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Galactic Centre hypershell model for the North Polar Spurs

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ABSTRACT

The bipolar-hypershell (BHS) model for the North Polar Spurs (NPS-E, -W, and Loop I) and counter southern spurs (SPS-E and -W) is revisited based on numerical hydrodynamical simulations. Propagations of shock waves produced by energetic explosive events in the Galactic Centre are examined. Distributions of soft X-ray brightness on the sky at 0.25, 0.7, and 1.5 keV in the $\pm 50^\circ \times \pm 50^\circ$ region around the Galactic Centre are modelled by thermal emission from high-temperature plasma in the shock-compressed shell considering shadowing by the interstellar H I and H₂ gases. The result is compared with the *ROSAT* wide field X-ray images in R2, 4, and 6 bands. The NPS and southern spurs are well reproduced by the simulation as shadowed dumbbell-shaped shock waves. We discuss the origin and energetics of the event in relation to the starburst and/or active galactic nucleus activities in the Galactic Centre.

Key words: ISM: individual objects: (North Polar Spur)–ISM: jets and outflows–galaxy: nucleus–galaxies: individual: objects (the Galaxy)–X-rays: diffuse background.

1 INTRODUCTION

Nuclear activities in spiral galaxies are evidenced by a variety of ejection phenomena such as jets, rings, lobes, winds, and shells of different morphologies and scales from sub-parsecs to several tens of kpc, which include those in the Milky Way (e.g. Oort 1977; Sofue 2000). The discovery of the *Fermi* Bubble (Su, Slatyer & Finkbeiner 2010) has stimulated further discussions of the outflow activity in the Galactic Centre (GC). The origin and physical properties have been investigated in relation to the associated X-ray features including the North Polar Spur (NPS; Totani 2006; Carretti et al. 2013; Fujita, Ohira & Yamazaki 2013; Kataoka et al. 2013, 2015; Ackermann et al. 2014; Fang & Jiang 2014; Mou et al. 2014; Crocker et al. 2015; Inoue et al. 2015; Sarkar, Nath & Sharma 2015; Tahara et al. 2015).

The largest scale GC phenomenon so far reported in the Milky Way is the bipolar hypershells (BHSs) with an extent of several kpc and total energy of the order of $10^{55} \sim 10^{56}$ erg (Sofue 1977, 1984, 1994, 2000; Bland-Hawthorn & Cohen 2003), which is observed as the NPS and its counter spurs extending over $\sim 120^\circ$ on the

sky in radio continuum (Haslam et al. 1982) and X-ray emissions (Snowden et al. 1997).

In our BHS model (Sofue 2000), the giant spurs were interpreted as due to a dumbbell-shaped shock front induced by an explosive event at the GC $t \sim 15$ Myr ago with total energy of $\mathcal{E} \sim 10^{55}$ erg. In this paper, we revisit the BHS model by performing a numerical hydrodynamic simulation of a shock wave driven by high-rate energy injection into the GC. We simulate soft X-ray distributions and compare them with the *ROSAT* all-sky maps taking account of shadowing by the interstellar matter.

As to the energy source and its transfer to the kinetic energy of expansion of BHS, we consider the following cases and their combination.

(i) Starburst (SB) model: energy is released by multiple type II supernovae by nuclear starbursts and is accumulated as kinetic energy to drive a round shock wave or a wide-angle outflow (Sofue 2000). The SB requires fuelling of star-forming gas to the central region.

(ii) Active galactic nucleus (AGN) model: energy is released at the black hole in the nucleus and transformed to kinetic energy of the surrounding gas to drive a round shock wave or an outflow (Totani 2006; Mou et al. 2014).

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We also categorize the event according to the duration of energy injection.

(i) C (continuous injection) type: energy is continuously released and injected to the GC. It may occur intermittently by recurrent events.

(ii) E (point explosion) type: energy is released as a single point-like explosive event with a short time-scale in the nucleus. If the duration of energy supply in the above C type is sufficiently shorter than the whole event life, it may be regarded as E type.

There may be various hybrid combinations of these models and types. In this paper for the BHS, we consider the SB model of C type. This scenario is almost identical to a C type AGN model except for the required gas inflow in SB model.

2 HYDRODYNAMICAL SIMULATION OF BHSs

We have performed a numerical hydrodynamical simulation of the BHS by computing the propagation of a shock wave produced by an energy release at the GC, implicitly considering the SB model with the C type energy injection.

2.1 Hydrodynamical equations and simulation code

We used a hydrodynamical code of the flux-splitting method with second-order accuracy both in space and time (van Albada, van Leer & Roberts 1982; Mair et al. 1988; Nozawa, Kozasa & Habe 2006). This algorithm is an upwind scheme for the Euler equations and is well suited to solving problems involving a shock. The radiative cooling of gas ($T \geq 10^4$ K) is included, assuming the cooling function with the solar abundance (Fig. 1).

We assume that gas flow is axisymmetric around the rotation axis of the Galaxy for simplicity. We solve hydrodynamic equations in the cylindrical coordinate (r, z), assuming that the unperturbed gas in the disc and halo are rotation-supported but the rotation is not important for evolution of BHSs.

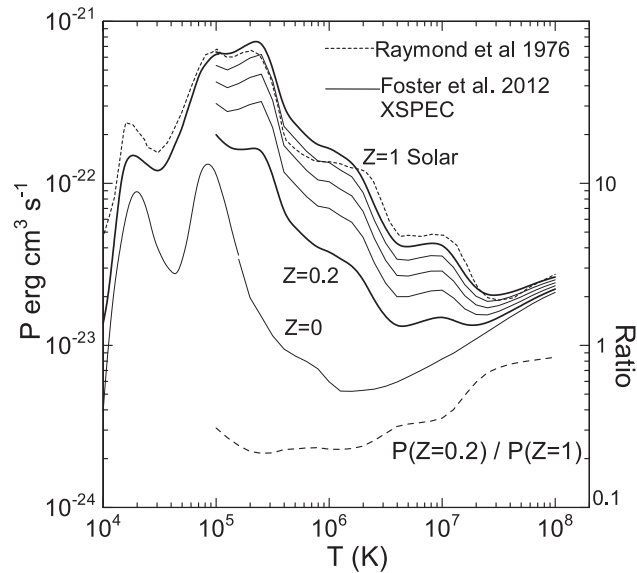


Figure 1. Cooling functions $P(T)$ from Raymond et al. (1976, thin dash) and Foster et al. (2012) generated by XSPEC (Arnaud 1976) for $Z = 0$ to 1.0. The ratio of the cooling rates for $Z = 0.2$ to 1.0 is shown by the thick dashed line. The solar abundance ($Z = 1$) is taken from Anders & Grevesse (1989).

The hydrodynamic equations of gas are given by

$$\frac{\partial \rho}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho v_r) + \frac{\partial}{\partial z} (\rho v_z) = \dot{\rho}, \quad (1)$$

$$\frac{\partial}{\partial t} (\rho v_r) + \frac{1}{r} \frac{\partial}{\partial r} (r \rho v_r^2) + \frac{\partial}{\partial z} (\rho v_r v_z) = -\frac{\partial p}{\partial r} - \rho \frac{\partial \Phi}{\partial r}, \quad (2)$$

$$\frac{\partial}{\partial t} (\rho v_z) + \frac{1}{r} \frac{\partial}{\partial r} (r \rho v_r v_z) + \frac{\partial}{\partial z} (\rho v_z^2) = -\frac{\partial p}{\partial z} - \rho \frac{\partial \Phi}{\partial z}, \quad (3)$$

$$\begin{aligned} \frac{\partial}{\partial t} \left(\rho \left(\epsilon + \frac{1}{2} v^2 \right) \right) + \frac{1}{r} \frac{\partial}{\partial r} \left(r \left(\frac{\gamma}{\gamma-1} p + \frac{1}{2} \rho v^2 \right) v_r \right) \\ + \frac{\partial}{\partial z} \left(\left(\frac{\gamma}{\gamma-1} p + \frac{1}{2} \rho v^2 \right) v_z \right) \\ = \dot{\mathcal{E}} - n^2 P(T) - \rho \left(v_r \frac{\partial \Phi}{\partial r} + v_z \frac{\partial \Phi}{\partial z} \right). \end{aligned} \quad (4)$$

Here, ρ is the gas density, v_r and v_z are r and z components of the velocity with $v = \sqrt{v_r^2 + v_z^2}$, $P(T)$ is the cooling function, Φ is the gravitational potential of the Galaxy, $\gamma = 5/3$ is the adiabatic constant for ideal gas, $\epsilon = p/[(\gamma - 1)\rho]$ is the specific internal energy, $\dot{\rho}$ is the mass injection rate per unit volume, and $\dot{\mathcal{E}}$ is the energy injection rate per unit volume. The viscosity, thermal conductivity, and the self-gravity of the gas are neglected. The cooling function $P(T)$ was taken from Raymond, Cox & Smith (1976) for solar abundance as shown in Fig. 1. Note that the cooling function is almost identical to that by Foster et al. (2012) in the temperature range under consideration.

2.2 Circumstantial and initial conditions

The gravitational potential Φ is assumed to be given by the Miyamoto & Nagai (1975) model,

$$\Phi(r, z) = -\frac{GM}{\sqrt{r^2 + (a + \sqrt{z^2 + b^2})^2}}, \quad (5)$$

where G is the gravitational constant, $M = 10^{11} M_\odot$, $a = 20$ kpc, and $b = 1$ kpc.

