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A Theoretical Study on Multiscale Reaction Network Extracted from Single Molecule Time Series

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Abstract

Ensemble experiments can access only average characteristics of biomolecular systems, thus, the individual behavior of single molecules cannot be distinguished. In contrast, single molecule (SM) experiments manifest the detailed complexity in kinetics and dynamics of these multiscale biological processes at the single molecule level. The complex dynamics of single molecules, such as the On/Off blinking of nano-particles, the opened/closed gating of ion channels, the bound/unbound kinetics in cell signaling processes, are often probed experimentally in the form of time series with finite discrete levels. The main goal of SM experiments is to extract kinetics and dynamical information from the observable time series. However, how one can extract such information from an observed one-dimensional time series is still an unresolved question.

In the analysis of SM time series, hidden Markov models (HMM) are often used to provide insights on the complex mechanism of molecular machinery. To derive HMM from SM time series that incorporates non-exponential kinetics and molecular memory is one of the most contemporary and intriguing subjects in the analysis of single molecule biology. In this thesis, I reviewed a recently developed mathematical approach which provides not only interpretation of the complex kinetics but also new insights into biological function buried in ensemble measurements. This method, based on information theory, is free from any a priori assumption, such as local equilibrium, detailed balance, or number of states. Mathematically, it is proved that its scheme is the simplest representation that can predict the future outcome maximally. This approach is known as State Space Network (SSN). The SSN is a type of HMM that takes into account both multiple states buried in the measurement and memory effects in the process of the observable whenever they exist. The states of SSN depend not only on the present value of the observable but also on the past values along the course of time evolution so that the state-to-state transitions are Markovian even though dynamical correlation may exist in the time series.

The scheme of SSN was based on the assumption that a given time series is stationary and long enough. Time series obtained from SM experiments always suffer from as an insufficient number of data points and sometimes may be non-stationary. To overcome these difficulties, a generalization of SSN was developed by using a multiscale decomposition scheme based on discrete wavelet transforms in our laboratory (1). The main drawback to apply this decomposition scheme to time series is that it depends on the choice of wavelet basis function. Instead of wavelet decomposition, I introduced a simple but efficient skipping step method (SSM) to decompose the original time series into a set of time series at different timescales. The SSM can deal with the nature of multiscale nature and nonstationarity for a discrete time series in the framework of SSN.

Previously, in an in vitro reconstituted system of the recognition process between epidermal growth factor receptor (EGFR) on the plasma membrane and its adaptor protein Ash/Grb2 (2), non-exponential

kinetics in the association and dissociation processes were found. In addition, the association kinetics abnormally depends on the concentration of Grb2 owing to reaction memory concealed in the conformation of EGFR. Two extreme reaction schemes for the association process were proposed (3); one of them is called defect diffusion model in which, the system visits many dissociated states with different rate constants to reach a specific target state for association. The other is called multiple-reaction channel model where all (dissociated) states with different association rate constants directly connected to the associated state independently. However, they could not identify the actual, most plausible kinetic scheme that reflects the observed kinetics objectively.

To demonstrate the versatility of my scheme, I investigated the time series of the EGFR-Grb2 system. It was found that a newly-derived analytical expression of autocorrelation function from SSN combined with SSM successfully reproduce the autocorrelation for a wide range of timescale up to the timescale that loses the memory, 3 s. It was found that the underlying SSNs are in between the defect diffusion model and multiple-reaction channel model and change their topographical structure as a function of the timescale: while the corresponding SSN is simple at the short timescale (0.033 s to 0.1 s), the SSN at the longer timescales (0.1 s to 3 s) becomes rather complex in order to capture multiscale kinetics emerging at longer timescales.

The Y1068F mutant of EGFR replaced tyrosine (Y) 1068 in EGFR (whose phosphorylation has been reported to construct the primary strong Grb2 binding site) for analyzing the exponential properties and memory effects in association and dissociation kinetics. The SSNs for the mutant (Y1068F) EGFR are simpler than the wild type EGFR, indicating the existence of non-Markovian nature in the wild type more than the mutant (Y1068F) EGFR. In addition, the SSN can capture the heterogeneity of the memory in the process depending on each state. By looking into splitting patterns as an increase of the history length for the shortest time scale SSN of the wild type EGFR at low concentration of Grb2, it was found that visiting the unbound form of the wild EGFR-Grb2 system approximately resets all information of history or memory of the process.

To implement the direct relationship between the states in the multiscale SSNs and the underlying high-dimensional conformation of the system, it is necessary to construct a series of SSNs in terms of a set of different single-molecule time series data from systematic mutations of amino-residues. I expect that one may identify which amino residues perform to yield non-Markovian kinetics by monitoring the morphological changes of the network. This may be regarded as ϕ value analysis of protein folding kinetics to infer the energy landscape in the framework of SM biology.

To my son Aydin Arushanyan Zaman

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Introduction

Protein-protein interactions play a vital role in biomolecular system of living cells, such as cell signaling in a cell which is comprised of a series of protein molecules and their interactivities. These protein interactions often involve in complex mechanisms and that show inhomogeneous dynamics, because of the significant conformational changes in proteins. Moreover, the dynamics may be different from time to time for the same individual molecules (7, 8, 9, 10, 11, 12, 13, 14, 15). These protein interactions even at single molecule level are amplified along the signaling pathways. So it is crucially important to study the underlying mechanism of protein interaction at both ensemble and single levels to extract the root of protein interactions in the cell signaling.

There are several well known techniques such as gel filtration, Western blotting, nuclear magnetic resonance (NMR), X-ray crystallography etc, by which one can get information about proteins and their reactions. In gel filtration method one obtained information about macroscopic level of protein such as the molecular weight distribution etc. NMR and X-ray crystallography are used to investigate highly dynamic, partial inhomogeneous molecules and complexes. Recently NMR static and ensemble structural studies of protein complexes indicate that protein interaction sites or domains undergo dramatic conformational changes from disordered to ordered states upon complex formation (16). However, inhomogeneity and complexity of protein conformational (structural) changes are extremely difficult to be identified and analyzed in an ensemble measurement e.g., NMR, X-ray crystallography etc, because they can access only averaged characteristics, thus the individual behavior of single molecules cannot be characterized. Therefore, to characterize inhomogeneous, static and dynamic disorder (13, 14, 17), memory landscapes (18) of enzymatic reactions, as well as dynamic polymorphisms of protein structures (19, 20), single-molecule (SM) experiments are useful because they remove the inhomogeneity and manifest the detailed complexity in dynamics of these multiscale protein-protein process by study-

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ing one molecule at a time (2, 21). SM experiments have allowed researchers to explore small scale systems with high spatial and temporal resolution. Main advantage of this type of experiment is the removal of ensemble averaging by creating the actual distribution of values for an experimental observed parameter (e.g. wavelength, intensity etc) (2). It is able to reveal and diagnose the events of extremely low probability i.e., repeatedly excitation of one molecule or measuring hundreds of different molecules and identify previously unknown reaction intermediates (22).

The complex dynamics of a single-molecule systems, such as the ON/OFF blinking of nano-particles (23), the opened/closed gating of ion channels (24, 25), the bound/unbound kinetics (2) in cell signaling processes, are often probed experimentally in the form of time series with finite discrete levels, and such time traces contain detailed dynamic information. The main goal of SM measurement is to extract the kinetics and dynamical information from such direct observable time trace (2, 15, 18, 21, 22, 23, 26, 27, 28, 29, 30, 31, 32). It obviously comes to mind that, what information and how can one learn from such one dimensional time series? How to identify the pattern buried in SM time series? How many states exist on this time series? How are they connected?. Those are very regular questions for analyzing time series. So, it is necessary to establish a firm theoretical modeling method of the underlying mechanism of molecular machinery from observed SM time series to explore single molecule dynamics. From this perspective, it is useful to introduce a computational, data- or hypothesis- driven approaches in an effort to facilitate the discovery of the kinetics in the process. There are many conventional data-driven techniques in terms of interpreting and analyzing SM measurements, such as multi-parametric networks based on Monte Carlo simulation (33), reaction diffusion model with photon statistics (34), hidden Markov model (1, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45), aggregated markov model (46, 47, 48), semi-Markovian kinetic scheme (49), kinetic network model (50), and also Bayesian approach (51). Markov process is very commonly used to interpret kinetics because of its useful and convenient properties even though the observable data may not be a Markov chain.

In the analyses of SM time series, Hidden Markov Model (HMM) are often used to provide insights on the complex mechanism of molecular machinery (1, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45). However, to derive HMM from single molecule time series that incorporates non-exponential behavior and molecular memory of the process and, to assign the physical correspondence of the constructed states are yet one of the most contemporary and intriguing subjects to be resolved. Moreover, most existing methods (for mathematical modeling) depend on a huge amount of fitting parameters, e.g., algorithms using maximum likelihood estimator to obtain the parameters of the HMM (22). These methods, in general, require the initial assumption of model parameters, such as network structure and number of states.

Recently a novel data-driven modeling was developed to naturally derive the underlying multiscale state space network (SSN) from single molecule time series based on information theory (1, 39, 40, 52, 53, 54). The SSN is regarded as a certain type of HMM that represents the complex kinetics such as non-exponentiality and the molecular memory of the process, and identifies the physical correspondence. The states of SSN depend not only on the present value of the observable but also on the past information along the course of time evolution so that the state-to-state transitions are Markovian even dynamical correlation may exist in the time series. In addition, most conventional methods (e.g. HMM) are state-labeled i.e., producing a symbol when a state is visited. On the other hand, the SSN is edge-labeled i.e., producing a symbol when a transition is made. I newly derive an analytic expressions of kinetic properties such as autocorrelation function and dwell time distribution of a given discrete time series in terms of the intrinsic properties of SSNs.

The original idea of the SSN was developed in 1980s (52, 53, 54) aiming at discovering the pattern or module of dynamical features buried in a given stationary time series. Time series obtained from SM experiments always suffer from the problem of insufficient number of data points and sometimes may be non-stationary. To overcome these difficulties, a generalization of SSN has been developed in our laboratory by using a multiscale decomposition scheme based on discrete wavelet transforms to decompose the time series into components at different scales (1, 39, 40). It has been reported (1, 39, 40) in a single-molecule electron transfer experiment of the NADH: flavin oxidoreductase(Fre) complex (55) that the topographical features of the SSN change as a function of timescales to capture the transition from abnormal to normal diffusion observed in the protein fluctuation. The main drawback to apply this decomposition scheme to the time series is that it depends on the choice of wavelet basis function. Instead of wavelet decomposition, here I introduced a simple, but efficient skipping step method (SSM) to decompose the original time series into a set of time series at different timescales. The SSM can deal with the nature of multiscale and nonstationarity for a discrete time series in the framework of SSN.

To demonstrate my methods, I analyzed the time series measured in an *in vitro* reconstituted system (by Morimatsu *et al.*) of the recognition process between epidermal growth factor receptor (EGFR) on the plasma membrane and its adaptor protein Ash/Grb2 (2). EGFR is a single membrane spanning protein, which associates with EGF at the extracellular matrix of the cell, the association between them induces conformational changes in the extracellular domain of EGFR that transmit the external signal into the cytoplasm. Thus Grb2 (is one of the adapter protein of EGFR) links activated EGFR to downstream signaling molecules to induce functional changes in cells (See Appendix for more detail) (2). To understand the signal flows in the cells comprehensively, it is important to clarify the association and dissociation kinetics between EGFR and whole molecules of Grb2, as it is the initial key stage inside the

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cell. Previously, it has been studied only dissociation process of this system using surface plasmon resonance (56, 57) and tryptophan fluorescence (58). Morimatsu *et al.* (2) first time studied the association and dissociation kinetics between EGFR and Grb2 at the single molecule level. In the SM experiments (2), they observed the repeated binding and release of fluorophore Grb2-Cy3 at different concentration of Grb2. They measured the durations from the onset of association to the dissociation of Grb2 molecules and from the dissociation of Grb2 molecule to the association of the next Grb2 molecule. Dissociation and association kinetics between EGFR and Grb2 were analyzed by the distribution of ON dwell times(=waiting time for dissociation) and OFF dwell times(=waiting time for association). It was found that dissociation and association process between EGFR and Grb2 showed non-single exponential kinetics, and the association kinetics depend nonlinearly on the concentration of Grb2. This non-single exponential properties and concentration dependency of Grb2 were suggesting the existence of molecular memory in the signaling process (2) (See Fig. 1.1).

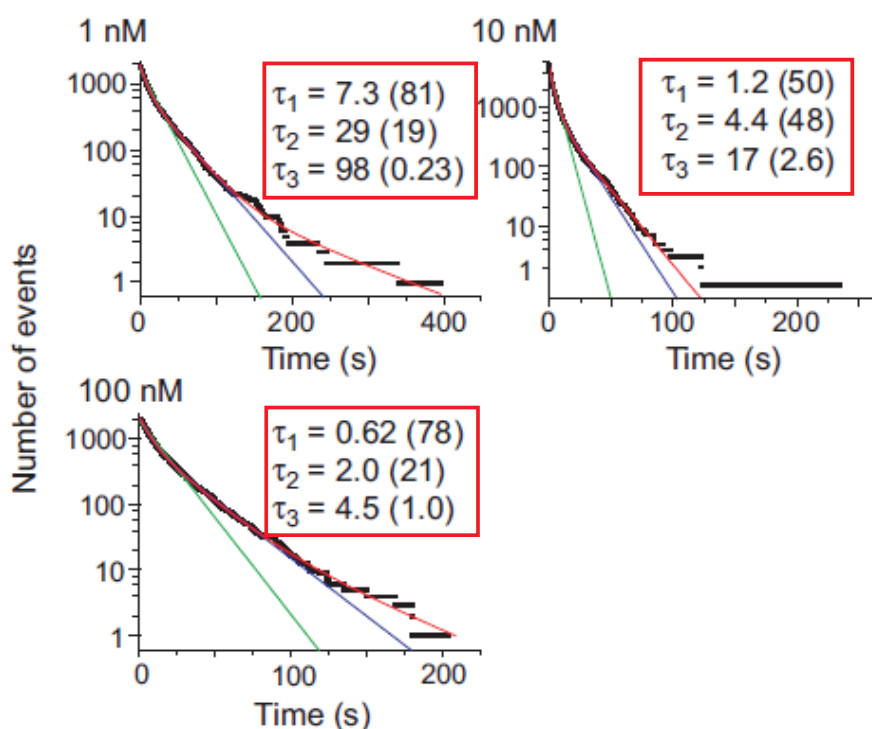


Figure 1.1: Dissociation kinetics: Cumulative histograms of the OFF dwell times for each concentration of Grb2 were fitted with a single (green) and a sum of two (blue) or three (red) exponential functions. Time constants are from fitting with the three exponential functions. Numbers in the parentheses are percentages of each fraction. The time constants (for major component) were not inversely proportional to the Grb2 concentration. This figure was published from (2).

For analyzing multiple-exponential kinetics in association process, two extreme reaction schemes were proposed (3);

- Defect diffusion model: In this model, the system visits many unbounded (dissociated) states to reach a specific target state for association, but the rate constants from one state to another state are not unique. The main problem arises from this model is that only one special path exists for the association that is not always possible in the real system. In addition, there is no path between the associated state and the dissociated state.
- Multiple-reaction channels with different association rate constants: In this system, many unbound (dissociated) states exist and each of them are connected to associate state with different association rate constants. Moreover, these dissociated states are independent from each other. Likewise, there is no path from the associated state to the dissociated state.

However, they could not identify the actual, most plausible kinetic scheme that reflects the observed kinetics objectively. Without any initial assumption of model parameters or more detailed information about the correlation between reactions, one cannot reach a constructive conclusion from their investigations.

In this thesis, I presented a data-driven HMM model (termed as SSN) with generalization to non-stationary time series, which best balances all conflict arising in this system. In the SSN construction, encoded past information in the state, SSNs are able to represent the complex kinetics such as non-single exponential properties and molecular memories, and identify the physical correspondence of EGFR-Grb2 process.

The objective of this research is to extract the most plausible kinetics properties of the recognition between EGFR and Grb2 from one dimensional time series free from *a priori* assumption. This objective will be completed by demonstrating two proposed schemes to EGFR-Grb2 process as well as describing the association and dissociation kinetics between EGFR and Grb2 (2) from the properties of constructed SSNs.

The overall outline of the thesis is schematically shown in Fig. 3.5: I extract SSNs at different timescales that capture the association and dissociation process between EGFR and Grb2 from the observed time series (2). It was found that the underlying SSNs are in between the defect diffusion model and multiple-reaction channel model.

This thesis is organized as follows:

1. INTRODUCTION

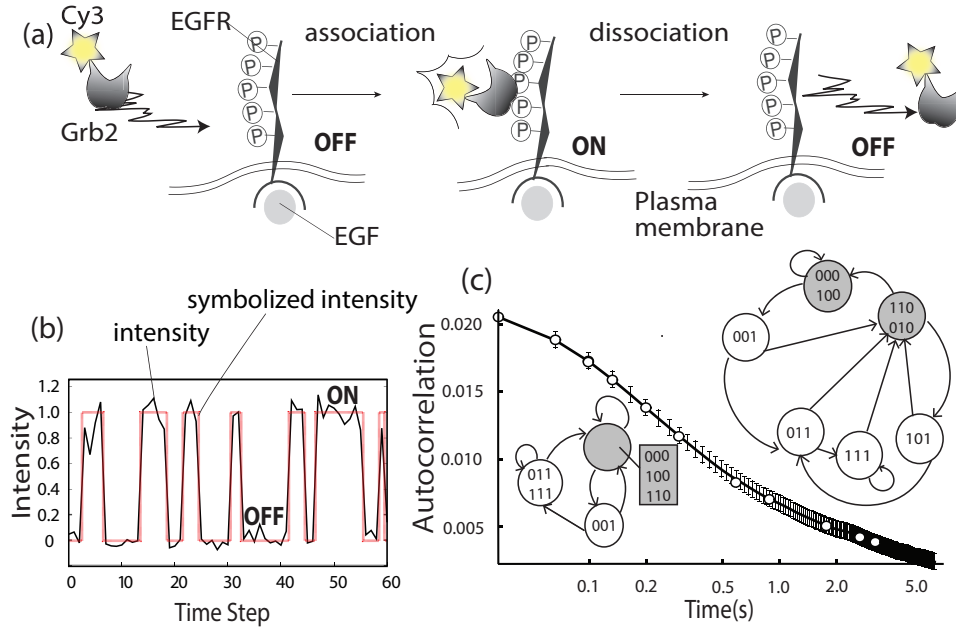


Figure 1.2: The brief procedure to extract the underlying multiscale SSNs from the observed fluorescence intensity time series of EGFR and Grb2 association process. (a) a schematic picture of the *in vitro* reconstituted system of signal processing in a single cell. The time duration of the binding between EGFR and Grb2 can be monitored from the duration of high fluorescence intensity from Cy3 attached to Grb2 detected using total internal reflection fluorescence microscope. In the *in vitro* experiment, repeated binding and release of fluorescent spots at the same position on the glass surface were observed up to a sufficiently long period (18 min). These correspond to the interaction between Cy3- Grb2 and phosphorylated EGFR in the plasma membrane fragments attached to the glass coverslip. Because simultaneous binding or release of multiple spots at the same position on the glass surface were hardly detected, EGFR is considered to exist in the monomer form (2). (b) the fluorescence intensity time trace reflecting the bound (ON) and unbound (OFF) forms of Grb2 to EGFR. In the data analysis, the time series were transformed into binary time series, from which the SSNs are constructed. (c) autocorrelation function and the associated SSNs for different timescales. The solid line and different color dots denote the autocorrelation obtained from the discrete time series, and the analytical evaluation based on the SSNs, respectively.

