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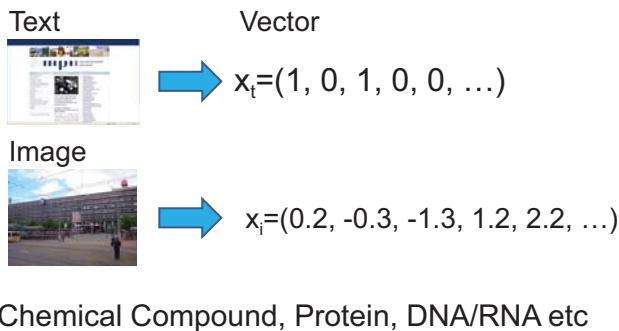
SketchSort: An Efficient Nearest Neighbor Graph Construction Method

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Outline

- Motivation
- Method
- Experiments and Results

Data represented as vector



Locality Sensitive Hashing

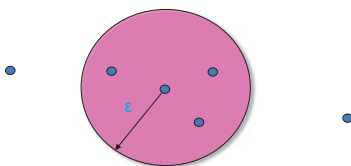
(Gionis et al,99)

- Mapping vector to binary string (*sketch*)
- Conserve the distance in the original space
 - Enable to store gigascale data in main memory
 - Speed up learning algorithms

 $x = (0.2, -0.3, -1.3, 1.2, 2.2, \dots)$  $s = 10101011101010101$

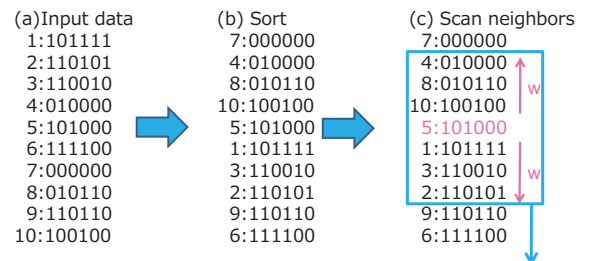
All Pairs Similarity Search

- Finding all neighbor pairs from sketches
 - Find all pairs (i, j) , $i < j$, $\Delta(x_i, x_j) \leq \epsilon$
- Enable to build a neighborhood graph
 - semi-supervised learning, spectral clustering, ROI detection in images, retrieval of protein sequences



Single Sorting Method (SSM)

- Find neighbors by sorting sketches
 - Various applications ex) google news



Drawbacks of Single Sorting

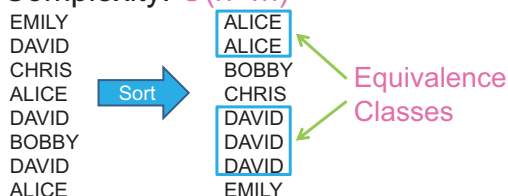
- Need a large number of distance calculation for achieving reasonable accuracy.
- Can not derive an analytic estimate of the fraction of missing neighbors.

Overview of SketchSort

- Employ the multiple sorting method (MSM) as a building block
 - Enumerate all pairs within Hamming distance d from a string pool $S=\{s_1, \dots, s_n\}$
- A number of distance calculation is significantly reduced
- A bound of the expected fraction of missing neighbors can be obtained.

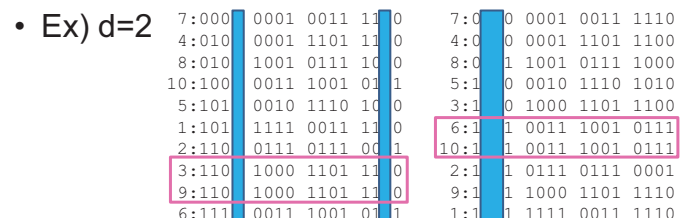
Special case: Finding identical strings($d=0$)

- Radix sort, and partition the strings into equivalence classes: $O(n)$
- Build edges between all pairs in **equivalent classes**: $O(m)$
- Complexity: $O(n+m)$



Multiple sorting method ($d > 0$)

- Mask d characters in all possible ways
- Perform radix sort $\binom{l}{d}$ times
- Time exponential to d , polynomial to the string length l
- Still linear to the number of strings!!

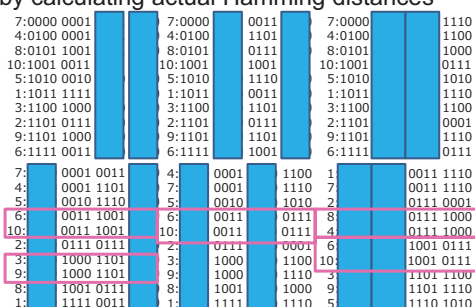


Blockwise masking

- Mask d blocks in all possible ways
- The number of sorting operations reduced
- Non-neighbors might be detected

- Filtered out by calculating actual Hamming distances

■ Ex) $d=2$



Recursive Algorithm

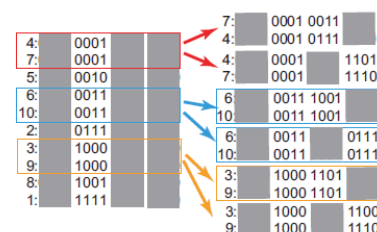


Figure 5: Updating equivalence classes in block concatenation. Strings in a block are sorted and equivalence classes (shown as square frames) are detected. A next block is concatenated to each equivalence class and sorted again.