The initial gas density was assumed to have the distribution represented by

$$\rho(r, z) = \rho_1 \exp(-(z/z_1)^2) + \rho_2 \exp(-(z/z_2)^2) + \rho_3. \quad (6)$$

Here, ρ is the density, z is the height from the galactic plane, z_i is the scale thickness of the disc and halo, and r is the distance from the rotation axis. Suffices 1, 2, and 3 denote quantities representing the disc, halo and intergalactic gas, respectively, with $\rho_1 = 3 \times 10^{-24} \text{ g cm}^{-3}$, $\rho_2 = 3 \times 10^{-26} \text{ g cm}^{-3}$, and z_1 and z_2 are 0.1 and 1 kpc. The last term represents the intergalactic gas of density of the order of $10^{-29} \text{ g cm}^{-3}$. The initial temperatures in the disc and halo gases were taken to be 10^4 and 2×10^6 K, respectively. The thus settled gas distribution is in between the plane-parallel (Yao et al. 2009; Sakai et al. 2014) and spherical (Miller & Bregmann 2013) models for the hot halo gas distribution as inferred from X-ray observations.

The numerical simulations were performed for the two cases, one for E-type injection with a point-like explosion at the nucleus, and the other for C type with continuous energy injection into the GC. In both cases, total energy of $\mathcal{E} = 4 \times 10^{56} \text{ erg}$ was given as thermal

energy into a sphere of 50 pc radius. In the C-type injection, the energy was supplied to the volume continuously at a rate of $d\mathcal{E}/dt = 4.0 \times 10^{55}$ erg Myr⁻¹, and total energy of $\mathcal{E} = 4 \times 10^{56}$ erg in 10 Myr, where we also assumed mass supply at a rate of $dM/dt = 1 M_{\odot}\text{yr}^{-1}$.

The initial gas was left free in the gravitational potential with the distribution mimicking multiple-layered discs composed of a low-temperature disc and high-temperature halo by equation (6). The gas is at rest initially in the potential, but moves slowly towards hydrostatic distribution. Since the motion is slow, the ambient gas appears almost motionless in contrast to the rapid shock wave propagation. The gravitational and hydrodynamical accelerations are included in the equation of motion.

2.3 Metallicity and cooling

In the present simulation, the solar abundance was assumed not only because the code was written for a fixed solar abundance, but also because the metallicity in the GC and halo is not well modelled. The gas in the BHS is a mixture of different components with different abundances from extremely high to primordially low. Namely, the BHS includes the ejected/snowplowed gas from the galactic disc and the GC with high star formation rate and therefore high metallicity, $>Z_{\odot}$ (Najarro et al. 2009; Uchiyama et al. 2013), and the halo gas for which some authors prefer high metallicity of $Z = Z_{\odot}$ (Sakai et al. 2014) but the others prefer lower value at $Z = 0.2Z_{\odot}$ (Miller & Bregman 2013; Kataoka et al. 2015). Also, intergalactic gas supposed to have lower metallicity may be included.

Therefore, we here assume solar abundance $Z = 1Z_{\odot}$ as an average during the whole life of the BHS evolution. The metallicity influences the simulation through cooling rate. However, it is shown in Section 4, that the cooling does not affect the BHS dynamics and evolution significantly. Note also that we adopted the observed metallicity, $Z = 0.2Z_{\odot}$, when calculating the ‘present’ brightness of the NPS for comparison with the observations.

2.4 Results for C- (BS) versus E- (AGN) type energy injections

The calculated result for C- (continuous; BS like) type injection is shown in Figs 2–4. The shock front expands spherically in the initial ~ 1 Myr, and then, it is elongated into the halo, composing dumbbell-shaped symmetric bubbles with respect to the galactic disc, which we call the BHS. Detailed description of the structure and evolution is given in the next subsection.

In this paper, we describe the result of C type in detail, which was found to fit the NPS morphology better than the E-type result. However, we do not intend to deny the E-type event, which might be simpler to explain the shell phenomena without worrying about multiple, complicated phenomena recurrently occurring in the GC.

For comparison, we show the result for E (point explosion; AGN like)-type injection in Fig. 5 for $t = 3$ Myr. The global structure and evolution of the produced shock wave shell is similar to that for C type. However, the general shock wave structure is much simpler. The highest density appears at lower latitudes, whereas the highest temperature was attained in the polar region in the front shock facing the halo gas. The central region has much smoother structure compared to that for C type, having a simple cavity of low density and low temperature. Since no wind blows, no bow shock or a cone structure is produced near the disc.

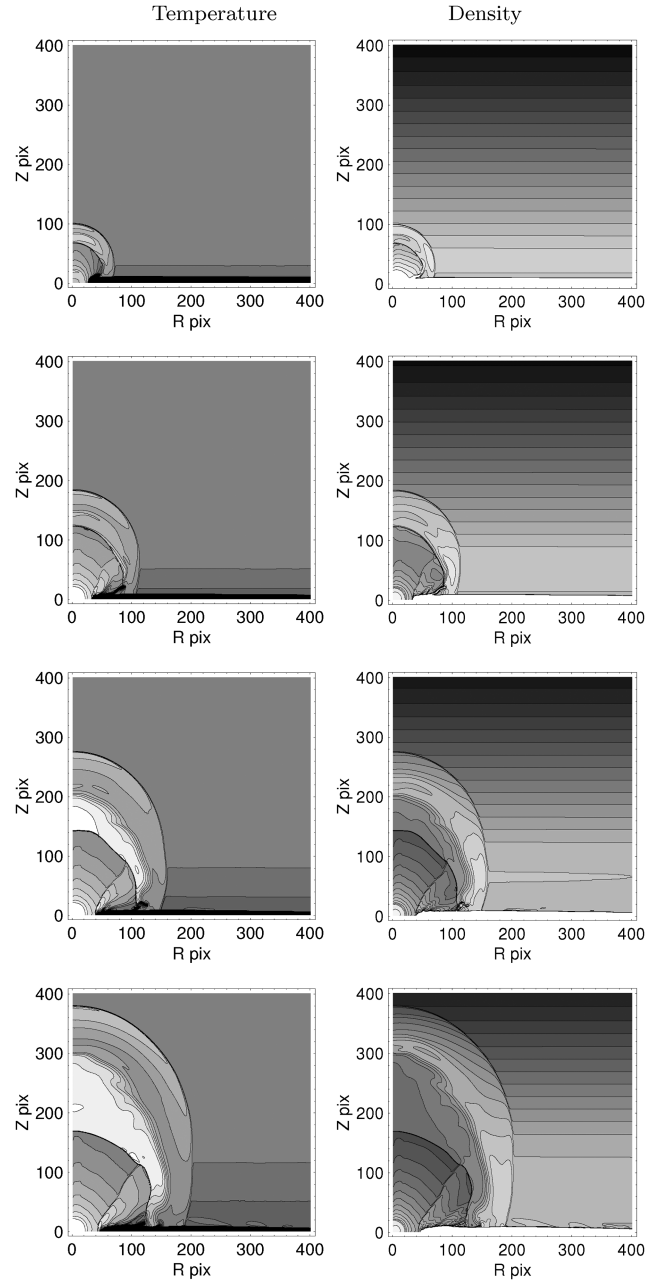


Figure 2. Hydrodynamical simulation of type C (continuous) injection model for density and temperature distributions from $t = 2$ to 7 Myr. Density contours are drawn at $\log \rho$ (H cm^{-3}) = -4 (black) to -1 (white) at equal dex interval $\Delta \log \rho = 0.2$, and temperature from $\log T$ (K) = 5 to 8 at dex interval 0.2. 1 pixel corresponds to 20 pc and the frame covers 8 kpc by 8 kpc region with the GC at the lower-left corner and the galactic plane horizontal.

2.5 BHS by C-type injection for SB model

The simulated result for the C-type BHS evolution corresponding to the SB model is shown in Figs 2–4. Fig. 6 shows cross-sections along constant heights at $z = 2$ and 4 kpc at $t = 10$ Myr, and Fig. 7 shows radial cross-sections at altitude angle $\Theta = 30^\circ$ and 45° from the galactic plane.

The central disc within a few hundred pc is disrupted to yield a hole inside a ring around the nucleus. Due to the continuous injection of mass, there appears an outward flow. When the outflow

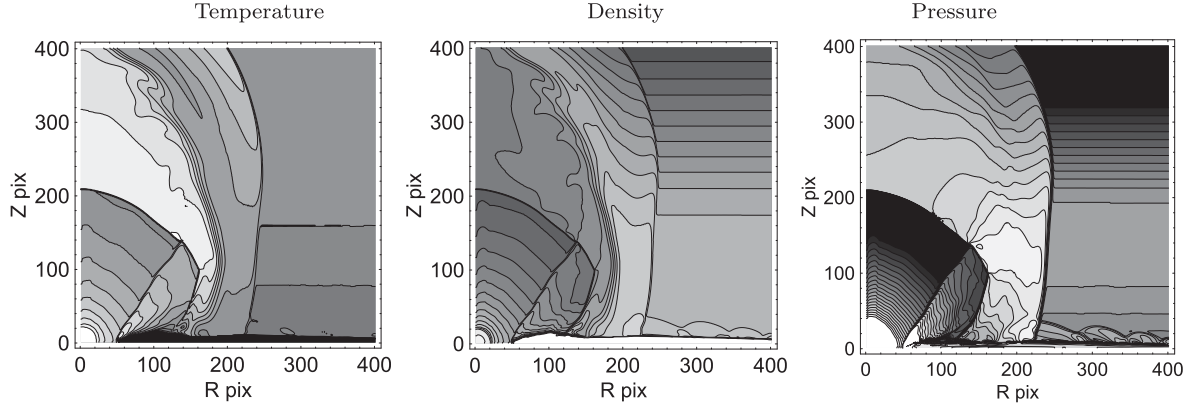


Figure 3. Same as Fig. 2 at 10 Myr for the temperature, density, and the pressure. The pressure contours are at every 0.1 dex from 10^{-13} to 10^{-11} erg cm $^{-3}$. This result is used for the analysis and comparison with the ROSAT observations of the NPS.

