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A Study of National Accounts Tables of the Soviet Union and Its Industrial Structure

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In the first part of this paper the revised "Income-Goods" table combined with IBMF (Interindustry Balance of Money Flow) is shown and then, using the table, in the second one I focus on statistical analysis of the industrial structure of the Soviet Union. The so-called "Income-Goods" table which I have been studying for these past few years was offered by V. D. Belkin and his group in 1975.¹⁾ This unique table is formed from an I-O table, to which sectors showing revenue and expenditure are attached on the outside of it. As a whole, Belkin's table has succeeded in seizing both goods and income flows, including the redistribution of income in national accounts. Whereas the IBMF, presented in Sh. B. Sverdlik's new book, *Social Products and Money Flow*, also is a creative table, resembling an I-O table in character, i. e., in this table a change of state budget-credit expenditure has an influence on the money flow of each industry through each coefficient; also the change in final demand in an I-O table regulates the output of each industry, so that the former as well as the latter acquires an operational function. In addition to this, Sverdlik has shown to us three I-O tables, which include outer columns of intermediate transactions of the Soviet Union in 1959, 1966, and 1972, and are completely restored, although these were only 9 interindustry transactions. According to his book, the 1972 I-O table (hitherto unpublished) had the following sectors: 97 sectors of industries, 5 sectors of constructions, 2 sectors of agricultures, forestry, freight transportation, communications serving production, trade and public dining services, state procurement of all agricultural products, distribution of materials, supplies and products among enterprises and organizations associated with material production and other branches of material production.²⁾

I. Construction of Revised "Income-Goods" Table

First of all, the I-O table and the IBMF constructed by Sverdlik are shown and the data used is examined. *Table 1* offers both these tables compounded as one table. The section from the 1st row to the 16th row and the 1st column to the 30th column, except for the 15th column (hereinafter described as "1-16; 1-30/15"), refers to the I-O table, and the section "1-10, 12, 17-20; 1-16" (in gothic figures) refers to IBMF.

Table 2 is the 7-sector I-O table reconstructed by V. Treml. As you see, it is of the conventional static, open, Leontief type in purchasers' prices, and it is used to provide a set of control totals for the sectors omitted from the published USSR table, as well as for some elements of final demand and value added. Its output

1) See the list of references (1) and (2), Belkin and his group.

2) See (5) Sverdlik, page 39.

Table 1. The Compounded table of the both tables (I-O table and IBMF)

(1972. billion rubles)