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- In Sec. 2: I briefly describe the construction procedure of the state space network (SSN) with its one of the most important properties. Next I newly present an analytical expression of autocorrelation by using the general properties of the SSN. I also implement the dwell time distribution by the previous manner. Owing to the lack of sample points and non-stationarity of the time series, I introduce a simple scheme called skipping step method (SSM) to derive the underlying SSNs at different timescales.
 - In Sec. 3.1 : To illustrate my proposed methods, I applied both the theoretical methods to a three-state Markovian network. It was found that, successfully constructed SSNs reproduce autocorrelation function of three states Markovian network. The structure of SSNs of this model changes as a function of number of time steps. When time step equals to nine, the SSN becomes Markovian (which depends only on present time step) implying that, with more than nine steps the system does not depend on the past. Finally I applied my SSN analysis combined with the SSM to analyze fluorescence intensity time trace of the binding and unbinding processes between EGFR and Grb2 under different concentrations of Grb2 in an *in vitro* reconstituted system (2). The autocorrelation function from SSN combined with SSM successfully reproduce the autocorrelation up to timescales that loses the memory. The SSNs change their topographical properties as a function of timescale and the existence of multistate in this process and their connectivities are newly established. In addition, the constructed SSN can capture the heterogeneity of the memory in the process depending on each state. By looking into splitting patterns as an increase of the history length for the shortest time scale SSN of the wild type EGFR and the Y1068F mutant of EGFR, I marked out the memory effects on association and dissociation kinetics (59) in this thesis.
 - In Sec. 4.1: In this section, I briefly describe the conclusion of my research including some prospective futures works.
 - In Appendix. 5.1: I reviewed some previous studies of EGFR and its family. Also I have showed some important properties of the SSN and SSM.

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Theory

2.0.1 A brief description of how to construct State Space Network (SSN)

Here I present the brief procedure for constructing state space network (SSN) (53). If the underlying kinetics have some memories (or information from the past events), the states in the SSN are defined not only by the present value of the observable but also by the past subsequence(s) of the values (with a specific range). In short, the range of the past subsequence denoted by L_{past} hereinafter, corresponds to the characteristic timescale of correlation of the event. This method starts from discretizing a continuous time series $\mathbf{x} = \{x(t_1), x(t_2) \cdots, x(t_N)\}$ into a symbolic time series $\mathbf{s} = \{s(t_1), s(t_2) \cdots, s(t_N)\}$. One does not require the system in question to be locally equilibrated or satisfy detailed balance. The choice of a suitable symbolization scheme and the number of symbols depend on the nature of time series, experimental setup, signal-to-noise ratio, and so forth (40, 60, 61).

The second step is to evaluate the transition probabilities from different subsequences (called past subsequences) to the future symbols, e.g., the transition probability $P(s_i | s_2 s_1)$ for any symbol s_i ($i=1, \dots$, the total number of symbols) to appear at a time, say t , followed by a particular subsequence $s_2 s_1$ in which one observes a specific value s_1 at time $t - 1$ and s_2 at time $t - 2$ by tracing the whole time series. Similarly, the transition probabilities for all other past subsequences $s_j s_k$ with past length two will be evaluated. The suitable value of L_{past} depends on the nature of the underlying dynamics of the time series: L_{past} roughly corresponds to the characteristic timescale of correlation and L_{past} is unity when the process (the time series) is Markovian. The actual value of L_{past} was taken to be the minimal value at which the structural property of the constructed SSN does not change even when increasing the value of L_{past} (1) (See Appendix in detail).

The third step is to derive states in the network by using the transition probabilities for the past subsequences. The transition probabilities for past subsequences whose length is optimal in capturing

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memory in the process provide all information required to predict the future. Then the question is this: can I define a state by not the single instant value but the past subsequences along the time series? Another feature to be desired for the kinetic scheme is to be simplest while maintaining the predictable power. Therefore, states are defined as follows: for a given L_{past} , if the transition probabilities are regarded as the same, I group them together into a set called a “state” (denoted by S_I hereinafter). This is because all composite past subsequences in the “state” generate the same future symbols associated with the same probabilities, implying that the grouping does not lose any predictable power while the grouping simplifies and reduces the possible number of the states.

The final step is to link the states with each other to form a network. The transition probability from a state S_I to another state S_J producing symbol s_j , denoted by $P(S_J s_j | S_I)$, yields the weight of the transition from S_I to S_J in the network with the generated s_j . Here, the next state S_J is uniquely determined by the current state S_I and the next symbol s_j (see the next Sec. 2.0.1.1 for the special case). Because all memory effects are encoded in the definition of states, the transition from S_I to S_J is Markovian.

Now I demonstrate the above procedure by considering a simple binary time series ... UBUUBBUBUBB ..., where B and U denote, for example, the bound and the unbound forms between a substrate and a receptor protein, respectively. Let us start to investigate the transition probability of zero length $L_{\text{past}} = 0$. This corresponds to the residential probability of each form U or B. Suppose that I have these values as $P(U|null) = 0.77$ and $P(B|null) = 0.23$. Here the number of states is set to be one, and the prediction of the future will be performed without any information of the current value of the time series and the past subsequence (See Fig. 2.1(a)). Then I increase the value of L_{past} by one and check if the network changes by the increment in L_{past} . Suppose again that I have $P(U|U) = 0.91$, $P(B|U) = 0.09$, $P(U|B) = 0.33$, and $P(B|B) = 0.67$.

Since the transition probabilities from the given symbols U and B are different, I must have, at least, more than two states (See Fig. 2.1(b) with $L_{\text{past}} = 1$). If the transitions actually require only the information of the current values, i.e., Markovian process in the time series, this SSN would be the desired one. In order to confirm if this is the case, the process needs to continue by increasing L_{past} and check if the topological feature of the SSN does not change. For $L_{\text{past}} = 2$, there are four possible past subsequences {UU,UB,BB,BU} and imagine that their corresponding transition probabilities are $P(U|UU) = 0.90$, $P(B|UU) = 0.10$, $P(U|UB) = 0.21$, $P(B|UB) = 0.79$, $P(U|BU) = 0.90$, $P(B|BU) = 0.10$, $P(U|BB) = 0.39$ and $P(B|BB) = 0.61$, respectively.

Since I group BU and UU but differentiate BB and UB as the individual states according to the rule as in Fig. 2.1(c), the topology of the SSN changes from that with $L_{\text{past}} = 1$. This implies that the SSN

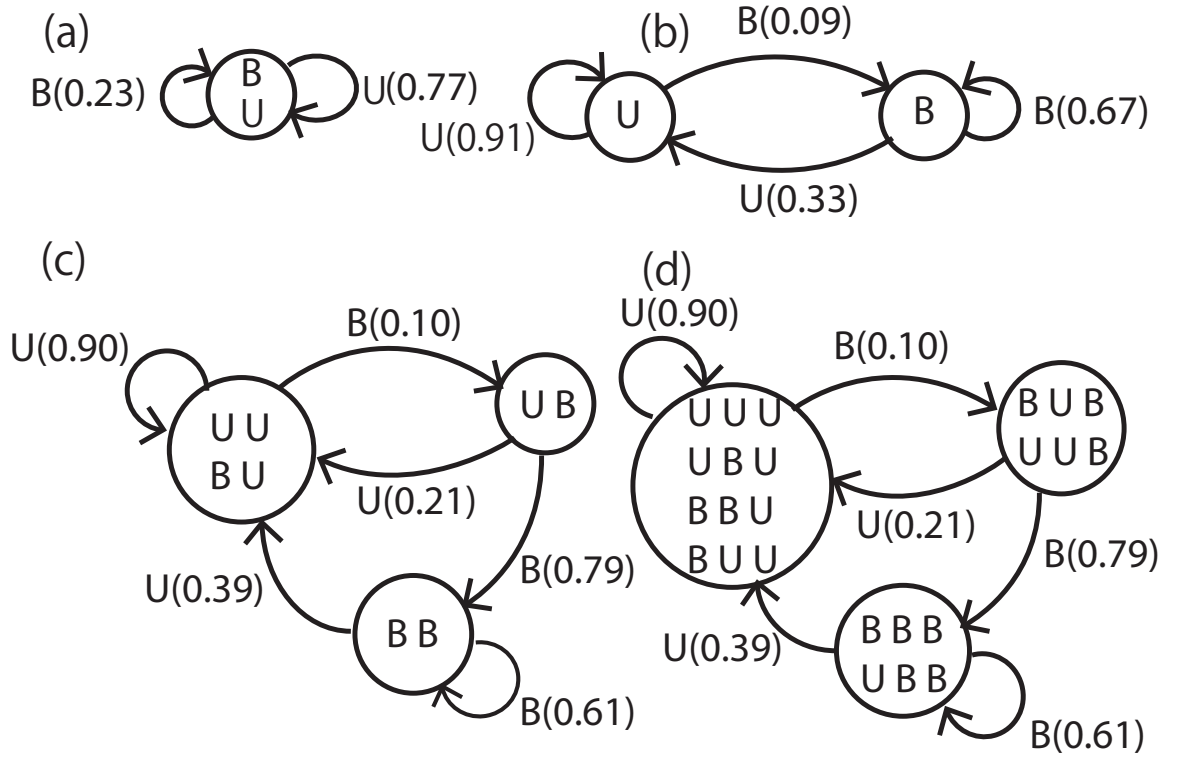


Figure 2.1: An illustrative example of the SSN construction procedure as a function of L_{past} by using a binary time series $\dots \text{UBUUBBUBUBB} \dots$ where B and U denote, e.g., two distinct conformations. (a) $L_{\text{past}} = 0$. (b) $L_{\text{past}} = 1$. (c) $L_{\text{past}} = 2$. (d) $L_{\text{past}} = 3$. The state is represented by a circle. The directed links between the states is represented by a label with the next symbol to be generated by the transitions and the corresponding transition probabilities inside the parenthesis for the link.

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with $L_{\text{past}} = 1$ is not the converged one and the process of the time series is not Markovian. Fig. 2.1(d) shows the corresponding SSN with $L_{\text{past}} = 3$. I find that the topographical features of the SSN is the same as that with $L_{\text{past}} = 2$. Therefore $L_{\text{past}} = 2$ is regarded as the optimal L_{past} yielding the converged SSN. Once I refer to the one step forward in time from the current time for the prediction of the future ($L_{\text{past}} = 2$), the process of the “state”-to-“state” transitions becomes Markovian in nature although the process of the “observable”-to-“observable”, i.e., time series of the observable itself, is non-Markovian (Actually this binary time series in this example was generated from a three-states Markovian model whose transition probabilities are taken from Fig. 2.1(c)).

In practice, the convergence of the topographical nature of the SSN is thoroughly examined by using the information amount (Shannon entropy for the residential probabilities of states in SSN) and mathematically the converged SSN is regarded as the minimal but the most predictable model to capture all the statistical information of a given time series. Readers who are interested in the mathematical details can refer to the reviews (40, 53, 62).

2.0.1.1 The Deterministic Properties of the Constructed SSN

In the algorithm to construct the SSN from time series (62), the length of the future sequences, L_{future} , is chosen to be one and only the length of the past subsequences, L_{past} , is varied. The use of $L_{\text{future}} = 1$ aims to obtain a better statistical sampling of the transition probabilities, but on the other hand, the non-deterministic situation can occur: a SSN is called deterministic if the current state with a next symbol to be produced can uniquely identify the next state to be visited, otherwise called non-deterministic. The advantage of the deterministic network is that there is a one-to-one correspondence between the symbolic sequences (i.e., the time series) and the state sequences that are generated by the SSN. This allows us to keep track of the time evolution of the states by referring to the time series.

Non-deterministic SSN can occur when $L_{\text{past}} > L_{\text{future}}$. To guarantee the constructed SSN to be deterministic, a simple procedure was employed in which non-deterministic states are made to split until they become deterministic as illustrated in Fig. 2.2. In Fig. 2.2 (a), suppose that the state containing the sequences UB and BU are combined together because their transition probabilities for future symbols are regarded as the same. Nevertheless their target state to be visited is not uniquely fixed for a given future symbol, e.g. the sequence BU links to the state containing the sequence UU by producing the symbol U, whereas the sequence UB has a self-link to the same state by producing the *same* symbol U. In this non-deterministic situation, we may not uniquely generate the corresponding state sequence from the given time series. In such cases I split the sequences BU and UB from one state into two different states to obtain the deterministic network as shown in Fig. 2.2(b).

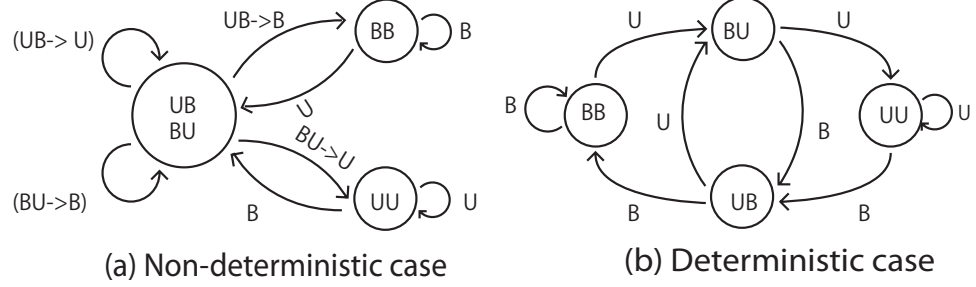


Figure 2.2: (a) An example of non-deterministic SSN with $L_{\text{past}} = 2$ for two symbols U and B. Here each state consists of a set of past sub-sequences having the same transition probability to the next symbol. Depending on the past sub-sequences (UB or BU) visited, the production of the next symbol (U or B) from the non-deterministic state leads to different target states. (b) The corresponding deterministic SSN obtained by splitting the state consisting of UB and BU into two different states.

2.0.2 Derivation of Time Autocorrelation Function

Using the properties of SSN, I can analytically derive the autocorrelation function of the original time series. Autocorrelation is the expectation value of two values at time t and $t + N$, $s(t)$ and $s(t + N)$. For the sake of brevity I denote these values at time t and $t + N$ as s_{i_1} and $s_{i_{N+1}}$ hereinafter. For this derivation, I first need to derive an analytic expression for a joint probability between s_{i_1} and $s_{i_{N+1}}$. The detailed procedure is as follows: Let us define the notations of symbols to be generated and the associated states denoted as in Fig. 2.3. By using a chain rule, the joint probability between the two symbols s_{i_1} at time t and s_{i_2} at time $t + 1$ becomes

$$\begin{aligned}
 P(s_{i_2}, s_{i_1}) &= \sum_{I_1} P(s_{i_2}, S_{I_1}, s_{i_1}), \\
 &= \sum_{I_1} P(s_{i_2} | S_{I_1} s_{i_1}) P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
 &= \sum_{I_1} P(s_{i_2} | S_{I_1}) P(S_{I_1} | s_{i_1}) P(s_{i_1}),
 \end{aligned} \tag{2.1}$$

$$\tag{2.2}$$

where the last equality of Eq. (2.2) follows from Markovian property of SSN. The conditional probability of s_{i_2} , given a state S_{I_1} and a symbol s_{i_1} , i.e., $P(s_{i_2} | S_{I_1}, s_{i_1})$, does not depend on the symbol s_{i_1} resulting in $P(s_{i_2} | S_{I_1}, s_{i_1}) = P(s_{i_2} | S_{I_1})$. In the same manner, for a joint probability between s_{i_1} at time t

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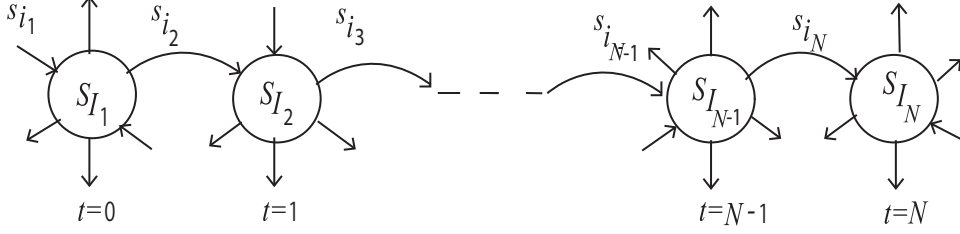


Figure 2.3: A possible time series from the state S_{I_1} to $S_{I_{N+1}}$. Here a state S_{I_t} is represented by a circle with the incoming symbol to the state denoted by s_{i_t} ($t = 1, 2, \dots$).

and s_{i_3} at time $t + 2$,

$$\begin{aligned}
 P(s_{i_3}, s_{i_1}) &= \sum_{I_2 I_1} P(s_{i_3}, S_{I_2}, s_{i_2}, S_{I_1}, s_{i_1}), \\
 &= \sum_{I_2 I_1} P(s_{i_3} | S_{I_2}) P(S_{I_2} s_{i_2} | S_{I_1}) P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
 &= \sum_{I_2 I_1} P(s_{i_3} | S_{I_2}) T_{I_2 I_1}^{(i_2)} P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
 &= \sum_{I_2 I_1} P(s_{i_3} | S_{I_2}) \left(\sum_{i_2} T_{I_2 I_1}^{(i_2)} \right) P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
 &= \sum_{I_2 I_1} P(s_{i_3} | S_{I_2}) \mathbf{T}_{I_2 I_1} P(S_{I_1} | s_{i_1}) P(s_{i_1}).
 \end{aligned} \tag{2.3}$$

Here the transition probability $P(S_{I_2} s_{i_2} | S_{I_1})$ is denoted by $T_{I_2 I_1}^{(i_2)}$ and, for the sake of simplicity, we introduce a notation $\mathbf{T}_{I_2 I_1}$ to represent $\mathbf{T}_{I_2 I_1} = \sum_{i_2} T_{I_2 I_1}^{(i_2)}$. To extend Eq. (2.3) for time $t + 3$ I get

$$\begin{aligned}
 &P(s_{i_4}, s_{i_1}) \\
 &= \sum_{I_3, i_3, I_2, i_2, I_1} P(s_{i_4}, S_{I_3}, s_{i_3}, S_{I_2}, s_{i_2}, S_{I_1}, s_{i_1}), \\
 &= \sum_{I_3, i_3, I_2, i_2, I_1} P(s_{i_4} | S_{I_3}) P(S_{I_3} s_{i_3} | S_{I_2}) P(S_{I_2} s_{i_2} | S_{I_1}) \\
 &\quad P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
 &= \sum_{I_3, i_3, I_2, i_2, I_1} P(s_{i_4} | S_{I_3}) T_{I_3 I_2}^{(i_3)} T_{I_2 I_1}^{(i_2)} P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
 &= \sum_{I_3, I_1} P(s_{i_4} | S_{I_3}) \left(\sum_{I_2} \mathbf{T}_{I_3 I_2} \mathbf{T}_{I_2 I_1} \right) P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
 &= \sum_{I_3 I_1} P(s_{i_4} | S_{I_3}) (\mathbf{T}^2)_{I_3 I_1} P(S_{I_1} | s_{i_1}) P(s_{i_1}).
 \end{aligned} \tag{2.4}$$

Finally I get the expression for the joint probability between s_{i_1} at time t and $s_{i_{N+1}}$ at time $(t + N)$ as follows:

$$\begin{aligned}
& P(s_{i_{N+1}}, s_{i_1}) \\
&= \sum_{I_N, I_{N-1}, \dots, I_1} P(s_{i_{N+1}} | S_{I_N}) \mathbf{T}_{I_N I_{N-1}} \mathbf{T}_{I_{N-1} I_{N-2}} \cdots \\
&\quad \mathbf{T}_{I_3 I_2} \mathbf{T}_{I_2 I_1} P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
&= \sum_{I_N I_1} P(s_{i_{N+1}} | S_{I_N}) (\mathbf{T}^{N-1})_{I_N I_1} P(S_{I_1} | s_{i_1}) P(s_{i_1}).
\end{aligned} \tag{2.5}$$

I factorize this transition matrix $\mathbf{T}$ into $\mathbf{T} = \mathbf{Q}\mathbf{\Lambda}\mathbf{Q}^{-1}$ where $\mathbf{Q}$ means the square matrix ($n \times n$) (n is number of states in SSN) whose column is the eigenvector of the transition matrix, $\mathbf{\Lambda}$ the diagonal matrix whose diagonal elements are the corresponding eigenvalues of the transition matrix, and $\mathbf{Q}^{-1}$ the inverse matrix of $\mathbf{Q}$, respectively. By using the factorization, Eq. (2.5) can be written as

$$\begin{aligned}
& P(s_{i_{N+1}}, s_{i_1}) \\
&= \sum_{I_N I_1} P(s_{i_{N+1}} | S_{I_N}) \left[(\mathbf{Q}\mathbf{\Lambda}\mathbf{Q}^{-1})^{N-1} \right]_{I_N I_1} \\
&\quad P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
&= \sum_{I_N I_1} P(s_{i_{N+1}} | S_{I_N}) (\mathbf{Q}\mathbf{\Lambda}^{N-1} \mathbf{Q}^{-1})_{I_N I_1} \\
&\quad P(S_{I_1} | s_{i_1}) P(s_{i_1}), \\
&= \sum_C \left[\sum_{I_N} P(s_{i_{N+1}} | S_{I_N}) \mathbf{Q}_{I_N C} \right] \lambda_C^{N-1} \\
&\quad \left[\sum_{I_1} \mathbf{Q}_{C I_1}^{-1} P(S_{I_1} | s_{i_1}) P(s_{i_1}) \right], \\
&= \sum_C A_C B_C \lambda_C^{N-1}, N \geq 1
\end{aligned} \tag{2.6}$$

where λ_C is the C -th diagonal element of $\mathbf{\Lambda}$ and $A_C = \sum_{I_N} P(s_{i_{N+1}} | S_{I_N}) \mathbf{Q}_{I_N C}$ and $B_C = \sum_{I_1} \mathbf{Q}_{C I_1}^{-1} P(S_{I_1} | s_{i_1}) P(s_{i_1})$. Since $\mathbf{T}$ is a probability matrix, it always has one eigenvalue equal to unity.