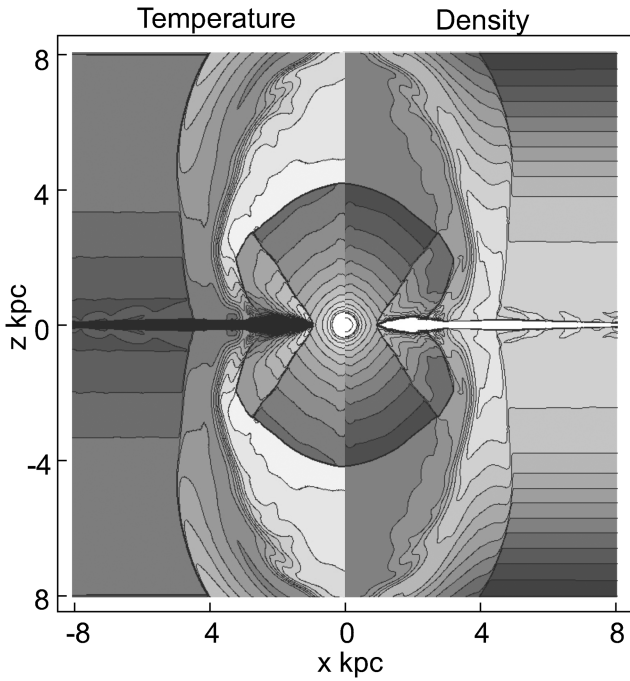


Figure 4. Same as Fig. 2 at 10 Myr for the density and temperature for convenience of comparison and correspondence. This figure reveals the BHS structure of the shock front propagating in the galactic disc and halo. Also interesting feature is seen as the inner bipolar cone feature produced by a high-velocity outflow as a bow shock against the galactic disc.

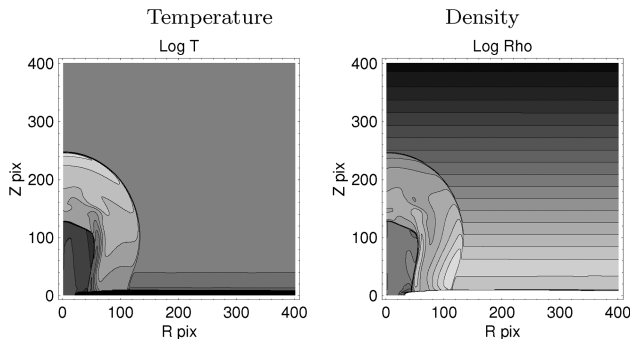


Figure 5. Same as Fig. 2 at 3 Myr for E-type energy injection. The BHS resembles that for C type, while the central region is smoother and the cone feature does not appear.

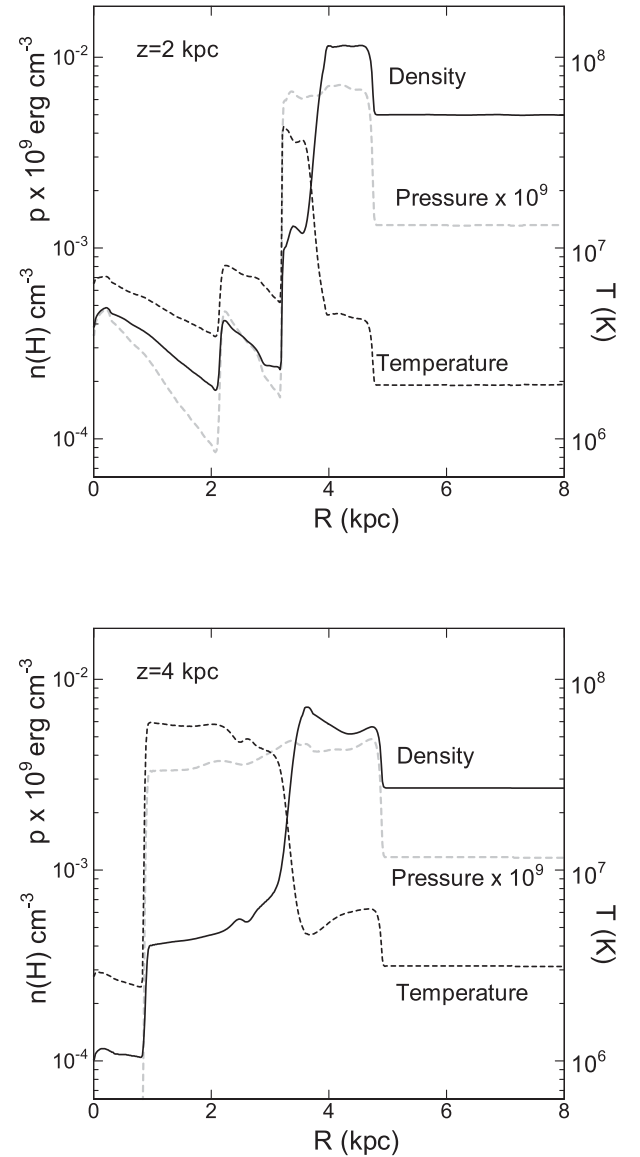


Figure 6. Density (full line), temperature (dashed), and pressure (grey dash) distributions at constant height $z = 2$ and 4 kpc at $t = 10$ Myr.

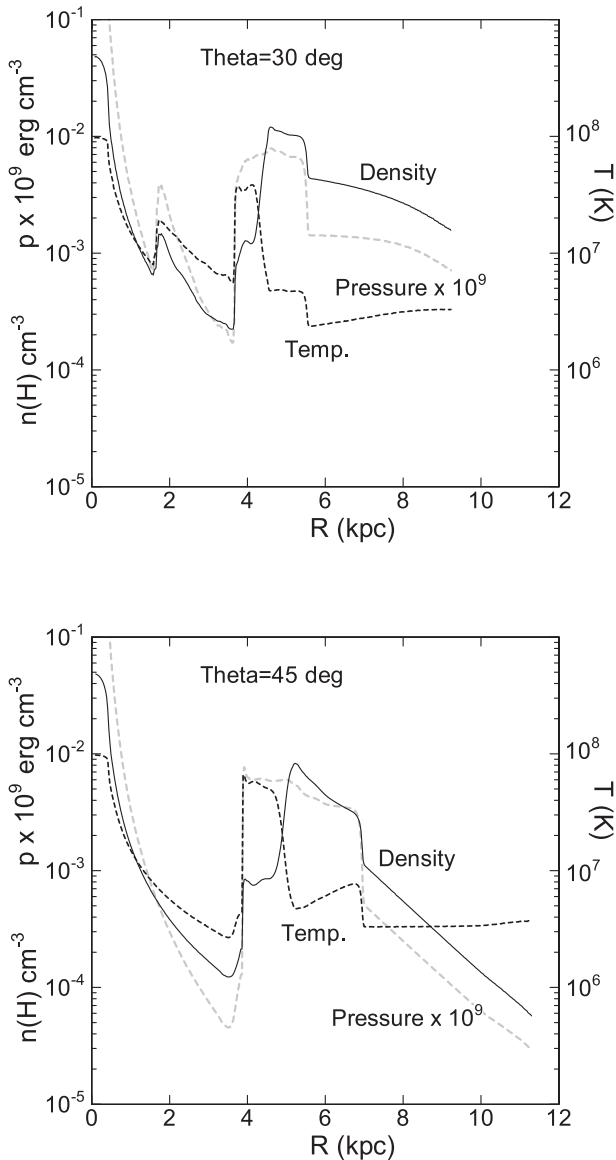


Figure 7. Radial distributions of density (full), temperature (dash), and pressure (grey dash) at altitude angle 30° and 45° at $t = 10$ Myr.

encounters the wall of the hole, it produces a shock-compressed ring, and a bow shock is produced, which extends into the halo as a cone-shaped, high-pressure discontinuity. By the constantly injected energy, the central region is kept at high temperature and high density. We will discuss the central region in more detail in Section 4.

When the outflow encounters the halo gas, it produces round-shaped shock wave. The shock-front velocity is decelerated near the galactic plane by the interaction with the dense ambient gas. The shock front expands spherically in the initial ~ 1 Myr, and is elongated into the halo as the time elapses. In the halo, the expanding velocity increases due to energy injection at the centre as well as by the jet-acceleration mechanism of Sakashita (1971) in exponentially decreasing gas density.

When BHS reaches high altitude at $z \sim 6$ kpc and encounters the intergalactic gas, the front suffers from decelerating force. However, due to the continuous supply of gas and energy from inside, the front still continues to expand at increasing velocity.

Fig. 4 shows enlargement of the result at 10 Myr with the density and temperature in a mirror plot for convenience of comparison and recognizing the mutual correspondence. The figure reveals more clearly the BHS structure of the outer shock front propagating in the halo. Also impressive in this figure is the inner bipolar conical horn feature, which is a bow shock against the galactic disc produced by a high-velocity wind from the centre (see the discussion section).

As shown in Figs 6 and 7 the densest shell follows the shock front, while the highest temperature is attained inside the shell, facing the cavity. The dense shell, where the emission measure is largest, has temperature around ~ 0.3 keV (3.5×10^6 K), in agreement with the observed temperature in the NPS (Kataoka et al. 2015). On the other hand, the high-temperature inner shell facing cavity, where $T \sim 4$ keV ($\sim 5 \times 10^7$ K), has density one to two orders of magnitude less than that in the dense shell. Hence, the emission measure in the high-temperature cavity is much lower than in the dense shell, so the X-ray emission is much weaker compared to the shell.

3 SOFT X-RAY SKY

3.1 Emission measure

Using the calculated density distribution by the BHS model, we calculated the emission measure along the line of sight s ,

$$EM = \int (\rho/m_H)^2 ds. \quad (7)$$

During the integration, we avoided the contribution from the ambient disc and halo gases by setting a minimum temperature of gas at $T_{\min} = 3 \times 10^6$, which is the halo gas temperature as represented by flat temperature beyond 5 kpc in Fig. 6. By this condition, the lower temperature disc is also avoided from integration. This limitation does not cause significant underestimation of emission measure (EM) in the NPS, because the temperature inside the BHS is mostly higher than 3×10^6 K (Fig. 6).

