



Title	Experimental and numerical studies on failure behaviours of sandstones subject to freeze-thaw cycles
Author(s)	Yahaghi, Javad; Liu, Hongyuan; Chan, Andrew; Fukuda, Daisuke
Citation	Transportation geotechnics, 31, 100655 https://doi.org/10.1016/j.trgeo.2021.100655
Issue Date	2021-11
Doc URL	http://hdl.handle.net/2115/90378
Rights	© <2021>. This manuscript version is made available under the CC-BY-NC-ND 4.0 license http://creativecommons.org/licenses/by-nc-nd/4.0/
Rights(URL)	http://creativecommons.org/licenses/by-nc-nd/4.0/
Type	article (author version)
File Information	2nd Revision - Freez-thaw Experimental-Numerical---FinalVersion-13Sep2021.pdf



[Instructions for use](#)

Experimental and Numerical Studies on Failure Behaviours of Sandstones Subject to Freeze-Thaw Cycles

Javad Yahaghi¹, Hongyuan Liu^{1*}, Andrew Chan¹ and Daisuke Fukuda^{1,2}

¹School of Engineering, University of Tasmania, Hobart, TAS 7001, Australia

²Faculty of Engineering, Hokkaido University, Hokkaido 060-8628, Japan

Abstract

The freeze-thaw induced damage of rock affects the durability and serviceability of geo-structures, especially those constructed in the regions frequently impacted by climatic changes. A series of laboratory tests including P-wave velocity tests, freeze-thaw tests, uniaxial compression strength (UCS) tests and Brazilian tensile strength (BTS) tests are conducted to investigate the physical-mechanical properties and failure behaviours of Tasmanian sandstones subjected to various freeze-thaw cycles. It is observed that the P-wave velocity, BTS and UCS of the sandstone decrease as the number of freeze-thaw cycles increases, in which the decreasing rate from 0 to 20 freeze-thaw cycles was more pronounced than that from 20 to 40 and 40 to 60 freeze-thaw cycles. Moreover, it is found that the main failure mode of the sandstone changes from axial splitting to shearing along a single plane in the UCS tests and from central smooth fractures to a central zigzag fracture in the BTS tests with the number of freeze-thaw cycles increasing. Three-dimensional (3D) numerical modellings are then conducted using a self-developed 3D hybrid finite-discrete element method (HFDEM) parallelized on the basis of general-purpose graphic processing units (GPGPU) to further investigate the failure mechanisms of Tasmanian sandstones subjected to various freeze-thaw cycles in the UCS and BTS tests. The 3D numerical modellings agree very well with the experimental observations that the physical-mechanical parameters of the sandstone degrade with the increasing number of the freeze-thaw cycles. Moreover, the 3D numerical modellings reveal the deterioration and failure mechanisms of sandstones subjected to various freeze-thaw cycles. For the sandstone specimens without subjecting to freeze-thaw cycles, axial splitting is the main failure pattern while tensile and mixed-mode damages are the dominant failure mechanism in the UCS tests. For the sandstone subjecting to various freeze-thaw cycles, the increasing number of freeze-thaw cycles causes the macroscopic cracks to propagate, interact and coalesce in the shear behaviour resulting in the final shear fracture pattern in the UCS test. The 3D numerical modellings of the BTS test show that, although, for both the models with and without subjecting to freezing and thawing cycles, a central fracture is the eventual failure pattern, the failure surface becomes more zigzag as the number of freeze-thaw cycles increases.

* Corresponding author: Dr Hongyuan Liu (Email: Hong.Liu@utas.edu.au and Tel: 0061 6226 2113):

33 Keywords: Freeze-thaw cycles, rock, sandstone, UCS, BTS, 3D fracture process analysis and FDEM

34 **1. Introduction**

35 Rock is one of the most common natural construction materials on Earth. Cold regions,
36 including permafrost areas and seasonally freezing areas, constitute a large portion of Earth's
37 continent. More than 20% of the continental surface in the northern hemisphere are occupied
38 by permafrost, whereas more than half of the surface experiences seasonal freezing and
39 thawing [1]. In the southern hemisphere, Antarctica is known as the coldest continent on the
40 Earth. In most coastal regions of Antarctica, the mean annual temperature is around -12°C
41 while the lowest surface temperature ever recorded is -89°C at Russian Vostok station within
42 Australian Antarctic Territory [2]. Tasmania has a generally cooler and wetter climate than that
43 in other states of Australia. The temperature of Tasmania in winter can go as low as -14°C in
44 the highlands such as Central Plateau although the coastal areas rarely go below freezing and
45 the summer temperatures can reach up to 41°C . While increasing human economic activities
46 have led to the construction of more and more geotechnical engineering structures in cold
47 regions, it is expected that, in the future, more infrastructures will be constructed in southern
48 hemisphere.

49 Any kind of natural rocks and geo-structures in these cold regions are not only subjected to
50 external loads but also experiencing severe environmental effects. Freeze and thaw induced
51 settlement is a common phenomenon observed in seasonal freezing areas and is the cause of
52 significant damage to the built infrastructure [3], [4]. As an example, an uplifting displacement
53 of 88 mm has been caused by the freeze and thaw cycles and has led to the deformations and
54 crackings of the supporting concrete structure of the centre columns of the Myllypuro Ice Rink
55 facility in Finland [3]. Long-term monitoring of average global temperatures indicate an
56 ongoing change of the climate [5], which has resulted increasing temperatures in permafrost.
57 The increasing temperature leads to thawing of portions of the permafrost area and thickening
58 of the upper crust layer where the active freezing-thawing cycles occur, which then result in
59 considerable settlement of the ground surface damaging infrastructures. Therefore,
60 understanding the behaviour of rock upon the freezing and thawing cycles is essential to adapt
61 the operation practices, design philosophies and develop suitable methods to minimize the
62 damages [6].

63 One of the earliest documented cases of investigating the behaviour of grounds subjected to
64 the freezing and thawing cycles was the use of artificial freezing at Brunkeberg tunnel in
65 Stockholm in 1876 [7]. As the industrial development was accelerating in northern Russia to

66 develop railways and mining operations in the late nineteenth century, the study of permafrost
67 as an applied science began to protect civil structures from freeze-thaw damages [1]. The
68 deterioration of rock under frost-heave and freeze-thaw cycles has become an unavoidable
69 concern in engineering such as road, railroad, bridge, tunnelling, pipeline, and building
70 constructions [8]–[10].

71 The deterioration of rock under freeze-thaw actions has been investigated by many researchers
72 through relating one or more physical-mechanical properties of rocks such as moisture content,
73 mineralogical composition, texture, rock strength, and pore microstructure to single factor of
74 freeze-thaw actions such as temperature range, frequency and applied stress. However, the
75 freeze-thaw action and loading are both repetitive cycles and the joint action may worsen the
76 damage of rock and lead to severe deterioration of the long-term mechanical properties of rock.
77 Tan et al. [10] found that the elastic modulus, compressive strength and cohesive strength of
78 biotite granite decreased significantly with the number of freeze-thaw cycles increasing. A
79 statistical model was developed by Bayram [11] to estimate the UCS of limestones after
80 subjecting to freeze-thaw cycles. Another statistical model was proposed to experimentally
81 investigate various rock index properties, including the dry density, ultrasonic velocity, point
82 load strength, and slake-durability test indexes, after freeze-thaw cycles [12]. Wang et al. [13]
83 investigated the physical properties of sandstone specimens subjected to freeze-thaw cycles,
84 including the density, porosity, P-wave velocity, UCS, and deformation modulus. Various
85 researchers have extensively studied the mechanical behaviours of transversely isotropic rocks
86 such as slate subjected to freeze-thaw cycles and developed some corresponding models [14]–
87 [21]. Moreover, another study [22] conducted triaxial compression tests with various confining
88 pressures of 5, 10 and 20 MPa to investigate the change of wave velocities, mechanical
89 properties and permeability characteristics of red sandstone. The specimens were divided into
90 four groups, and underwent 0, 4, 8 and 12 freezing and thawing cycles. It was found that the
91 increase of the numbers of freeze-thaw cycles decreased the UCS, elastic modulus, cohesion,
92 angle of internal friction and P-wave velocity of the red sandstone. It was concluded that the
93 damage of rock caused by the freeze-thaw cycles led to the changes of microstructure and then
94 mechanical performance. Ultrasonic and mechanical tests including compression, tension and
95 shear, of red sandstones subjected to freeze-thaw cycles were carried out in another study,
96 which concluded that the red sandstone performed worse as the numbers of freeze-thaw cycles
97 increased [23]. Generally the rock with a lower porosity has a higher strength so that a greater
98 suction force (hence, a lower temperature) is required for the low porosity rocks to crack [24]

99 during the freeze-thaw tests. According to Matsuoka [24], high porosity rocks begin to crack
100 at 0 to -1 °C and terminate at about -5 °C in the freeze-thaw tests, while in medium porosity
101 rocks the cracking temperature is between -3 °C and -6 °C and in low porosity rocks the
102 cracking starts below -4 °C.

103 To summarize the findings above, although many researches have been conducted based on
104 laboratory tests to investigate the effect of freeze-thaw cycles and have shown a decrease of
105 the mechanical properties of the rocks with the freeze-thaw cycles increasing, there is no
106 consensus on the effects of the specific number of freeze-thaw cycles, freezing temperature
107 and combination of freeze-thaw cycles with loads on the deterioration of rock subjected to
108 various number of freeze-thaw cycles.

109 In order to gain a further understanding of the effect of freeze-thaw cycles on the rock
110 deterioration and failure, some scholars have implemented numerical methods to analyse the
111 freeze-thaw induced damage besides the experimental methods. A simple linear stress-strain
112 constitutive relationship was implemented into a two-dimensional (2D) plane strain finite
113 element model with a thermal-mechanical-flow coupling to simulate freeze-thaw experiments
114 [25]. An isogeometric analysis-based numerical model was applied to simulate the thermo-
115 hydromechanically coupled processes in ground freezing [26]. Another research conducted
116 numerical analyses to investigate the stability of a rock mass slope subjected to freeze-thaw
117 cycles [27], in which the freeze-thaw coefficient of the rock was firstly measured and the
118 generalized Hoek-Brown criterion was then employed to determine the parameters of slope
119 rock mass establishing a numerical rock slope excavation model. According to another
120 numerical study, the volume expansion from the freeze-thaw cycles applied an stable force on
121 joints which resulted in the tensile stress concentration area emerging at the joint tip [28]. In
122 another research [29], the variations of the modal parameters such as resonant frequencies,
123 damping ratios and mode shapes were analysed to assess the freeze-thaw resistance of
124 limestone through a finite element model.

125 These numerical studies greatly increased our understanding of the effect of freeze-thaw cycles
126 on the physical-mechanical behaviour of rocks. However, most of those numerical modellings
127 are conducted in two-dimension (2D). Three-dimensional (3D) modelling is seldom conducted
128 to investigate the effect of freeze-thaw cycles on the deterioration of the physical-mechanical
129 parameters and failure progressive process although 3D modellings of rock failure process
130 under mechanical loads using various numerical methods have been conducted in literatures

131 [30], [31], [32], [33]. Moreover, although complex thermo-mechanical-hydro coupling
132 modelling or even 3D modelling have been conducted using finite element methods (FEM) in
133 several literatures, the fracture behaviour of rocks is not modelled due to the limitation of
134 continuum mechanics – based FEM in dealing with rock fracture and fragmentation. Besides,
135 there is a lack of research on the effect of freeze-thaw cycles on the deterioration of rocks in
136 Australia or even southern Hemisphere. Therefore, further research is necessary to investigate
137 the fracture mechanism of rock under freeze-thaw cycles using advanced numerical methods
138 which are capable of modelling rock fracture.

139 Correspondingly, the main aim of the present work is to experimentally investigate the
140 physical-mechanical and failure behaviours of Tasmanian sandstones subjected to the freezing
141 and thawing cycles and then numerically simulate them using a self-developed 3D hybrid
142 finite-discrete element method (HFDEM), which is parallelized on the basis of general purpose
143 graphic processing units (GPGPU) and capable of modelling rock fracture and fragmentation
144 [34]–[36].

145 The remaining part of this paper is organized as follows; both the experimental testing method
146 and numerical method are firstly presented. The deterioration of the physical-mechanical
147 properties of the sandstone subjected to various freeze-thaw cycles are then quantified using
148 the experimental testing method and discussed on the basis of damage mechanics, which
149 justifies that the freeze-thaw induced damage can be modelled by deteriorating the physical-
150 mechanical parameters of rocks with the number of freeze-thaw cycle increasing. After that, a
151 GPGPU-parallelized HFDEM is implemented to model the damaging mechanism and failure
152 progressive process of the sandstone subjected to various freeze-thaw cycles in the uniaxial
153 compression strength (UCS) tests and Brazilian tensile strength (BTS) tests. Finally, the results
154 from the experimental tests and numerical simulations are compared with each other to
155 conclude the deterioration and failure mechanism and the fracture patterns of the sandstones
156 subjected to various freeze-thaw cycles.