		Heavy industry	Light industry	Food industry	Construction	Agriculture (Socialized)	Agriculture (Private)	T & C	T & D	Other branches	Total interindustry use	Consumption				Financial institutions	Total (10+11+12+13+14+15)	Gross fixed capital formation						Increase in stocks			Others	Total (19+22+25+26+27)	Exports	Total supply		
												Services	Science	Household	Government			Productive			non-Productive			Productive							non-Productive	
																		Social	Private	Total	Social	Private	Total	Social	Private	Total						
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30			
Heavy industry	1	140.2 154.5	4.2 5.2	4.1 6.2	38.1 40.1	13.3 22.4	0.0 0.0	6.4 7.1	1.5 3.5	0.6 0.6	208.4 245.2	5.4 7.1	5.4 6.2	26.5 26.5	3.0 x ₁ (5.1)	32.8	322.9	32.6	0.6	32.6	4.3	0.3	4.6	4.2	0.0	4.2	0.3	17.8	59.5	15.0	822.9	
Light industry	2	2.8 2.8	41.4 41.6	0.8 0.8	0.6 0.6	0.4 0.4	0.0 0.0	0.2 0.2	0.3 0.1	0.1 0.1	46.6 48.0	0.0 0.0	0.0 0.0	44.5 44.5	1.8 x ₂ (1.8)	0.7	95.0	0.0	0.0	0.0	-	-	-	1.4	-	1.4	0.0	0.3	1.1	1.0	95.0	
Food industry	3	1.3 1.4	0.5 0.5	30.0 30.2	0.1 0.1	4.3 4.4	0.0 0.0	0.0 0.0	0.7 0.1	0.0 0.0	36.9 36.7	0.0 0.0	0.0 0.0	88.3 88.3	3.2 x ₃ (3.2)	0.6	128.8	0.0	0.0	0.0	-	-	-	-0.2	0.0	-0.2	0.0	-0.3	-0.5	0.9	128.8	
Construction	4	20.9 2.4	0.8 8.6	1.7 45.7	2.5 0.0	11.9 13.3	0.0 0.0	5.1 0.0	1.6 1.0	0.0 0.0	44.5 73.5	18.3 0.0	1.1 0.0	3.3 8.3	x ₄ (10.2)	0.7	77.4	0.9	0.0	0.9	-	-	-	2.9	0.0	2.9	0.0	-1.9	1.9	0.7	81.8	
Agriculture (Socialized)	5	2.4 0.0	8.6 0.3	45.7 4.7	0.0 0.0	13.3 10.8	0.0 0.0	0.0 0.0	0.2 0.0	0.0 0.0	70.2 15.8	0.0 0.0	0.0 0.0	8.3 20.1	x ₅ (0.7)	-(0.7)	81.8	0.0	0.2	0.2	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.2	0.0	35.9	
Agriculture (Private)	6	0.0 0.0	0.3 0.3	4.7 4.7	0.0 0.0	10.6 10.8	0.0 0.0	0.0 0.0	0.0 0.0	0.0 0.0	15.6 15.8	0.0 0.0	0.0 0.0	20.1 20.1	x ₆ (0)	0.0	35.9	-	-	-	-	-	-	-	-	-	-	-	-	-	29.5	
Transportation & communications	7	24.3 24.3	0.9 0.9	2.3 2.3	0.1 0.1	1.4 1.4	0.0 0.0	0.0 0.0	0.2 0.2	0.3 0.3	29.5 29.5	0.0 0.0	0.0 0.0	0.0 0.0	x ₇ (0)	0.0	29.5	-	-	-	-	-	-	-	-	-	-	-	-	-	25.2	
Trade & distribution	8	6.3 6.3	2.9 2.9	10.9 10.9	0.0 0.0	4.6 4.6	0.0 0.0	0.0 0.0	0.5 0.5	25.2 25.2	0.0 0.0	0.0 0.0	0.0 0.0	0.0 0.0	x ₈ (0)	0.0	25.2	-	-	-	-	-	-	-	-	-	-	-	-	-	5.4	
Other branches	9	1.6 1.7	0.1 0.1	0.1 0.1	0.2 0.2	0.1 0.1	0.0 0.0	0.1 0.0	0.1 0.2	0.1 0.1	2.3 2.5	0.0 0.0	0.0 0.0	2.9 2.9	x ₉ (0.2)	-(0.2)	5.4	-	-	-	-	-	-	-	-	-	-	-	-	-	5.4	
Total purchases	10	178.9 214.5	58.9 60.9	98.6 102.7	39.1 43.6	37.4 60.7	10.6 10.8	6.6 18.0	3.0 8.1	1.6 1.6	434.7 520.9	5.4 25.4	5.4 7.3	190.3 193.9	8.9 x ₁₀ (21.2)	33.2	644.7	78.0	0.2	78.2	33.9	3.6	37.5	8.5	0.0	8.5	0.3	15.1	139.6	17.6	801.9	
Depreciation	11	17.7	0.8	1.6	3.6	6.5	0.6	4.4	1.9	0.0	37.1	3.5	0.9	7.8	3.2																	
Labor income	12	45.8 45.8	6.7 6.7	5.3 5.3	25.8 25.8	25.9 25.9	24.7 25.1	9.2 9.2	10.4 10.4	3.4 3.4	157.2 157.6	6.8 6.8	6.1 6.1	0.0 0.0	27.4 (27.4)	-(27.4)	231.8															
Surplus product	13	65.3	21.1	19.4	8.9	9.0	-	9.3	9.9	0.4	143.3	-0.1	0.3	-	2.8																	
Value added (12+13)	14	111.1	27.8	24.7	34.7	34.9	24.7	18.5	20.3	3.8	300.5	6.7	6.4	-	30.2																	
Gross value of output (10+11+14)	15	307.7	87.5	124.9	77.4	78.8	35.9	29.5	25.2	5.4	29.6	15.6	12.7	-	42.3																	
Imports	16	15.2	7.5	3.9	-	3.0	0.0	-	-	-	-	-	-	-	-																	
Services	17	-	-	-	-	-	-	-	-	-	-	-	-	-	-																	
Science	18	3.6	0.5	0.6	0.5	0.2	0.0	1.0	0.7	0.0	7.1	0.1	0.0	12.7	7.4	-	124.1*															
Total expenditure (10+12+17+18)	19	263.9	68.1	108.6	69.9	86.8	35.9	28.2	19.2	5.0	685.6	32.3	13.4	0.0	-	124.1*	661.0															
Government & Financial Institutions	20	59.0	26.9	20.2	7.5	-5.0	0.0	1.3	6.0	0.4	116.3	-16.7*	-0.7*	206.6			124.1*															
Total supply (15+16 or 19+20)	21	322.9	95.0	128.8	77.4	81.8	35.9	29.5	25.2	5.4	801.9	15.6	12.7	-	43.3																	