A result for $t = 10$ Myr is shown in Fig. 8 by a contour map in the $50^\circ \times 50^\circ$ sky, as well as by cross-sections along constant latitudes, $b = 20^\circ$ and 30° . The peak values across the BHS are obtained to be $EM \simeq 0.1\text{--}0.37 \text{ cm}^{-6} \text{ pc}$ at $b = 10^\circ$ and 40° .

Fig. 9 shows the simulated EM plotted against latitude. Plotted together are the EM values determined by *Suzaku* observations along the NPS at $b \sim 10\text{--}50^\circ$ (Kataoka et al. 2015). The calculated values are greater than the observed values, which are $EM \sim 0.06\text{--}0.3$, by a factor of ~ 1.5 . Similar values, $\sim 0.1 \text{ cm}^{-6} \text{ pc}$, have been obtained by Willingale et al. (2003) based on a local shell origin of NPS.

3.2 Emission

We calculated the emissivity of X-rays using the computed density and temperature, assuming a metallicity of $Z = 0.2 Z_\odot$ and cooling functions given by Foster et al. (2012) as shown in Fig. 10 obtained by using XSPEC (Arnaud 1996). The surface brightness on the sky at photon energy E was calculated by integrating the emissivity along the line of sight,

$$B = \frac{1}{4\pi} \int \frac{dP(E)}{dE} n_e^2 ds. \quad (8)$$

Here, $dP(E)/dE$ is the spectral emissivity per unit volume and unit density per unit photon energy E , and n_e is the electron density assumed to be equal to the ion density $n_e \simeq \rho/m_H$. The brightness B is expressed in Jy str^{-1} .

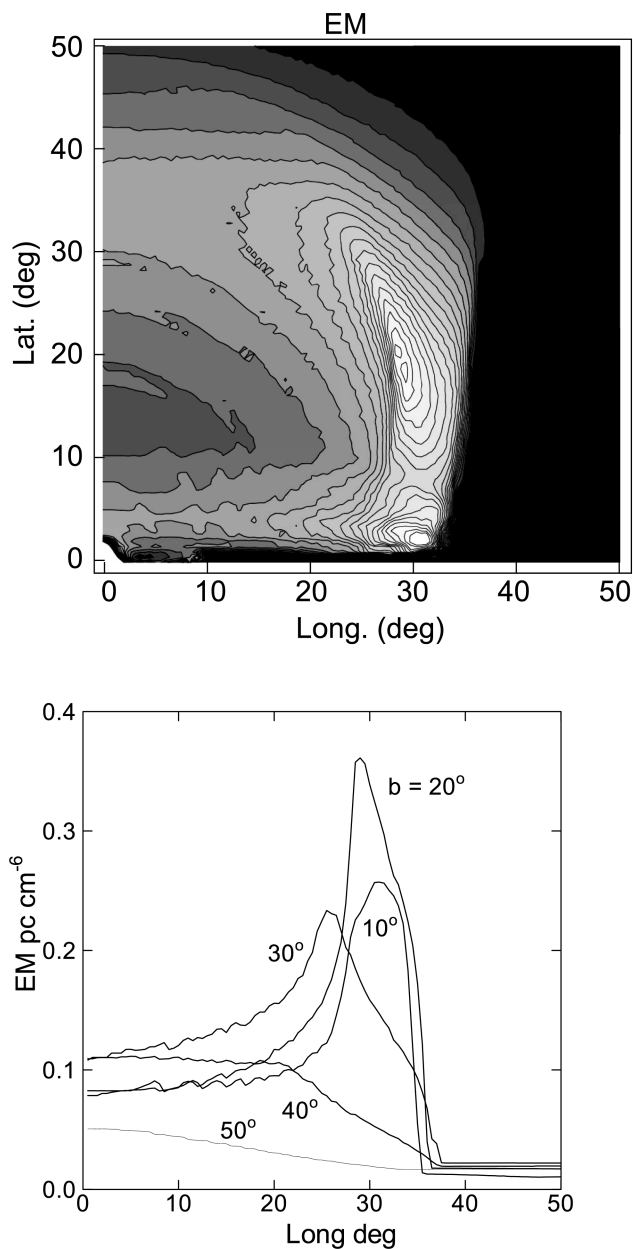


Figure 8. (Top) Distribution of the emission measure EM on the sky at $t = 10$ Myr. 2 pixels corresponds to 1 deg. (Bottom) Cross-sections along constant latitudes at $b = 0^\circ$ to 50° .

The spectral emissivity was averaged by E , assuming a Gaussian response function with a full width at half-maximum $\Delta E = 0.5E$ around the centre energy E . Fig. 10 shows the thus obtained spectral emissivity as functions of the plasma temperature for fixed photon energies at $E = 0.25, 0.7$, and 1.5 keV, approximately representing the *ROSAT* R2, 4, and 7 bands.

3.3 Absorption and shadowing

The optical depth of X-ray emission is defined by $\tau = N\sigma_i$, where σ_i is the absorption cross-section for the i -th band. X-ray absorption coefficient by metals in the interstellar gas with solar abundance was calculated by using ‘ISMabs’ (Gatuzz et al. 2015) implemented in

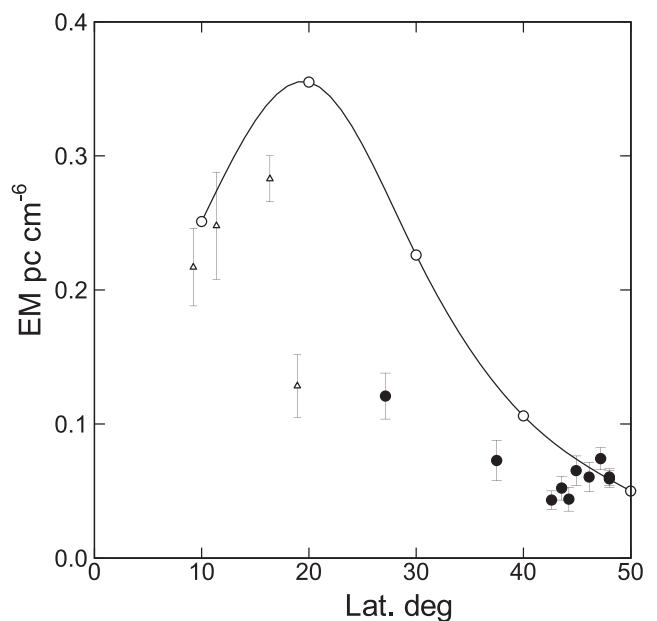


Figure 9. Variation of EM with b along the BHS ridge (full line), compared with measured EM by Kataoka et al. (2015) along the NPS (big dots). Small triangles are southern Claw and NE clump inside the *Fermi* Bubble, and hence not to be compared here.

XSPEC as shown in Fig. 11, and the adopted values are listed in Table 1.

The H atom column density $N(\text{H})$ was calculated using observed integrated intensities of the H I and $\text{CO } (J = 1 - 0)$ line emissions. We used the Argentine–Leiden–Bonn All-Sky H I Survey (Kalberla et al. 2005) and the Columbia Galactic Plane CO Survey (Dame, Hartman & Thaddeus 2001). The total column density $N(\text{H})$ of hydrogen atoms is obtained by

$$N(\text{H}) = C_{\text{H I}} I_{\text{H I}} + 2C_{\text{H}_2} I_{\text{CO}}, \quad (9)$$

where $I_{\text{H I}}$ and I_{CO} are integrated H I and CO line intensities.

The H I conversion factor was taken to be $C_{\text{H I}} = 1.82 \times 10^{18} \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s}$. The CO -to- H_2 conversion factor was assumed to be $C_{\text{H}_2} = 2.0 \times 10^{20} \text{ H}_2 \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s}$ for the local interstellar gas having the solar abundance (e.g. Bolatto, Wolfire & Leroy 2013). Fig. 12 shows a distribution map of the optical depth $\tau_4 = N(\text{H})/N_4$ for R4 band X-rays, which is equivalent to the distribution of the total H atom column density, except that the values are divided by N_4 . Optical depth maps for other bands are obtained by multiplying $\tau_i = \tau_4 N_4 / N_i$.

The absorption was calculated for fixed photon energy in each band, and hence, the model intensity distribution represents a monochromatic view of shadowed sky. In observations, however, the photon spectra are effectively hardened by the absorption within each band. However, the emissivity itself is a decreasing function of E . Fig. 11 shows the absorption cross-section and spectral emissivity, and the transmitted emission through gas with optical thickness unity, $\tau = 1$. The figure demonstrates that the absorption and emission dependencies with photon energy act to cancel each other, so that the transmitted emission has nearly a flat spectrum. Thus, we may conclude that the monochromatic treatment is a good approximation to the band-averaged surface brightness, sufficient for the present analysis.