157 **2. Research Methods**

158 **2.1. Experimental tests**

159 The target sandstone cores were obtained through diamond drilling with the drill size of HQT
160 from the construction site of the Museum of Old and New Art (MONA 42.8125° S, 147.2615°
161 E) located on the Berriedale peninsula in Tasmania, Australia. The diamond drilling was
162 conducted perpendicularly to the bedding plane and the sandstone specimen was then cut

163 perpendicularly to the axis of the drill cores, i.e. parallelly to the bedding plane but the
164 specimens around the bedding plane were dropped to avoid any obvious heterogeneities. Each
165 sandstone specimen for the UCS test had a diameter of 60 mm and a height of 165 mm while
166 that for the BTS test had a diameter of 60 mm and a height of 30 mm. Thus, the height to
167 diameter ratios of the rock specimens were 2.75 and 0.5 for the UCS and BTS tests, respectively,
168 and the sizes of the specimens met the requirements of ISRM for both UCS and BTS tests [37].
169 Before any UCS or BTS tests, P-wave velocities of all the rock specimens were measured using
170 a Pundit PL-200 testing equipment from Proceq, as shown in Fig. 1.

171 After that, the rock specimens were divided into 4 sets with 6 specimens in each set (three for
172 UCS and another three for BTS). One set of specimens were directly subjected to the UCS and
173 BTS tests. This set corresponded to the reference case of zero freeze-thaw cycle. For other 3
174 sets of specimens, before either UCS or BTS tests were conducted, the specimens were firstly
175 immersed in the pure water for two weeks and then put into a climatic cabinet for freeze-thaw
176 tests. A climatic controlled cabinet with an environmental chamber controller (Fig. 2. i)) was
177 employed for the freeze-thaw tests, during which the conditions of the climatic cabinet, i.e.
178 temperatures and moistures were set following those in previous researches [22], [38]–[40] and
179 corresponding to the climatic conditions in Tasmania. As can be seen from Fig. 2. ii), one cycle
180 consisted of 9 hours of freezing time (which included 1 hour for reducing the temperature from
181 +20 to -20 °C and 8 hours at the constant of -20 °C) and 9 hours of thawing time (which
182 included 1 hour for increasing the temperature from -20 to +20 °C and 8 hours at the constant
183 of +20 °C), which were efficient for the heat transfer and uniform temperature distribution
184 during each phase according to previous researches [22], [38]–[40]. During the switch between
185 the freeze-thaw cycles, the temperature varied between +20 °C to -20 °C by the changing rate
186 of 0.67 °C/min. The humidity in the climatic cabinet was kept 100%, which made sure that the
187 specimens would not lose any moistures although they were not sealed. The number of freeze-
188 thaw cycles for three sets of the rock specimens was set as 20, 40 and 60.

189 After the freeze-thaw tests, the P-wave velocities of cylindrical sandstone specimens along
190 their axial directions were measured again under the room temperature +20 °C. Finally, the
191 UCS and BTS tests were conducted for all the specimens in each set using a Matest high
192 stability compression testing apparatus with an automatic servo-controlled system (Fig. 3) by
193 following the ISRM standards. The testing system includes a hydraulic loading system with
194 the capacity of 2000 kN, an electronic measurement system and a data acquisition and
195 processing UTMII software which records all testing data in a USB disc drive.

196 2.2. Numerical methods and models

197 2.2.1 Introduction to the numerical method of GPGPU-parallelized HFDEM

198 GPGPU-parallelized HFDEM is to be implemented to model the damaging mechanism and
199 failure progressive process of the sandstones subjected to various freeze-thaw cycles in the
200 UCS and BTS tests. It is a hybrid finite-discrete element method (HFDEM) developed by the
201 authors [41] on the basis of the open source Y library [42] and further parallelized by the
202 authors on the basis of general-purpose graphic processing units (GPGPU) [36]. The GPGPU-
203 parallelized HFDEM has passed a series of fundamental rock mechanics tests [41], [43] and
204 provides a powerful numerical tool to investigate the fracture and fragmentation of rocks under
205 various static and dynamic loading conditions. Compared with the numerical methods
206 reviewed in the introduction section, GPGPU-parallelized HFDEM can naturally model the
207 damage and cracking behaviour of rocks induced by the freeze-thaw cycles and the fracture
208 and fragmentation of rocks in the UCS and BTS tests through its damaging and fracturing
209 algorithm, i.e. transition from continuum to discontinuum, which is explained in next paragraph
210 since a complete introduction of GPGPU-parallelized HFDEM can be found in the authors'
211 former publications [36], [41].

212 In GPGPU-parallelized HFDEM, rocks are modelled in 3D and discretized into an assembly
213 of tetrahedral finite elements in the same way as that in the traditional FEM. Different from the
214 traditional FEM, initially zero-thickness cohesive elements are inserted between any adjacent
215 finite elements, which may damage and then completely break to allow open and/or slide to
216 occur depending on local loading conditions there. The damage of the cohesive elements
217 follows the concept of a smeared crack [35], [44], as shown in Fig. 4. Once the Mohr-Coulomb
218 strength criterion with tension cut-off is satisfied, the cohesive element damages in either
219 tensile or shear modes, i.e. mode-I or mode-II, following the tensile or shear softening curves
220 shown in Fig. 4. i) and ii), respectively. The corresponding mode-I and mode-II damage
221 variables are defined as $D_I = (o - o_p)/o_t$ and $D_{II} = (s - s_p)/s_t$, respectively, where o and s
222 are the opening and sliding displacements, respectively, o_p and s_p are the elastic limits of the
223 opening and sliding displacements, and o_t and s_t are the ultimate limits of the opening and
224 sliding displacements. The mixed-mode damage variable is defined as $D_{Mixed} =$
225 $\min\left(1, \sqrt{D_I^2 + D_{II}^2}\right)$.

226

227 2.2.2 Numerical models

228 The modelled cylindrical specimens have a size of 60 mm in diameter and 165 mm in height
229 in the UCS test (Fig. 5. i)) and a size of 60 mm in diameter and 30 mm in height for the BTS
230 test (Fig. 5. ii)). For the UCS test, two loading plates with each having a size of 70 mm in
231 diameter and 10 mm in height were placed at the top and bottom of the specimens and moved
232 towards each other with a constant vertical loading rate of 5 cm/s to apply a uniaxial load on
233 the cylindrical specimens through Coulomb frictional contacts. The cylindrical specimen was
234 completely free except the contacts. The cylindrical model was discretised into 97,162
235 tetrahedral elements, 19,511 nodes and 143,639 initially zero-thickness cohesive elements. For
236 the BTS test, two square loading plates with each having a length of 60 mm and a width of 30
237 mm were placed at the top and bottom of the specimens and moved towards each with a
238 constant vertical loading rate of 5 cm/s, too. The BTS model was discretised into 64,513
239 tetrahedral elements, 12,307 nodes and 125,222 initially zero-thickness cohesive elements. The
240 input parameters assigned to the models are obtained following an iterative calibration
241 procedure until the stress-strain curve and the failure pattern from the simulations closely
242 matched those obtained from the laboratory tests. Four sets of separate calibrations were
243 performed for both control specimens and those subjected to 20, 40 and 60 freezing and
244 thawing cycles. The input parameters obtained during the calibration procedures generate
245 acceptable strength and elastic properties as well as fracture patterns, which, however, are not
246 a unique set [45]. Although the loading velocity of the simulation is higher than that in the
247 laboratory experiment, it has been demonstrated that a quasi-static loading condition is ensured
248 through the artificial critical damping scheme with viscous damping coefficient [36], [46]. A
249 mass scaling factor of 10 is further applied to reduce the computing time of the 3D FDEM
250 simulations, which won't affect the obtained simulation results notably [36], [46].

251 It must be emphasized that the input parameters related to fracturing (i.e. tensile strength,
252 cohesion, internal friction angle and fracture energies) in FDEM should be considered as
253 microscale parameters and are different from the general macroscale mechanical parameters as
254 obtained in the UCS and BTS tests. Meanwhile, the macroscopic input parameters including
255 elastic modulus and Poisson's ratio, can be directly obtained from experimental tests. In quasi-
256 static condition, gravity is neglected since the density has no physical meaning in this case. For
257 model calibration purposes, it is convenient to classify the input parameters into the following
258 categories: (1) penalty terms and numerical control parameters namely contact penalty, and
259 cohesive penalty, (2) macroscopic parameters, including the elastic modulus (E), and Poisson's

260 ratio (ν), and (3) microscopic parameters including microscopic tensile strength, microscopic
261 cohesion and microscopic internal friction angle. For (1), we follow the procedure for the
262 determination of these values established in [36], [47]. For macroscopic physical parameters
263 in (2) appropriate values can be directly established according to those from direct
264 measurements. One of the most critical steps in modelling with FDEM is the calibration of
265 input microscale parameters in (3). In general, the calibration process is a tedious trial and error
266 process against the physical testing results. Table 1 lists the input parameters of the numerical
267 modelling for the control specimen, which is defined as the specimen without subjecting to any
268 freezing and thawing cycles and the specimens subjected to 60 freezing and thawing cycles
269 which selected among three specimens with its UCS and elastic modulus closest to the average.

270

271 **3. Experimental and numerical results and analyses**

272 **3.1. Deterioration of physical-mechanical properties of sandstones subjected to various** 273 **freeze-thaw cycles**

274 Table 2 summarizes the variations of the P-wave velocity, elastic modulus, UCS and BTS of
275 the sandstones subjected to 0, 20, 40 and 60 freeze-thaw cycles. Fig. 6. i) illustrates the change
276 of the P-wave velocity of the sandstone with the increasing number of freeze-thaw cycles. In
277 terms of the average value, the P-wave velocity reduced by 9%, 23% and 24% after 20, 40 and
278 60 freeze-thaw cycles, respectively. The reason might be that the increased freeze-thaw cycles
279 resulted in increased micro cracks, which led to the reduction of P-wave velocity. Moreover,
280 the size of pores become larger with the freeze-thaw cycle increasing, which resulted in longer
281 time for waves to transmit through the specimens due to longer path, or an increase in
282 discontinuities leading the decrease of the P-wave velocity. As shown by the trend line in Fig.
283 6. i) there was a linear correlation between the P-wave velocity and the number of the freeze-
284 thaw cycles.

285 As can be seen from Fig. 6. ii), the average value of BTS of sandstones decreases from 5.35
286 MPa to 5.24 MPa, 5.10 MPa and 5.06 MPa with the number of the freeze-thaw cycles
287 increasing from 0 to 20, 40 and 60, respectively. In other words, the tensile strengths of the
288 sandstones subjected to 20, 40 and 60 freeze-thaw cycles decrease by 2.1%, 4.4% and 5.5%,
289 respectively. The sandstone specimens subjected to the increased number of freeze-thaw cycles
290 have more microcracks [48], which decrease the ability of the sandstone for saving the strain
291 energy and thus reduce BTS. The correlation between BTS and the number of freeze-thaw

292 cycles is also linear, as shown in Fig. 5, and the correlation coefficient is larger than that in the
293 case of P-wave velocity.

294 The effect of the number of the freeze-thaw cycles on average value of UCS of the sandstone
295 is depicted in Fig. 6. iii), which shows the average UCS of the sandstones changes from 37.84
296 MPa to 35.18 MPa, 32.98 MPa and 29.15 MPa as the number of the freeze-thaw cycles
297 increases from 0 to 20, 40 and 60, respectively. Thus, the UCS of the sandstone decreases
298 overall as the number of the freeze-thaw cycles increases. There are some deviations in some
299 of results, which can be considered by the cause of inhomogeneity inside the specimens [49].

300 Since there are various microcracks induced by the freeze-thaw cycles in the sandstone
301 specimens, these pre-existing microcracks with respect to the axial loading direction first close
302 during the UCS test when the applied compressive stress reaches to the crack-closure stress.
303 Further compressions induce local tensile stresses, which may exceed the local tensile strength
304 at the tips of the pre-existing flaws and initiate the new cracks on those tips. Thereafter, these
305 cracks propagate in a manner of wing cracks, parallel to the applied maximum principal stress
306 [50] resulting in axial splitting. The increasing number of freeze-thaw cycles induces more
307 freezing loads to be applied on the microcracks and pores in the sandstone. The freezing load
308 then further increases the number and size of the microcracks and pores, which result in new
309 microcracks generated by freeze-thaw cycles facilitating the crack propagation to occur during
310 UCS discussed above. That is why, the UCS of sandstone reduces with the freeze-thaw cycles
311 increasing. The correlation in Fig. 6. iii) is still approximately linear although the correlation
312 coefficient is smaller.

313 Fig. 6. iv) shows the relationship between the elastic modulus of sandstones and the number of
314 freeze-thaw cycles. It can be seen from Fig. 6. iv) that, when the number of freeze-thaw cycles
315 is increased to 20, 40 and 50, the average elastic modulus reduces by 10.4%, 15.6%, and 16.9%,
316 respectively, compared with that of the sandstone without subjecting to the freeze-thaw cycles.
317 The correlation between the elastic modulus and the number of freeze-thaw cycles is also linear,
318 as shown in Fig. 6. iv), and the correlation coefficient is larger than that in the case of P-wave
319 velocity and UCS.