The timescale(s) of correlation (called lifetime(s) t_C) of the process can be calculated straightforwardly by

$$t_C = -\frac{1}{\log \lambda_C}. \tag{2.7}$$

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In the analysis of signal process, autocorrelation function is often used without normalization, that is, without subtraction of the mean and division by the variance (63). Since my SSN behaves as a stationary process at least for a timescale for which the SSN is constructed, I can define the autocorrelation function as the expectation value of the two symbols $s(t + \tau)$ and $s(t)$ without normalization, i.e.,

$$\begin{aligned}
 C(\tau) &= E[s(t + \tau)s(t)] \\
 &= \sum_{i_{\tau+1}i_1} s_{i_{\tau+1}}s_{i_1}P(s_{i_{\tau+1}}, s_{i_1}) \\
 &= \sum_C \sum_{i_{\tau+1}i_1} s_{i_{\tau+1}}s_{i_1}A_C B_C \lambda_C^{\tau-1}.
 \end{aligned} \tag{2.8}$$

2.0.3 Expression for Dwell Time Distribution:

Here I derive an analytical expression of dwell time distribution for a binary time series such as “ $\dots 111011100111000\dots$ ” where, for example, the symbol ‘1’ and ‘0’ correspond to ON and OFF level, respectively. Since I aim to develop the probability distribution of $P_{\text{ON}}(t)$ and $P_{\text{OFF}}(t)$, I can write the ON level probability distribution as:

$$\begin{aligned}
 P_{\text{ON}}(t) &= \frac{P(0, 1, \dots, 1, 0)}{P(0, 1, 0) + P(0, 1, 1, 0) + \dots + P(0, 1, \dots, 0)}, \\
 &= \frac{P(01^t0)}{\sum_{t'=1}^{\infty} P(01^{t'}0)}
 \end{aligned} \tag{2.9}$$

and $\sum_{t=1}^{\infty} P_{\text{ON}}(t) = 1$. Now I demonstrate it in terms of SSNs as follows: If the length of ON event is 1

$$\begin{aligned}
 P(0, 1, 0) &= \sum_{I_1 I_2} P(0, S_{I_2}, 1, S_{I_1}, 0), \\
 &= \sum_{I_1 I_2} P(0|S_{I_2})P(S_{I_2}1|S_{I_1})P(S_{I_1}|0)P(0), \\
 &= \sum_{I_1 I_2} P(0|S_{I_2})T_{I_2 I_1}^{(1)}P(S_{I_1}|0)P(0).
 \end{aligned} \tag{2.10}$$

If the length of ON event is 2,

$$\begin{aligned}
P(0, 1, 1, 0) &= \sum_{I_1 I_2 I_3} P(0, S_{I_3}, 1, S_{I_2}, 1, S_{I_1}, 0), \\
&= \sum_{I_1 I_2 I_3} P(0|S_{I_3})P(S_{I_3}1|S_{I_2})P(S_{I_2}1|S_{I_1}) \\
&\quad P(S_{I_1}|0)P(0), \\
&= \sum_{I_1 I_2 I_3} P(0|S_{I_3})T_{I_3 I_2}^{(1)} T_{I_2 I_1}^{(1)} P(S_{I_1}|0)P(0), \\
&= \sum_{I_1 I_3} P(0|S_{I_3})(T^{(1)})_{I_3 I_1}^2 P(S_{I_1}|0)P(0).
\end{aligned} \tag{2.11}$$

So, if the length of ON event is t ,

$$\begin{aligned}
P(0, 1^t, 0) &= \sum_{I_1 \dots I_{t+1}} P(0|S_{I_{t+1}})T_{I_{t+1} I_t}^{(1)} T_{I_t I_{t-1}}^{(1)} \dots \\
&\quad T_{I_2 I_1}^{(1)} P(S_{I_1}|0)P(0), \\
&= \sum_{I_1 I_{t+1}} P(0|S_{I_{t+1}})(T^{(1)})_{I_{t+1} I_1}^t P(S_{I_1}|0)P(0).
\end{aligned} \tag{2.12}$$

Finally I can write the ON level probability as follows:

$$\begin{aligned}
P_{\text{ON}}(t) &= \frac{\sum_{I_1 I_{t+1}} P(0|S_{I_{t+1}})(T^{(1)})_{I_{t+1} I_1}^t P(S_{I_1}|0)P(0)}{\sum_{t'=1}^{\infty} P(01^{t'}0)}, \\
&= \frac{\sum_{I_1 I_{t+1}} P(0|S_{I_{t+1}})(T^{(1)})_{I_{t+1} I_1}^t P(S_{I_1}|0)P(0)}{\sum_{t'=1}^{\infty} \sum_{I_1 I_{t'+1}} P(0|S_{I_{t'+1}})(T^{(1)})_{I_{t'+1} I_1}^{t'} P(S_{I_1}|0)P(0)}.
\end{aligned} \tag{2.13}$$

For more simplification the numerator can be written as following,

$$\begin{aligned}
&\sum_{I_1 I_{t+1}} P(0|S_{I_{t+1}})(T^{(1)})_{I_{t+1} I_1}^t P(S_{I_1}|0)P(0) \\
&= \sum_{I_1 I_{t+1}} P(0|S_{I_{t+1}})(H\Lambda' H^{-1})_{I_{t+1} I_1}^t P(S_{I_1}|0)P(0), \\
&= \sum_{I_1 I_{t+1}} P(0|S_{I_{t+1}})H_{I_{t+1} c}(\lambda'_c)^t H_{c I_1}^{-1} P(S_{I_1}|0)P(0), \\
&= \sum_c L_c(\lambda'_c)^t K_c,
\end{aligned} \tag{2.14}$$

where $L_c = \sum_{I_{t+1}} P(0|S_{I_{t+1}})H_{I_{t+1} c}$ and $K_c = \sum_{I_1} H_{c I_1}^{-1} P(S_{I_1}|0)P(0)$.

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In above, I factorize the transition matrix $T^{(1)}$ into three matrices; H is the square matrix ($n \times n$) (n is number of states in SSN) whose column is the eigenvector of the transition matrix, Λ' is the diagonal matrix whose diagonal elements are the corresponding eigenvalues of the transition matrix, and H^{-1} is the inverse matrix of H . I have $T = H\Lambda'H^{-1}$ by diagonalization. For the denominator of Eq. 2.13, since $I_{I'+1}$ and I_1 are dummy variables, I can simply replace them by I' and I respectively. The denominator in Eq. 2.13 becomes

$$\begin{aligned}
 & \sum_{t=1}^{\infty} \sum_{I'I} P(0|S_{I'}) (T^{(1)})_{I'I}^t P(S_I|0) P(0) \\
 &= \sum_{t=1}^{\infty} \sum_{I'I} P(0|S_{I'}) (H\Lambda'H^{-1})_{I'I}^t P(S_I|0) P(0), \\
 &= \sum_c L_c \sum_{t=1}^{\infty} (\lambda'_c)^t K_c, \\
 &= \sum_c L_c \frac{\lambda'_c}{1 - \lambda'_c} K_c.
 \end{aligned} \tag{2.15}$$

After combining Eq. 2.14 and Eq. 2.15, I have

$$P_{\text{ON}}(t) = \frac{\sum_c L_c (\lambda'_c)^t K_c}{\sum_c L_c \frac{\lambda'_c}{1 - \lambda'_c} K_c}. \tag{2.16}$$

Using the same procedure I can derive the OFF state probability distribution.

2.0.4 Skipping Step Method (SSM)

For the application of SSN to SM time series obtained experimentally, there are two related obstacles: one is a problem of insufficient sampling in constructing the transition probabilities in the SSN procedure, and the other is the possible nonstationarity of the time series. The latter is a problem because the original SSN scheme was developed for stationary data. The former problem may be inherent to SM measurements such as Fluorescence Resonance Energy Transfer (FRET) measurement especially when the fluorophores (dye) used in the experiment suffer from photobleaching, which shortens the lifetime of the fluorophores and, thus, the length of the time series available.

The latter, nonstationarity problem occurs in two different situations. One is that a given time series is intrinsically nonstationary irrespective of the length of time series. The other one is: if all finite characteristic timescales of the system are sufficiently shorter than the length of the time series observed by a measurement, the time series in the experiment should be stationary at equilibrium. However, the time series is regarded as nonstationary even at equilibrium if there exists characteristic timescales of

the system comparable or longer than the length of time series monitored. To analyze nonstationary time series, the original algorithm presented in Sec. 2.0.1 cannot be applied straightforwardly because it is formulated for stationary time series.

To overcome these problems, a generalization of SSN was developed by a multiscale decomposition scheme based on discrete wavelet transforms (1, 39, 40). In the scheme, first, the original nonstationary time series is decomposed into a set of time series at different timescales in a hierarchical manner. Time series that are much longer than their transition timescales are expected to be stationary. It was found for single molecule electron transfer experiment of the NADH:flavin oxidoreductase (Fre) complex that the time series constructed at each timescale shows stationary behavior for a time region shorter than the individual timescales (1, 39, 40). The original SSN construction scheme may be applied to the stationary time series components, and the set of SSNs constructed for the stationary time series components are combined to get a single SSN covering a wide range of the original time series.

Possible drawbacks for this scheme developed for continuous time series are: First, the result of the wavelet decomposition depends on the choice of wavelet basis function. For example, most wavelet basis functions result in the so-called Gibbs phenomenon (64) when applied to discrete time series. That is, a finite sum of the Fourier series has artificially large oscillations near a discontinuous jump, and a huge number of Fourier components is required to approximate the discontinuous jumps (A similar situation should meet for most wavelet basis functions). Second, in the wavelet decomposition, as timescales of wavelet components become longer, the number of ‘independent’ samples at the long timescales becomes fewer (known as down sampling problem). One may obtain almost the same number of samples at all different timescales by shifting the time origin along the original time series. However, the more the timescale increases, the less the generated time series become independent. This is because the wavelet basis function operates on segments of time series which are overlapping despite the shifting of the time origin.

In turn, the SSM proposed in this article does not need to specify any basis function and is free from the Gibbs phenomenon. Every possible skipping step yields an independent skipped step time series, thus it is free from the downsampling problem. On the other hand, the properties of SSN (as an HMM) do not disappear even in non-convergent SSN by using SSM. Regardless of the skipping step used and the convergence of the SSN with respect to the past subsequence length (L_{past}), the SSN remains minimal in state complexity and predictivity (at least up to L_{past}). First, since different past subsequences with the same transition probabilities to the future are grouped to the same state, the state complexity attains its minimum for a given L_{past} . In other words, all other ways of grouping for the same L_{past} necessarily result in a higher state complexity. Second, this grouping of subsequences to construct the

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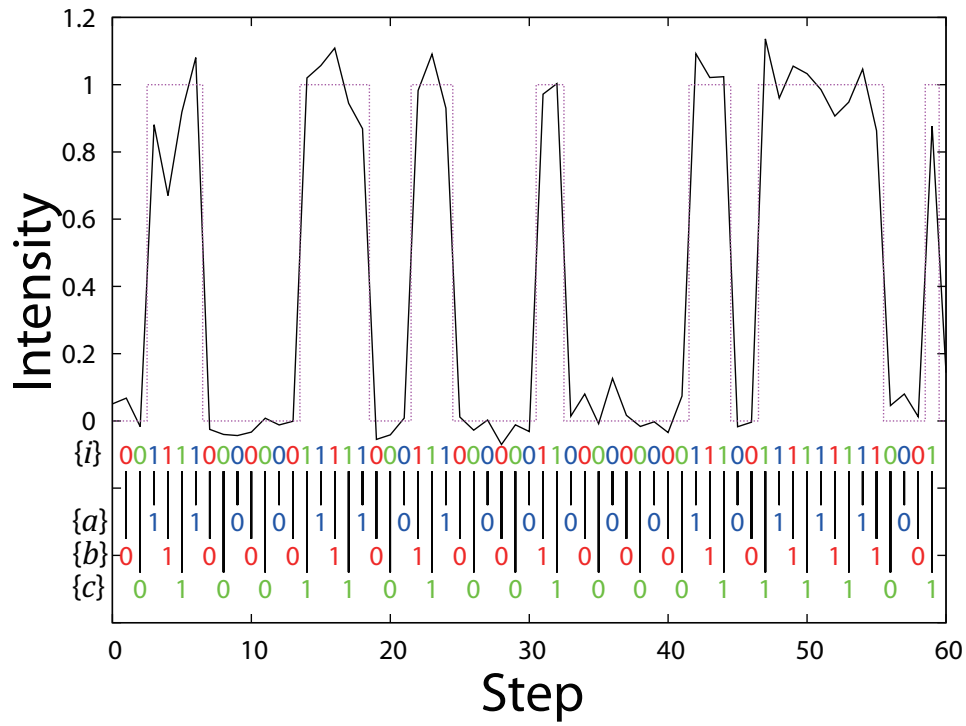


Figure 2.4: An original symbolic time series $\{i\}$ colored with red, green, and blue. By skipping every three steps, the time series is decomposed into three distinct time series of a blue time series $\{a\}$, a red time series $\{b\}$, and a green time series $\{c\}$. The black solid and pink dashed lines denote the original time series and the discrete ON/OFF time series, respectively.

SSN together with its Markovian state-to-state transition probabilities preserves the joint probability of the observable sequences and, therefore, is as predictive as the situation where all details of the original past subsequences are kept up to the given L_{past} (62). Therefore, SSNs constructed from the skipped step time series make it possible to capture kinetics with timescale corresponding to the skipping step. As the size of the skipping step increases, the resultant SSN is expected to describe slower kinetics. However, the skipped time series do not contain any data in between the skipping steps and this might make it difficult to relate the results of the SSM to some of experimentally detectable quantities such as the dwell time distributions (The mathematical derivation for dwell time distribution will be published elsewhere).

Here I explain the SSM in the case of skipping step three (SK 3). For SK 3, the original time series is decomposed into three time series, each of which is constructed by sampling from the original time series every three steps. Let the original time series be $\mathbf{s} = \{s(t_1), s(t_2) \cdots, s(t_N)\}$ and let $N = 3m + 1$, (m is an integer), for simplicity. Then, the three time series are $\mathbf{s}_1 = \{s(t_1), s(t_4) \cdots, s(t_N)\}$, $\mathbf{s}_2 = \{s(t_2), s(t_5) \cdots, s(t_{N-2})\}$ and $\mathbf{s}_3 = \{s(t_3), s(t_6) \cdots, s(t_{N-1})\}$, respectively. In Fig. 2.4 I show the decomposition of the original symbolic time series into three symbolic time series. Combining these three time series $\mathbf{s}_1$, $\mathbf{s}_2$ and $\mathbf{s}_3$, I can obtain the original time series $\mathbf{s}$.

The structure of SSN constructed from the skipped time series reflects dynamics at the timescale that corresponds to the skipping step. Time series of complex process can have various correlation timescales. If the time series involves (a) longer correlation timescale(s) than the skipped step, the transition probabilities along the skipped time series may depend on the subsequences (resampled every skipped step), reflecting their histories or memories. Contrastingly, if the time series involves (a) shorter correlation timescale(s) than the skipped step, the subsequences of the skipped time series are expected to have no memory and their future symbol distributions do not depend on these subsequences. These subsequences are grouped into one state in the SSN within the skipped step resolution. Therefore, as the skipping step increases, the SSN tends to have fewer states (unless the system experiences a wider region on the underlying state space than the region scanned by the shorter skipping step). If the timescale of the skipping step becomes longer than the characteristic timescale of correlation, all the subsequences of the skipping step time series lose their memory and are merged into a single state.

The SSM is useful to examine long time memory. Suppose that I am restricted solely on the original time series (i.e., the time series of the skipping step one). If the topographical feature of SSNs constructed for the time series does not converge when L_{past} increases, it indicates that the time series has longer memory than L_{past} , which requires us to examine long time memory existing in the time series.

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However, when L_{past} increases, the number of the samples (the length of the time series) required to estimate the transition probabilities increases exponentially (the number of possible subsequences grows like $N_s^{L_{\text{past}}}$ where N_s denotes the number of symbols) and roughly L_{past} cannot exceed the logarithm of the length of the time series divided by the logarithm of the number of symbols N_s (62). Therefore, the examination of long time memory at looking by the change in the topographical property of SSN constructed for the original time series with respect to L_{past} might become erroneous. Contrastingly, with the idea of skipping step, as the skipping step m increases, the number of samples to be required does not increase at all because, as an increase of SK m , the number of the decomposed time series increases as well, which compensates the lack of independent sampling moderately. Therefore, the SSM does not suffer from the lack of sampling and the scrutiny of the topographical properties of SSNs as a function of m makes it possible to examine long time memory buried in the time series.

3

Result and Discussion

3.1 An Illustration of our Construction Scheme of Multiscale SSNs for a Three-State Markovian Network

In this subsection I illustrate our method by using a simple model system that consists of a receptor protein A and a substrate B (See Fig. 3.1). Suppose that the protein A has two conformations A_1 and A_2 , and when the protein A binds to the substrate B there exists two distinct bound forms denoted by $A_1 B$ and $A_2 B$. The other state corresponds to the unbound form denoted by $A+B$. The former two bound states are assigned as ON states whereas the latter the unbound state as an OFF state (indicated by gray circle in Fig. 3.1). For this model, with generating a binary time series of length 100,000 using Monte Carlo method (ON and OFF levels are represented by “1” and “0”), let us construct the underlying SSNs by using the procedure presented in Sec. 2.0.1. The SSNs converged at each skipping step with $L_{\text{past}} \leq 2$ are shown in Fig. 3.2, and the residential probabilities of the states of the SSN of skipping step one are given, with those of the three-state model, in Table 3.1. One can see that the SSN at the skipping step one has the same number of states as the three-state model does: one corresponds to the OFF state whereas the other two correspond to the ON state although the residential probabilities in the ON states S_0 and S_1 are different from those of $A_1 B$ and $A_2 B$. The reason for this discrepancy between the network structure of the model and that of the SSN is as follows: In general, depending on the topological features of the underlying network, e.g., some networks may have some redundancy, the underlying network may not be the simplest model to generate the time series, and therefore the converged SSN constructed is not necessarily the same to the underlying network. This is because the SSN scheme deals with only a time series, and is designed to construct the simplest but most predictive network by capturing all statistical and kinetic information buried in the one-dimensional time series.