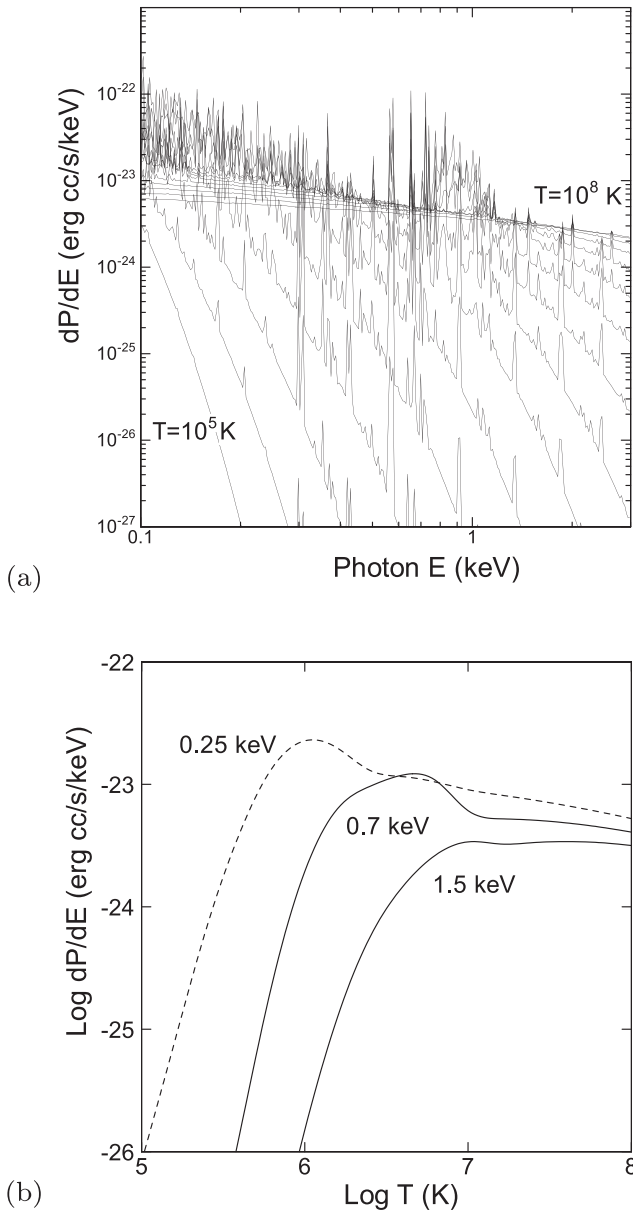


Figure 10. (a) Spectral emissivity for $Z = 0.2 Z_{\odot}$ against emitted photon energy for different plasma temperatures at every 0.2 dex temperature from $T = 10^5$ to 10^8 K as calculated by *xSPEC* (Arnaud 1996; Foster et al. 2012). (b) Spectral emissivity against temperature for fixed emitted photon energies at $E = 0.25, 0.7$, and 1.5 keV averaged by Gaussian band response with full width of $\Delta E = 0.5E$ as calculated by using (a).

3.4 Brightness

Fig. 13 shows the thus computed distribution of the X-ray brightness on the sky in the central $\pm 50^\circ \times \pm 50^\circ$ region at $t = 10$ Myr in for 0.25, 0.7, and 1.5 keV (approximating *R2*, *R4*, and *R7* bands), showing the intrinsic intensity distributions without suffering from interstellar absorption. These maps are then multiplied by $\exp(-\tau_i)$ to yield shadowed brightness distributions using τ_i distribution as shown in Fig. 12. Figs 14 and 15 show the simulated shadowed X-ray sky and *ROSAT* images, respectively, both in contour representations. The model brightness unit is Jy str^{-1} , while *ROSAT* brightness in $10^{-6} \text{ counts s}^{-1} \text{ arcmin}^{-2}$. Fig. 16 is a colour-coded representation compared with the *ROSAT* colour map.

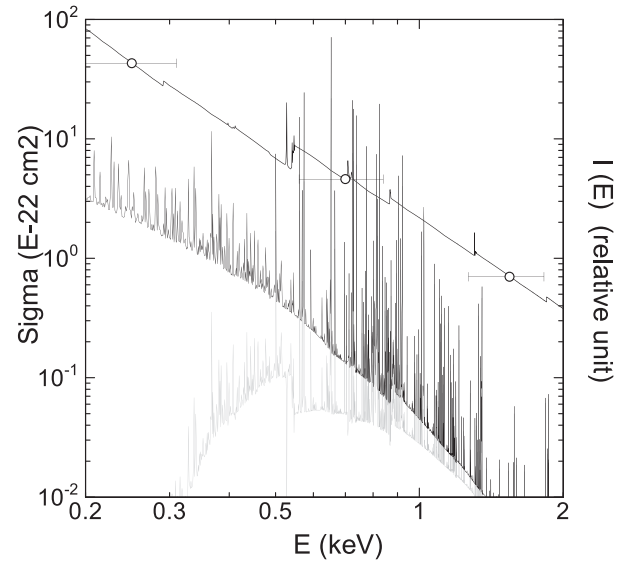


Figure 11. Absorption cross-section for $Z = 1 Z_{\odot}$ (upper line), spectral emissivity $dP(E)/dE$ (second line) for $E = 0.3$ keV, and $dP(E)/dE \exp(-\sigma/\sigma_4)$ (grey line) for *R4* band as obtained by *ISMabs* (Gatuzz et al. 2015) in *xSPEC* (Arnaud 1996), demonstrating that the transmitted X-ray emission has nearly flat spectrum through a gas around $\tau \sim 1$. Approximate *R2*, *R4*, and *R7* band energy and band widths are marked by circles.

Table 1. Representative energies for *R2*, *R4*, and *R7* bands used for simulation, and band-averaged absorption cross-sections calculated using ‘*ISMabs*’ (Gatuzz et al. 2015) implemented in *xSPEC* (Arnaud 1996).

Band	E (keV)	σ_i (10^{-22} cm^2)	$N_i = 1/\sigma_i$ (10^{20} cm^{-2})
<i>R2</i>	0.25	43	2.3
<i>R4</i>	0.7	5.0	20.0
<i>R7</i>	1.5	0.7	142

As in Fig. 13, the BHS shows up as the dumbbell-shaped structure of symmetric spurs extending towards the galactic poles. The observed NPS is well reproduced by the simulation. The western counter part of NPS (NPS-W) at $(l, b) \sim (-30^\circ, +10^\circ - 40^\circ)$, the South Polar Spurs SPS-E and SPS-W are also seen in the *ROSAT* map, though not clear as in the north (see the next section for cross-sections).

The BHS spurs near the galactic plane are heavily obscured by the H I and molecular gas layers, spurs, and clouds. Various shadow features are evident, silhouetting the BHS and halo X-ray emissions. Particularly, the *R4* band NPS ridge is strongly shadowed by the Aquila Rift at $(l, b) \sim (25^\circ, 12^\circ)$, where the Rift’s ridge crosses the NPS nearly perpendicularly. The *R7* band emission is less obscured, and shows more intrinsic structures. However, the observed *ROSAT* *R7* band image is too noisy to show up the detailed structure of the spurs.

The 0.25 keV ($\sim R2$) emission is strongly absorbed by the local interstellar gas, and only high-latitude emission weakly remains as northern and southern polar caps. The simulated 0.25 keV brightness is an order of magnitude darker than the intrinsic brightness. This is due to heavy extinction with large optical depth at $|b| < \sim 30^\circ$, particularly, due to the H I and H₂ spurs and flares of the Aquila Rift. Although the simulated and *ROSAT* *R2* band images are similar to each other, they may not be further compared

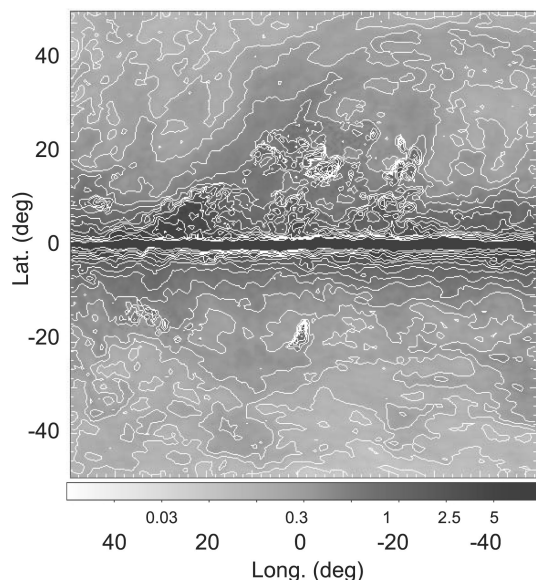


Figure 12. Optical depth for X-rays in *R4* band, which is equal to the column density divided by the critical column density, $\tau_4 = N(\text{H})/N_4$, where $N(\text{H}) = N(\text{H I}) + 2N(\text{H}_2)$. Contours are drawn at logarithmic interval of 0.05 dex from $\tau_4 = 0$ to 10. Optical depth for other bands are obtained by $\tau_i = \tau_4 N_4/N_i$.

seriously, because the observed *R2* emission is a mixture of local emissions such as the Solar Wind Charge eXchange and the Local Hot Bubble.

4 DISCUSSION

The shock front was shown to expand spherically in the initial ~ 1 Myr, and is elongated into the haloes composing dumbbell-shaped symmetric bubble features with respect to the galactic disc. Expected X-ray brightness distributions were calculated for the central $\pm 50^\circ \times \pm 50^\circ$ region at three different energies (0.25, 0.7, and 1.5 keV), approximately corresponding to *R2*, *R4*, and *R7* *ROSAT* bands. Shadowing by the interstellar H I and H_2 gases was taken into account to compute the brightness distributions on the sky.

The simulated X-ray maps at elapsed time $t \sim 10$ My approximately reproduces the morphological features of the NPS and SPS as observed by *ROSAT*. The modelled emission measure was found to be greater than those from *Suzaku* observations at a couple of tens positions by a factor of ~ 1.5 . Below, we consider about the implication of the results and discuss some problems exhibited by this study.

4.1 Simulation versus observation

4.1.1 *ROSAT* count rate versus Jy str^{-1}

The *ROSAT* data are represented in terms of count rate of the instrument in unit of $\text{counts s}^{-1} \text{ arcmin}^{-2}$, but not calibrated to intensity, whereas the simulated result is presented in unit of Jy str^{-1} .¹ In order to obtain quantitative comparison, we calibrated the *ROSAT* data into Jy str^{-1} using the *Suzaku* observations of the EM and plasma temperature in the region near the *Fermi* Bubbles including NPS and southern spurs obtained by Kataoka et al. (2015).

¹ $1 \text{ Jy} = 10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1} = 2.41798 \times 10^{-9} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ eV}^{-1}$.