320 The mechanisms of the deterioration of the physical-mechanical properties of sandstones may
321 be that the increased freeze-thaw cycles resulted in increased micro cracks. Jiang et al. [51]
322 investigated the deterioration mechanisms using scanning electron microscope (SEM) and then
323 concluded that the freeze-thaw cycles increased the width of microcracks resulting in

324 microscopic structure changes. Niu et al. [52] pointed out these microscopic structure changes
 325 of the rocks were due to the coupling effects of water and temperature variation after
 326 conducting experimental studies on crack coalescence behaviour of double unparallel fissure-
 327 contained sandstone specimens subjected to freeze-thaw cycles under uniaxial compression.
 328 The effect of water includes the dissolution and stress effects while temperature variation
 329 damages rocks by means of different temperature gradients and phase transitions of water
 330 during the freeze-thaw process [52], [53]. Moreover, Zhou et al. [54] and Niu et al. [52]
 331 investigated the microstructure around the crack tips in sandstones with and without subjecting
 332 to freeze-thaw cycles by SEM and concluded the nature of the failure of the flawed rock mass
 333 under freeze-thaw cycles lies in the fatigue damage of rocks. They further elaborated the stress
 334 fields around the tips of pre-existing fissures periodically redistributed due to the repeated frost-
 335 heaving actions in response to various freeze-thaw cycles, which led to the fatigue damage
 336 around these tips of the fissures and contributed to the failure evolution of the flawed rock mass.
 337 To better characterize the deterioration of the physical-mechanical properties of the Tasmanian
 338 sandstones subjected to the freeze-thaw cycles, a damage variable, D , is defined on the basis
 339 of the average uniaxial compressive strength as Eq. 1:

$$340 \quad D = \frac{\bar{\sigma}_c - \bar{\sigma}'_c}{\bar{\sigma}_c} \quad \text{Eq. 1}$$

341 where $\bar{\sigma}_c$ is the average uniaxial compressive strength of the sandstone specimens without the
 342 freeze-thaw cycles and $\bar{\sigma}'_c$ is that of the specimens subjected to the freeze-thaw cycles. The
 343 damage variables obtained using Eq. 1 are summarized in Table 1 for the sandstones subjected
 344 to 0, 20, 40 and 60 freeze-thaw cycles, which clearly shows that the damage variable increases
 345 as the number of the freeze-thaw cycles increases.

346 **3.2. Three-dimensional modelling of the failure process of the sandstones without** 347 **subjecting to freeze-thaw cycles**

348 Fig. 7. i) and ii) shows the modelled rock failure progressive process in terms of the
 349 distributions of the minor principal (i.e. compressive) stress and the damage variable [i.e., D ,
 350 $D=1$ means macroscopic (broken) CE6 while $D=0$ corresponds to intact], respectively, at
 351 different loading stages (points A-F in the stress-strain curve in Fig. 7. iii) in the FDEM
 352 simulation of the UCS test for specimens without subjecting to freezing and thawing cycles.
 353 Fig. 7. i) A shows the stress in the specimen at the stage before the onset of nonlinearity in the
 354 stress-strain curve. The growth of unstable microscopic cracks commences as the loading

355 displacement continues and extends until the peak stress of the stress-strain curve is reached
356 (point B in Fig. 7. iii)). Afterwards, macroscopic cracks form due to the propagation and
357 coalescence of the microscopic cracks coalescence, which results in the loss of bearing capacity
358 of the sandstones. As can be seen in Fig. 7. i) C-E, the stress begins to decrease with increasing
359 strain (point C-E in Fig. 7. iii)). Finally, the formed macroscopic cracks propagate further,
360 resulting in the complete failure of sandstones (point F in Fig. 7. iii)).

361 Fig. 7. ii) shows the distributions of all damage (including pure mode-I, pure mode-II and
362 mixed-mode) (A-F-1) and pure mode-II damage (F-2) at different loading stages. As can be
363 seen from the comparison between Fig. 7. ii) A-F-1 and F-1, the tensile and mixed-mode
364 damage is the dominant failure mechanism at both pre-peak stage (A-B in Fig. 7. iii)) and post-
365 peak stage (C-F-1 in Fig. 7. iii)). The modelled tensile and mixed-mode failure mechanism is
366 consistent with the multiple axial splitting failures observed in the experiments considering the
367 limitation of FDEM in modelling pure mode I failure mechanism and usually treating it as
368 mixed-mode failure mechanism for the numerical simulations with unstructured meshes [29].
369 After that, at final stage of strain softening (F-1 in Fig. 7. iii)), the formed tensile and mixed-
370 mode cracks propagate and coalescence forming the axial splitting failure pattern.

371 Fig. 8. i) and ii) illustrates the modelled rock failure progressive process in terms of the
372 distributions of the horizontal stresses and the damage variable D at different loading stages
373 (points A-D in the stress-strain curve in Fig. 8. iii)) in the FDEM simulation of the BTS test. It
374 can be seen from Fig. 8. i) A that uniform tensile stress fields are formed around the central
375 line of the disc and there is no failure at the stage before the peak stress (points A in Fig. 8.
376 iii)). Once the indirect tensile strength of the rock is reached (points B in Fig. 8. iii)), tensile
377 macroscopic cracks initiate around the central diametrical line of the rock disc. After that, the
378 macroscopic cracks start to propagate along the central diametrical line, as shown in Fig. 8. i)
379 C. Till this stage, the tensile damage is the dominant failure mechanism, as indicated by the
380 mixed-mode damage in Fig. 8. ii) A-C. Finally, the further propagation and coalescence of the
381 formed macroscopic cracks split the rock disc into two halves (Fig. 8. ii) D), during which there
382 are some shear damages around the two loading locations. Thus, the modelled failure
383 mechanism and fracture pattern are consistent with those observed in the experiments.
384 However, the numerical modelling shows a single failure surface along the central diametrical
385 line of the disc while the experiment indicates multiple failure surfaces. Double checking of
386 the final fracture pattern in Fig. 8. ii) D reveals that there are multiple unmerged macro fractures
387 around the main fracture surface, which are similar to those observed in the BTS experiment.

388 **3.3 Three-dimensional modelling of the failure process of the sandstones subject to** 389 **various freeze-thaw cycles**

390 Fig. 9. i) and ii) illustrates the modelled rock failure progressive process in terms of the
391 distributions of the principal stress and the damage variable at different loading stages (points
392 A-F in the stress-strain curve in Fig. 9. iii) in the FDEM simulation of the UCS test of the
393 sandstone subjected to 60 freezing and thawing cycles. Fig. 9. i) A shows the stress distribution
394 in the specimen at the pre-peak stress stage and the stress is lower than that at the same stage
395 in the control model (Fig. 7. i) A). At the peak stress (point B in Fig. 9. iii)), which is smaller
396 than that of the control model (Fig. 7. i) B), the microscopic cracks propagate form a
397 macrocrack (Fig. 9. ii) B). As can be seen from Fig 9. i) C-E, the stress begins to decrease with
398 increasing strain (point C-E in Fig. 9. iii)). At the final stage (Fig. 9. i) F), the formed
399 macroscopic cracks propagate further, resulting in the complete failure of sandstones (point F
400 in Fig. 9. iii)).

401 Fig. 9. ii) A-F-1 and F-2 show the distributions of all damage and the pure mode-II damage
402 only, respectively, at different loading stages. It should be noted that all damage includes the
403 pure mode-I, pure mode-II and mixed-mode damages. At the peak stress (point B in Fig. 9. iii)),
404 the dominant failure mechanism is the tensile and mixed-mode damages, which is also more
405 manifest than that in the previous modelling of the control specimen at the peak stress. Similar
406 to the modelling of the control model, the macro cracks form after the peak stress and the
407 mixed-mode damage continues to be the dominant failure mechanism (Fig. 9. ii) C-F-1).
408 Finally, during the late strain-softening stage, the tensile and mixed-mode cracks propagate,
409 interact and coalesce in the mode-II damage mechanism resulting in the final shear failure
410 pattern (Fig. 9. ii) F-2).

411 The modelled failure progressive processes of the sandstone subjected to 60 freeze-thaw cycles
412 in the BTS test are illustrated in Fig. 10. i), ii) and iii) in terms of the distributions of the
413 horizontal stresses, the evolution of the damage variable D, and the completed stress-strain
414 curve, respectively. Before the peak stress (point A in Fig. 10. iii)), almost uniform tensile
415 stresses around the central diametral line of the disc are observed again. At the peak load, the
416 macroscopic cracks are initiated in the mixed-mode along the central diametrical line of the
417 rock disc (Fig. 10. i) B). Compared with the control model, this model presents severe mixed-
418 mode damages at this stage due to the low physical-mechanical parameters for the rock
419 subjected to 60 freeze-thaw cycles. Afterward, the macroscopic cracks propagate along the

420 central diametrical line (Fig. 10. i) C) splitting the rock disc into two halves (Fig. 10. i) D). The
421 comparison between the failure mechanisms shown in Fig. 10. ii) C (mixed-mode I-II damage
422 only) and D (all damages) indicates that the mixed-mode damage is still dominant in the BTS
423 modelling of the sandstone subjected to various freezing and thawing cycles.

424 **4 Discussions**

425 **4.1 Comparisons between the experimental and numerical stress-strain curves of the** 426 **sandstones subject to various freeze-thaw cycles**

427 Fig. 11. i-iv) compares the axial stress versus axial strain curves obtained from both
428 experimental tests and numerical simulations of sandstones subjected to various freeze-thaw
429 cycles in the UCS tests, in which, the crack initiation stress (dark blue colour marks) and peak
430 stress (red colour marks) from both the laboratory tests and numerical simulations are marked
431 and their values presented in Table 3. It can be seen from Fig. 11. that the experimental and
432 numerical stress-strain curves agree well with each other in the terms of the linear elastic stage,
433 crack initiation stress, nonlinear crack growth stage, peak strength, post-peak unstable crack
434 growth stage and brittle failure behaviour although the numerical simulations fail to model the
435 initial compaction stage. All stress-strain curves from the laboratory tests show a nonlinear
436 downward concave shape in the initial compaction stage, which are omitted in Fig. 11. for the
437 convenience of the comparisons between the laboratory tests and numerical simulations. The
438 initial compaction stage is resultant from the closure of initial pores and fissures within the
439 rocks subjected to various freeze-thaw cycles. The numerical simulations consider those initial
440 pores and fissures caused by various freeze-thaw cycles through deteriorating the physical-
441 mechanical parameters of the rocks. Thus, it is reasonable that the numerical simulation is
442 unable to simulate the initial compaction stage. It is obvious from Fig. 11. and Table 3. that the
443 linear elastic stage and crack initiation stress from the laboratory tests and numerical
444 simulations are comparable, which also show that they decrease as the number of freeze-thaw
445 cycles increases. The numerical simulations are able to capture the nonlinear crack growth
446 stages, too, although the exact forms of the nonlinear crack growth stages are not the same as
447 those from the laboratory tests. The peak strength and post-peak unstable crack growth stage
448 of the stress-strain curves from the numerical simulation have an acceptable conformity with
449 those from the experimental tests, too. However, the post-peak stress curves from the
450 experimental tests become flatten with the number of freeze-thaw cycles increasing, i.e.
451 somewhat ductile crack growth in the early phase of the post-peak unstable crack growth stage,
452 which has not been captured by the numerical simulations. After that, a sudden loss of bearing

453 capacities does happen for all the stress-strain curves obtained from the laboratory tests, which
454 is well captured by all numerical simulations.

455 **4.2 Comparison between the experimental and numerical failure patterns of the** 456 **sandstones subject to various freeze-thaw cycles**

457 Fig. 12. compares the final failure patterns of of the sandstone specimens subjected to various
458 freeze-thaw cycles in the UCS tests obtained from both laboratory experiments and numerical
459 simulations. It is found that all specimens without undergoing freeze-thaw cycles failed in axial
460 splitting during the laboratory UCS tests (Fig. 12. i)A). For the specimens subjected to 20
461 freeze-thaw cycles, one of the specimens still failed in axial splitting model while the other two
462 specimens failed in shearing along a single plane during the laboratory UCS tests (Fig. 12. i)
463 B). The failure mode of all the specimens subjecting to 40 freeze-thaw cycles changed to the
464 shear failure although shearing along a single plane was only observed for one specimen and
465 the other two specimens failed in double shear (Fig. 12. i) C). Moreover, all the specimens
466 subjected to 60 freeze-thaw cycles failed in the shearing mode along a single plane (Fig. 12. i)
467 D). Thus, the analysis of the failure mode shows that it changes from the axial splitting to
468 various shear failure modes in the laboratory UCS tests of sandstones subjecting to with an
469 increasing number of freeze-thaw cycles. Moreover, it is noted that the shearing along a single
470 plane is the most common failure mode of the specimens in the laboratory UCS tests after
471 subjecting to the freeze-thaw cycles. As it is clear from Fig. 12. ii) A, the failure pattern of the
472 control specimen from the numerical simulations was axial splitting failure, which agrees with
473 the experimental observation (Fig. 12. i) A). With the number of freeze-thaw cycles increasing,
474 the failure pattern changed to the shear failure pattern, as shown in Fig. 12. ii) B, C and D
475 which agrees with the experimental observation, too (Fig. 12. i) B, C and D).