3. RESULT AND DISCUSSION

It is noted that the statistical complexity (which quantifies how complex the network model is) of the underlying network is larger than that of the constructed SSN for the three-state model, implying that the constructed SSN is indeed a simpler representation of the process (i.e., statistical complexity is 0.796 for the constructed SSN but 0.980 for the original three-state model).

Fig. 3.2 shows the SSNs constructed at skipping step 1 (SK 1), 3 (SK 3), 9 (SK 9) and 27 (SK 27) with the autocorrelation computed numerically by the formula $C(\tau) = \frac{1}{N-\tau} \sum_{i=1}^{N-\tau} s_i s_{i+\tau}$ (where s_i and N are the value at time i and the total length of time series), and the comparison to the autocorrelation computed analytically in terms of the obtained SSNs. These different SSNs can reproduce autocorrelation function at different timescales corresponding to their skipping step. At SK 1, we have three states whereas at SK 3 there are two states. At nine steps, the autocorrelation almost converges to the asymptotic value $\left(\frac{1}{N} \sum_{i=1}^N s_i\right)^2$, implying that, with the increment of more than nine steps, the next outcome does not ‘remember’ or ‘refer to’ the current outcome. Hence, the SSN becomes the same as that from a simple coin toss at SK 9. The network constructed at SK 27 turns out to be the same as at SK 9, which means that the SSNs up to SK 9 are enough to capture all autocorrelation of the system.

Table 3.1: The residential probabilities of the three-state model and the corresponding SSN. The SSN is constructed with the significance level $\alpha = 0.01$, $L_{\text{past}} = 2$ and the skipping step one. The state S_0 contains subsequences 11, the state S_1 01, and the state S_2 10 and 00, respectively.

	Three-state model	SSN
ON	$P(A_1 B)=0.20$	$P(S_0)=0.69$
	$P(A_2 B)=0.57$	$P(S_1)=0.08$
OFF	$P(A + B)=0.23$	$P(S_2)=0.23$

For comparison, I superimpose an autocorrelation function calculated directly from the ON/OFF time series on the autocorrelation function evaluated analytically by the SSNs at different skipping steps in Fig. 3.2. These two autocorrelation functions coincide within the error bar of the autocorrelation function. Table 3.2 presents the time intervals for which the autocorrelation is reproduced by each SSN constructed for each different skipping step. Note that for this three-state model the generated time series is perfectly stationary and the SSN at SK 1 can reproduce correlations at all time ranges.

Table 3.2: The time region for which each SSN constructed for different skipping step 1, 3, 9, and 27 reproduces the autocorrelation. Note that the increment of the intervals is different with each other dependent on the SK m , and the total step length is 100,000.

SK 1	SK 3	SK 9	SK 27
0 ~ 100,000	3 ~ 99,999	9 ~ 99,999	27 ~ 99,981

3.1 An Illustration of our Construction Scheme of Multiscale SSNs for a Three-State Markovian Network

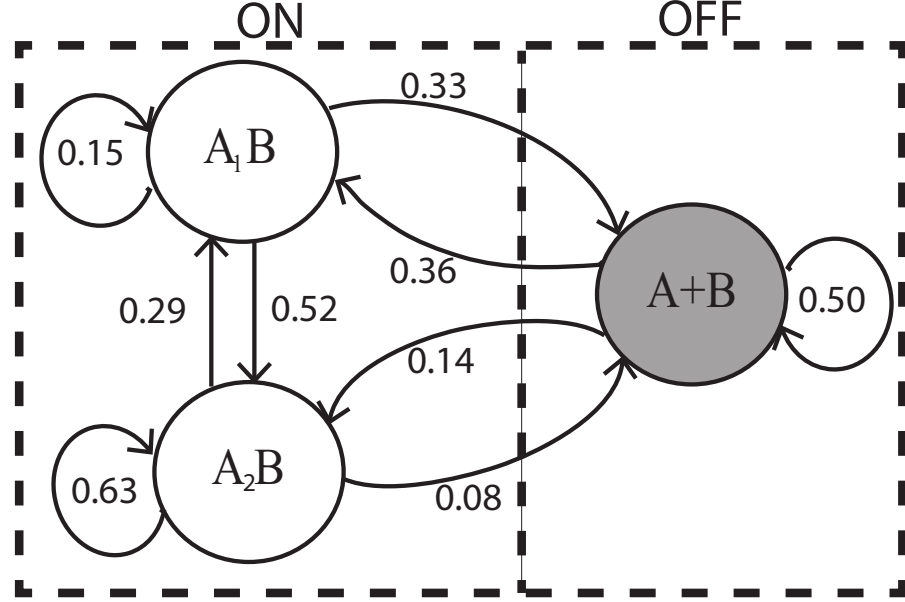


Figure 3.1: A Markovian network model composed of three states in which two states belonging to ‘ON’ are not visually distinguishable in the time series. The transition probabilities per unit time among these three states are denoted by the numbers associated with links.

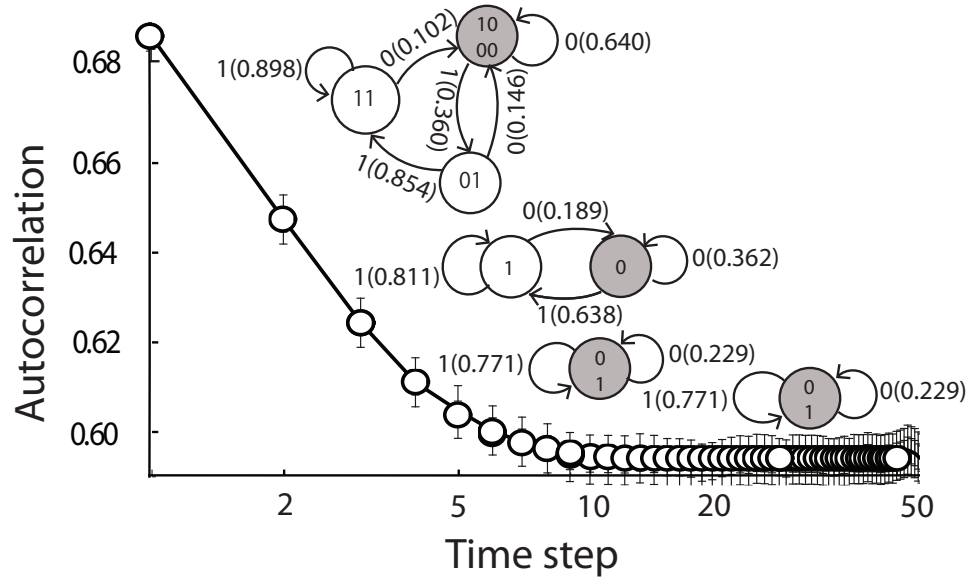


Figure 3.2: The SSNs constructed at SK 1, SK 3, SK 9, and SK 27 shown from the left top to the right bottom for the three-state model. The autocorrelation function derived numerically from the time series is indicated by black line with the error bar denoted by vertical short lines. Those derived analytically in terms of the constructed SSNs are denoted by empty circles (the time range each SSN can reproduce is summarized in Table 3.2). The shaded and empty circles denote the OFF and ON states, respectively.

3. RESULT AND DISCUSSION

To further demonstrate that the constructed SSN can capture not just solely (second order) autocorrelation function but all statistical information buried in the time series s_i ($i = 1, \dots, N$), I illustrate the other quantities, mutual information, and third-order correlation function. The mutual information $I(\tau)$ between values at different times i and $i + \tau$, s_i and $s_{i+\tau}$, is defined as follows (65):

$$I(\tau) = \sum_{s_i, s_{i+\tau}} p(s_i, s_{i+\tau}) \log \frac{p(s_i, s_{i+\tau})}{p(s_i)p(s_{i+\tau})}, \quad (3.1)$$

which quantifies the amount (in bits) of the future (current) information $s_{i+\tau}$ (s_i) learned by the current (future) information s_i ($s_{i+\tau}$). The third-order correlation function $C(\tau_1, \tau_2)$ is defined by

$$C(\tau_1, \tau_2) = \frac{1}{N - \max\{\tau_1, \tau_2\}} \sum_{i=1}^{N - \max\{\tau_1, \tau_2\}} s_i s_{i+\tau_1} s_{i+\tau_2}. \quad (3.2)$$

Both quantities are computed numerically for the three-state toy model and the obtained SSN by generating the time series by Monte Carlo simulations with the Park and Miller random number generator algorithm (66).

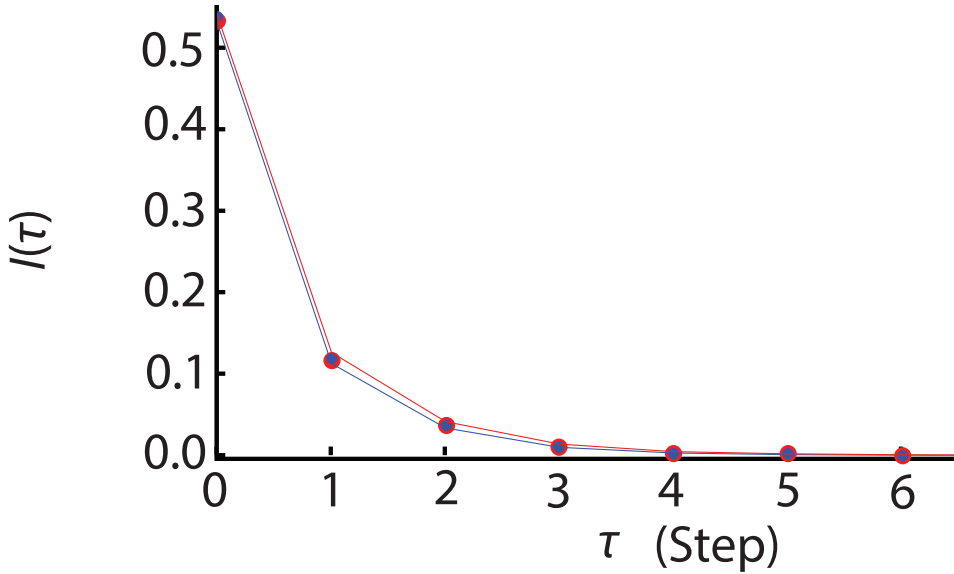


Figure 3.3: The mutual information $I(\tau)$ as a function of the lag τ derived from the time series of the original toy model and the SSN. The lines and dots denote $I(\tau)$ for the original toy model and the SSN derived from the time series, respectively, which are generated by the Monte Carlo simulation with 100,000 (depicted by the red color) and 1,000,000 (depicted by the blue color) steps.

Fig. 3.3 shows the mutual information $I(\tau)$ as a function of τ for the original toy model and the SSN. Here I generate a set of time series with the total Monte Carlo step of 100,000 (depicted by the

3.1 An Illustration of our Construction Scheme of Multiscale SSNs for a Three-State Markovian Network

red) and that with the total step of 1,000,000 (indicated by the blue) from the SSN (dots) and the three-state toy model (lines). The difference between mutual information curves for both models calculated by using 100,000 and 1,000,000 data points are not so significant in this scale, although the greater number of data points 1,000,000 gives rise to a better coincidence between the original toy model and the constructed SSN. In Fig. 3.4 the third-order correlation functions $C(\tau_1, \tau_2)$ are given for the original toy model (indicated by the solid lines) and for the obtained SSN (dots) as a function of τ_1 at some fixed values of τ_2 using 100,000 Monte Carlo steps. The third-order correlation function with $\tau_2 = 0$, $C(\tau_1, 0)$, (the red line and the red dots) corresponds to the second order correlation with which the third-order correlation function with $\tau_2 = k$ ($k = 2, 4, 6, 8, 10$), $C(\tau_1, k)$, intersects or coincides at $\tau_1 = k$. For both, it is found that the mutual information and third-order correlation function are well reproduced by the obtained SSN. It should be noted that these are just demonstration to exhibit how SSN can capture any statistical quantities buried in the original model (See the mathematical proof in Ref. (67)).

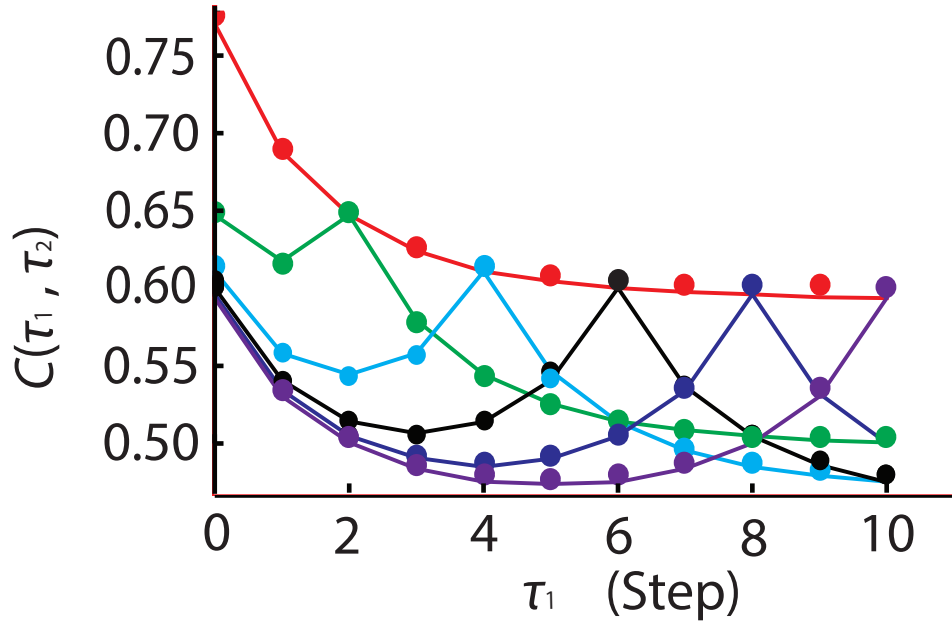


Figure 3.4: The third-order correlation functions $C(\tau_1, \tau_2)$ as a function of τ_1 with some fixed values of τ_2 , derived numerically from the time series generated by the original model (indicated by the solid lines) and that by the SSN (dots). Different colors mean the different values of τ_2 , i.e., $\tau_2 = 0$ (red), 2 (green), 4 (light blue), 6 (black), 8 (dark blue), and 10 (purple). The total Monte Carlo step is 100,000.

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3.1.1 Application to Recognition Kinetics between EGFR and Grb2

3.1.1.1 A Brief Description of an *in vitro* Reconstituted Receptor-Adapter Recognition Experiment

I apply our multiscale decomposition scheme based on skipping step method to the association and dissociation kinetics between EGFR and Grb2. This interaction serves as a crucial step in signal processing in a live cell (2) (See also Fig. 3.5). Here I briefly describe the experimental setting. The plasma membrane fraction from epithelial carcinoma A431 cells was immobilized to the coverslip, and Grb2 labeled with the fluorophore Cy3 were added into the solution. Morimatsu *et al.* (2) observed “intermittent pulses” repeatedly at the same positions on the glass surface by EB CCD camera equipped with an MCP image intensifier. The pulse arises from binding and release processes of the Cy3-Grb2 with EGFR localized at the cytoplasmic side of the membrane fragments. For the sake of simplicity, I abbreviate Cy3-Grb2 simply as Grb2 hereinafter. The onset of EGFR-Grb2 association results in a fluorescent spot at the corresponding location on the camera, and conversely, the termination of fluorescence corresponds to dissociation. Movies of single molecule interactions between EGFR and Cy3-Grb2 were recorded at the video rate of $1/30\text{ s}^{-1}$ during 18 min within a given observation field. The effects of bleaching and blinking of Cy3 on the on- and off-times were expected to be minimal because the decay time for bleaching was found to be 15s and blinking occurred only once in 147s under the same excitation conditions. These time constants were much longer than those of the on-times (2). Simultaneous binding or release of multiple spots at the same position on the glass surface were hardly detected, suggesting that EGFR exists in the monomer form. The SM time series are symbolized as a bound state by symbol ‘1’ (fluorescent) and an unbound state by ‘0’ (nonfluorescent) by introducing an appropriate threshold (2). Single instantaneous transitions in one frame such as $1 \rightarrow 0 \rightarrow 1$ and $0 \rightarrow 1 \rightarrow 0$ were excluded from the analysis, because two frame averaging was applied to the raw images as a pretreatment in order to reduce shot noise (2).

Single exponential kinetics were not observed between the bound and unbound forms, indicating that multiple states exist within both forms. In addition, the association rate does not increase in proportion to the Grb2 concentration but increases gradually slower than the linear dependence. It was also shown that non-Markovianity exists in the ON/OFF time series of the recognition kinetics between EGFR and Grb2. The non-Markovianity could not be simply interpreted in terms of a multistate Markovian model whose unseen states were solely determined from the individual off-time and on-time distributions (3). It was thus conjectured that molecular memory exists in the conformational fluctuation of EGFR such that the EGFR conformation may change upon binding with a Grb2, and after the Grb2 dissociates from

3.1 An Illustration of our Construction Scheme of Multiscale SSNs for a Three-State Markovian Network

the EGFR, the EGFR conformation may need to relax to the unbound form that is favored for Grb2 binding.

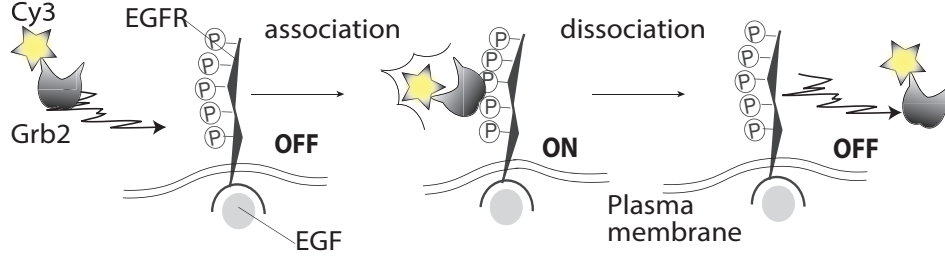


Figure 3.5: A schematic picture of the *in vitro* reconstituted system of signal processing. The time duration of the binding between EGFR and Grb2 can be monitored from the duration of high fluorescence intensity from Cy3 attached to Grb2 detected using total internal reflection fluorescence microscope. These correspond to the interaction between Cy3-Grb2 and phosphorylated EGFR in the plasma membrane fragments attached to the glass coverslip.

Y1068F mutant: EGFR has five major tyrosine residues that are actively phosphorylated after ligand binding. The Y1068F mutant of EGFR replaces tyrosine (Y) 1068 in EGFR (whose phosphorylation has been reported to construct the primary strong Grb2 binding site (68)) by phenylalanine (F) to prevent phosphorylation (69). Exponential properties and memory effects in association and dissociation kinetics were analyzed for the Y1068F mutant (2, 3). The Y1068F mutant of EGFR showed non-exponential features in the dissociation kinetics (i.e., in the dwell time distribution of the bound form) at all concentrations, which was the same as the wild type EGFR (2). However, the association kinetics (i.e., the dwell time distribution of the unbound form) at 1 nM Grb2 concentration showed that it is approximated by a single exponential kinetics for a wide range of timescales with the loss of correlation (2, 3).