T & C Transportation & communication.

T & D Trade & distribution.

Gothic figures—mean the data of IBMF and others the data of I-O Table.

Source: See Sverdlik, pp. 86~89 and pp. 104~105.

Table 2. the 7-sector table reconstructed by V. Trembl

(1972. billion rubles)

	Heavy industry	Light industry	Construction	Agriculture and forestry	T & C	T & D	Other branches	Total inter-industry use	Consumption	Investment and other	Exports	Total final demand	Total supply
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
1. Heavy industry	138,654.9	9,113.0	38,058.0	13,575.0	5,875.4	1,669.6	789.5	207,735.4	39,795.0	59,293.7	13,478.9	112,567.6	320,303.0
2. Light industry	6,250.1	72,661.8	746.9	4,698.6	223.6	936.9	64.6	85,582.5	139,178.0	1,161.4	3,564.1	143,903.5	229,486.0
3. Construction	0	0	0	0	0	0	0	0	0	77,400.0	0	77,400.0	77,400.0
4. Agriculture and forestry	2,820.0	59,349.7	49.9	23,948.3	5.1	250.7	46.3	86,470.0	29,059.0	2,319.0	708.0	32,086.0	118,556.0
5. Transportation & communications	24,326.2	3,207.5	93.9	1,377.7	25.9	195.5	303.3	29,530.0	0	0	0	0	29,530.0
6. Trade & distribution	6,481.8	13,735.7	0	4,555.3	0	0	512.2	25,285.0	0	0	0	0	25,285.0
7. Other branches	1,215.1	211.8	178.9	130.3	0	129.2	6.5	1,871.8	2,528.0	318.2	72.0	2,918.2	4,790.0
8. Total purchases	179,748.1	158,279.5	39,127.6	48,285.2	6,130.0	3,181.9	1,722.4	436,474.7	210,560.0	140,492.3	17,823.0	368,875.3	805,350.0
9. Depreciation	17,869.0	2,341.0	3,568.0	6,959.0	4,698.0	1,813.0	52.0	37,300.0	14,840.0	0	0	14,840.0	52,140.0
10. Labor income	46,090.0	10,923.0	25,750.0	51,239.0	9,071.0	11,118.0	1,006.0	155,197.0					
11. Surplus product	64,323.3	42,202.1	8,954.4	8,855.8	9,631.0	9,172.1	1,864.6	145,003.3					
12. Imports	12,272.6	15,740.4	0	3,217.0	0	0	145.0	31,375.0					
13. Total supply	320,303.0	229,486.0	77,400.0	118,556.0	29,530.0	25,285.0	4,790.0	805,350.0					
14. GVO	308,030.4	213,745.6	77,400.0	115,339.0	29,530.0	25,285.0	4,645.0	773,975.0					

T & C Transportation & communications.

T & D Trade & distribution.

GVO Gross value of output.