476 Fig. 13. compares the final failure patterns of of the specimens subjected to various freeze-
477 thaw cycles in the BTS tests obtained from both laboratory experiments and numerical
478 simulations. It can be seen from Fig. 13. A that the failure pattern of the specimens subjecting
479 to zero freeze-thaw cycles from both laboratory experiments and numerical simulations was
480 central multiple splitting fractures. The failure pattern of central multiple splitting fractures is
481 the dominant failure mode in the BTS test of sandstones with a relatively higher tensile strength
482 since the central multiple splitting fractures are developed in order to release the stored high
483 strain energy. The main failure pattern changed to a central fracture for most of the specimens

484 treated by various freeze-thaw cycles Fig. 13. B-D, which can be explained by the increasing
485 number of microcracks in sandstones caused by various numbers of freeze-thaw cycles.

486 The change of the failure patterns from the axial splitting failure to shear failure in the UCS
487 tests and those from the central multiple splitting failures to the central single fracture in the
488 BTS tests can be explained in terms of the pre-existing cracks, the local fatigue-damage zones
489 around these pre-existing cracks caused by the freezing and thawing cycles [51, 53], and their
490 propagations during the uniaxial loading of the sandstones subjected to various freeze-thaw
491 cycles. Under uniaxial loading in the UCS test, the pre-existing cracks become free to
492 propagate when they are aligned parallel to the maximum principal stress (mostly tensile). In
493 other words, the specimen fails in axial splitting mode when the microstructure of a specimen
494 cannot prevent the propagation of these cracks [55], which is the case for the sandstone without
495 subjecting to the freeze-thaw cycles. For the sandstone subjected to the freeze-thaw cycles,
496 local fatigue-damaged zones form around the pre-existing cracks according to [51, 53], which
497 are further motivated during the loading process. When the compressive loads are applied
498 during the UCS tests, the pre-existing cracks propagate through these local fatigue damaged
499 zones. Since these local fatigue damaged zones are not necessary to be parallel to the maximum
500 principal stress, the coalescences of the pre-existing cracks take place in adjacent or in close
501 proximity to the tips of the suitably oriented microcracks and releases the strain energy in the
502 form of shear failure, which is why macroscopic shear failure patterns are observed during the
503 UCS tests of the sandstones subjected to more freeze-thaw cycles. Similarly, during the BTS
504 tests of the sandstones without subject to the freeze-thaw cycles, the pre-existing cracks aligned
505 along the loading diametral line are forced to initiate and propagate resulting in smooth central
506 splitting fracture patterns. For the sandstone samples subjected to various freeze-thaw cycles,
507 the freeze-thaw cycles induce the local fatigue-damaged zones around the tips of the pre-
508 existing cracks, which cause the pre-existing crack to initiate, propagate and coalesce through
509 these local fatigue-damage zones resulting in more zigzag central splitting fracture patterns.

510 However, the 3D numerical simulations model the random pre-existing defects in sandstones
511 through non-uniform meshes and model the freeze-thaw induced damages through
512 deteriorating physical-mechanical properties of the sandstones subjected to various freeze-
513 thaw cycles. Thus, the 3D numerical simulations fail to capture the local fatigue-damaged
514 zones around the tips of the pre-existing defects due to the freeze-thaw cycles although the 3D
515 numerical simulations well capture the deterioration mechanism and failure process of the

516 sandstones including the transition of the failure patterns of the sandstones with the number of
517 freeze-thaw cycles increasing.

518 **5. Conclusions**

519 A series of laboratory tests were firstly conducted to investigate the physical-mechanical
520 behaviours of Tasmanian sandstones subjected to different freezing and thawing cycles, which
521 includes P-wave velocity, UCS, BTS and freeze-thaw tests. A self-developed 3D GPGPU-
522 parallelized FDEM is then employed to model the failure processes of these sandstones with
523 the focus on clarifying the damage mechanisms of the sandstones subjected to various freeze-
524 thaw cycles. The following specific conclusions were obtained:

- 525 • The laboratory tests showed that P-wave velocity, UCS and BTS of Tasmanian
526 sandstones reduced with the number of freeze-thaw cycles increasing. Their reduction
527 rates from 0 to 20 freeze-thaw cycles were higher than those from 20 to 40 cycles and
528 from 40 to 60 cycles.
- 529 • The main failure pattern of the sandstone changed from axial splitting to shearing in the
530 UCS tests and from smooth central fractures to a zigzag central fracture in the BTS tests
531 with the number of freeze-thaw cycles increasing.
- 532 • The GPGPU-parallelized 3D modelling reproduces the failure processes of Tasmanian
533 sandstones subjected to various freeze-thaw cycles in the UCS and BTS tests, which
534 validates the experimental observations that the physical-mechanical parameters of the
535 sandstone degrade with the increasing number of freeze-thaw cycles.
- 536 • The 3D modelling clarifies the deterioration and failure mechanisms of sandstones
537 subjected to various freeze-thaw cycles. For the sandstone without subjecting to freeze-
538 thaw cycles, axial splitting is the main failure pattern in the UCS test since tensile and
539 mixed-mode damages are dominant failure mechanisms observed in the corresponding
540 3D modelling. For the sandstones subjecting to various freeze-thaw cycles, the
541 increasing number of freeze-thaw cycles causes the macroscopic cracks initiated and
542 nucleated by the tensile and mixed-mode damages to propagate, interact and coalesce
543 in the mode-II failure mechanisms resulting in the final shear fracture pattern in the
544 UCS test. For both the control model and that subjected to freezing and thawing cycles
545 in the BTS test, a central splitting fracture is the dominant failure pattern, which,
546 however, is accompanied by zigzag fractures in the BTS test of the specimens subject
547 to various freeze-thaw cycles.

548 **Acknowledgements**

549 The first author would like to thank the support of Tasmanian Postgraduate Research
550 Scholarships which enable him to conduct his PhD study at University of Tasmania.

551

552 **Data availability**

553 The raw/processed data required to reproduce these findings are available from the
554 corresponding author upon request.

555

556 **References**

- 557 [1] D. A. Streletskiy, N. I. Shiklomanov, and F. E. Nelson, “Permafrost, Infrastructure, and
558 Climate Change: A GIS-Based Landscape Approach to Geotechnical Modeling,” *Arctic,*
559 *Antarct. Alp. Res.*, vol. 44, no. 3, pp. 368–380, 2012.
- 560 [2] “Australian Antarctic Division.” [Online]. Available: <http://www.antarctica.gov.au>.
- 561 [3] Y. Zhang and R. L. Michalowski, “Thermal-Hydro-Mechanical Analysis of Frost Heave and
562 Thaw Settlement,” *J. Geotech. Geoenvironmental Eng.*, vol. 141, no. 7, p. 04015027, 2015.
- 563 [4] G. Sinnathamby, H. Gustavsson, and L. Korkiala-tanttu, “Frost Heave and Thaw Settlement
564 Estimation of a Frozen Ground Frost Heave and Thaw Settlement Estimation of a Frozen
565 Ground,” no. November, 2015.
- 566 [5] G. Krinner *et al.*, “Long-term climate change: Projections, commitments and irreversibility,”
567 *Clim. Chang. 2013 Phys. Sci. Basis Work. Gr. I Contrib. to Fifth Assess. Rep. Intergov. Panel*
568 *Clim. Chang.*, vol. 9781107057, pp. 1029–1136, 2013.
- 569 [6] Y. Zhang, “Thermal-Hydro-Mechanical Model for Freezing and Thawing of Soils,” 2014.
- 570 [7] G. F. Gambino and J. P. Harrison, “Rock Engineering Design in Frozen and Thawing Rock:
571 Current Approaches and Future Directions,” *Procedia Eng.*, vol. 191, no. June, pp. 656–665,
572 2017.
- 573 [8] N. Matsuoka and J. Murton, “Frost weathering: recent advances and future directions,”
574 *Permafrost Periglacial Process.*, vol. 19, no. 2, pp. 195–210.
- 575 [9] M. Krautblatter, D. Funk, and F. K. Günzel, “Why permafrost rocks become unstable: A rock-
576 ice-mechanical model in time and space,” *Earth Surf. Process. Landforms*, vol. 38, no. 8, pp.
577 876–887, 2013.
- 578 [10] X. Tan, W. Chen, J. Yang, and J. Cao, “Laboratory investigations on the mechanical properties
579 degradation of granite under freeze–thaw cycles,” *Cold Reg. Sci. Technol.*, vol. 68, no. 3, pp.
580 130–138, Sep. 2011.
- 581 [11] F. Bayram, “Predicting mechanical strength loss of natural stones after freeze–thaw in cold
582 regions,” *Cold Reg. Sci. Technol.*, vol. 83–84, pp. 98–102, Dec. 2012.
- 583 [12] İ. Ince and M. Fener, “A prediction model for uniaxial compressive strength of deteriorated
584 pyroclastic rocks due to freeze–thaw cycle,” *J. African Earth Sci.*, vol. 120, pp. 134–140, Aug.
585 2016.
- 586 [13] P. Wang, J. Xu, S. Liu, S. Liu, and H. Wang, “A prediction model for the dynamic mechanical
587 degradation of sedimentary rock after a long-term freeze-thaw weathering: Considering the
588 strain-rate effect,” *Cold Reg. Sci. Technol.*, vol. 131, pp. 16–23, Nov. 2016.

- 589 [14] J. C. Jaeger, "Shear Failure of Anisotropic Rocks," *Geol. Mag.*, vol. 97, no. 01, p. 65, Feb.
590 1960.
- 591 [15] Y. M. Tien and M. C. Kuo, "A failure criterion for transversely isotropic rocks," *Int. J. Rock
592 Mech. Min. Sci.*, vol. 38, no. 3, pp. 399–412, Apr. 2001.
- 593 [16] Y. M. Tien, M. C. Kuo, and C. H. Juang, "An experimental investigation of the failure
594 mechanism of simulated transversely isotropic rocks," *Int. J. Rock Mech. Min. Sci.*, vol. 43, no.
595 8, pp. 1163–1181, Dec. 2006.
- 596 [17] Y.-K. Lee and S. Pietruszczak, "Application of critical plane approach to the prediction of
597 strength anisotropy in transversely isotropic rock masses," *Int. J. Rock Mech. Min. Sci.*, vol.
598 45, no. 4, pp. 513–523, Jun. 2008.
- 599 [18] O. Saeidi, V. Rasouli, R. G. Vaneghi, R. Gholami, and S. R. Torabi, "A modified failure
600 criterion for transversely isotropic rocks," *Geosci. Front.*, vol. 5, no. 2, pp. 215–225, Mar.
601 2014.
- 602 [19] M. Asadi and M. H. Bagheripour, "Modified criteria for sliding and non-sliding failure of
603 anisotropic jointed rocks," *Int. J. Rock Mech. Min. Sci.*, vol. 73, pp. 95–101, Jan. 2015.
- 604 [20] M. Singh, N. K. Samadhiya, A. Kumar, V. Kumar, and B. Singh, "A nonlinear criterion for
605 triaxial strength of inherently anisotropic rocks," *Rock Mech. Rock Eng.*, vol. 48, no. 4, pp.
606 1387–1405, Jul. 2015.
- 607 [21] X. Tan, H. Konietzky, T. Frühwirth, and D. Q. Dan, "Brazilian Tests on Transversely Isotropic
608 Rocks: Laboratory Testing and Numerical Simulations," *Rock Mech. Rock Eng.*, vol. 48, no. 4,
609 pp. 1341–1351, Jul. 2015.
- 610 [22] J. Yu, X. Chen, H. Li, J. Zhou, and Y. Cai, "Effect of freeze-thaw cycles on mechanical
611 properties and permeability of red sandstone under triaxial compression," *J. Mt. Sci.*, vol. 12,
612 no. 1, pp. 218–231, Jan. 2015.
- 613 [23] P. Wang, J. Xu, X. Fang, P. Wang, G. Zheng, and M. Wen, "Ultrasonic time-frequency
614 method to evaluate the deterioration properties of rock suffered from freeze-thaw weathering,"
615 *Cold Reg. Sci. Technol.*, vol. 143, no. June 2016, pp. 13–22, 2017.
- 616 [24] N. Matsuoka, "Microgelivation versus macrogelivation: Towards bridging the gap between
617 laboratory and field frost weathering," *Permafrost. Periglac. Process.*, vol. 12, no. 3, pp. 299–
618 313, 2001.
- 619 [25] K. M. Neaupane, T. Yamabe, and R. Yoshinaka, "Simulation of a fully coupled thermo–
620 hydro–mechanical system in freezing and thawing rock," *Int. J. Rock Mech. Min. Sci.*, vol. 36,
621 no. 5, pp. 563–580, 1999.
- 622 [26] Y. W. Bekele, H. Kyokawa, A. M. Kvarving, T. Kvamsdal, and S. Nordal, "Isogeometric
623 analysis of THM coupled processes in ground freezing," *Comput. Geotech.*, vol. 88, pp. 129–
624 145, 2017.
- 625 [27] X. Luo, N. Jiang, X. Fan, N. Mei, and H. Luo, "Effects of freeze-thaw on the determination
626 and application of parameters of slope rock mass in cold regions," *Cold Reg. Sci. Technol.*,
627 vol. 110, pp. 32–37, 2015.
- 628 [28] H. Lin, D. Lei, R. Yong, C. Jiang, and S. Du, "Analytical and numerical analysis for frost
629 heaving stress distribution within rock joints under freezing and thawing cycles," *Environ.
630 Earth Sci.*, vol. 79, no. 12, pp. 1–17, 2020.
- 631 [29] Y. I. Fogue-Djombou, S. Corn, L. Clerc, D. Salze, and E. Garcia-Diaz, "Freeze-thaw
632 resistance of limestone roofing tiles assessed through impulse vibration monitoring and finite
633 element modeling in relation to their microstructure," *Constr. Build. Mater.*, vol. 205, pp. 656–