X-ray brightness B at photon energy $E = 0.7$ keV was calculated by using the measured EM for plasma temperature of $T = 0.3$ keV (Kataoka et al. 2015) adopting the cooling function for a metallicity $Z = 0.2 Z_\odot$ as shown in Fig. 1. Individual values were also multiplied by $\exp(-\tau)$ with τ being the optical depth for N_{H} at corresponding positions. Fig. 17 shows the thus calculated brightness plotted against the *ROSAT* count rate in *R4* band at the same positions.

Removing the exceptionally large value near the top-right corner, we applied the least-squares linear fitting, and obtained the straight line. The slope of the fitting is adopted as the calibration factor $X(R4)$ as $X(R4) = 0.398 \pm 0.021 \text{ mJy str}^{-1} (1.0 \times 10^{-6} \text{ counts s}^{-1} \text{ arcmin}^{-2})^{-1}$. Using the thus determined factor, we compare the intensities by simulation and observations.

4.1.2 Intensities

Fig. 18 shows cross-sections of the *R4* band intensity by observation (dots) and 0.7 keV by simulation (thick lines) along constant latitudes at $b = +30^\circ$ to -30° . The plots were obtained as follows: the original *ROSAT* *R4* map was convolved by a Gaussian function with a half width of 1 pixel (0.2). Then, pixel values along three rows at $b = +20^\circ \pm 0.2$ and $-30^\circ \pm 0.2$ were plotted by circles. The intensity scales are both in mJy str^{-1} .

The observed northern cross-section at $b = +20^\circ$ exhibits double horn peaks of NPS and NPS-W. The NPS-W is contaminated by the bulge emission whose eastern half is heavily shadowed by the Aquila Rift. The simulated cross-section shows the double horn feature symmetrically to the GC.

The southern cross-section at $b = -30^\circ$ by simulation, particularly SPS-E, well fits the observation in the shape. The SPS-W is again contaminated by the bulge emission as the round enhancement around the GC.

Although the agreement of peak intensities in the NPS is excellent, the simulated intensities are generally higher than the observations. We may eye-estimate the simulated-to-observed intensity ratios at the peaks in Fig. 18 to obtain $B_{\text{simu}}/B_{\text{obs}} = 1.6 \pm 0.8$. This ratio is directly related to the emission measure, and therefore, the gas density in the BHS and the ambient halo gas as $\rho_{\text{simu}}/\rho_{\text{obs}} \sim 1.3$.

4.1.3 Metallicity

Although we assumed $Z = Z_\odot$ as the marginal value for the entire evolution of BHS, it is, in reality, variable with time and place. In the early phase of expansion, the BHS is dominated by the high-metal gas in the GC and the disc where $Z > Z_\odot$. As it expands into the halo, the BHS becomes dominated by the swept halo gas and intergalactic gas with $Z < Z_\odot$. However, the radiative cooling does not contribute much to the dynamical evolution of the BHS, namely simulations assuming a different metallicity would result in almost the same result.

On the other hand, the X-ray brightness was calculated for the observed metallicity in the galactic halo with $Z = 0.2 Z_\odot$. Hence, the metallicity in the simulation and in the brightness calculation is not fully consistent with each other. A consistent modelling would be a subject for the future.

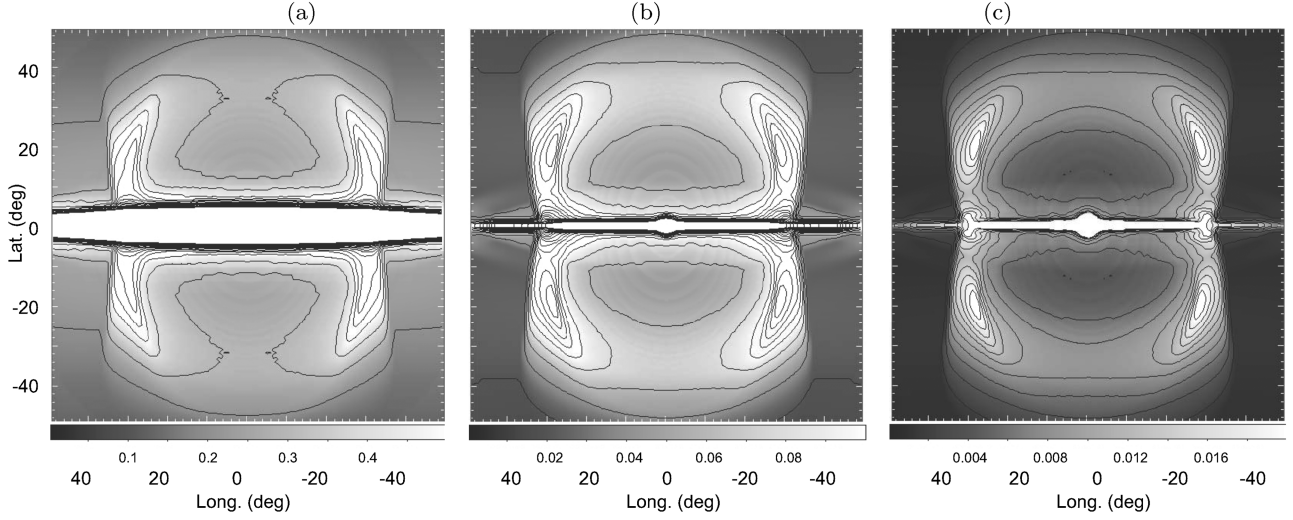


Figure 13. (a) Simulated brightness distribution at 0.25 keV ($\sim R2$) at $t = 10$ Myr in the central $\pm 50^\circ \times \pm 50^\circ$ region. Contours are at 0, 0.1, 0.2, ..., 1.9, 2.0 Jy str⁻¹. (b) Same, but 0.7 keV ($\sim R4$) with contours at 0, 0.01, 0.02, ..., 0.19, 0.2 Jy str⁻¹. (c) Same, but 1.5 keV ($\sim R7$) with contours at 0, 0.002, 0.004, ..., 0.018, 0.02 Jy str⁻¹.

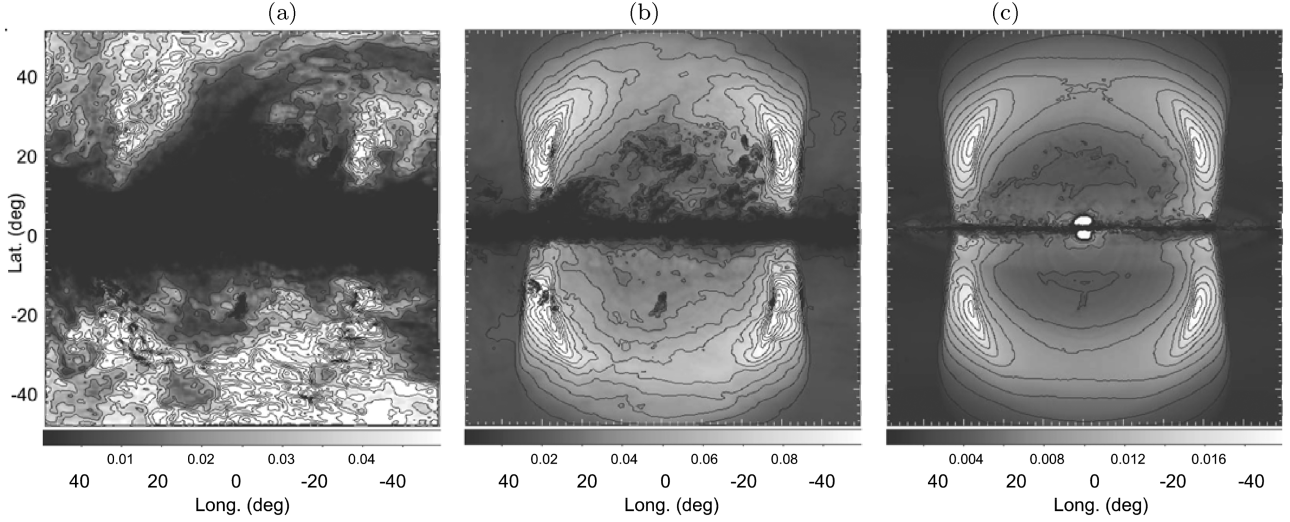


Figure 14. (a) Simulated shadowed X-ray brightness as Fig. 13(a) with contours at 0, 0.01, 0.02, ..., 0.16, 0.17 Jy str⁻¹. (b) Same as 13(b), but shadowed with the same contour levels. (c) Same as 13(c), but shadowed with the same contour levels.

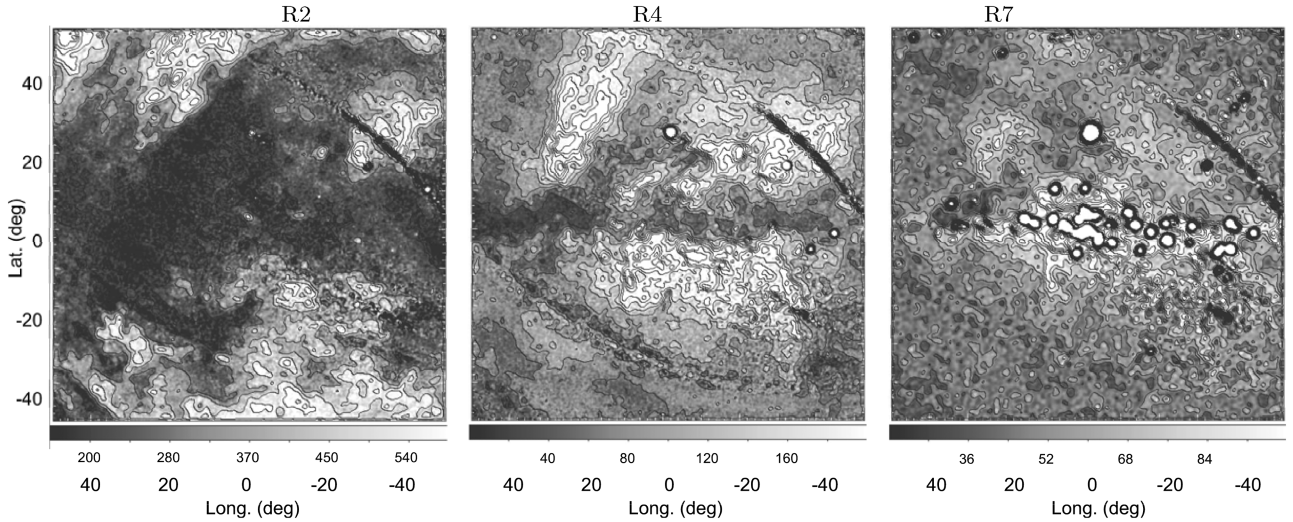


Figure 15. ROSAT images in R2, 4, and 7 bands. Contour levels are: R2: 100, 200, 300, ...; R4: 30, 60, 90, ...; R7: 20, 30, 40, ... 10^{-6} counts s⁻¹ arcmin⁻². MNRAS **459**, 108–120 (2016)