Source: See V. Trembl

values correspond to the concept of total supply (gross value of output plus imports) rather than to domestic output. The use of a total supply concept is a common Soviet practice in regard to highly aggregated tables.

Now let us compare Sverdlik's table with Treml's (see *table 3*). The two have almost the same data and the differences between them are minor. That means that Sverdlik's table may be reconstructed in much the same way with Treml's one. As Sverdlik says, his table, like Treml's 7-sector table, is reconstructed on an "establishment (ВЕДОМОСТВО)" basis, on which most Soviet economic statistics are recorded and reported. According to Sverdlik, so far as mutual transactions between organizations, enterprises and establishments on a "current-account-plan" are concerned, and so far as their current transactions with the financial-credit systems, "state budget" and "credit-cash-plan" are concerned, the IBMF formed from the I-O table on an "establishment" basis at purchasers' price may play an important role.³⁾ Thus, in order to compile the IBMF, there are no compulsion to make adjustments in their primary data, both inputs and outputs, but there is merely a requirement to enlarge a practical index system of financial balances. Concerning purchasers' price table, while in the I-O table valued at producers' price, the transaction of goods and services are valued at the price of shipment from producers, each transaction in the I-O table at purchasers' price is valued at purchasers' price including trade margin, transportation and distribution charges and excise (turnover) taxes, which accompanied the transaction of goods, as well as producers' cost and profits. As a consequence, in current purchasers' price tables the transportation and distribution rows reflect costs incurred not on sales of output, but on transportation in a manufacturing process.⁴⁾

As for treating imports on an I-O table, in general there are two methods. One is so-called "non-competitive import type", which treats imports and domestic goods as different products by the reason that they are produced in the different economic region, even if they are of the same quality. The another is "competitive import type" in which imports and domestic products are treated in the same way if they are of the same quality or are classified into the same sector. However, in the Sverdlik's I-O table, imports are neither separated into competing and noncompeting, nor into intermediate and final products. Instead, all imports are treated as competing; they are assigned to the appropriate producing sectors and are combined with those sectors' domestic output. Thus, the total value of each sector's sales equals its domestic production plus imports, i. e., total supply. Whereas exports are recorded in the conventional manner, as a vector in the final demand quadrant.

3) See (5) Sverdlik, page 41.

4) "Major difference in two types of Input-Output Tables is only whether the distributive margin is included in each transaction or not. However, this is a considerable difference from the aspect of making use of them. Since the table at Purchasers' Price shows the cost of production and the consumption according to the actual trade situation, it is convenient for the comparison with other economic data. While, in the Table at Producers' Price, the difference in valuation of transaction due to the difference in the distributive margin rate can be avoided, and it is suitable for the calculation of the repercussion effect." (See (5) Government of Japan, p. 138)

Table 3- A comparison of both tables (Trem1's & Sverdlik's)

A Study of National Accounts Tables of the Soviet Union and Its Industrial Structure