- 634 667, 2019.
- 635 [30] J. Bi, X. P. Zhou, and Q. H. Qian, “The 3D Numerical Simulation for the Propagation Process
636 of Multiple Pre-existing Flaws in Rock-Like Materials Subjected to Biaxial Compressive
637 Loads,” *Rock Mech. Rock Eng.*, vol. 49, no. 5, pp. 1611–1627, 2016.
- 638 [31] X. P. Zhou and J. Bi, “3D Numerical Study on the Growth and Coalescence of Pre-existing
639 Flaws in Rocklike Materials Subjected to Uniaxial Compression,” *Int. J. Geomech.*, vol. 16,
640 no. 4, 4015096, 2016.
- 641 [32] Y. Wang, X. Zhou, Y. Wang, and Y. Shou, “A 3-D conjugated bond-pair-based peridynamic
642 formulation for initiation and propagation of cracks in brittle solids,” *Int. J. Solids Struct.*, vol.
643 134, pp. 89–115, 2018.
- 644 [33] Y. T. Wang, X. P. Zhou, and M. M. Kou, “Three-dimensional numerical study on the failure
645 characteristics of intermittent fissures under compressive-shear loads,” *Acta Geotech.*, vol. 14,
646 no. 4, pp. 1161–1193, 2019.
- 647 [34] M. Mohammadnejad, S. Dehkhoda, D. Fukuda, H. Liu, and A. Chan, “GPGPU-parallelised
648 hybrid finite-discrete element modelling of rock chipping and fragmentation process in
649 mechanical cutting,” *J. Rock Mech. Geotech. Eng.*, vol. 12, no. 2, pp. 310–325, Apr. 2020.
- 650 [35] D. Fukuda, M. Mohammadnejad, H. Liu, S. Dehkhoda, and A. Chan, “Development of a
651 GPGPU-parallelized hybrid finite-discrete element method for modeling rock fracture,” *Int. J.*
652 *Numer. Anal. Methods Geomech.*, vol. 43, no. 10, pp. 1797–1824, Jul. 2019.
- 653 [36] D. Fukuda, M. Mohammadnejad, H. Liu, Q. Zhang, and J. Zhao, “Development of a 3D
654 Hybrid Finite-Discrete Element Simulator Based on GPGPU-Parallelized Computation for
655 Modelling Rock Fracturing Under Quasi-Static and Dynamic Loading Conditions,” *Rock*
656 *Mech. Rock Eng.*, vol. 53, no. 3, pp. 1079–1112, Mar. 2020.
- 657 [37] *The ISRM Suggested Methods for Rock Characterization, Testing and Monitoring: 2007-2014.*
658 Springer International Publishing, 2015.
- 659 [38] P. Wang, J. Xu, X. Fang, and P. Wang, “Energy dissipation and damage evolution analyses for
660 the dynamic compression failure process of red-sandstone after freeze-thaw cycles,” *Eng.*
661 *Geol.*, vol. 221, pp. 104–113, 2017.
- 662 [39] M. Mutlutürk, R. Altindag, and G. Türk, “A decay function model for the integrity loss of rock
663 when subjected to recurrent cycles of freezing-thawing and heating-cooling,” *Int. J. Rock*
664 *Mech. Min. Sci.*, vol. 41, no. 2, pp. 237–244, Feb. 2004.
- 665 [40] Q. Ma, D. Ma, and Z. Yao, “Influence of freeze-thaw cycles on dynamic compressive strength
666 and energy distribution of soft rock specimen,” *Cold Reg. Sci. Technol.*, vol. 153, no. March
667 2017, pp. 10–17, 2018.
- 668 [41] H. Y. Liu, Y. M. Kang, and P. Lin, “Hybrid finite–discrete element modeling of geomaterials
669 fracture and fragment muck-piling,” *Int. J. Geotech. Eng.*, vol. 9, no. 2, pp. 115–131, 2015.
- 670 [42] A. A. Munjiza, *The Combined Finite-Discrete Element Method*. Wiley, 2004.
- 671 [43] H. Y. Liu, H. Han, H. M. An, and J. J. Shi, “Hybrid finite-discrete element modelling of
672 asperity degradation and gouge grinding during direct shearing of rough rock joints,” *Int. J.*
673 *Coal Sci. Technol.*, vol. 3, no. 3, pp. 295–310, 2016.
- 674 [44] A. Munjiza and K. R. F. Andrews, “Penalty function method for combined finite–discrete
675 element systems comprising large number of separate bodies,” *Int. J. Numer. METHODS Eng.*
676 *Int. J. Numer. Meth. Engng.*, vol. 49, no. January 1999, pp. 1377–1396, 2000.
- 677 [45] B. S. A. Tatone and G. Grasselli, “A calibration procedure for two-dimensional laboratory-
678 scale hybrid finite–discrete element simulations,” *Int. J. Rock Mech. Min. Sci.*, vol. 75, pp. 56–

679 72, Apr. 2015.

680 [46] T. Heinze, G. Jansen, B. Galvan, and S. A. Miller, “Systematic study of the effects of mass and
681 time scaling techniques applied in numerical rock mechanics simulations,” *Tectonophysics*,
682 vol. 684, pp. 4–11, 2016.

683 [47] M. Mohammadnejad, D. Fukuda, H. Y. Liu, S. Dehkhoda, and A. Chan, “GPGPU-parallelized
684 3D combined finite–discrete element modelling of rock fracture with adaptive contact
685 activation approach,” *Comput. Part. Mech.*, vol. 7, no. 5, pp. 849–867, 2020.

686 [48] B. Ke, J. Zhang, H. Deng, and X. Yang, “Dynamic characteristics of sandstone under coupled
687 static-dynamic loads after freeze-thaw cycles,” *Appl. Sci.*, vol. 10, no. 10, 2020.

688 [49] K. Park, K. Kim, K. Lee, and D. Kim, “Analysis of effects of rock physical properties changes
689 from freeze-thaw weathering in Ny-Ålesund region: Part 1-experimental study,” *Appl. Sci.*,
690 vol. 10, no. 5, 2020.

691 [50] A. Bobet and H. H. Einstein, “Fracture coalescence in rock-type materials under uniaxial and
692 biaxial compression,” *Int. J. Rock Mech. Min. Sci.*, vol. 35, no. 7, pp. 863–888, Oct. 1998.

693 [51] H. Jiang, Z. Mo, X. Hou, and H. Wang, “Association rules between the microstructure and
694 physical mechanical properties of rock-mass under coupled effect of freeze-Thaw cycles and
695 large temperature difference,” *Sains Malaysiana*, vol. 46, no. 11, pp. 2215–2221, 2017.

696 [52] Y. Niu, X. P. Zhou, J. Z. Zhang, and Q. H. Qian, “Experimental study on crack coalescence
697 behavior of double unparallel fissure-contained sandstone specimens subjected to freeze-thaw
698 cycles under uniaxial compression,” *Cold Reg. Sci. Technol.*, vol. 158, pp. 166–181, 2019.

699 [53] Q. Wang, J. Liu, X. Zhu, J. Liu, and Z. Liu, “The experiment study of frost heave
700 characteristics and gray correlation analysis of graded crushed rock,” *Cold Reg. Sci. Technol.*,
701 vol. 126, no. August 2007, pp. 44–50, 2016.

702 [54] X. P. Zhou, Y. Niu, J. Z. Zhang, X. C. Shen, Y. Zheng, and F. Berto, “Experimental study on
703 effects of freeze-thaw fatigue damage on the cracking behaviors of sandstone containing two
704 unparallel fissures,” *Fatigue Fract. Eng. Mater. Struct.*, vol. 42, no. 6, pp. 1322–1340, 2019.

705 [55] A. Basu, D. A. Mishra, and K. Roychowdhury, “Rock failure modes under uniaxial
706 compression, Brazilian, and point load tests,” *Bull. Eng. Geol. Environ.*, vol. 72, no. 3–4, pp.
707 457–475, 2013.

708

709 List of Tables

710 Table 1. Physical-mechanical properties of Tasmanian sandstones subject to various freeze-thaw (F-T)
711 cycles

712 Table 2. Input parameters used in the FDEM simulations of the behaviour of the control specimens and
713 the specimens subjected to 60 freezing and thawing cycles in the UCS tests

714 Table 3. Comparisons between the experimental and numerical stress and elastic modulus
715

716

717 List of Figures

718 Fig. 1. Pundit PL-200 equipment for measuring P-wave velocities of the cylindrical rock specimens

719 Fig. 2. Climatic controlled cabinet for the freeze-thaw tests

720 Fig. 3. Servo-controlled high stability compression testing apparatus for the UCS and BTS tests

721 Fig. 4. Constitutive behaviour of cohesive elements under the tension and shear & sliding conditions: i)
722 under tension conditions, and ii) under shear and sliding conditions (Modified after [36])

723 Fig. 5. Fig. 5. 3D numerical models for simulating the behaviour of the sandstones in the UCS and BTS
724 tests: i) UCS and ii) BTS

725 Fig. 6. Deterioration of the physical-mechanical parameters of the sandstones subjected to various
726 freeze-thaw cycles i) P-Wave velocity, ii) Brazilian tensile strength, iii) uniaxial compressive
727 strength, and iv) elastic modulus

728 Fig. 7. 3D modelling of the failure process of the sandstones without subjecting to any freeze-thaw
729 cycles in the UCS test: i) Distribution of minor principal (most compressive) stresses in selected
730 loading steps, ii) Distribution of the damage variable in selected loading steps, and iii) Stress-
731 strain curve
732 Fig. 8. Final failure patterns observed in the UCS tests of the sandstones subjected
to various freeze-thaw cycles

733 Fig. 8. 3D modelling of the failure process of the sandstones without subjecting to any freeze-thaw
734 cycles in the BTS test: i) Distribution of horizontal stresses, ii) Distribution of the damage
735 variable, and iii) Stress-strain curve

736 Fig. 9. 3D modelling of the UCS test of the sandstone subjected to 60 freeze-thaw cycles: i) Distribution
737 of minor principal (most compressive) stresses in selected loading steps, ii) Distribution of the
738 damage variable in selected loading steps, and iii) Stress-strain curve

739 Fig. 10. 3D model of the BTS test for the sandstone subjected to 60 freezing and thawing cycles: i)
740 Distribution of horizontal stresses, ii) Distribution of the damage variable, and iii) Stress-strain
741 curve

742 Fig. 11. Comparisons of the stress-Strain curves from both experimental tests and numerical simulations
743 of the UCS tests of the sandstones subjected to various freezing and thawing cycles: i) 0 freeze-
744 thaw cycle, ii) 20 freeze-thaw cycles, iii) 40 freeze-thaw cycles, and iv) 60 freeze-thaw cycles

745 Fig. 12. Comparisons between the failure patterns of the sandstones subjected to 0 (A), 20 (B), 40 (C)
746 and 60 (D) freeze-thaw cycles in the UCS tests obtained from i) laboratory experiments and ii)
747 3D numerical simulations

748 Fig. 13. Comparisons between the failure patterns of the sandstones subjected to 0 (A), 20 (B), 40 (C)
749 and 60 (D) freeze-thaw cycles in the BTS tests obtained from i) laboratory experiments and ii)
750 3D numerical simulations

751
752
753
754
755
756
757
758
759
760
761
762
763
764
765
766
767

768 Table 1. Physical-mechanical properties of Tasmanian sandstones subject to various freeze-thaw (F-
 769 T) cycles

Specimen	Number of F-T Cycles	P-wave before F-T (m/s)	P-wave after F-T (m/s)	BTS (MPa)	UCS (MPa)	Elastic Modulus (GPa)	Average damage variable
S0-1	0	2448	-	5.53	30.93	4.5	0
S0-2		2843	-	5.87	38.93	7.9	
S0-3		2815	-	5.17	36.76	7.7	
S20-1	20	2192	1697	5.97	27.70	5.6	0.07
S20-2		2816	2646	4.82	39.59	8.2	
S20-3		2758	2539	4.91	38.26	7.1	
S40-1	40	2659	2297	4.67	34.06	6.7	0.13
S40-2		2821	2443	5.57	42.16	9.9	
S40-3		2820	2492	5.11	31.89	6.3	
S60-1	60	2753	1262	5.10	22.90	4.9	0.23
S60-2		2845	2389	5.23	30.40	6	
S60-3		2618	2323	4.83	34.16	7.3	