3.1.2 Correlations in Recognition Kinetics and the Underlying SSNs

To uncover the multiplicity of states and molecular memory in the process and its dependence on the mutation of the Y1068F mutant, I apply the SSN scheme combined with our SSM to the symbolized, binary SM time series of association and dissociation processes of the wide type EGFR and the Y1068F mutant at 1 nM concentration of Grb2. The structural property of the SSNs quantified by Shannon entropy of the states was found to show some locally convergent SSNs at L_{past} equal to 2 or 3 while the entropy continuously increases for a further increase of L_{past} . This local convergence indicates the existence of the timescale separation, i.e., the local convergence of SSN means that the dynamics faster than the timescale of $L_{\text{past}} = 2-3$ can be regarded as randomized and stationary such as being trapped in some energy basins. However, the longer timescale dynamics is considered to experience nonstationary

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basin-hopping processes among different basins. Hence, in this report, I chose $L_{\text{past}} = 3$ for all SSNs to be analyzed (in Appendix) with the skipping step 1, 3, 9, and 27 (corresponding to $0.0333\cdots (=1/30)$, 0.1, 0.3 and 0.9 s) so that L_{past} -times of a skipping step is equal to one increment of the next skipping step timescale.

Fig. 3.6 exemplifies the autocorrelation function of the symbolic time series at 1 nM concentration of Grb2 for the wild type EGFR and the Y1068F mutant (Also for concentration 10 nM and 100 nM see Fig. 5.4 and 5.5 in Appendix). The observed autocorrelation function is satisfactorily reproduced by the analytical formula based on the obtained SSNs covering different time domains by different skipping steps for all concentration of Grb2. The corresponding time intervals or ranges the SSN can capture the autocorrelation, constructed at different skipping steps, are given at 1 nM concentration for the wild type EGFR and the Y1068F mutant in Table 3.3. For example, at 1 nM concentration of Grb2 with the wild type EGFR, the constructed SSNs can reproduce the autocorrelation function at the timescale from 0 s to 0.133 s with the skipping step 1, abbreviated as SK 1 (in the unit/increment of 1/30 s), from 0.1 s to 0.3 s with SK 3 (0.1 s), 0.3 s to 0.9s with SK 9 (0.3 s), and 0.9 s to 3.6 s with SK 27 (0.9 s). Remind that the history lengths automatically built in the SSN (i.e., the timescale of each skipping step multiplied by a factor of three ($L_{\text{past}} = 3$)) are 0.1 s, 0.3 s, 0.9 s, and 2.7 s at SK 1, SK 3, SK 9, and SK 27, respectively. This implies that the SSNs at SK 1 and SK 27 can capture the autocorrelation beyond the timescale of the history length in the SSN, while those at SK 3 and SK 9 cannot.

In turn, as seen in Table 3.3 in Appendix, compared to the SSNs of the wild type, the SSN of the Y1068F mutant tends to reproduce longer timescales' autocorrelation at each skipping step: for example, the SSNs with SK 27 can capture the correlation from 0.9 s to 4.5 s at all concentration compare to those for the wild type (ca. 0.9 s to 3.6 s) and 0.9 s to 2.7 s (10, 100 nM)).

Let us now look into the structure of the SSNs, especially the compositions of the ON and OFF states and their splitting as a function of the skipping step. Fig. 3.7 presents the corresponding SSNs at each skipping steps for the wild type EGFR and the Y1068F mutant at 1 nM concentration of Grb2. To visualize which states have mutually similar transition probability distributions, I embed states of *all* SSNs of both the wild type and the Y1068F mutant EGFR (70) into the one-dimensional Euclidean space (the horizontal axis): the more the states have mutually similar transition probability distributions, the closer they are located. To quantify the similarity between two transition probability distributions, I used the Hellinger distance (71) defined by $D[I, J] = \frac{1}{\sqrt{2}} \sqrt{\sum_{s_i} (\sqrt{P(s_i|S_I)} - \sqrt{P(s_i|S_J)})^2}$ where, e.g., $P(s_i|S_I)$ is the transition probability for producing a next symbol s_i from the state S_I . The position of each state along the vertical axis is chosen simply for visual clarity. The size of circle reflects the residential probability of the state; the larger the size of circle, the more the system resides in that state. Hereinafter,

3.1 An Illustration of our Construction Scheme of Multiscale SSNs for a Three-State Markovian Network

I call all states where the EGFR and Grb2 are currently bound (i.e., the (rightmost) last symbol appearing in a subsequence constituting the state is '1') *ON state* (indicated by white circles). Likewise, I call all states where they are currently unbound (i.e., the last symbol appearing in a subsequence constituting the state is '0') *OFF state* (gray circles). A state corresponds to a series of snapshots of conformations to end up either in the bound and unbound forms of the EGFR and Grb2.

The numbers of ON and OFF states, wiring pattern, residential and transition probabilities for the states are dependent on which timescale each SSN represents. It should be noted that this behavior is the same as observed in the analysis of single-molecule electron transfer experiment of the NADH:flavin oxidoreductase (Fre) complex (55) in which the topographical features of the SSN change as a function of timescale in order to recover the hierarchical diffusion property in the protein fluctuation (1, 39, 40).

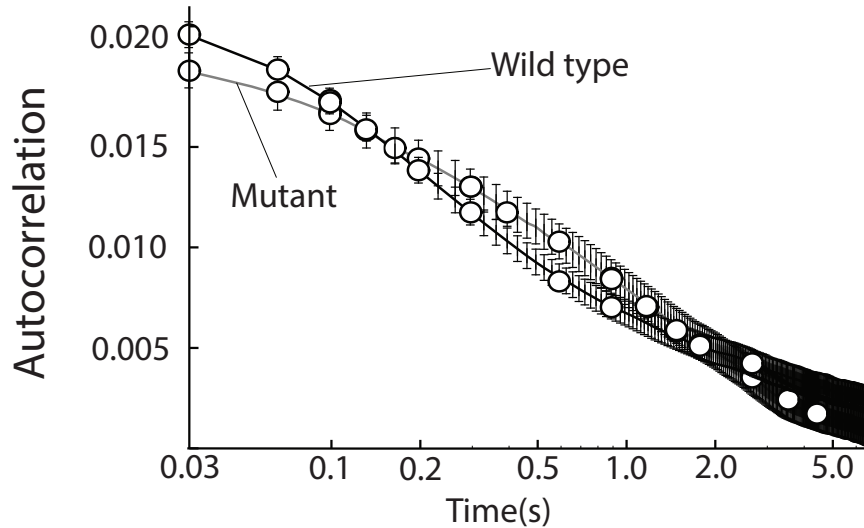


Figure 3.6: Autocorrelation for the ON/OFF time series of the association and dissociation processes between the wild type and the Y1068F mutant at 1nM concentration of Grb2. The autocorrelation function derived numerically from the time series is indicated by black line in the wild type and gray line in the mutant with the error bar denoted by vertical short lines. Those derived analytically in terms of the constructed SSNs are denoted by open circles.

In both the wild type and the mutant, for SK 1 and SK 3, I have only one OFF state whose composite subsequences of length three are terminated by symbol '0'. Note that since time series is binary with L_{past} being three, the maximum numbers of ON states and OFF states are four ($2^2 = 4$), respectively, i.e., eight in total. At SK 1, one can find that one OFF state and two ON states (the wild type) and one ON state (the Y1068F mutant) are sufficient to capture the correlation in this timescale. The existence of only one OFF state implies that irrespective of the paths to reach at the symbol '0', i.e., either $1 \rightarrow 1 \rightarrow 0$,

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$1 \rightarrow 0 \rightarrow 0$, or $0 \rightarrow 0 \rightarrow 0$, transition probabilities are the same (within a certain significance level). In the other terms, the transition probabilities only depend on the latest symbol '0'. On the contrary, while only one ON state exists in the Y1068F mutant, the existence of two ON states in the wild type implies that the next symbol to be generated is dependent on the paths to arrive at the bound form '1' [i.e., either $(1 \rightarrow 1 \rightarrow 1, 0 \rightarrow 1 \rightarrow 1)$ or $0 \rightarrow 0 \rightarrow 1$]. Note that any consecutive paths or links that will end up with each state produce a series of the symbols '0' and '1' along the path (remind that each link has not only the transition probability but also the symbol to be generated), which coincides with the symbolic sequences consisting of the state. Namely, heterogeneous memory effects are encoded in the internal structure of the states, and equivalently in the topology of the SSN.

As an increase of skipping step to three, i.e., for a time series resampled every three steps over the original time series, the OFF state still persists as a single state but the ON state splits further. The number of the ON states reaches at the maximum number of four at the longer skipping timescales SK 9 and SK 27 in the wild type while it changes from four to three as an increase of the skipping timescales from SK 9 to SK 27 in the Y1068F mutant. In turn, the number of the OFF states does not reach the maximum number as the skipping steps increase from 1 to 27. It should be noted in Fig. 3.7 that, for the Y1068F mutant, the center of the two OFF states at SK 9 is almost identical although the two OFF states at SK 9 for the wild type are located at distinctively different positions (shown with a dash closed curve in the figure).

Namely, the SSN constructed for the Y1068F mutant is interpreted as effectively having a single OFF state up to the timescale of $1/30 \text{ s} \times 9 \times 3 \sim 0.9 \text{ s}$, while it splits to two OFF states when the skipping step increases from 9 to 27.

Compared to the three-state model presented in the previous section, for which the SSN tends to be simpler as the length of the skipping step increases (i.e., the longer the timescale, the smaller the number of the states), the state splittings in the OFF and ON states at longer timescales (at least, from SK 9 to SK 27) suggest that the multiple states are required to capture the kinetic complexity inherent to those timescales in the EGFR-Grb2 systems. This results from the multiscale, nonstationary nature of the ON/OFF time series of the recognition kinetics. This is interpreted as follows: for short timescale, the SSN (SK 1) structures in both the wild type and the mutant are simple since the conformation fluctuation of the EGFR is more likely to be confined within a single (super) basin on the energy landscape, making the system behave rather stationary and random. However, for the longer timescales (i.e., SK 9 and SK 27) the EGFRs can perform large conformational changes and, therefore, move between larger (super) basins on the energy landscape (72), implying the emergence of more complex structure of the SSN in order to capture the complex kinetics. At 10 nM and 100 nM concentration of Grb2 for the wild type

3.1 An Illustration of our Construction Scheme of Multiscale SSNs for a Three-State Markovian Network

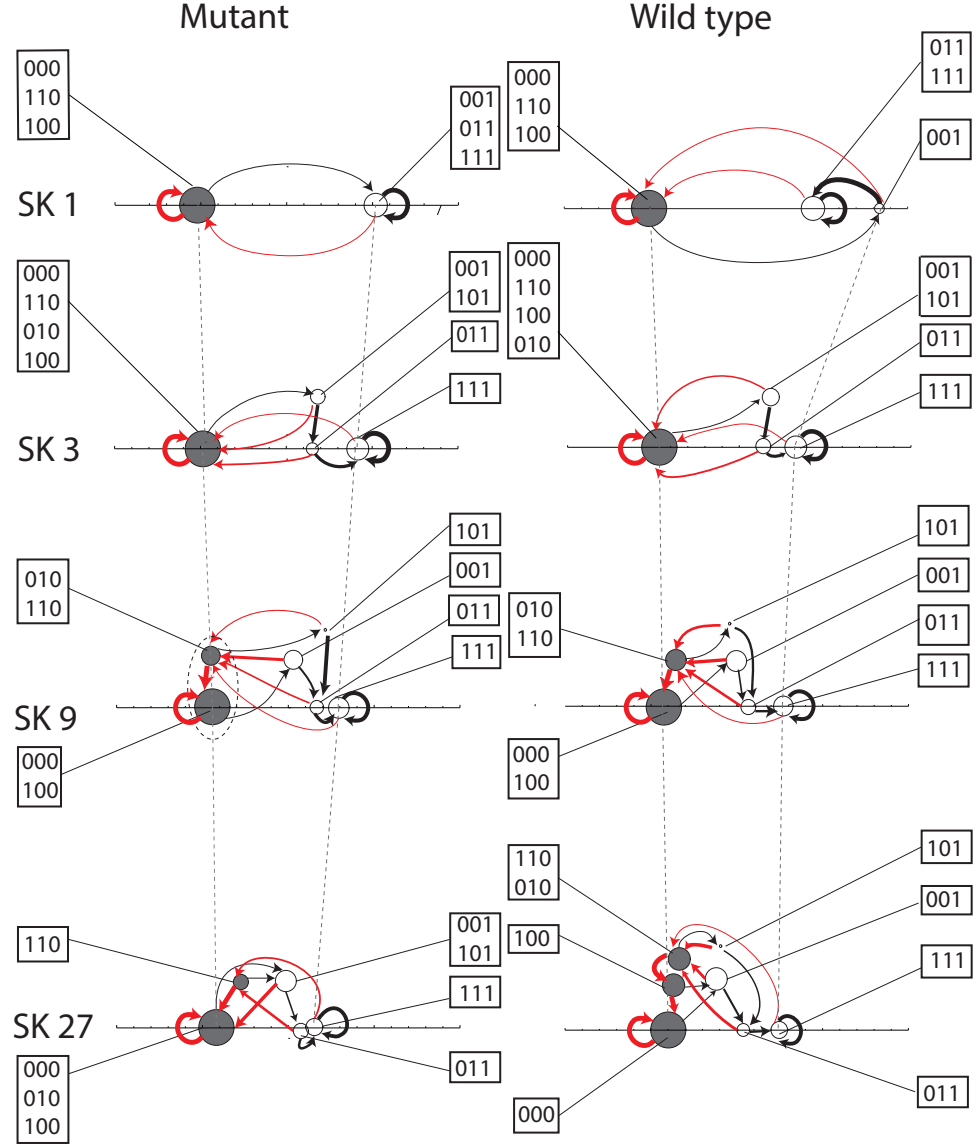


Figure 3.7: The SSNs of the wild type and the Y1068F mutant at 1 nM concentration of Grb2 for different skipping steps. The horizontal axis reflects the mutual proximity of the transition probability distributions associated with the individual states in arbitrary unit (a.u.) (See the text in detail). The choice of vertical axis is arbitrary. Open (gray colored) circles denote the ON (OFF) states. The states enclosed by the dashed curve in SK 9 for mutant emphasize that their transition probabilities are almost identical. The size of the circle is proportional to the logarithm of the residential probability of the state: the bigger the circle is, the longer the system resides in that particular state (for visualization of the states whose area is less than 0.005 a.u.^2 , I introduced the minimum size of 0.005 a.u.^2). The red (black) colored links assign as producing next symbol '0' ('1') (whose destination is either of the OFF (ON) states). The weight of the links reflects the state-to-state transition probabilities.

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Table 3.3: The time intervals for which the autocorrelation is reproduced by each SSN constructed for each different skipping step at three different concentration of Grb2 for the wild type EGFR. Note again that the increment of the time intervals is different with each other dependent on the SK m : 0.033 s, 0.1 s, 0.3 s, and 0.9 s for $m = 1, 3, 9$, and 27, respectively. The unit of time is in second.

[Grb2]	SK 1	SK 3	SK 9	SK 27
1 nM	0.0 ~ 0.133	0.1 ~ 0.3	0.3 ~ 0.9	0.9 ~ 3.6
10 nM	0.0 ~ 0.133	0.1 ~ 0.3	0.3 ~ 0.9	0.9 ~ 2.7
100 nM	0.0 ~ 0.133	0.1 ~ 0.3	0.3 ~ 0.9	0.9 ~ 2.7

Table 3.4: The time intervals for which the autocorrelation is reproduced by each SSN constructed for each different skipping step at three different concentration of Grb2 in the case of the Y1068F mutant EGFR. See also the caption in Table 3.3.

[Grb2]	SK 1	SK 3	SK 9	SK 27
1 nM	0.0 ~ 0.20	0.1 ~ 0.4	0.3 ~ 1.2	0.9 ~ 4.5
10 nM	0.0 ~ 0.167	0.1 ~ 0.4	0.3 ~ 0.9	0.9 ~ 4.5
100 nM	0.0 ~ 0.167	0.1 ~ 0.4	0.3 ~ 0.9	0.9 ~ 4.5

EGFR (See Table 3.3 in Appendix), it was found that solely the SSN constructed at SK 1 captures the autocorrelation function beyond the timescale automatically built in the SSN.

Both at 10 nM and 100 nM, there exists solely a single OFF state at SK 1 and the OFF state splits into three and four at 10 and 100 nM at SK 3, in contrast to the case at 1 nM where the OFF state still persists as a single state (See Figs.5.6 and 5.7 in Appendix). This implies that at higher concentration of Grb2 the next Grb2 molecule encounters the wild type EGFR more frequently compared to the case of 1 nM after a dissociation of a Grb2 molecule bound to the EGFR. In contrast to 1 nM, the number of the ON states reaches at the maximum number four at timescales longer than SK 3.

However, it should be also noted worthy that, from the overall tendency of relative positions of the states at 1 nM concentration of Grb2, the locations of the states (i.e., the center of the circles) tend to merge all together as an increase of the skipping step from 1 to 27 in both the wild type and the Y1068F mutant. That is, the longer the skipping step the closer the states' transition probability distributions become, implying that the state transitions become less sensitive on the past (remind the three-state model in Appendix). Moreover, as for the overall tendency, the network topology is also found to be simpler in the mutant than that in the wild type (i.e., the total number of states for each SSN is equal to or less than that of the wild type at each skipping step and the number of the OFF states does not reach

3.1 An Illustration of our Construction Scheme of Multiscale SSNs for a Three-State Markovian Network

at the maximum of $2^2 = 4$).

I also analyzed the lifetime constants of correlation (Eq. (2.7)) at different skipping steps SK 1, 3, 9, and 27 for the wild type and the Y1068F mutant of EGFR in Appendix (see Table 5.1 and 5.2 in Appendix) for all concentrations of Grb2. As for the overall tendency, as the skipping step increases (with longer timescale), the number of (largely) weighted components of lifetime constants increases more. However, the appearance of lifetime constants with comparable weights is different between the wild type and the Y1068F mutant. For example, at 1 nM concentration there exists only one major component (92-100%) up to SK 27 in the mutant. On the contrary, while only one major component persists to exist up to SK 9 (86-98%), it turns out to be diversified at SK 27 in the wild type. The diversification of the lifetime constants as the skipping step increases looks more apparent in the wild type than in the mutant.

3.1.3 Heterogeneity of Non-Markovian Property Buried in SSNs

The most striking consequence of our method is that our method can capture heterogeneity of memory that depends on the states and, equivalently, on the topological nature of the complex network. Fig. 3.8 presents the corresponding SSNs of Grb2 for the wild type and the Y1068F mutant of EGFR with $L_{\text{past}} = 1, 2, 3, 4$ and 5 for SK 1 at 1 nM concentration (the visualization scheme is the same as in Fig. 3.7). In this thesis, the memory refers to the degree of non-Markovianity of the time series, i.e., memory of the process, if it exists, is manifest in the length of the optimal past sequences L_{past} used in defining the states of SSN.

Let us look into the change pattern of SSNs as an increase of L_{past} . At $L_{\text{past}} = 2$, the state composed of “10” and “00” subsequences is regarded as the OFF state (denoted by gray color) the system currently visits the unbound form “0” (i.e., the rightmost symbol is 0). “10” implies that the system visited the bound form “1” at the previous step and makes a transition to the unbound form, while “00” implies that the system maintains to reside in the unbound form. Likewise, both the state composed of “11” and that composed of “01” are regarded as the ON state (i.e., the rightmost symbol is 1) while they are rather differentiated as distinct states in the wild type EGFR. However, in the Y1068F mutant of EGFR, “11” and “01” are regarded as the same ON state up to $L_{\text{past}} = 3$.