		Heavy industry		Light industry		Construction		Agriculture & forestry		T & C		T & D		Other branches		Total inter-industry use		Consumption		Investment & other		Exports		Total final demand	
		T	S	T	S	T	S	T	S	T	S	T	S	T	S	T	S	T	S	T	S	T	S	T	S
Total purchases	A	179.7	178.9	158.3	157.5	39.1	39.1	48.3	48.0	6.1	6.6	3.2	3.0	1.7	1.6	436.5	434.7	210.6	210.0	140.5	139.6	17.8	17.6	368.9	367.2
	B	1.004		1.005		1.000		1.000		0.924		1.067		1.063		1.004		1.003		1.006		1.011		1.005	
Depreciation	A	17.9	17.7	2.3	2.4	3.6	3.6	7.0	7.1	4.7	4.4	1.8	1.9	0.1	0.0	37.3	37.1	14.8	15.4	0	0	0	0	14.8	15.4
	B	1.011		0.958		1.000		0.986		1.068		0.947		—		1.005		0.961		—		—		0.961	
Labor income	A	46.1	45.8	10.9	12.0	25.8	25.8	51.2	50.6	9.1	9.2	11.1	10.4	1.0	3.4	155.2	157.2								
	B	1.007		0.908		1.000		1.012		0.989		1.067		0.250		0.987									
Surplus product	A	64.3	65.3	42.2	40.5	9.0	8.9	8.9	9.0	9.6	9.3	9.2	9.9	0.1	0.4	145.0	143.3								
	B	0.985		1.042		1.011		0.989		1.032		0.929		0.250		1.012									
Imports	A	12.3	15.2	15.7	11.4	0	0	3.2	3.0	0	0	0	0	0.1	0	31.4	29.6								
	B	0.809		1.377		—		1.067		—		—		—		1.061									
Total supply	A	320.3	322.9	229.5	223.8	77.4	77.4	118.6	117.7	29.5	29.5	25.3	25.2	4.8	5.4	805.4	801.9								
	B	0.992		1.025		1.000		1.008		1.000		1.000		0.889		1.004									
Gross value of output	A	308.0	307.7	213.7	212.4	77.4	77.4	115.3	114.7	29.5	29.5	25.3	25.2	4.6	5.4	774.0	772.3								
	B	1.001		1.006		1.000		1.005		1.000		1.000		0.852		1.002									

T: I-O table of Trem1.
 S: I-O table of Sverdlik.
 B=TA/SA.

Table 4. Revised "Income-goods" table

		Productive												Non-Productive					Others	Exports	Total	Revenue or Income												
		G. F. C. F.				I. S.				G. F. C. F.				I. S.	Industries & others	Construction	Total	Service sec.				Science sec.	Household	Government	F. I.	Total								
		Industries & others	Construction	Industries & others	Construction	Service sec.	Science sec.	Household	Government	Service sec.																								
1	2	4	5	6	7	8	9	10	11	12	13(1)	13(2)	14(1)	14(2)	15(4)	15(5)	15(6)	15(7)	16(4)	17	18	19	20	21	22	23	24	25	26	27	28			
Semi-Productive Activities	Industries & others	1	a_{11} 395.6	a_{13} 39.1	c_4 5.4	c_5 5.4	c_6 190.3	c_7 8.9	644.7			k_{11} 32	k_{12} 1.7	i_{11} 8.2	i_{12} 0.3	k_{14} 1.4	k_{15} 0.8	k_{16} 0.3	k_{17} 2.1	i_{14} 0.3	p_1 15.1	e_1 17.6	x_1 724.5	$k_{11}+i_{11}$ 40.2	k_{21} 42.0	82.2								
	Construction	2	0	0	0	0	0	0	0			k_{21} 42	k_{22} 2.5	0	0	k_{24} 18.3	k_{25} 1.1	k_{26} 3.3	k_{27} 10.2	0			x_2 77.4	$k_{12}+i_{12}$ 2.0	k_{22} 2.5	4.5								
	Non-productive sectors	4 5 7	0	0	0	0	0	0	0														15.6	$k_{14}+i_{14}$ 12.7	k_{24} 42.0	20.0								
	Depreciation	8	d_1 33.5	d_2 3.6	d_4 3.5	d_5 6.1	(d_6) 27.4	d_7 3.2	d 44.7															d_1 33.5	d_2 3.6	d_0 37.1	d_4 3.5	d_5 0.9		d_7 3.2	d 44.7			
	Labor income	9	w_1 131.4	w_2 25.8	w_4 6.8	w_5 6.1	—	w_7 27.4	w 197.5																									
	Surplus product	10	p_1 134.4	p_2 8.9	p_4 -0.1	p_5 0.3	—	p_7 2.8	p 146.3															p_1 134.4	p_2 8.9	p_0 143.3	p_4 -0.1	p_5 0.3		β_7 2.8	p 146.3			
	Imports	11	m_1 29.6	m_2 0	m_4 0	m_5 0	m_6 0	m_7 0	m 29.6															m 29.6										
Total supply	12	x_1 724.5	x_2 77.4	x_4 15.6	x_5 12.7	x_6 190.3	x_7 42.3	x 1062.8	15.6	12.7	(m') 190.3	42.3	74	4.2	8.2	0.3	19.7	1.9	3.6	12.3	0.3	15.1	17.6											
Expenditure	Industries & others	13	A_{11} 435.8	A_{21} 42.0	0	S_1 6.6	W_1 131.4	B_1 108.7	X_1 724.5			$k_{11}(32)$ $k_{21}(42)$		i_{11} 8.2																			B_{13} 108.7	197.5
	Construction	14	A_{12} 41.1	A_{22} 2.5	0	S_2 0.5	W_2 25.8	B_2 7.5	X_2 77.4				$k_{12}(1.7)$	i_{12} 0.3																			B_{14} 7.5	12.5
	Service sec.	16	C_4 7.1	C_4 18.3	—	S_4 0.1	W_4 6.8	B_4 -16.7	X_4 15.6				$k_{22}(2.5)$		$k_{14}(1.4)$ $k_{24}(18.3)$					i_{14} 0.3												B_{16} -16.7	3.4	
	Science sec.	17	C_5 6.2	A_5 1.1	0	—	W_5 6.1	B_5 -0.7	X_5 12.7							$k_{15}(0.8)$ $k_{25}(1.1)$																B_{17} -0.7	1.2	
	Household	18	C_6 190.6	A_6 3.3	c_5 12.7	S_6 0	—	B_6 25.2	X_6 231.8	c_5 12.7	S_6 0.0	$c_6(m')$ 190.3					$k_{16}(0.3)$ $k_{26}(3.3)$														B_{18} (-m')	231.8		
	Government	19	C_7 11.0	A_7 10.2	0	S_7 7.4	W_7 27.4		F				F_8 42.3																			(m')	(m')	
	Financial institutions	20	F_1 32.7	F_2 0	F_4 2.9	F_5 -1.9	F_6 34.3		124.0		F_4 2.9	F_5 -1.9																					(m')	62.0
Total revenue	21	X_1 724.5	X_2 77.4	X_4 15.6	X_5 12.7	X_6 231.8	B 124.0	X 1186.6	x_4 15.6	x_5 12.7	x_6 190.3	x_7 42.3	74	4.2	8.2	0.3	19.7	1.9	3.6	12.3	0.3	15.1	17.6									124.0		