770
 771
 772
 773
 774
 775
 776
 777
 778
 779
 780
 781
 782
 783
 784
 785
 786
 787
 788
 789
 790
 791
 792

793 Table 2. Input parameters used in the FDEM simulations of the behaviour of the control specimens and
 794 the specimens subjected to 60 freezing and thawing cycles in the UCS tests

Parameter	Unit	Control	60 freeze-thaw cycles
Density	kg/m ³	2200	2200
Young's modulus	GPa	7.7	6.1
Poisson's ratio	-	0.25	0.25
Microscopic tensile strength	MPa	5.35	5.05
Microscopic cohesion	MPa	10	7.7
Microscopic internal friction angle	°	25.5	25.5
Microscopic mode I fracture energy	J/m ²	80	50
Microscopic mode II fracture energy	J/m ²	300	180
Normal contact penalty	GPa	77	61
Cohesive normal penalty	GPa	770	610
Cohesive tangential penalty	GPa	770	610

795
 796
 797
 798
 799
 800
 801
 802
 803
 804
 805
 806
 807
 808
 809
 810
 811
 812
 813
 814
 815
 816
 817

818 Table 3. Comparisons between the experimental and numerical stress and elastic modulus

		Crack initiation stress (MPa)	Peak strength (MPa)	Elastic modulus (GPa)
Control	Experimental	36.88	38.93	7.9
	Numerical	37.07	38.50	7.5
20 Freeze-Thaw cycles	Experimental	34.72	38.26	7.1
	Numerical	32.37	34.30	6.7
40 Freeze-Thaw cycles	Experimental	29.69	31.89	6.3
	Numerical	28.70	31.69	6.2
60 Freeze-Thaw cycles	Experimental	28.03	30.40	6.0
	Numerical	27.42	29.38	6.1

819

820

821

822

823

824

825

826

827

828

829

830

831

832

833

834

835

836

837

838

839

840

841

842

843

844



845

846 Fig. 1. Pundit PL-200 equipment for measuring P-wave velocities of the cylindrical rock specimens

847

848

849

850

851

852

853

854

855

856

857

858

859

860

861

862

863

864

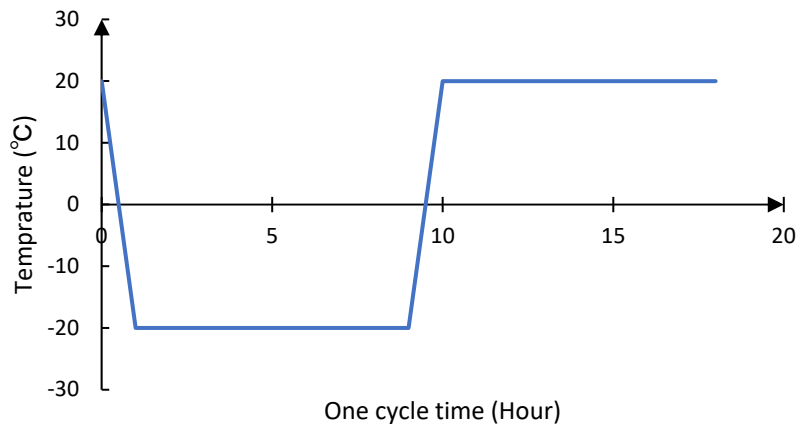
865

866

867



i) Climatic controlled cabinet together with a assembly of tested samples



ii). Generalized temperature versus time curve of one freeze-thaw cycle

Fig. 2. Climatic controlled cabinet for the freeze-thaw tests

868
869
870
871
872
873
874
875
876
877
878
879
880



Fig. 3. Servo-controlled high stability compression testing apparatus for the UCS and BTS tests

881
882
883
884
885
886
887
888
889
890
891
892
893
894
895
896
897
898
899
900

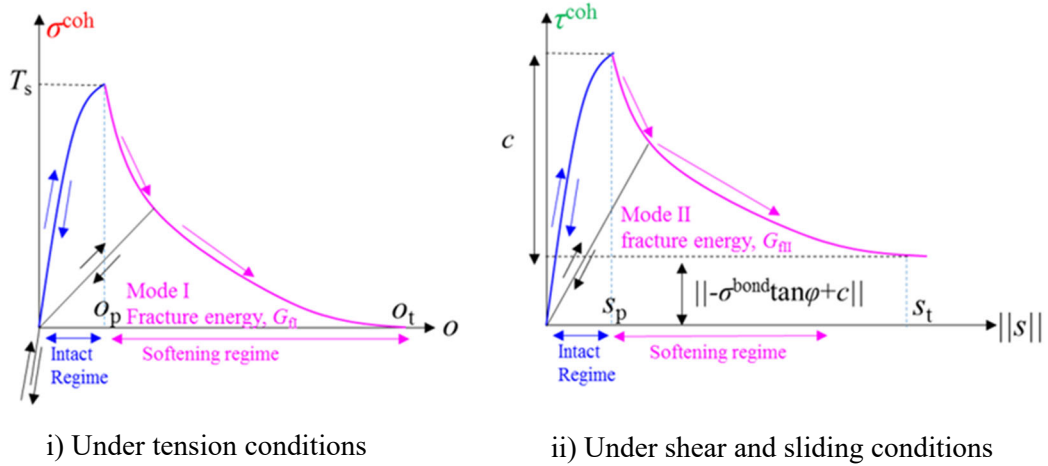
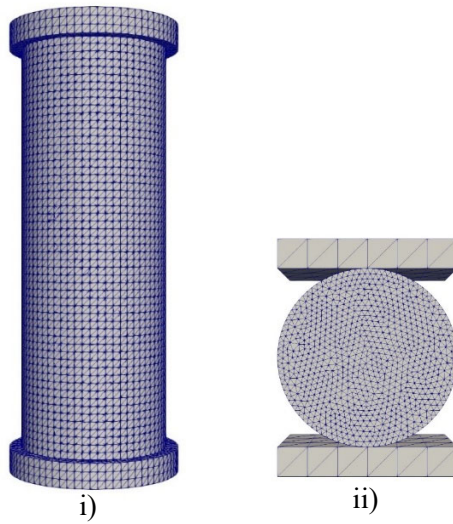


Fig. 4. Constitutive behaviour of cohesive elements under the tension and shear & sliding conditions: i) under tension conditions, and ii) under shear and sliding conditions (Modified after [36])

901
902
903
904
905
906
907
908
909
910
911
912
913
914
915
916
917
918
919
920
921
922
923
924
925



926

927 Fig. 5. 3D numerical models for simulating the behaviour of the sandstones in the UCS and BTS tests:

928

i) UCS and ii) BTS

929

930

931

932

933

934

935

936

937

938

939

940

941

942

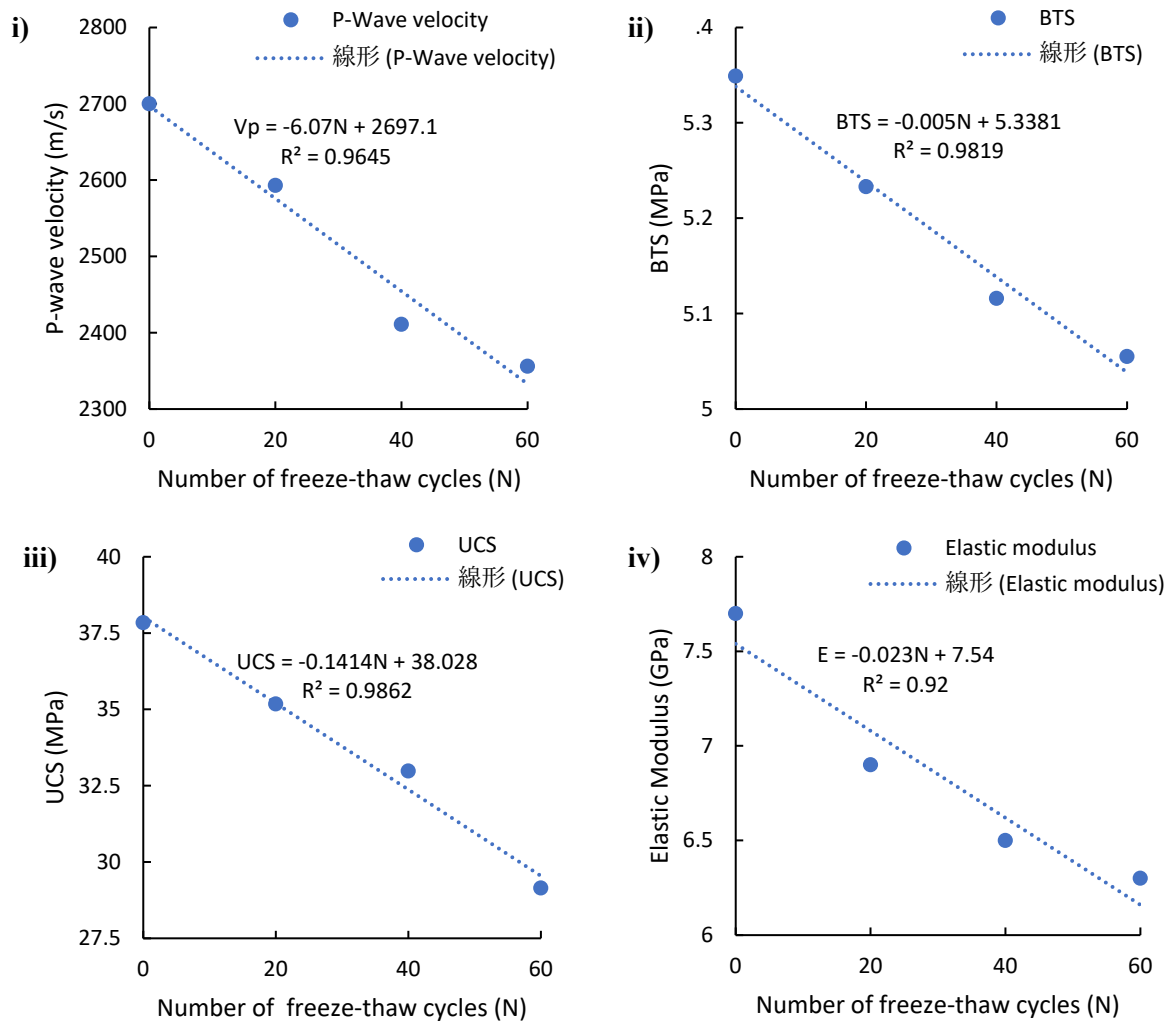
943

944

945

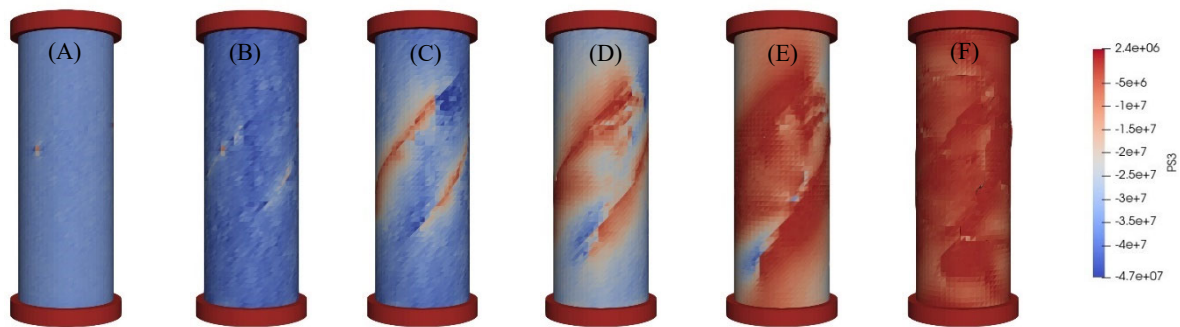
946

947

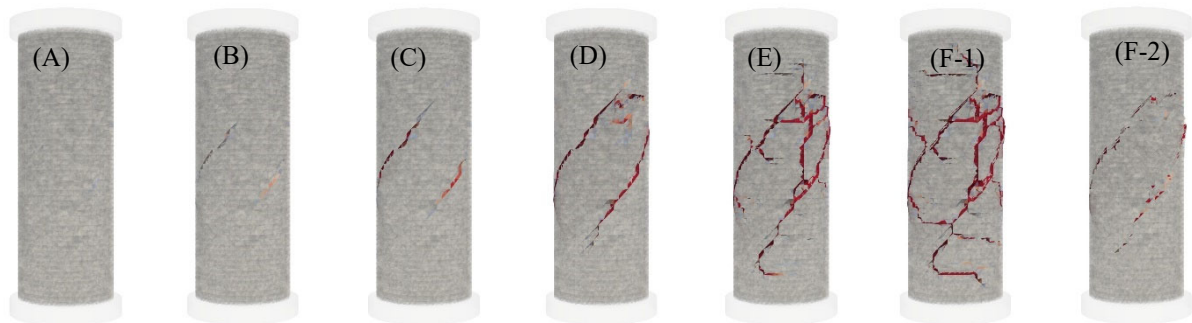


948 Fig. 6. Deterioration of the physical-mechanical parameters of the sandstones subjected to various
 949 freeze-thaw cycles i) P-Wave velocity, ii) Brazilian tensile strength, iii) uniaxial compressive strength,
 950 and iv) elastic modulus