SketchSort

- Basic idea: Map vectors to strings and apply MSM
- Not good: Create long strings and apply MSM at once
- Replication:
 - Create Q independent string pools of length l
 - apply MSM to each string pool
- Report the pairs less than a threshold ϵ

$$\Delta(x_i, x_j) \leq \epsilon$$

Duplication Checks

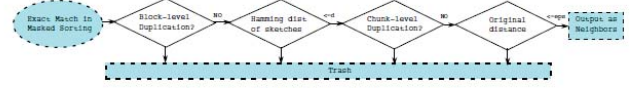


Figure 2: Global flow of our approach.

- Block-level duplication check
 - Define dictionary order of blocks, and take only minimum combinations of blocks.
ex) $d=2$
 $(1,2) < (1,3) < (1,4) < (2,3) < (2,4) < (3,4)$
- Chunk-level duplication check
 - Take only minimum chunks.

Two types of errors

- True edges E^* , Our results E
- Type-I error (false positive): A non-neighbor pair has a Hamming distance within d in at least one replicate

$$F_1 = \{(i, j) \mid (i, j) \in E, (i, j) \notin E^*\}.$$
- Type II-error (false negative): A neighbor pair has a Hamming distance larger than d in all replicates

$$F_2 = \{(i, j) \mid (i, j) \notin E, (i, j) \in E^*\}.$$

Bound of type-II error: Missing edge ratio

- Basically, type-II error is more crucial
 - type-I errors are filtered out by distance calculations
- Missing edge ratio (type-II error) is bounded as

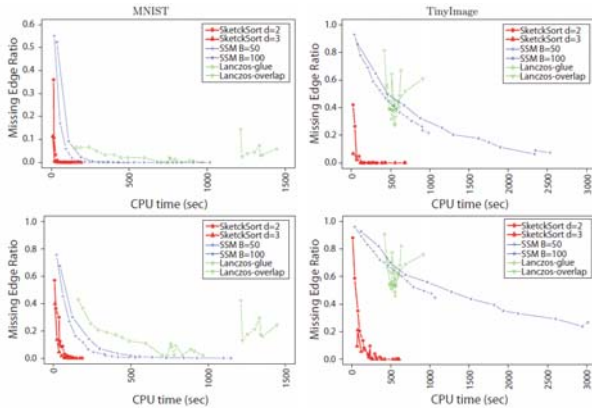
$$E \left[\frac{|F_2|}{|E^*|} \right] \leq \left(1 - \sum_{k=0}^{\lfloor d \rfloor} \binom{\ell}{k} p^k (1-p)^{\ell-k} \right)^Q,$$

where p is an upper bound of the non-collision probability of neighbors

$$p = \frac{\arccos(1 - \epsilon)}{\pi}.$$

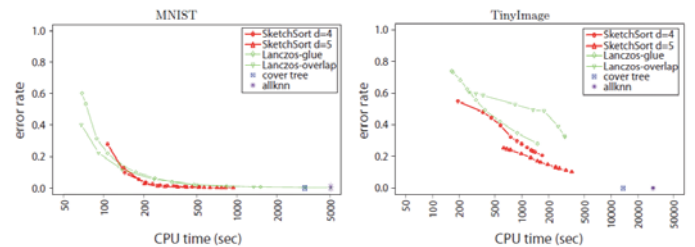
Results for All Pairs Similarity Search

Faster and more accurate than recent methods



All pairs similarity search on MNIST and TinyImage datasets for cosine distance thresholds 0.10 Π (top) and 0.15 Π (bottom).

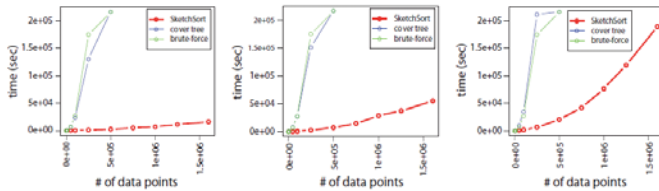
Results for 5-nearest neighbor search



Error rate for 5-nearest neighbor search on MNIST and TinyImage datasets

All Pairs Similarity Search in 1.6 Million Images

- Set parameters so as to keep missing edge ratio no more than 1.0×10^{-6}
- Enable to detect similar pairs nearly exactly
- Take only 4.3 hours for 1.6 million images**



Near duplication detection in up to 1.6 million images at threshold 0.05 (left), 0.10 (middle) and 0.15 (right)

A C++ implementation of SketchSort is available from

<http://code.google.com/p/sketchsort/>

The screenshot shows the project page for SketchSort on Code.google.com. The page includes a search bar, navigation links (Project Home, Downloads, Wiki, Issues, Source, Administer), and a description of the software. The 'Introduction' section explains that SketchSort is a software for all pairs similarity search. The 'Quick Start' section provides instructions on how to compile and run the software. The 'Usage' section lists command-line options. The 'Format of input file' section describes the input file format. The 'Project Home' sidebar on the right contains links to the project's homepage, code, and issues.