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Table 5. The tabular form of revised "Income-goods" table

	1 ~ 8	9 ~ 19	20 ~ 22	
1 } 7	I	III	IV	
8 } 12	II			V
13 } 21	VIII	VII		VI

note: →: the flow of goods.
 ⇨: the flow of income.
 VIII: IBMF.
 IV: a special district.

As next step, we would like to explain the structure of the revised "income-goods" (see table 4), which integrates both tables (IBMF and the I-O table). For that purpose table 5 will be of much use for us. As you see, table 5 may be divided into the 8 following sections, and arabic figures at the inner margin of table 5 correspond with arabic figures at the same place of table 4. Section I in table 5 refers to intermediate transactions, section II—the crude value added sector, section III—the final demand sector, including consumption, accumulation (gross fixed capital formation by productive- and nonproductive sectors, increase in stocks by sectors), others and exports, section IV—a special district different from the other area in entering way, which may be shown by symbols at the same area in table 4, section V—the first-income-distribution sector, where it is shown that each income including depreciation belongs to each sector arranged at the upper margin of the table, section VI—the income redistribution sector, i. e., the transfer transaction sector, section VII—the final expenditure, where every transaction means purchasing goods and service from section III and section VIII—IBMF table.

Getting the explain back on table 4, we find an ordinary I-O table in the section "1-12; 1-19", around which there are some receiving and expending income- or transfer-transaction sectors ("13-21; 1-28" and "1-21; 20-28"). IBMF is included in a quadrant (southwest) "13-21; 1-8". About this IBMF we must pay special attention to the fact that the data of this IBMF is given as a transposed matrix, which means that the data of the columns of IBMF in table 4 corresponds to the data of the row of IBMF in table 1. The first column (industry & others) in the quadrant of IBMF measures the flows of revenue of this sector from sectors shown at the left side of this table (from the 13th row to the 20th row) through the object - transaction. This flow of revenue corresponds to the flow of products of "industry & others" sold to the topmost sectors of this table. Here (a_{11}) means the product of "industry & others" delivered to and consumed as raw material by "industry & others" itself (inner transaction), while (A_{11}) means the product delivered to but not entirely consumed by its sector, i. e., $(A_{11}) - (a_{11})$ means the increase of stocks in this sector (a kind of investment). If, for example, government