The topographical nature of the SSN with $L_{\text{past}} = 3$ is preserved with the SSN constructed with $L_{\text{past}} = 2$ (the SSN converges approximately in such a short timescale from 0.067 s to 0.1 s). However, as the value of L_{past} gets larger, i.e., 4 and 5, the SSN of the wild type and the mutant EGFR changes gradually in order to capture different kinetics emerging at longer timescales: while the OFF state persists as a single state for a timescale from 0 s to 0.167 s ($=1/30 \text{ s} \times 5$), some ON states split with

3. RESULT AND DISCUSSION

increasing L_{past} while others do not. For example, the ON state (111,011) observed at $L_{\text{past}} = 3$ splits into three distinct states of (1111), (0111), (0011) at $L_{\text{past}} = 4$ but the ON state (001) at $L_{\text{past}} = 3$ does not split with longer L_{past} , corresponding to (0001) and (10001,00001) at $L_{\text{past}} = 4$ and 5, respectively. I found the similar pattern of splitting for 100 nM concentration of Grb2 for the wild type EGFR. This splitting arises from the non-Markovian nature of the process. Hence, scrutiny of the splitting pattern can provide comprehensive understanding of molecular memory in the time domain where the SSNs are constructed. A simple inspection tells us that, whenever the system once visits the unbound form “0” (the latest timings in the subsequences belonging to the individual states are indicated by red in Fig. 3.8), all the path information of how the system reaches at the unbound form are ‘reset’ (i.e., the transition probability distributions become independent on the history once the system arrives at the unbound form “0”). When the EGFR-Grb2 system visits the unbound form, the history, or memory, is approximately reset in the original time series for a length of 0.167 s.

It should be noted, however, that the number of possible subsequences grows very rapidly ($\sim 2^{L_{\text{past}}}$), which make the sampling statistics worse at larger L_{past} . For example, at $L_{\text{past}} = 27$, $2^{27} = 134,217,728$, the length of the binary time series observed experimentally is 18 minutes, recorded every 1/30 s, yielding 32,727 data points. It is apparent that SSN analysis cannot be straightforwardly extended to large values of L_{past} . This is the main reason why I introduce the skipping step algorithm combined with the original SSN scheme. In principle, if I could increase L_{past} large enough, I should end up with a Markovian network (i.e., the state-to-state transition is Markovian) when the timescale of correlation of the process is finite. However the state of SSN may not be the underlying actual conformational state on the $(3n - 6)$ dimensional coordinate space (n is the number of all atoms). It is because 1) conformational dynamics on the $(3n - 6)$ dimensional coordinate space can, in general, associate memory or correlation, and 2) even if the conformational dynamics has no memory effect in high dimension and a Markovian network is yielded, states constructed from the projected one-dimensional time series cannot be reflected in full by all hidden $(3n - 6)$ dimensional coordinate space, but are expected to correspond to some effective conformational states that can be deduced from the projected time series.

3.2 Measure to quantify the possibility of Dwell time distribution

In this thesis, I used the skipping step method to capture the multiscale kinetics of the recognition process between EGFR and Grb2. A drawback of the skipping step method is that it is not straightforward to relate the multiscale kinetics captured by the SSNs directly to the dwell time distribution. However, we can quantify the possibility to replicate the dwell time up to a certain skipping step. I

3.2 Measure to quantify the possibility of Dwell time distribution

evaluate the ratio f between the frequency of a subsequence corresponding to the consecutive dwell for some time in ON level (e.g., 111111 (=111 at SK 3) for the system dwelling at the ON level for seven steps) and the sum of the frequencies of all other possible subsequences observed in the original binary time series within this time duration. For example, for the ON dwell time at SK 3, I define f as $F_{1111111} / \sum_{i,j,k,l \in \{0,1\}} F_{1ij1kl1}$ where F denotes the frequency observed in the original time series and i, j, k, l denotes either of 0 (=OFF) or 1 (=ON). I calculate f associated with the ON dwells for all skipping step at each concentration. It was found at the low concentration (1 nM) of Grb2 for the wild type EGFR that, in the original binary time series (i.e., SK 1 case), this f at SK 3 is exactly unity. That is, there exists no observation in which the binding Grb2 releases within 0.2 s after the Grb2 once binds to the EGFR. Note that, the more the skipping step increases, the more the frequency of the subsequences such as 111 found in a time series resampled per a skipping step m becomes differentiated from that of the subsequences such as $\underbrace{111 \cdots 1}_{3m}$ in the original time series; 111 does not necessarily mean that the EGFR-Grb2 system resides in the bound form *consecutively* for a time period of $3m$. Moreover, f was found to be smaller than unity at 10, and 100 nM, respectively indicating that it is not possible to construct dwell time distribution from SK 3.

In the previous report (3), a single exponential behavior was observed for the association kinetics of the Y1068F mutant for a wide range of timescales longer than 100 s, implying that only a single state is required for the OFF dwell time distribution. As pointed out in Sec. 2.0.4, the skipping step algorithm enables us to deal with long timescale correlation prevented from the sampling problem because of the exponential growth of the number of possible pattern. However, in compensation, the longer the timescale to be analyzed, the more the implication of “dwell” in a skipped time series become obscure, i.e., f deviates more and more from unity. It was found that f associated with the OFF state of the Y1068F mutant is 1.000 at SK3 and 0.994 at SK 9 but 0.962 at SK 27, respectively. That is, up to the skipping step 9, the OFF state corresponds to a state where the system resides continuously (> 99.4%) at the unbound form for the period of the skipped step m multiplied by L_{past} (=0.9 s for SK 9), but a few percentage (3.8%) of the OFF state at SK 27, at least once, go to and return back from the bound form during the period of $m \times L_{\text{past}}$ (=2.7 s). This is the reason why the total number of the OFF states become two as an increase of skipping step from 9 to 27 in the Y1068F mutant.

Finally let us articulate the summary of the results of SSNs combined with SSM in relation to the previous experimental observation (2).

1. It was found in Ref. (2) that the analyses of dwell time distributions (i.e., distributions of the time period for which the system dwells continuously at either 1 or 0) clarified that the ON and

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OFF states must contain multiple states, though the non-Markovian properties of the EGFR-Grb2 recognition kinetics of ON/OFF time series could not be simply described by the multiple states whose number was evaluated from the non-single exponential features of the dwell time distributions. It has been discussed in the experiments (2) that the appearance of multiple states is due to either the conformational fluctuations of EGFR or the different binding sites between the EGFR with the Grb2. In our current SSN scheme combined with the SSM, the extraction of the states is based not on the dwell time distribution but on the pattern buried in the time series, multiple states are naturally detected for the EGFR-Grb2 system, with encoding memory effects.

2. Our formula reproduces their autocorrelation function for a wide range of timescales up to about 3 s, and the topographical structure of the SSNs changes as an increase of the timescale: while the corresponding SSN is rather simple at the short timescale (0.033 to 0.1 s), the SSN at the longer timescales (0.1 s to ~ 3 s) becomes complex for the elucidation of hierarchically organized kinetics appearing at the longer timescale in the wild type and the Y1068F mutant of EGFR. This is interpreted as being captured in some super basin to attain stationary behavior in the short timescale. One possible scenario to make the SSN more complex as an increase of the timescale is that partial interactions between the wild type EGFR and the Grb2 occurring faster than the experimental time resolution (2). Such partial interactions possibly change the conformation of proteins, and conformational memory produced after dissociation can affect the reduction of the on-rates, which leads to the structural change of SSNs.
3. It is found that, when the system once visits the unbound form of EGFR $\cdots$ Grb2, the system approximately loses history or memory. This manifests the existence of heterogeneity of molecular memory, i.e., dependent on paths or states, the degree to what extent the system possesses the memory can be different. The interpretation is that the conformational dynamics of the unbound EGFR relax fast enough before the binding of the next Grb2. On the contrary, the bound states of the EGFR-Grb2 system keep splitting as L_{past} increases, suggesting slower relaxation dynamics for the bound EGFR-Grb2 complex. In the Y1068F mutant, the bound state does not split up to 0.133 s (i.e., $L_{\text{past}} = 3$) in Fig. 3.8, indicating the dynamics of the bound state relax faster than those of the wild type.
4. In the experiments, the Y1068F mutant showed non-exponential features in the dissociation kinetics at all concentration similarly to the wild type (2). However, the association kinetics (= the dwell time distribution at the unbound form) at 1 nM concentration showed that it is approximated by a single exponential kinetics for a wide range of timescales (2, 3). The SSNs for the Y1068F

3.2 Measure to quantify the possibility of Dwell time distribution

mutant is interpreted to reflect such complexity of kinetics: the SSNs for the Y1068F mutant has effectively a single OFF state up to the timescale of ~ 1.2 s at 1 nM (See Fig. 3.7), while at 10 nM the single OFF state found at SK 1 splits into two and more at the larger SK 9 and 27 (See also Fig. 5.6) in Appendix.

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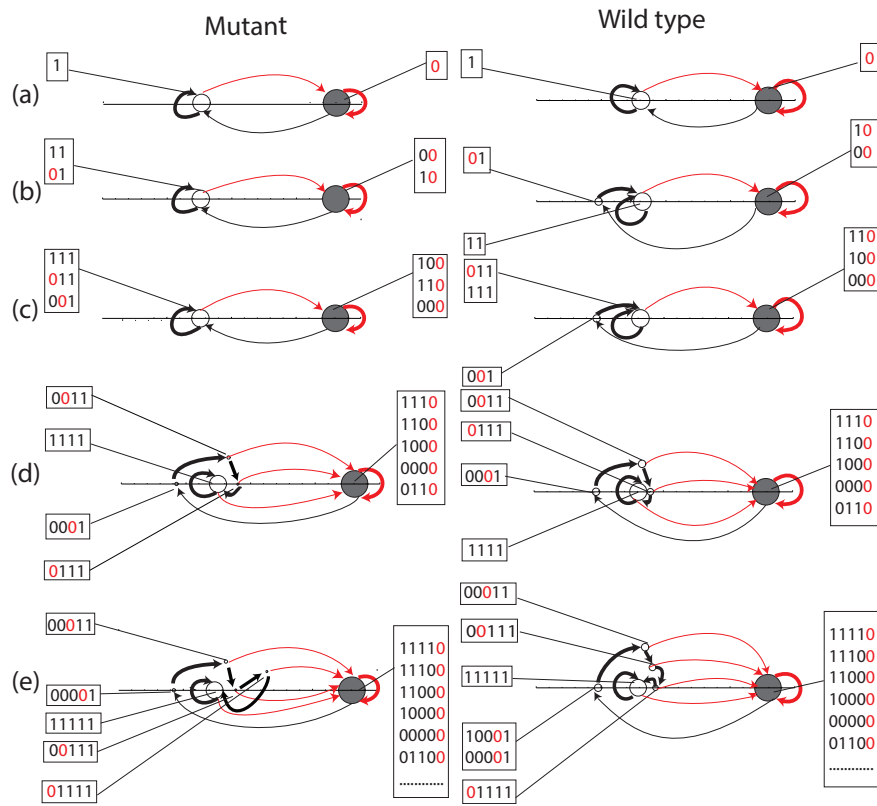


Figure 3.8: The state splitting as increasing L_{past} at 1 nM for the recognition reaction between the wild type and the Y1068F mutant EGFR, and Grb2. (a) $L_{\text{past}}=1$, (b) $L_{\text{past}}=2$, (c) $L_{\text{past}}=3$, (d) $L_{\text{past}}=4$ and (e) $L_{\text{past}}=5$. The meaning of state, links and their colors are the same as in Fig. 3.7.

4

Conclusion

4.1 Conclusion and Perspectives

In this thesis I have presented a novel scheme to extract the multiscale state space network that takes into account multiple nature of the states unseen in measurements and non-Markovianity of the process solely from SM time series. The crux is the combination of a nonlinear time series analysis recently developed on the basis of information theory (1, 39, 40, 52, 54, 67) with the SSM. I also derived the exact formula for the autocorrelation function of the symbolic time series. In this thesis, I demonstrated the potential of my theory by applying to the ON/OFF SM time series of the recognition kinetics between the wild type and the Y1068F mutant of EGFR and Grb2 for an *in vitro* reconstituted system at all concentrations of Grb2 (2, 3). Mathematically there is no difficulty to generalize this theory into non-binary time series having more than two symbols. However, as the number of symbols increases much more than two, the statistical accuracy becomes worse. Improper symbolization may also lose the essential information to be retrieved.

I have also derived the exact formula for the dwell time distribution for binary time series (the extension to non-binary time series is straightforward). However, a drawback of SSM is that it is not straightforward to relate the multiscale kinetics captured by the SSNs directly to the dwell time distribution. So, I have quantified the possibility to replicate the dwell time up to a certain skipping step from the EGF-Grb2 recognition kinetics of ON/OFF time series. It needs more mathematical study to recover this problem. One of the possible solution is to combine all networks for different skipping steps and construct one network.

Appropriate symbolization of time series depends on the experimental setting. In general, the observed time traces are contaminated by several sources of extrinsic and intrinsic noises. It is of crucial

4. CONCLUSION

importance to extract the actual time trace of a physical quantity (e.g., interdy distance) desired for the further analysis from a raw data (e.g., photon arrival times at the donor and acceptor channels) (73). An accurate assignment of ON/OFF levels is very difficult due to the intrinsic and extrinsic noises in SM fluorescence measurements. Also, the distribution of on-level depends on the choice of binning time and threshold level (74). Recently, it was shown that the existence of dynamic disorder of single enzymatic turnover reactions depends on how one assigns the ON/OFF levels and the most widely used binning and thresholding approach may yield a misleading interpretation (61). In addition, the choice of a bin width introduces an artificial time scale to the measurement and raised the possibility of missed transitions due to information lose in each bin (75) and also a hard threshold is vulnerable to detect of false transitions of state to state. Yang group applied a change point analysis method, to analyze the statistics of switching among different levels, which avoids binning the data. Nonetheless, this method involves various explicit and implicit assumptions. So, in my ongoing project, I am investing raw data to identify the change point of time series i.e. assigning “on-off” trajectories based on CUSUM and bootstrap method. These two methods are more flexible in order to deal with low intensity fluctuations at the background (noise) compared with other existing methods. Furthermore, these methods are simpler to handle any kind of data set. Since some subsequences involving one step transitions in the ON/OFF time series were removed from the analyses (2), it is desired to confirm how such removals would affect in the analyses based on above change point detection method.

Recently, it is found that conformation fluctuations are not only the reasons for concentration dependency on rate constant of association process (47) for this EGFR-Grb2 system. To identify the origin that may induce Grb2 dependence on this process, it is better to investigate more facts by using appropriate method, such as flux balance analysis (FBA) (76) by decomposing the transition matrix of SSN.

It should also be noted that the SSN scheme groups a set of past subsequences (into a single state) whose transition probability distributions are regarded as identical within an error tolerance determined by the significance level. The grouping and resultant states depend on this significance level and even if two past subsequences are grouped into a certain state for a specific significance level, it might not be the case for another significance level. Therefore, a SSN constructed for a certain significance level may mislead the precise interpretation concerning the underlying SSN. Therefore, the visualization of the SSN projected onto the metric space that reflects the proximity of transition probability distribution is very crucial to capture the essence of the network structure.

In the literature, a state is often regarded as a conformation or, a set of conformations or, more generally, a set of static conformation composed of an energy basin. Importantly, when the process is non-Markovian, in order to keep such a static concept of states, one needs to introduce the so-called

memory kernel in an *ad hoc* fashion. In the SSN construction, instead of introducing the memory kernel whose physical interpretation is absent, the concept of states become “dynamic”, i.e., the sequence of snapshots of conformation changes. From my standpoint, compared to introducing *ad hoc* memory kernel which is normally fitted to the experimentally observed autocorrelation, the concept of states in SSN is regarded as showing a solid connection to conformations (is not static but dynamic fashion). However, direct connections between the high dimensional protein conformations and states obtained from the SSN analysis may not be established solely based on the information of a one-dimensional time series. This limitation is inherent to most of all measurements, but I expect that a systematic survey of the dependence on several amino acid residue mutations provides more concrete identification of the state in relation to the identity of the role of amino acid residues. This may be regarded as ϕ value analysis of protein folding kinetics to infer the energy landscape in the framework of SM biology.

The nonstationary features and the timescale dependence of the constructed networks are the natural consequence arising from the property of the system in question, whenever states are defined along the time series. One of the alternative data-driven approaches to construct a network is to utilize dwell-time time series, which is the series of the consecutive dwell times at the individual levels such as ON and OFF (46). It is interesting to compare the results of these complimentary approaches as one of the forthcoming subjects.

4. CONCLUSION

5

Appendix

5.0.1 Overview of EGFR and EGFR family

Cell signaling is a part of a complex system of communication, governs basic cellular activities and coordinates cell actions. Cells interact with extracellular stimulus via the membrane bound receptors e.g. receptor tyrosine kinases (RTKs (See Fig. 5.2)). These receptors for most growth factors like epidermal growth factor (EGF) transfer signal to tyrosine-specific protein kinases combined with adaptor protein in cytoplasm. They all follow a critical signaling pathway, which is directed from the cell surface to the nucleus. The binding of a growth factor (EGF) to its tyrosine kinase receptor (i.e EGFR) protein on the plasma membrane results as autophosphorylation and activate the Ras/Raf/MAPK cascade (6, 77). This cascade passes the signal to the nucleus through phosphorylation of transcription factors, leading to DNA synthesis and cell division (78, 79). The responds of this signal transduction are, in form of robust functions in the cell such as thermally fluctuation (i.e., chemical reactions in time and space scales), reordering the environment inside the cell.

A class of RTKs belonging to the family of ErbB plays a pivotal role in cell cycle. ErbB family consists of four receptors namely ErbB1(which known as EGFR), ErbB2 (HER2), ErbB3 (HER3), and ErbB4 (HER4) which are variously activated by signal molecules (4). All four members have in common an extracellular ligand-binding domain, a single hydrophobic transmembrane domain, and a cytoplasmic region, which contains a highly conserved tyrosine kinase domain and C-terminal tail (Fig. 5.1). However, tyrosine kinase of ErbB3 is not active due to the amino acids within the kinase domain (80). The extracellular domains are less conserved among the four (5).

