symbols respectively represent fluid inclusions with densities of 1.167, 0.914, and 0.704 g/cm³ in orthopyroxene.
Table 1 Variation of hot bands to the Fermi diad intensity ratio and Δ of CO₂ in HPOC at 153.8 and 7.2 MPa at different laser powers.

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a Densities calculated according to Span and Wagner\(^6\) EOS.

b Calculated from Equation (1).

c Error is standard deviation \((n = 5)\).

d HBR: Hot bands to the Fermi diad intensity ratio.
Table 2: Relation between $\Delta_{\text{calib}}$ and $P_{\text{ill}}$ obtained from natural fluid inclusions with various densities, and the density corrected for the effect of laser heating ($\rho_{\Delta_{\text{intercept}}}$) as estimated from the relation.

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<th>$\rho_{\Delta_{\text{intercept}}}$ b g/cm$^3$</th>
<th>$\rho_{\Delta_{\text{calib}}}$ c g/cm$^3$</th>
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<th>$\sigma_{P_{\text{ill}}}$ mW</th>
<th>$\Delta_{\text{calib}}$ cm$^{-1}$</th>
<th>$\sigma^e_{\Delta}$ cm$^{-1}$</th>
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\(^a\) Densities calculated using Span and Wagner\[^{60}\] EOS from measured partial homogenization temperatures of the carbonate phase to liquid; +25.4°C for opx06 fi005, +2.2°C for opx06 fi010, and –53.4°C for opx07 fi008. n.d.: not determined.

\(^b\) \(\rho_{\Delta\text{intercept}}\) was obtained by substituting \(\Delta\text{intercept}\) and 20°C into Equation (2).

\(^c\) \(\rho_{\Delta\text{calib}}\) was obtained by substituting \(\Delta\text{calib}\) and 20°C into Equation (2).

\(^d\) Density for this sample is obtained by substituting \(\Delta\text{intercept}\) into Equation of Kawakami et al.\[^{42}\] because the experimental calibration of Equation (2) of this study did not cover density lower than approx. 0.7 g/cm\(^3\).

\(^e\) Error is standard deviation (\(n = 5\)).

\(^f\) Error is standard error.
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