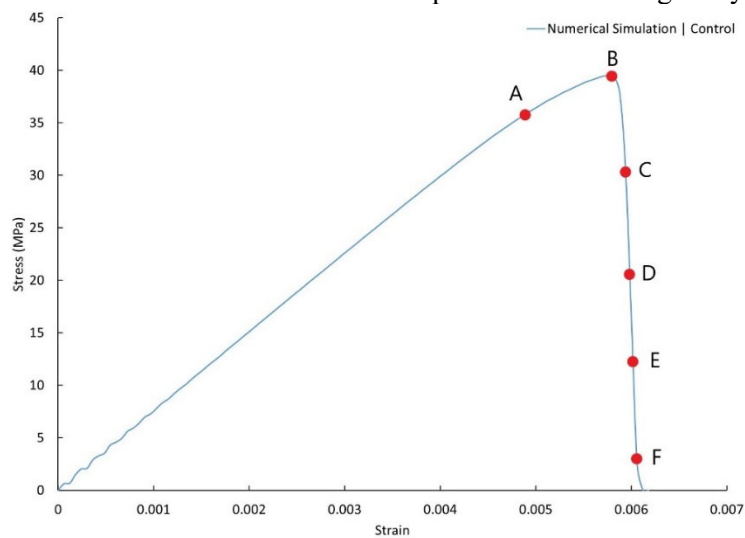
951
 952
 953
 954
 955
 956
 957
 958
 959
 960
 961



i) Distribution of minor principal (compressive) stresses



ii) Distribution of the damage variable (A-E and F-1: all damage including pure mode-I, pure mode-II and mixed-mode while F-2: pure mode-II damage only)



iii) Stress-strain curve

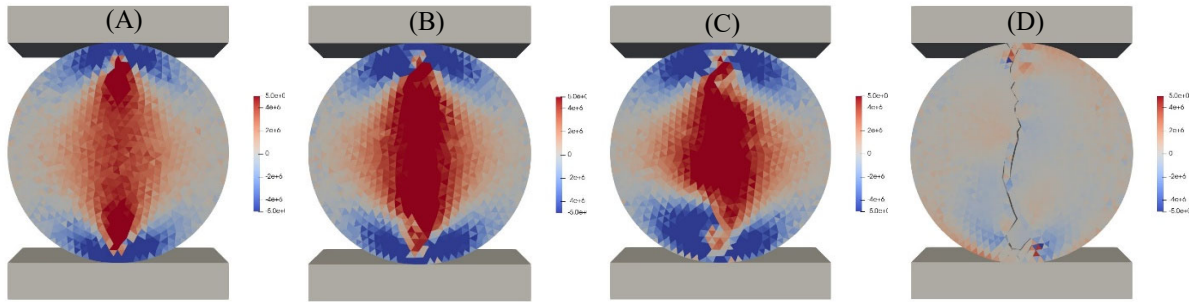
962 Fig. 7. 3D modelling of the failure process of the sandstones without subjecting to any freeze-thaw
 963 cycles in the UCS test: i) Distribution of minor principal (most compressive) stresses in selected loading
 964 steps, ii) Distribution of the damage variable in selected loading steps, and iii) Stress-strain curve

965

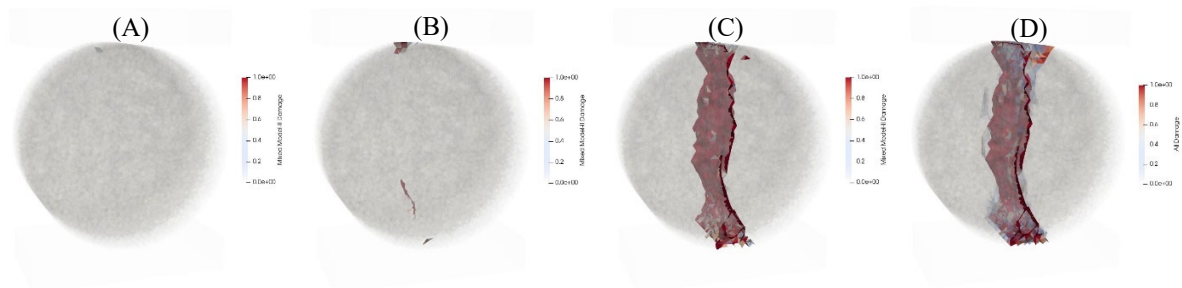
966

967

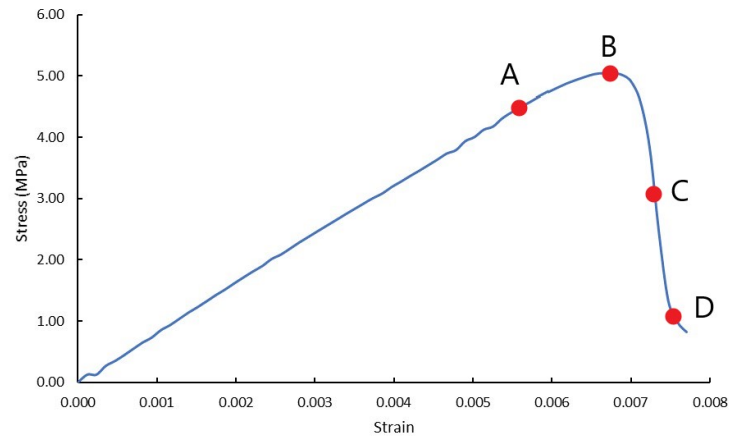
968



i) Distribution of horizontal stresses



ii) Distribution of the damage variable



iii) Stress-strain curve

969 Fig. 8. 3D modelling of the failure process of the sandstones without subjecting to any freeze-thaw
 970 cycles in the BTS test: i) Distribution of horizontal stresses, ii) Distribution of the damage variable,
 971 and iii) Stress-strain curve

972

973

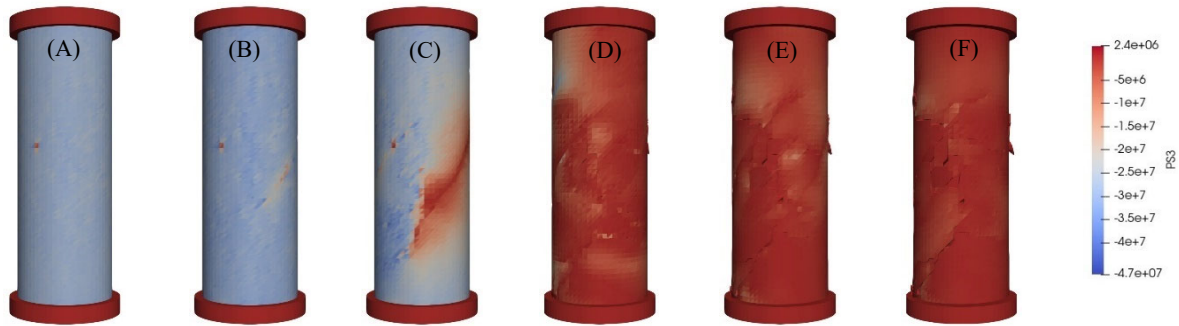
974

975

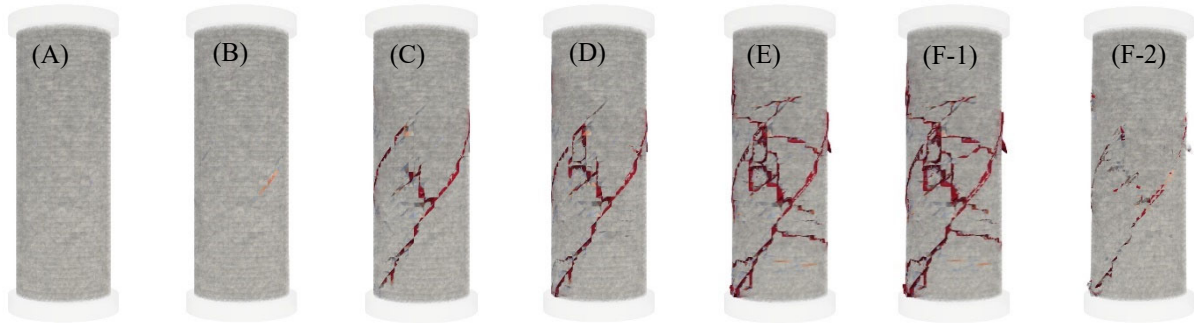
976

977

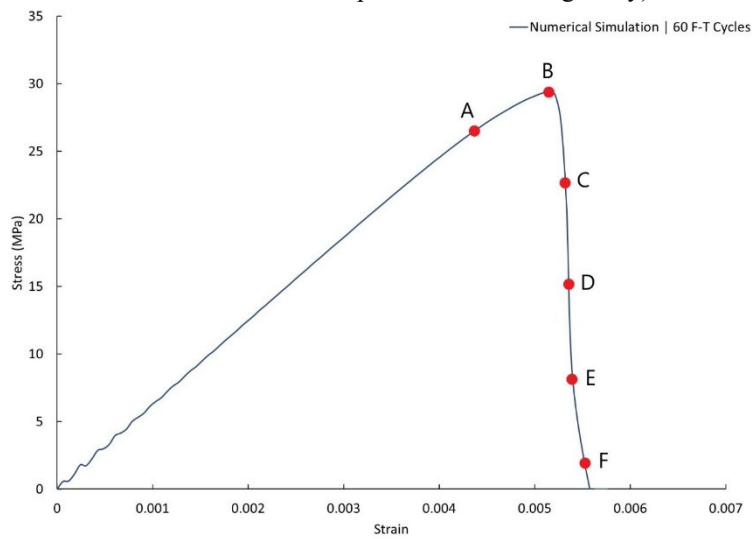
978



i) Distribution of minor principal (compressive) stresses



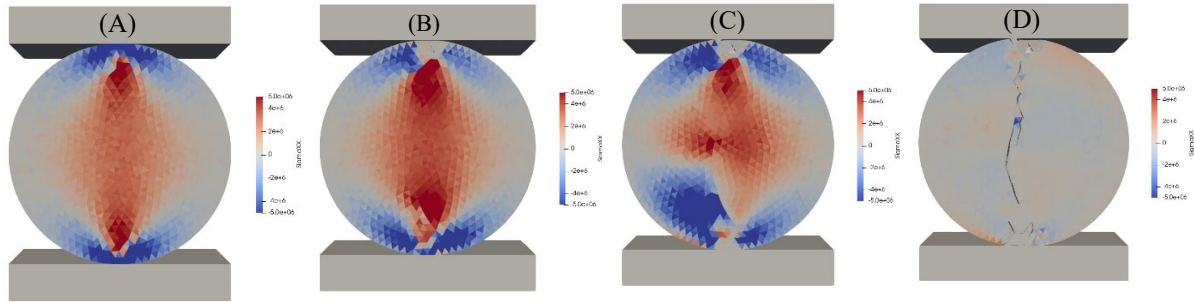
ii) Distribution of the damage variable (A-E and F-1: all damage including pure mode-I, pure mode-II and mixed-mode while F-2: pure mode-II damage only)



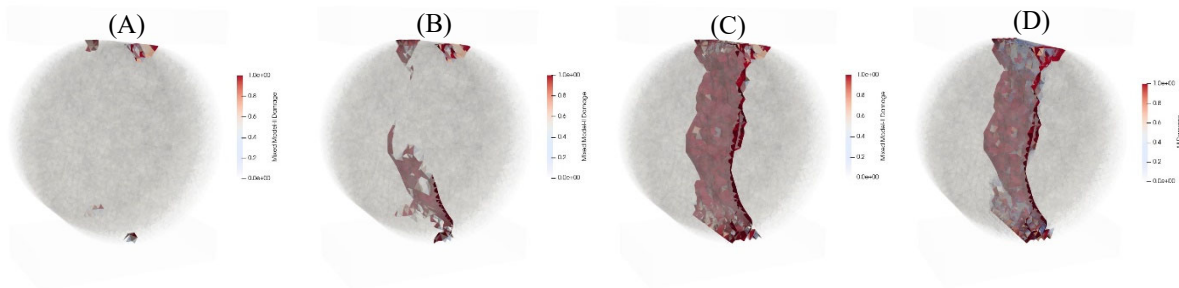
iii) Stress-strain curve

979 Fig. 9. 3D modelling of the UCS test of the sandstone subjected to 60 freeze-thaw cycles: i)
 980 Distribution of minor principal (most compressive) stresses in selected loading steps, ii) Distribution
 981 of the damage variable in selected loading steps, and iii) Stress-strain curve