Dimerization and phosphorylation of the epidermal growth factor (EGF) receptor (EGFR) are the initial and essential events of EGF-induced signal transduction. EGFRs can form dimer on the cell surface independent of ligand binding (80). It has been reported that the binding of EGF to an EGFR dimer

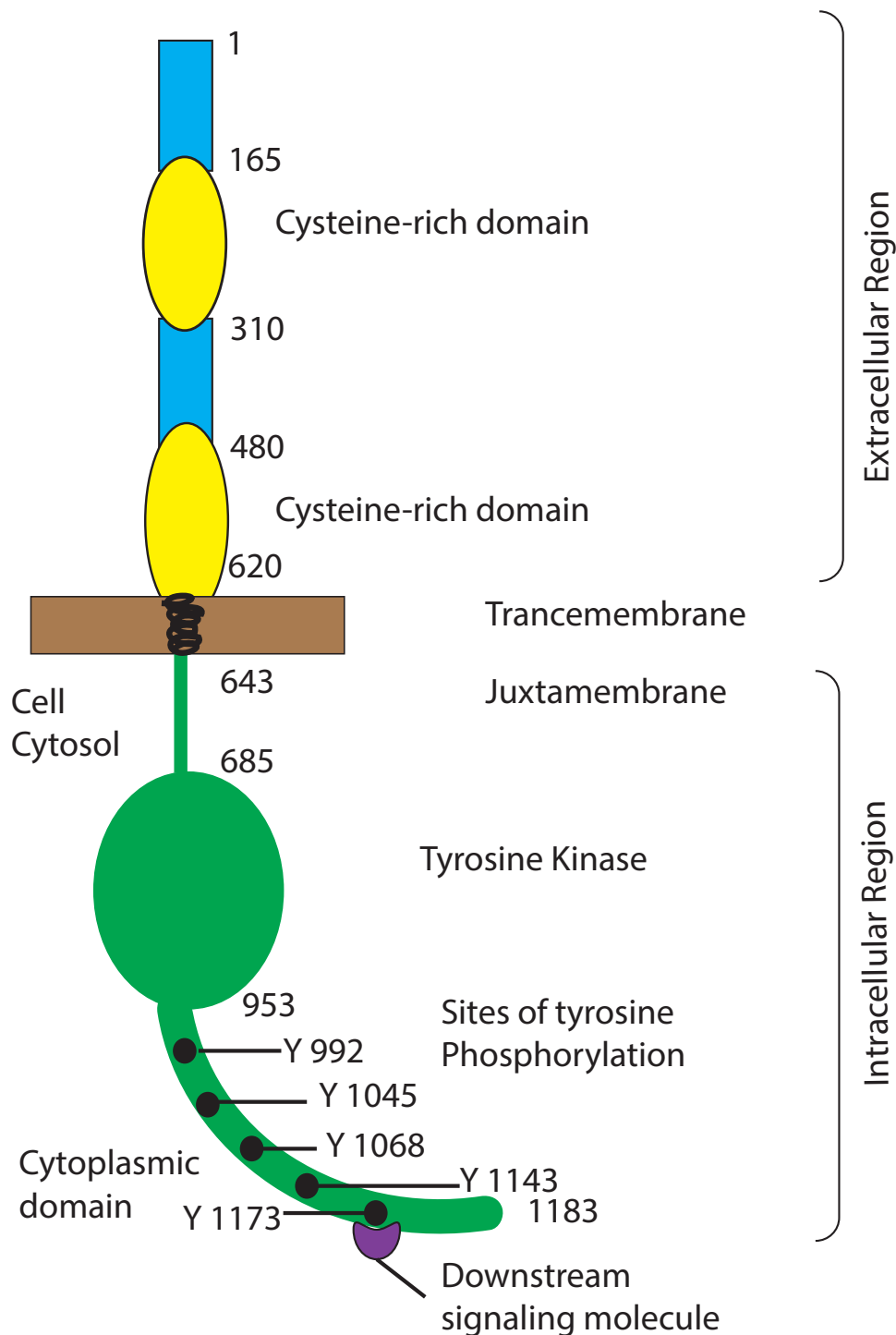


Figure 5.1: Basic Structure of EGFR demonstrating relevant domains. (I) The extracellular region consists of four domains (two of them are rich in cysteine). (II) Transmembrane domains. (III) The intracellular domains: (1) juxtamembrane domain; (2) tyrosine kinase domain; (3) regulatory region domain. The phosphorylation of several substrates by the tyrosine kinase domain of the EGFR receptor is responsible for activating the various signaling cascades that are shown in the tail of the EGFR in the cytosol. This figure was published from Refs. (4, 5).

is stronger than EGF binding of an EGFR monomer (80). Dimerized EGFR induces autophosphorylation of tyrosine residues in the c-terminal of EGFR by its own kinase domain. The resulting phosphorylated tyrosine residues serve as binding sites for molecules containing Src homology 2 domains and initiate intracellular signaling cascades linked to versatile cellular responses, including regulation of gene expression (4). These dimerized complexes are formed before second EGF molecule binds suggesting bivalent binding of EGF. “Twisting” model was proposed for this dimerization at where dimer EGFR performed as twister after activated by EGF (22). The cytoplasmic domain of EGFR contains a long tail of amino acids, and it has been shown that this domain causes a conformational change upon phosphorylation of tyrosine residues, which could affect interactions with cytoplasmic binding proteins.

5.0.2 Grb2

Adaptor proteins, known as secondary messenger of the signal transduction, have a variety of protein-binding modules which link to protein-binding partners together and initiate the larger signaling complexes. There are many types of adaptor proteins in cytoplasm which interact signaling proteins in the cell signal transduction process. MyD88, Grb2 and SHC1 are famous adaptor proteins of human cell. Grb2 is an adaptor protein involved in signal transduction for MAPK/ERK pathway (See Fig. 5.2). It contains one SH2 domain and two SH3 domains. These two SH3 domains direct complex formation with proline-rich regions of other proteins, and SH2 domain binds tyrosine phosphorylated sequences. In this thesis, one important issue is to investigate how growth factor receptors (EGFR) interact with adaptor protein (Grb2) in the cytoplasm and initiate signaling in cells i.e., from the outside of a cell, receptors activate a different set of cellular signaling leading to different outcome. The conformational changes in EGFR as a result the kinetic properties between Grb2 and intact EGFR could be complex and is still not clear (2).

5.1 Persistence of Markovian state with different skipping times

Here we show that if there exists only one unique state for a given symbol at SK 1, then there also exists only one unique state for the same symbol for arbitrary skipping time. Without loss of generality, we provide the proof for the case of SK 2. The generalization to the cases with arbitrary skipping time is straightforward. Mathematically, we show that if we have at SK 1

$$P(s_{i_1}|s_{i_0}^* s_{i_{-1}} s_{i_{-2}} \cdots) = P(s_{i_1}|s_{i_0}^*) = P(s_{i_1}|S_{i_0}^*) \quad (5.1)$$

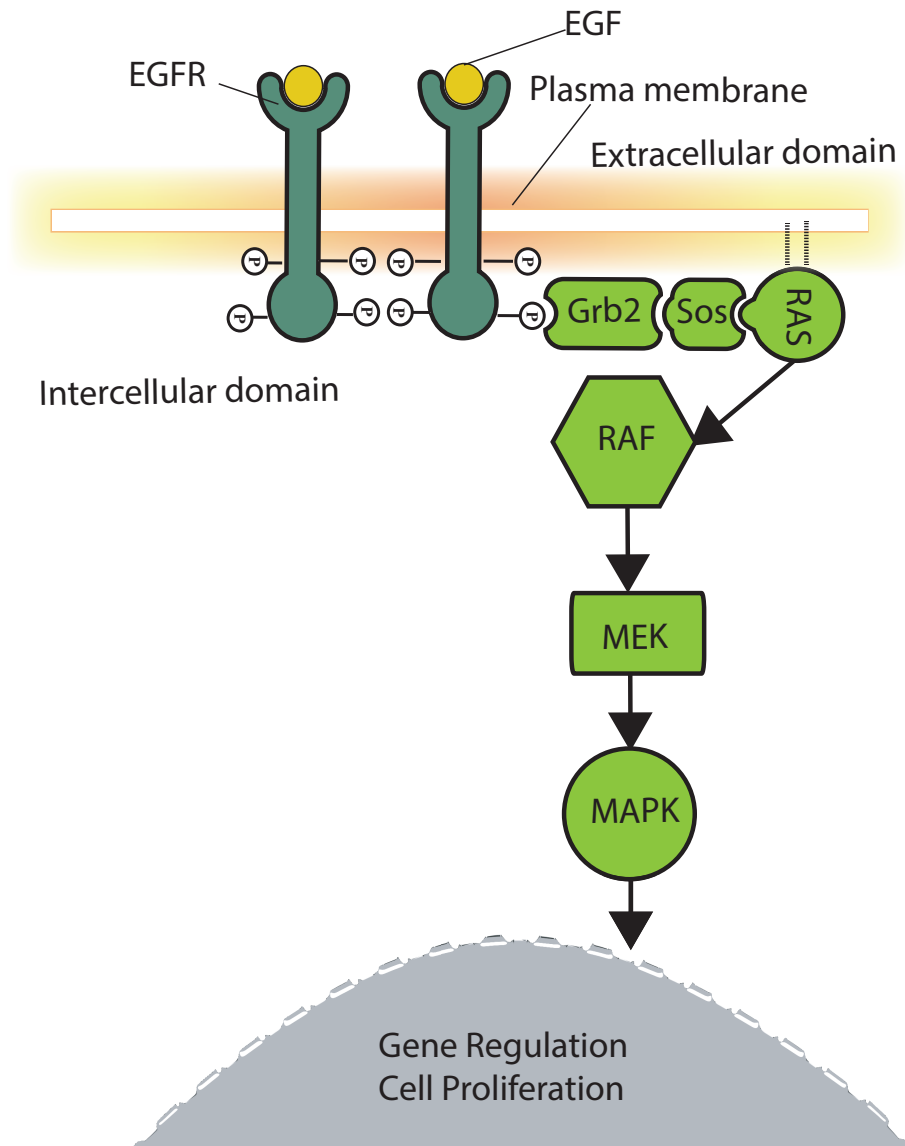


Figure 5.2: Very simple schematic example of intracellular signaling pathway activated EGFR and receptor tyrosine kinases. EGFRs dimerize in response to ligand binding. The ligand response is triggered into tyrosine kinase at which docking protein Grb2, which contains a domain that binds to the phosphotyrosine residues of the activated receptor. Then complex Grb2-SOS promotes the removal of GDP from a member of the Ras subfamily. Ras can then bind GTP and become active. After then activated Ras activates the protein kinase activity of RAF kinase. RAF kinase phosphorylates and switch on MEK (MEK1 and MEK2). MEK phosphorylates and operates a mitogen-activated protein kinase (MAPK) and finally activate nucleus or DNA (6).

5.1 Persistence of Markovian state with different skipping times

where $S_{I_0}^*$ is the only state associated with the given symbol $s_{i_0}^*$, then for any skipping time, e.g. SK 2, we also have

$$P(s_{i_2}|s_{i_0}^* s_{i-2} s_{i-4} \cdots) = P(s_{i_2}|s_{i_0}^*) \quad (5.2)$$

that implies the existence of one unique state containing all the possible subsequences $\cdots s_{i-4} s_{i-2} s_{i_0}^*$ for SK 2. It is noted that Eq. 5.2 and the first equal sign in Eq. 5.1 indicate that once the system visits the symbol $s_{i_0}^*$, the transition probabilities to the future symbol becomes Markovian regardless of the skipping time and therefore “resets” the memory of the system as discussed in the main text.

We first show that if Eq. 5.1 holds, we also have

$$\begin{aligned} P(s_{i_2} s_{i_1} | s_{i_0}^* s_{i-1} s_{i-2} \cdots) &= P(s_{i_2} s_{i_1} | s_{i_0}^*) \\ &= P(s_{i_2} s_{i_1} | S_{I_0}^*). \end{aligned} \quad (5.3)$$

This means that the Markovian property also holds in predicting more than one future symbol. By using the chain rules of the transition probability, we have

$$\begin{aligned} &P(s_{i_2} s_{i_1} | s_{i_0}^* s_{i-1} s_{i-2} \cdots) \\ &= P(s_{i_2} | s_{i_1} s_{i_0}^* s_{i-1} \cdots) P(s_{i_1} | s_{i_0}^* s_{i-1} \cdots) \\ &= P(s_{i_2} | s_{i_1} s_{i_0}^* s_{i-1} \cdots) P(s_{i_1} | s_{i_0}^*), \end{aligned} \quad (5.4)$$

where Eq. 5.1 is used in the last equality. Since both the subsequences $\cdots s_{i-2} s_{i-1} s_{i_0}^*$ and $s_{i_0}^*$ can be represented by the state $S_{I_0}^*$ according to Eq. 5.1, we then have $P(s_{i_2} | s_{i_1} s_{i_0}^* s_{i-1} \cdots) = P(s_{i_2} | s_{i_1} S_{I_0}^*) = P(s_{i_2} | s_{i_1} s_{i_0}^*)$. As a result, Eq. 5.4 becomes

$$\begin{aligned} &P(s_{i_2} s_{i_1} | s_{i_0}^* s_{i-1} s_{i-2} \cdots) \\ &= P(s_{i_2} | s_{i_1} s_{i_0}^* s_{i-1} \cdots) P(s_{i_1} | s_{i_0}^*) \\ &= P(s_{i_2} | s_{i_1} S_{I_0}^*) P(s_{i_1} | s_{i_0}^*) \\ &= P(s_{i_2} | s_{i_1} s_{i_0}^*) P(s_{i_1} | s_{i_0}^*) \\ &= P(s_{i_2} s_{i_1} | s_{i_0}^*). \end{aligned} \quad (5.5)$$

Next by summing over the symbol s_{i_1} in Eq. 5.3, we can easily obtain

$$P(s_{i_2} | s_{i_0}^* s_{i-1} s_{i-2} \cdots) = P(s_{i_2} | s_{i_0}^*) \quad (5.6)$$

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Now we are ready to show the equality in Eq. 5.2

$$\begin{aligned}
& P(s_{i_2} | s_{i_0}^* s_{i-2} s_{i-4} \dots) \\
&= \frac{P(s_{i_2} s_{i_0}^* s_{i-2} s_{i-4} \dots)}{P(s_{i_0}^* s_{i-2} s_{i-4} \dots)} \\
&= \frac{\sum_{s_{i-1} s_{i-3} \dots} P(s_{i_2} s_{i_0}^* s_{i-1} s_{i-2} s_{i-3} \dots)}{P(s_{i_0}^* s_{i-2} s_{i-4} \dots)} \\
&= \frac{\sum_{s_{i-1} s_{i-3} \dots} P(s_{i_2} | s_{i_0}^* s_{i-1} s_{i-2} s_{i-3} \dots) P(s_{i_0}^* s_{i-1} s_{i-2} \dots)}{P(s_{i_0}^* s_{i-2} s_{i-4} \dots)} \\
&= \frac{\sum_{s_{i-1} s_{i-3} \dots} P(s_{i_2} | s_{i_0}^*) P(s_{i_0}^* s_{i-1} s_{i-2} \dots)}{P(s_{i_0}^* s_{i-2} s_{i-4} \dots)} \\
&= P(s_{i_2} | s_{i_0}^*)
\end{aligned} \tag{5.7}$$

where Eq. 5.6 is used in the second last equal sign.

5.1.1 Result of L_{past} and significance Level

In this work, the construction of SSN from time series is performed by an algorithm developed by Klinkner and Shalizi (62). In order to assign the past subsequences of a time series to each state, the algorithm uses the Kolmogorov-Smirnov test (53) to compare the transition probabilities (from the past subsequences to the future value) up to a desired significance level (α). There is only one physical parameter required to be determined in the algorithm, namely, the length of the past subsequence, L_{past} , which should be long enough to capture statistical correlation presented in the time series. In general, one extracts the converged SSNs using the algorithm by checking if the statistical complexity (i.e. the Shannon entropy of residential probability of the states, $-\sum_I P(S_I) \log P(S_I)$) of the SSN converges with respect to L_{past} .

On the other hand, the significance level (α) is the probability that two subsequences are mistakenly assigned to different states even though they should belong to the same state. The choice of a very small value of α tends to assign subsequences to different states only when their transition probabilities to the future values are significantly different and, therefore, results in fewer states. On the other hand, the assignment of subsequences into different states is less strict if a large value of α is used. In our SSN construction, we worked with the range of α values in which the subsequences assignment is insensitive to the change of α .

In Fig. 5.3(a), we show the change of the statistical complexity associated with the time series for the three states model with SK 1. We can see that the converged SSN is given at $L_{\text{past}} = 2$. For time series with long correlation time which requires a large L_{past} to reach the converged SSN, one in general suffers from the sampling problem since the number of past subsequences grows exponentially with

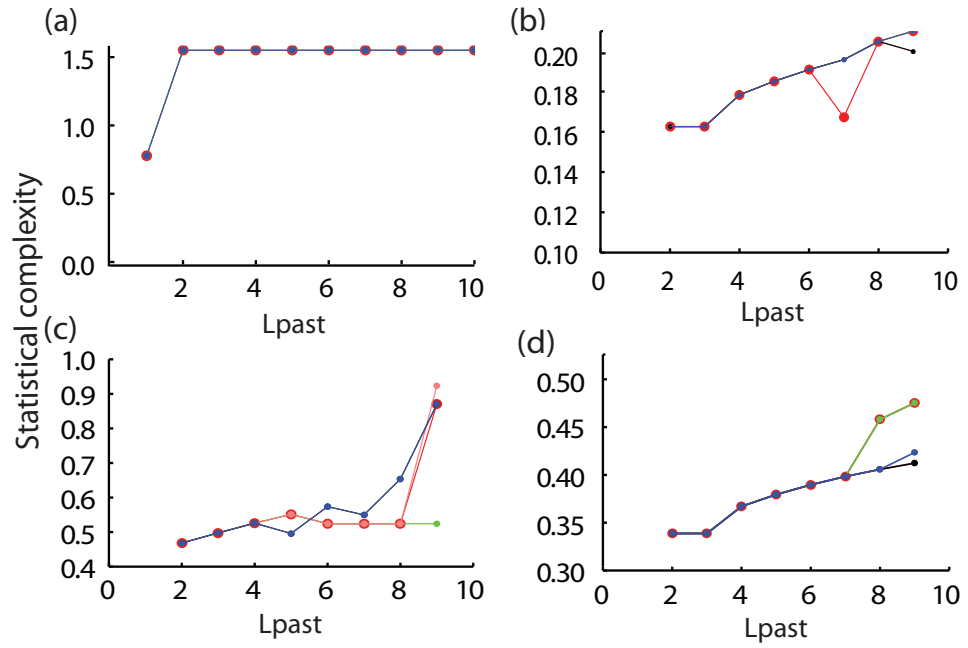


Figure 5.3: The statistical complexity versus L_{past} for different significance levels α in the Kolmogorov-Smirnov test for SK 1, with $\alpha = 0.1, 0.05, 0.01, 0.005$ and 0.001 for both (a) the three states model (Sec. 3.1) and the association and dissociation reaction between the wide type EGFR and Grb2 at (b) 1 nM, (c) 10 nM, and (d) 100 nM. Different colors correspond to different values of α : red 0.1, green 0.05, pink 0.01, black 0.005, and blue 0.001. In (a) $L_{\text{past}} = 2$ results in a converged SSN for the three states model. In the wild type EGFR case, $L_{\text{past}} = 3$ was chosen to yield the approximate (local) convergent network for (b) 1 nM, (c) 10 nM and (d) 100 nM.

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L_{past} . In this case, we resample our time series and apply the skipping step method as discussed in the main text. In the case of the three states model, we construct the converged SSNs for SK 1, SK 3, SK 9 and SK 27 with L_{past} equal to 2, 1, 0 and 0, respectively. In the EGFR case for all concentration, the statistical complexity increases very slightly and gradually (See, e.g., Fig. 5.3(b)-(d)) and it is difficult to conclude any convergent L_{past} . However, in the case of the wild type and the Y1068F mutant of EGFR we found some locally convergent network at L_{past} equal to 2 or 3. Hence, we chose $L_{\text{past}} = 3$ for all SSNs to be analyzed.

5.1.2 Results of autocorrelation of the wild type and the Y1068F mutant at 10 and 100 nM Grb2

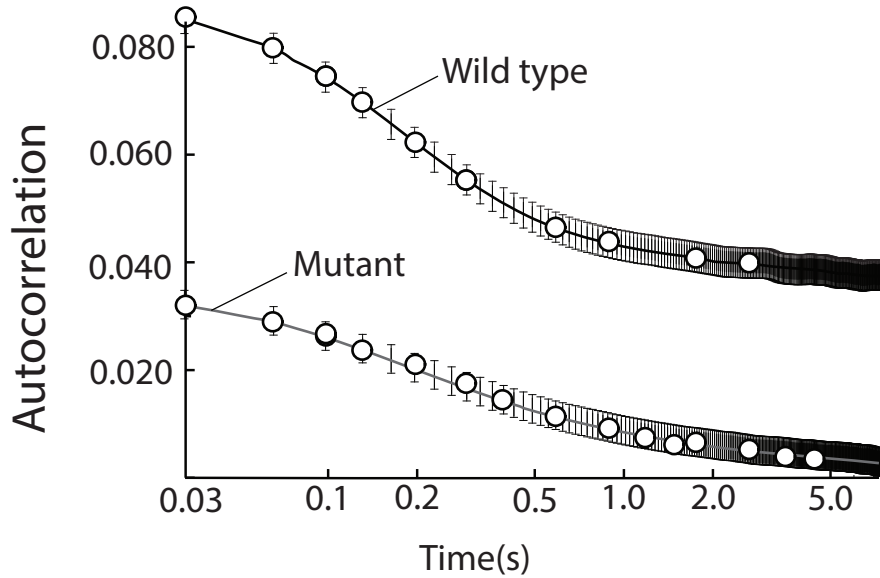


Figure 5.4: Autocorrelation for the ON/OFF time series of the association and dissociation processes between the wild type and the Y1068F mutant at 10 nM concentration of Grb2. See the caption of Fig. 3.6.