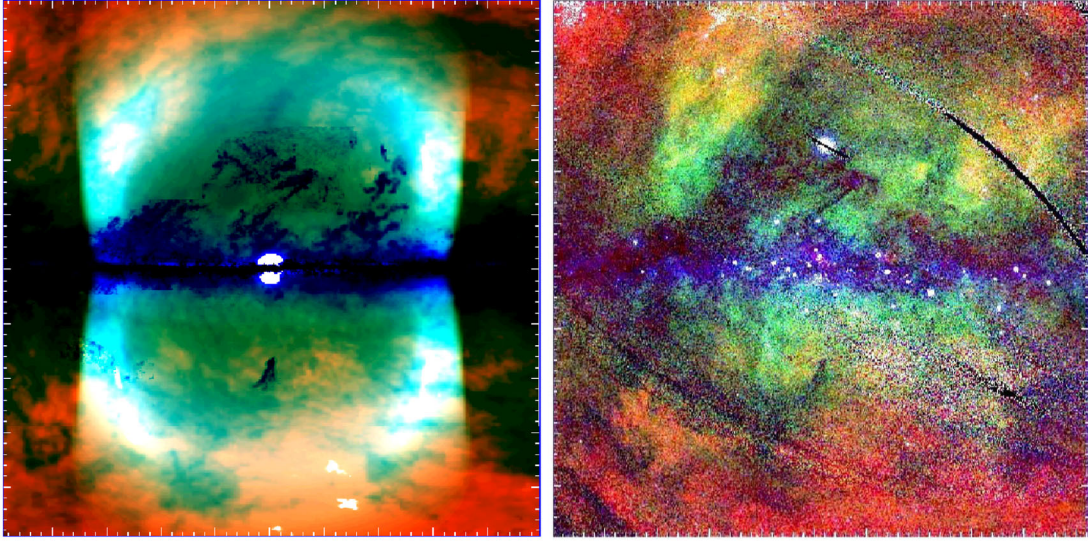


Figure 16. Same as Figs 14 and 15, but in colour-coded representation by red for 0.25/R2, green for 0.7/R4 and blue for 1.5 keV/R7 bands (left: BHS and right: ROSAT).

4.2 Energetics

We have presented the result of BHS simulation for a continuous energy injection (type-C injection) with $\mathcal{E} = 4 \times 10^{56}$ erg in the last 10 Myr presuming recurrent SB in the GC (SB model). The total injected energy is smaller than those estimated for super winds in SB galaxies (Heckman, Armus & Miley 1990), while greater than that for the SB galaxy M82 (Lacki 2014). It is also greater than that proposed for the GC in order to produce the *Fermi* Bubbles (Crocker et al. 2015).

4.2.1 Energy partitioning in the BHS

The total injected energy $\mathcal{E}_0$ is finally transformed to the thermal $\mathcal{E}_{\text{th}}$, kinetic $\mathcal{E}_{\text{kin}}$, and gravitational $\mathcal{E}_{\text{grav}}$ energies of the BHS as well as to the radiatively lost energy by cooling $\mathcal{E}_{\text{rad}}$:

$$\mathcal{E}_0 = \mathcal{E}_{\text{th}} + \mathcal{E}_{\text{kin}} + \mathcal{E}_{\text{grav}} + \mathcal{E}_{\text{rad}}. \quad (10)$$

Individual energies are approximately estimated using the figures presented in Section 2 as the following. The BHS mass is estimated to be $M_{\text{BHS}} \sim 5 \times 10^7 M_{\odot}$ for the both sides, each with a radius $R \sim 4$ kpc and thickness $\Delta R \sim 1$ kpc and mean density of $n \sim 0.005 \text{ cm}^{-3}$. The thermal energy is estimated for a mean temperature of $T \sim 3 \times 10^7$ K, where $\mathcal{R}$ being the gas constant. The kinetic energy is estimated for an expansion velocity $V_{\text{expa}} \sim 400 \text{ km s}^{-1}$. The gravitational energy can be estimated by $\Delta\Phi \sim GM_{\text{gal}}(1/z_0 - 1/z)$, where Φ is the gravitational potential, $z_0 \sim 2$ kpc and $z \sim 4$ kpc are the initial and the present heights of BHS gas. The galactic mass within a radius $r \sim z_0$ kpc is estimated by $M_{\text{gal}} \sim z_0 V_{\text{rot}}^2 / G \sim 1.8 \times 10^{10} M_{\odot}$ for a rotation velocity $V_{\text{rot}} \simeq 200 \text{ km s}^{-1}$. The radiative loss during $t \sim 10$ Myr is estimated for a cooling rate of $P(T) \sim 3 \times 10^{-23} \text{ erg cm}^3 \text{ s}^{-1}$ at $T \sim 3 \times 10^7$ K and $n \sim 10^{-2} \text{ cm}^{-3}$.

We now obtain:

$$\mathcal{E}_{\text{th}} = \int p dV \sim \mathcal{R} M_{\text{BHS}} T \sim 2.5 \times 10^{56} \text{ erg}, \quad (11)$$

$$\mathcal{E}_{\text{kin}} \sim 1/2 M_{\text{BHS}} V_{\text{expa}}^2 \sim 8 \times 10^{55} \text{ erg}, \quad (12)$$

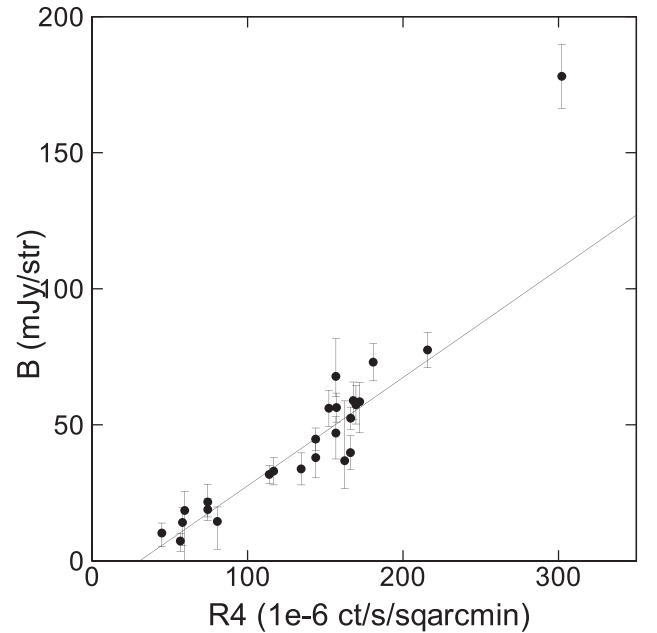


Figure 17. Surface brightness in mJy str^{-1} plotted against R4-band count rate at positions where EM and plasma temperature were determined by *Suzaku* observations (Kataoka et al. 2015).

$$\mathcal{E}_{\text{grav}} \sim M_{\text{BHS}} \Delta\Phi \sim 2 \times 10^{55} \text{ erg}, \quad (13)$$

$$\mathcal{E}_{\text{rad}} \sim t \int n^2 P(T) dV \sim 3 \times 10^{54} \text{ erg}, \quad (14)$$

and

$$\mathcal{E}_0 \sim 5 \times 10^{56} \text{ erg}. \quad (15)$$

The estimation using the figure may include an error of $\sim \pm 30$ per cent, that is the reason for the larger total energy than the input initial value of 4×10^{56} erg.

The relative fractions of the energies compared to $\mathcal{E}_0$ are rather accurate, and are: $\mathcal{E}_{\text{th}}/\mathcal{E}_0 \sim 0.7$, $\mathcal{E}_{\text{kin}}/\mathcal{E}_0 \sim 0.2$, $\mathcal{E}_{\text{grav}}/\mathcal{E}_0 \sim 0.06$, and $\mathcal{E}_{\text{rad}}/\mathcal{E}_0 \sim 0.01$. The small radiative loss implies that the BHS is almost adiabatic. This can be confirmed by the long cooling time, $t_{\text{cool}} \sim 9 \times 10^9$ yr, far longer than the expansion time of the shell. This implies that the BHS dynamics little depends on the cooling rate, and hence on the density and metallicity. Namely, the result will be not changed much even if we adopt smaller metallicity than the assumed value (1 solar).

4.2.2 Constraint on the total energy

We thus conclude that the total energy of the order of $\mathcal{E}_0 \sim 4 \times 10^{56}$ erg is inevitably required in order to reproduce the observed X-ray NPS and associated spurs in the BHS model for the given halo density. Thereby, the emission measure (density), temperature (velocity), and the linear size of the NPS are the strongest observational constraint on the total energy.

If the halo density is decreased by a factor of 1/1.3 as indicated by comparison with the emission measure observed with *Suzaku*, the total energy will be eased by the same factor, considering the Sedov's similarity factor $(\mathcal{E}_0/\rho_0)^{1/5}$ in the shock wave. Thus, we conclude that the total injected energy to drive the NPS is $\mathcal{E}_0 \sim 3 \times 10^{56}$ erg.