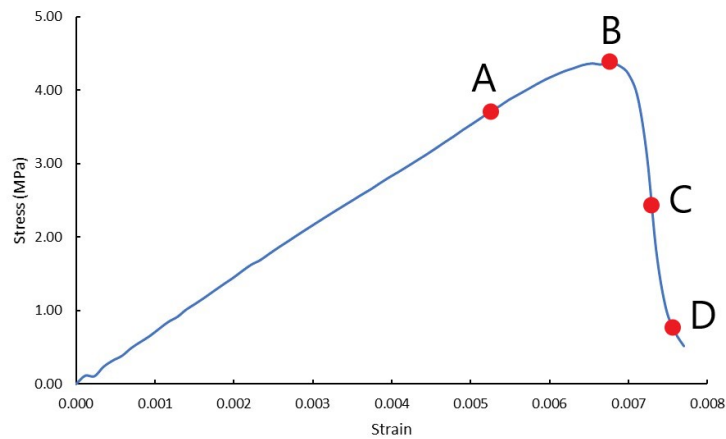
982
 983
 984
 985
 986
 987



i) Distribution of horizontal stresses



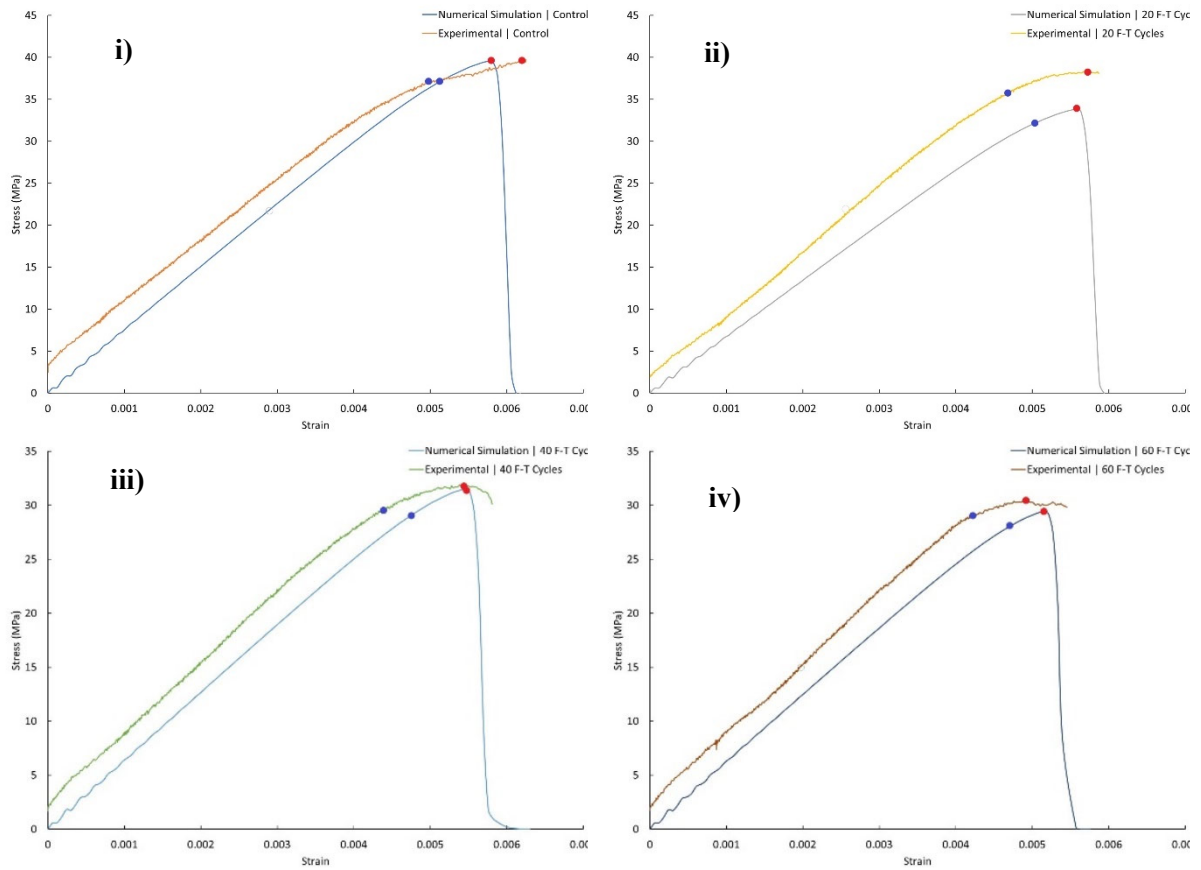
ii) Distribution of the damage variable



iii) Stress-strain curve

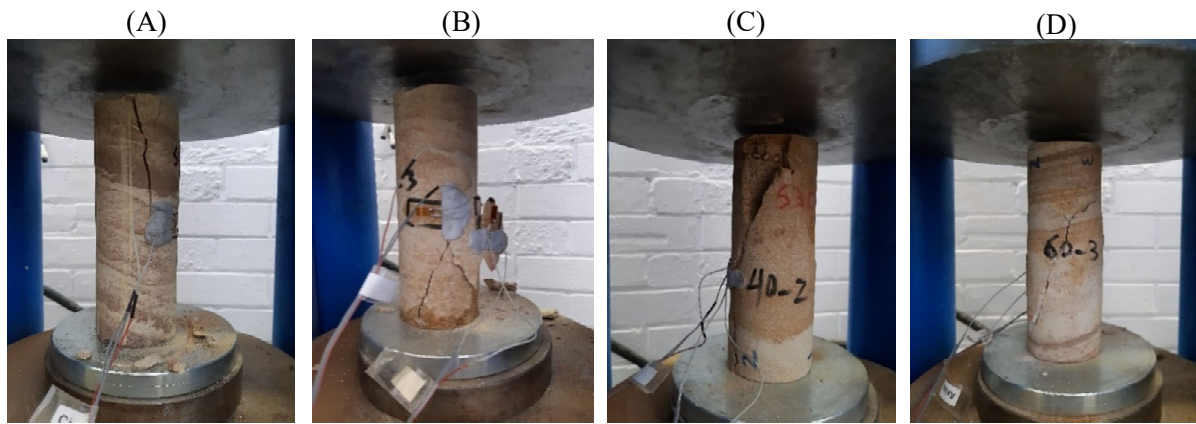
988 Fig. 10. 3D model of the BTS test for the sandstone subjected to 60 freezing and thawing cycles: i)
 989 Distribution of horizontal stresses, ii) Distribution of the damage variable, and iii) Stress-strain curve

990
 991
 992
 993
 994
 995
 996
 997
 998

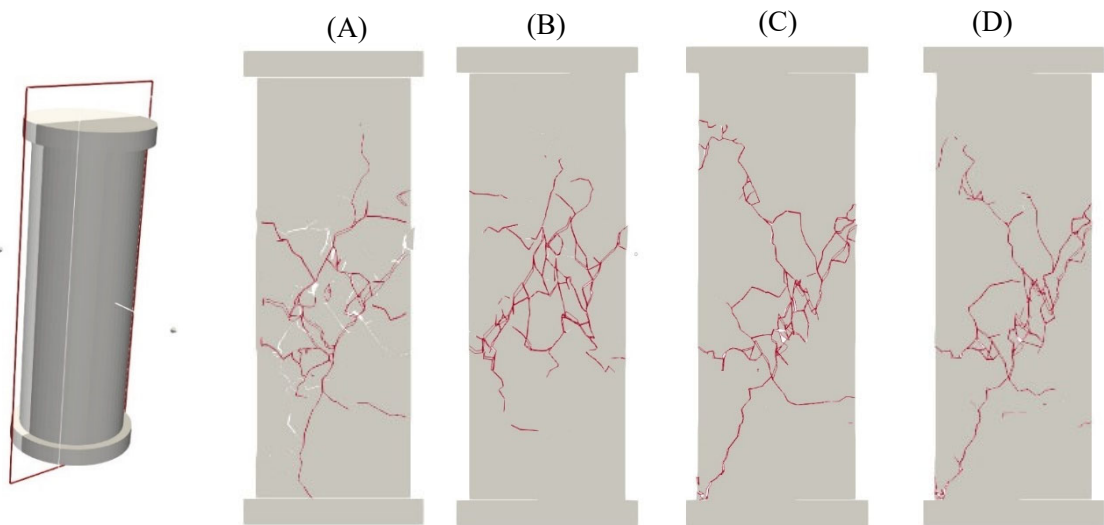


999 Fig. 11. Comparisons of the stress-Strain curves from both experimental tests and numerical simulations
 1000 of the UCS tests of the sandstones subjected to various freezing and thawing cycles: i) 0 freeze-thaw
 1001 cycle, ii) 20 freeze-thaw cycles, iii) 40 freeze-thaw cycles, and iv) 60 freeze-thaw cycles

1002
 1003
 1004
 1005
 1006
 1007
 1008
 1009
 1010
 1011
 1012
 1013
 1014
 1015
 1016



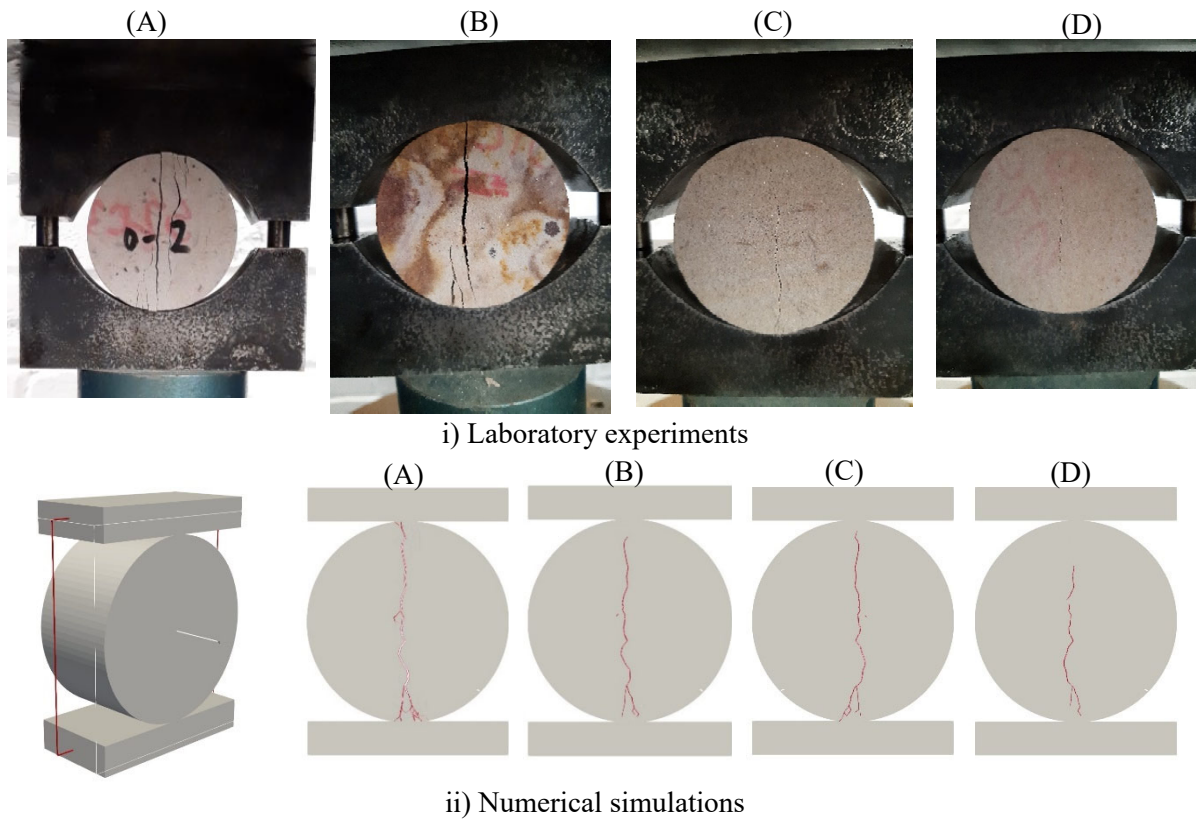
i) Laboratory experiments



ii) Numerical simulations

1017 Fig. 12. Comparisons between the failure patterns of the sandstones subjected to 0 (A), 20 (B), 40 (C)
 1018 and 60 (D) freeze-thaw cycles in the UCS tests obtained from i) laboratory experiments and ii) 3D
 1019 numerical simulations

1020
 1021
 1022
 1023
 1024
 1025
 1026
 1027
 1028
 1029
 1030
 1031



1032 Fig. 13. Comparisons between the failure patterns of the sandstones subjected to 0 (A), 20 (B), 40 (C)
 1033 and 60 (D) freeze-thaw cycles in the BTS tests obtained from i) laboratory experiments and ii) 3D
 1034 numerical simulations