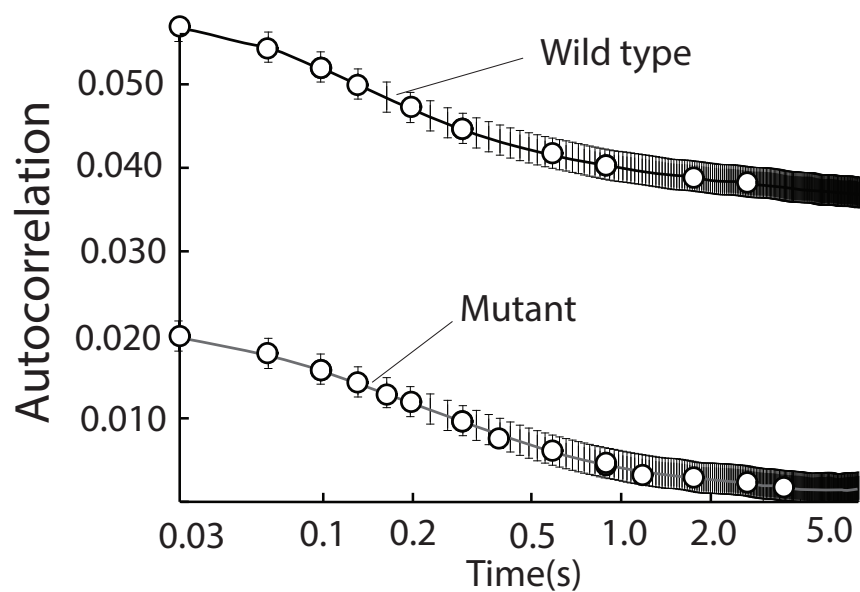


Figure 5.5: Autocorrelation for the ON/OFF time series of the association and dissociation processes between the wild type and the Y1068F mutant at 100 nM concentration of Grb2. See the caption of Fig. 3.6.

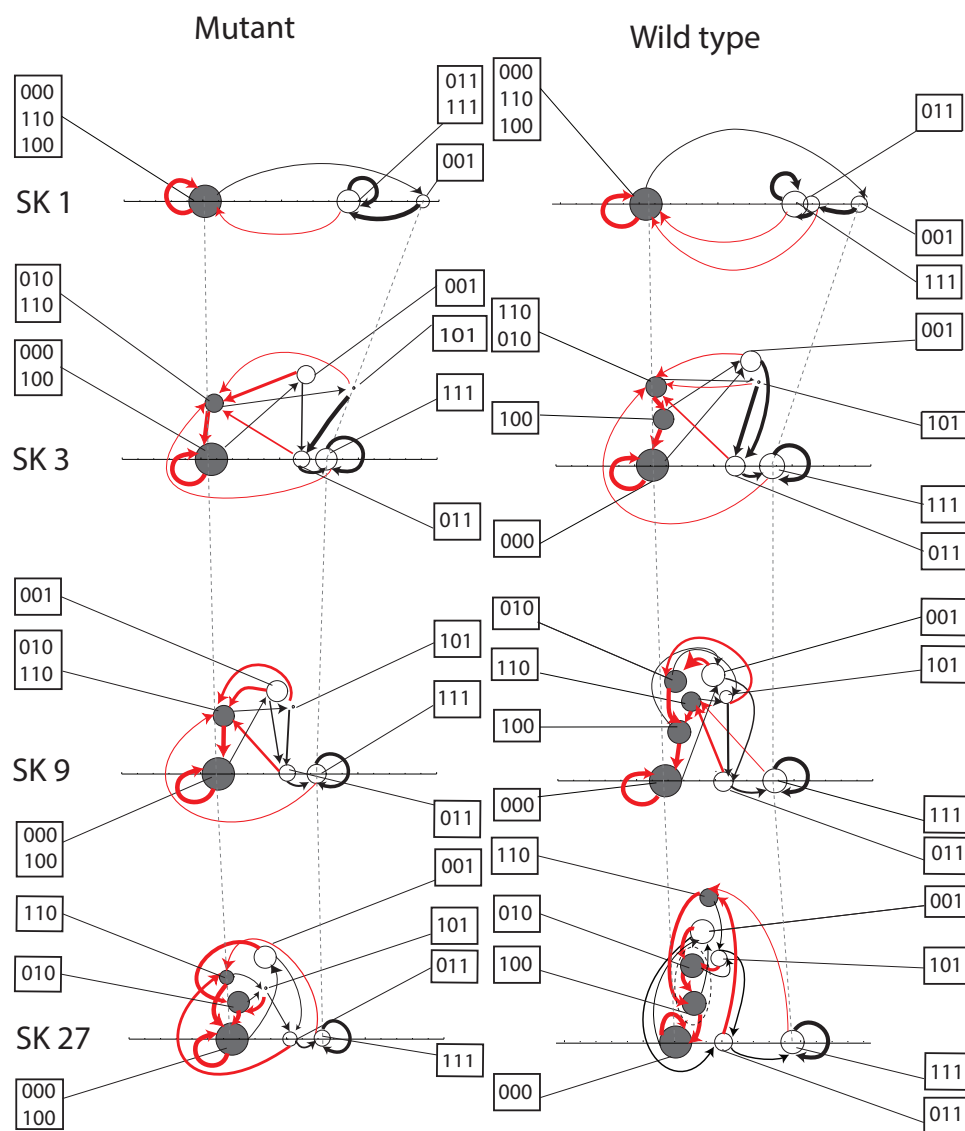


Figure 5.6: The SSNs of the wild type (right) and the Y1068F mutant (left) at 10 nM concentration of Grb2 for different skipping steps (SK 1, 3, 9, and 27 from the top to the bottom). See also the caption of Fig. 5.6 in the main text.

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5.1.3 The Visualization of the underlying SSNs of the wild type and the Y1068F mutant at 10 and 100 nM Grb2 and their lifetime constants

Table 5.1: The lifetime constants of the wild type EGFR at all concentration of Grb2 for each state space network. The lifetime constants are calculated from Eq. (5) (in the main text) and their weights are shown in parentheses.

[Grb2]	SK 1	SK 3	SK 9	SK 27
1 nM	0.0037 (2%)	0.028 (14%)	0.15 (14%)	0.023 (1%)
	0.37 (98%)	0.58 (86%)	1.29 (86%)	0.61 (39%)
				0.69 (25%)
				3.50 (35%)
10 nM	0.007 (8%)	0.06 (1%)	0.14 (0.02%)	0.47 (1%)
	0.43 (92%)	0.07 (14%)	0.18 (1.18%)	0.59 (2%)
		0.69 (85%)	0.28 (26%)	0.92 (33%)
			0.30 (14%)	1.09 (18%)
100 nM	0.004 (1%)	0.088 (0.6%)	0.12 (14%)	0.55 (14%)
	0.70 (99%)	0.055 (9.2%)	0.3 (6%)	0.62 (14%)
		0.086 (4.18%)	5.87 (80%)	1.12 (3%)
		0.21 (0.02%)		1.14 (5%)
		1.65 (86%)		21.0 (64%)

Table 5.2: The lifetime constants of the Y1068F mutant EGFR at all concentration for each state space network (The unit is of second). See also the caption of Table 5.1.

[Grb2]	SK 1	SK 3	SK 9	SK 27
1 nM	0.56 (100%)	0.02 (4%)	0.10 (0.97%)	0.42 (6%)
		0.92 (96%)	0.12 (0.03%)	0.47 (2%)
			1.46 (99%)	2.04 (92%)
10 nM	0.004 (0.99%)	0.04 (15%)	0.140 (8%)	0.41 (35%)
	0.32 (99.01%)	0.05 (2%)	0.145 (5%)	0.42 (35%)
		0.50 (83%)	1.0 (87%)	0.45 (2%)
100 nM	0.004 (1%)	0.03 (6%)	0.27 (13%)	1.30 (8%)
	0.29 (99%)	0.42 (94%)	2.43 (87%)	1.40 (26%)
				7.82 (66%)

References

- [1] C. B. Li, H. Yang and T. Komatsuzaki, *Proc. Natl. Acad. Sci. U.S.A.*, 2008, **105**, 536–541.
- [2] M. Morimatsu, H. Takagi, K. G. Ota, R. Iwamoto, T. Yanagida and Y. Sako, *Proc. Natl. Acad. Sci. U.S.A.*, 2007, **104**, 18013–18018.
- [3] H. Takagi, M. Morimatsu and Y. Sako, *Adv. Chem. Phys.*, 2012, **146**, 195–215.
- [4] A. Oyewale, K. F. Mark and S. Ravi, *Nat. Clin. Pra. Oncol.*, 2007, **4**, 118–129.
- [5] Y. Yarden and Sliwkowski, *Nat. Rev.*, 2001, **2**, 127–137.
- [6] B. Alberts, D. Bray, K. Hopkin, A. Johnson, J. Lewis, M. Raff, K. Roberts and P. Walter, *"Essential Cell Biology"*, NEW YORK AND LONDON: Garland Science, 2004.
- [7] R. Zwanzig, *Nonequilibrium Statistical Mechanics*, Oxford University Press, New York, NY, 2001.
- [8] J. Wang and P. Wolynes, *Phys. Rev. Lett.*, 1995, **74**, 4317–4320.
- [9] S. L. Yang and J. S. Cao, *J. Phys. Chem B*, 2001, **105**, 6536–6549.
- [10] Y. J. Jung, E. Barkai and J. R. Silbey, *J. Chem. Phys.*, 2002, **117**, 10980–10995.
- [11] X. S. Xie, *J. Chem. Phys.*, 2002, **117**, 11024–11032.
- [12] G. S. Harms, G. Orr, M. Montal, B. D. Thrall, S. D. Colson and H. P. Lu, *Biophys. J.*, 2003, **85**, 1826–1838.
- [13] H. Lu, L. Xun and X. Xie, *Science*, 1998, **282**, 1877–1882.
- [14] X. Tan, P. Nalbant, A. Toutchikine, D. Hu, E. Vorpagel, K. Harn and H. Lu, *J. Phys. Chem. B.*, 2004, **108**, 737–744.
- [15] V. Bierbaum and R. Lipowsky, *PLOS ONE*, 2013, **8**, 55366.

REFERENCES

- [16] P. E. Wrigth and H. J. Dyson, *J. Mol. Biol.*, 2001, **293**, 321–331.
- [17] O. A. Van, P. Blainey, D. Crampton, C. Richardson, T. Ellenberger and X. Xie, *Science*, 2003, **301**, 1235–1238.
- [18] L. Edman and R. Rigler, *Proc. Natl. Acad. Sci. U.S.A.*, 2000, **97**, 8266–8271.
- [19] X. Zhuang, H. Kim, M. J. B. Pereira, H. P. Babcock, N. G. Walter and S. Chu, *Science*, 2002, **296**, 1473–1476.
- [20] Y. Arai, A. Iwane, T. Wazawa, H. Yokota, Y. Ishii, T. Kataoka and T. Yanagida, *Biochem. Biophys. Res. Commun.*, 2006, **343**, 809–815.
- [21] X. Michalet, S. Weiss and M. Jaeger, *Chem. Rev.*, 2006, **106**, 1785–1813.
- [22] Y. Teramura, J. Ichinose, H. Takagi, K. Nishida, T. Yanagida and Y. Sako, *EMBO. J.*, 2006, **25**, 4215–4222.
- [23] W. Xu, J. S. Kong and P. Chen, *PhysChemChemPhys.*, 2008, **111**, 2767–2778.
- [24] K. Jacob, Rosenstein, R. Siddharth, R. Jared and L. S. Kenneth, *Nano. Lett.*, 2013, **13**, 2682–2686.
- [25] B. Hille, *Sinaure Associates: Sunderland, MA*, 2001, **13**, 2682–2686.
- [26] Y. Jai, D. S. Talaga, W. L. Lau, H. S. M. Lu, W. F. DeGrado and R. M. Hochtrasser, *Chem. Phys.*, 1999, **247**, 69–83.
- [27] D. S. Talaga, W. L. Lau, H. Roder, J. Y. Tang, Y. W. Jia, W. F. DeGrado and R. M. Hochstrasser, *Proc. Natl. Acad. Sci. U.S.A.*, 2000, **97**, 13021–13026.
- [28] D. S. . Talaga, Y. Jia, M. A. Bopp, A. Sytnik, W. A. DeGrado, R. J. Cogdell and R. M. Hochstrasser, *Springer Series in Chemical Physics*, 2001, **67**, 313–325.
- [29] E. Mei, J. Tang, J. M. Vanderkooi and R. M. Hochstrasser, *J. Am. Chem. Soc.*, 2003, **125**, 2730–2735.
- [30] B. Schuler, *ChemPhyChem.*, 2005, **6**, 1206–1220.
- [31] X. S. Xie and J. K. Trautman, *Annu. Rev. Phys. Chem.*, 1998, **49**, 441–480.
- [32] T. Ha, A. Y. Ting, J. Liang, W. B. Caldwell, A. A. Deniz, D. S. Chemla, P. G. Schultz and S. Weiss, *Proc. Natl. Acad. Sci. U.S.A.*, 1999, **96**, year.

-
- [33] A. S. JR, *J. App. Econometr.*, 1993, **8**, 63–84.
- [34] S. Kondo and T. Miura, *Science*, 2010, **329**, 1616.
- [35] M. Andrec, R. M. Levy and D. S. Talaga, *J. Phys. Chem. A.*, 2003, **107**, 7454–7464.
- [36] T. C. Messina, H. Kim, J. T. Giurleo and D. S. Talaga, *J. Phys. Chem. B.*, 2006, **110**, 16366–16376.
- [37] S. A. McKinney, C. Joo and T. Ha, *Biophys. J.*, 2006, **91**, 1941–1951.
- [38] L. R. Rabiner, *Proc. IEEE*, 1989, **77**, 257–289.
- [39] C. B. Li, H. Yang and T. Komatsuzaki, *J. Phys. Chem. B.*, 2009, **113**, 14,732–14,741.
- [40] C. B. Li and T. Komatsuzaki, *Extracting the Uderlying Unique Reaction Scheme from a Single-Molecule Time Series*, Springer Science, 2011.
- [41] I. V. Gopich and A. Szabo, *J. Chem. Phys.*, 2006, **124**, 154712.
- [42] K. A. Merchant, R. B. Best, J. M. Louis, I. V. Gopich and W. A. Eaton, *Proc. Natl. Acad. Sci. U.S.A.*, 2007, **104**, 1528.
- [43] I. V. Gopich and A. Szabo, *J. Phys. Chem. B*, 2005, **109**, 17683.
- [44] A. Baba and T. Komatsuzaki, *Proc. Natl. Acad. Sci. U.S.A.*, 2007, **104**, 19297–19302.
- [45] O. Flomenbom and R. J. Silbey, *Phys.Rev.E*, 2007, **76**,.
- [46] C. B. Li and T. Komatsuzaki, *Phys. Rev. Lett.*, 2013, **111**, 058301–5.
- [47] J. Yang and E. P. John, *J. Chem. Phys.*, 2012, **136**, 244506.
- [48] P. Kienker, *Proc. R. Soc.*, 1989, **B 236**, 269.
- [49] H. Wang and H. Qian, *J. Math. Phys.*, 2007, **48**, 013303.
- [50] D. Fey, R. Findeisen and E. Bullinger, *In: Proceedings of the 17th IFAC World Congres. International Federation of Automatic Control, Seoul, Korea*, 2008, 313–318.
- [51] R. Prado and M. West, *Time Series: Modeling, Computation, and Inference*, Chapman Hall, CRC Press Taylor Francis Group, 2010.
- [52] J. P. Crutchfield, *Nature Phys.*, 2012, **8**, 17–24.

REFERENCES

- [53] C. R. Shalizi and J. P. Crutchfield, *J. Stat. Phys.*, 2001, **104**, 819–881.
- [54] J. P. Crutchfield and K. Young, *Phys. Rev. Lett.*, 1989, **63**, 105.
- [55] H. Yang, G. Luo, P. Karnchanaphanurach, T. M. Louie, I. Rech, S. Cova, L. Xun and X. S. Xie, *Science*, 2003, **302**, 262–266.
- [56] Y. Chook, G. GD., C. Kay, E. Pai and T. Pawson, *J. Biol. Chem.*, 1996, **271**, 30472–30478.
- [57] M. Lemmon, J. Ladbury, V. MAndiyan, M. Zhou and J. Schlessinger, *J. Biol. Chem.*, 1994, **269**, 31653–31658.
- [58] D. Cussac, M. Frech and C. P, *EMBO. J.*, 1994, **13**, 4011–4021.
- [59] T. Sultana, H. Takagi, M. Morimatsu, H. Teramoto, C. B. Li, Y. Sako and T. Komatsuzaki, *J. Chem. Phys.*, 2013, **139**,.
- [60] L. P. Watkins and H. Yang, *Biophys. J.*, 2004, **86**, 4015.
- [61] T. Terentyeva, H. Engelkamp, A. Rowan, T. Komatsuzaki, J. Hofkens, C. B. Li, K. Blank and L. P. Watkins, *ACS Nano*, 2012, **6**, 346–354.
- [62] C. R. Shalizi, <http://www.cscs.umich.edu/~crshalizi/CSSR/>, 2003.
- [63] P. F. Dunn, *"Measurement and Data Analysis for Engineering and Science"*, New York: McGrawHill, 2005.
- [64] S. E. Kelly, *Applied and Computational Harmonic Analysis*, 1996, **3**, 72–81.
- [65] D. I. A. Henry, *Analysis of Observed Chaotic Data*, Springer, New York, USA., 1996.
- [66] S. Teukolsky, W. Vetterling and B. Flannery, *Numerical Recipes in Fortran 90*, Cambridge University Press, England, 1996.
- [67] C. R. Shalizi, K. L. Klinkner and J. P. Crutchfield, *Technical Report, Santa Fe Institute*, <http://arxiv.org/abs/cs.LG/0210025>, 2002.
- [68] J. Downward, P. Parker and M. D. Waterfield, *Nature*, 1984, **311**, 483–485.
- [69] R. Iwamoto, K. Hanada and E. Mekada, *J. Bio. Chem.*, 1999, **274**, 25906–25912.
- [70] T. F. Cox and M. A. A. Cox, *Multidimensional Scaling*, Chapman Hall, London, UK, 2001.

- [71] W. J. Krzanowski, *J. App. Stat.*, 2003, **30**, 743–750.
- [72] Y. Matsunaga, K. S. Kostov and T. Komatsuzaki, *J. Phys. Chem. A.*, 2002, **106**, 10898–10907.
- [73] L. P. Watkins, H. Chang and H. Yang, *J. Phys. Chem. A.*, 2006, **110**, 5191–5203.
- [74] H. C. Catherine, S. Orion, X. Wu, R. Purcell, C. Q. M. Drndic and M. Pelton, *Nano Lett.*, 2010, **10**, 1692–1698.
- [75] L. P. Watkins and H. Yang, *J. Phys. Chem. B.*, 2005, **109**, 617–628.
- [76] K. Raman and N. Chandra, *Brief. Bioinform*, 2009, **4**, 435–449.
- [77] M. H. Cobb, *Prog. Biophys. Mol. Biol.*, 1999, **71**, 479–500.
- [78] J. Plumpe, *Am. J. Physiol. Gastrointest. Liver Physiol.*, 2000, **278**, 173–183.
- [79] F. X. Pimentel-Muinos and B. Seed, *Immunity*, 1999, **11**, 783–793.
- [80] A. Wells, *International Journal of Biochemistry Cell Biology*, 1999, **31**, 637–643.
- [iv](#), [2](#), [3](#), [9](#), [19](#), [31](#), [41](#)