4.2.3 SB model and star formation rate

Given the total energy as above, the assumed rate of energy supply of $d\mathcal{E}/dt \sim 4 \times 10^{55}$ erg Myr $^{-1}$ is required in the C-type injection model, though reduced by a factor of 1/1.3. If we consider an SB model, it requires a type II supernova rate as high as $\sim 4 \times 10^5$ per 10 Myr, or 1 SN per 20 to 30 yr in the GC, comparable to the SN rate in the entire Galaxy. The assumed inflow rate of $dM/dt \sim 1 M_\odot \text{ yr}^{-1}$ is comparable, but slightly greater than the often quoted rate $dM/dt \sim 0.1 - 1 M_\odot \text{ yr}^{-1}$ (Kruijssen et al. 2014; Krumholz & Kruijssen 2015). Hence, it may be worth to consider other types of mechanism of energy injection energy in the GC.

4.2.4 AGN model with E-type energy injection

An additional or alternative energy source to drive the BHS could be the E-type energy injection at the centre. A powerful energy source without suffering from the problem about star formation and mass inflow would be the E-type explosion due to AGN activity at the Galactic nucleus, which occurs intermittently each with smaller energy (Totani 2006). In this case, the total energy is given by $\mathcal{E}_0 = \mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{AGN}}$, and the mass inflow rate is accordingly reduced with increasing AGN activity.

4.3 Central structures

4.3.1 Mach cone

Fig. 19 shows a central $\pm 25^\circ \times \pm 25^\circ$ region in the simulated 1.5 keV brightness compared with *ROSAT* R7 image. In the simulation, a cone-shaped bow shock is recognized as bipolar inclined spurs emerging from the central region, which is a sonic boom, or Mach cone, produced by the interaction of the outflow with the dense wall of the holed disc. The Mach angle of the cone is $\mu \simeq 58^\circ$, indicating that the Mach number is $\mathcal{M} = 1/\sin \mu \sim 1.12$. This is consistent

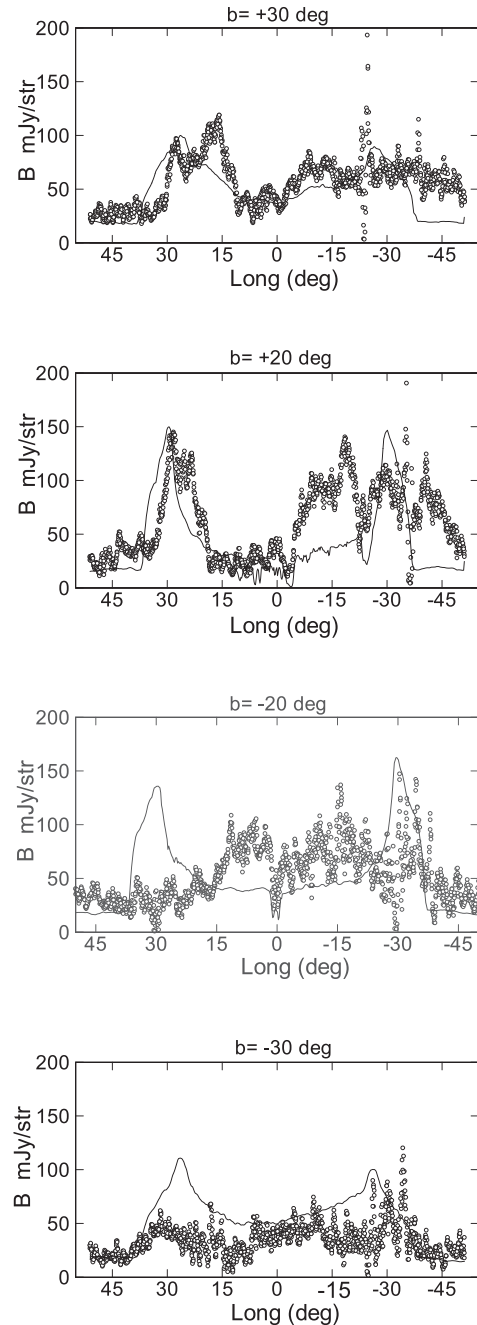


Figure 18. Simulated variations of 0.7 keV brightness along $b = +30^\circ$, $+20^\circ$, -20° , and $b = -30^\circ$ (thick lines) compared with those of *ROSAT* R4 band (circles). Both are shown by brightness in mJy str $^{-1}$.

with the postulated outflow velocity and temperature of the gas in the corresponding region.

The Mach cone morphologically reproduces the X-ray bipolar conical structure. However, the simulated cone is fainter compared to the observation. Brighter cone could be obtained, if the energy injection rate was not constant, but varied intermittently, so that the most recent injection was strong enough to enhance the cone's emissivity. This idea is consistent with the shorter time-scale, $\sim 10^6$ yr, suggested for the *Fermi* Bubbles with which the X-ray Claw feature in the southern spur is associated (Kataoka et al. 2013, 2015).

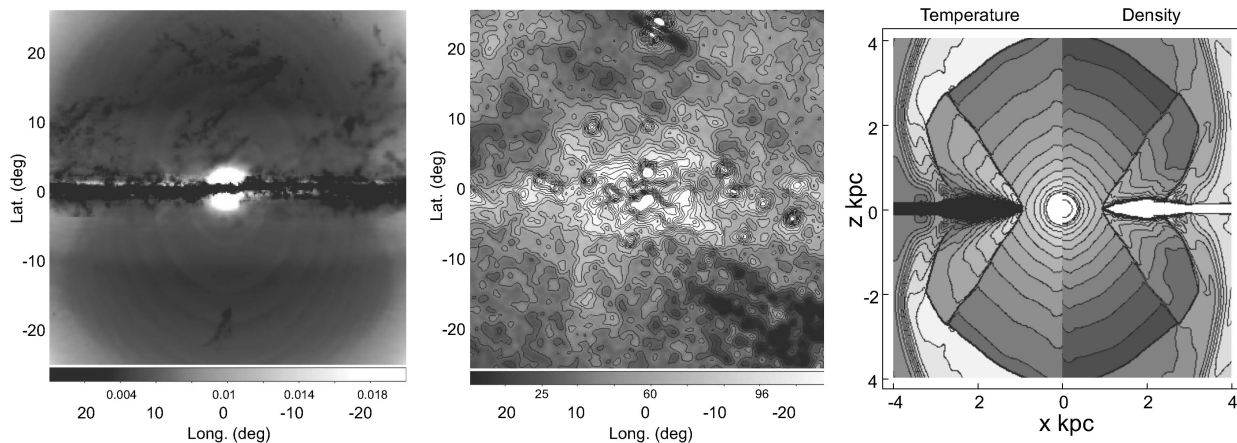


Figure 19. The Mach cone by simulation at 1.5 keV (left), *ROSAT* R7 band (middle) in the central $\pm 25^\circ \times \pm 25^\circ$ region, and simulated temperature and density distribution in the (x, z) plane for the central $\pm 4 \times \pm 4$ kpc. The *ROSAT* image is point source removed, and the contours are at 10, 20, . . . 200 *ROSAT* count rates.

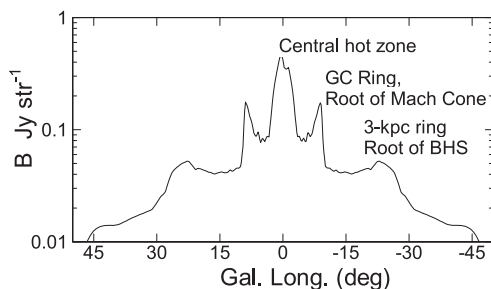


Figure 20. 1.5 keV intrinsic brightness along the Galactic plane, showing the central hot zone at GC, the 1 kpc ring at $l \sim 8^\circ$ corresponding to the root of hot cone, and the 3.3 kpc ring at $l \sim 24^\circ$.

4.3.2 Central hot zone and expanding rings

Fig. 20 shows a cross-section of the simulated distribution of 1.5 keV brightness along the galactic plane. There appear three characteristic regions. A round hot zone of high-temperature plasma is produced by the injection of SB thermal energy in the central ~ 300 pc at $|l| \leq 3^\circ$. A shock-compressed ring of radius ~ 1 kpc at the root of the hot cone at $l = \pm 8^\circ$ appears as the two horn-like enhancement of X-rays. A larger radius ring of a radius ~ 3.3 kpc appears as the broad maxima at $l \sim 24^\circ$ corresponding to the root of the BHS.

These three structures may be related to observed features in the GC at various wavelengths. The central hot zone may correspond to the high-temperature plasma at ~ 10 keV observed in hard X-ray emissions (Uchiyama et al. 2013). The 1 kpc ring may be a scaled up event of the various gas rings (Bania 1980; Sofue 1995; Law 2010; Krumholz & Kruijssen 2015). The 3.3 kpc compressed ring associated with BHS coincides with the 3 kpc expanding ring observed in the H I line longitude-velocity diagram (Oort 1977). As readily known by a fast-mode magnetohydrodynamic wave calculation (Sofue 1977), the compression occurs from outside of the disc by refraction and focusing of the shock wave propagating through the halo.

4.4 BHS morphology: asymmetry and intergalactic wind

In Figs 16 and 18, the observed north–south and east–west asymmetry is evident in the sense that the NPS is a few times brighter

than SPS and that the NPS-E and -W are inclined towards the west compared to the simulation.

The north–south asymmetry may indicate that the electron density in the north is significantly higher than in the south. Such an asymmetry of the BHS could be produced by an intergalactic wind or a motion of the Galaxy through the intergalactic gas (Sofue 1994). The wind will yield higher density and pressure in the northern halo, whereas the southern halo suffers from rarefaction due to shading by the galactic disc from the wind.

The axial asymmetry could also be explained by a wind from the east to west. Hence, we may speculate that an intergalactic wind blows from the galactic north-east towards south-west. Diagnosis of intergalactic wind using the BHS morphology would be a subject for future 3D simulations.

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