purchased C_7 (11.0) from the 1st sector and consumed c_7 (8.7) in government itself, then $(C_7 - c_7) = 2.1 = k_{17}$ means the increase of goods bought from the 1st sector, and the gross fixed capital formation (construction) in the government sector is recorded in $A_7 = 10.2 = k_{27}$.

What does F_1 ("20; 1") = 32.7 mean? The answer may be found in $F_{17} + F_{18}$ ("20; 17-18") = 15.1 + 17.6, i. e., it means that "Financial institutions (or Government)" has bought $b_1 = F_{17} = 15.1$ from the "others" sector and $e_1 = F_{18} = 17.6$ from the "exports" sector. In this case, "Financial institutions" (or Government, in practice "foreign trade association") buys export goods from the "Industries & others" sector and then sells them to foreign countries. On the other hand in the case of imports, as the table shows, the value of import goods (m_1) may be absorbed into the total supply value and its cost (or value of import goods) may be compensated for by selling goods of the 1st sector. Therefore, in so far as some goods of the 1st sector are purchased the cost of import goods should be borne in proportion to that ratio. The revenue from import goods concealed in gross sales will, sooner or later, be absorbed into the state budget as turnover tax or a profit-deduction system (some part of $(B_{13} = 108.7)$).

Now let us take up a case of imports of final demand goods (for example, consumers' goods — trace the flow of "m" in table 4). In this case we posit that consumers' goods imported are purchased by the "Household" sector with money drawn from bank savings (see "-m'" in B_{18}) and "government" gets the money by selling those goods (in practice, not "government" but "foreign trade association" — see "+m'" in "11; 26").

Now let us examine the balance relations in this table. We will prove the following equations (We assume, in this case, the following variables as given; $s_1 \sim s_7, cs, c_6, w_1 \sim w_7, k, l, b, e$, and I-O table):

$$(1) \quad A_{11} = a_{11} + k_{11} + i_{11} = 395.6 + 32 + 8.2 = 435.8$$

$$(2) \quad A_{12} = a_{12} + k_{12} + i_{12} = 39.1 + 1.7 + 0.3 = 41.1$$

$$(3) \quad A_{21} = a_{21} + k_{21} = 42.0$$

$$(4) \quad A_{22} = a_{22} + k_{22} = 2.5$$

$$(5) \quad C_4 = c_4 + k_{14} + i_{14} = 7.1$$

$$(6) \quad A_4 = k_{24} = 18.3$$

$$(7) \quad C_5 = c_5 + k_{15} = 5.4 + 0.8 = 6.2$$

$$(8) \quad A_5 = k_{25} = 1.1$$

$$(9) \quad C_6 = c_6 + k_{16} = 190.3 + 0.3 = 190.6$$

$$(10) \quad A_6 = k_{26} = 3.3$$

$$(11) \quad C_7 = c_7 + k_{17} = 8.9 + 2.1 = 11.0$$

$$(12) \quad A_7 = k_{27} = 10.2$$

$$(13) \quad F_1 = X_1 - (A_{11} + A_{12} + C_4 + C_5 + C_6 + C_7) = 32.7$$

$$(14) \quad F_2 = X_2 - (A_{21} + A_{22} + A_4 + A_5 + A_6 + A_7) = 0$$

$$(15) \quad F_4 = X_4 - cs = 2.9$$

$$(16) \quad F_5 = X_5 - \left(\sum_{i=1}^7 S_i \right) = -1.9$$

As a next step, we must determine B series in IBMF as follows:

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$$(17) \quad B_1 = X_1 - (A_{11} + A_{21} + S_1 + W_1) = 108.7$$

$$(18) \quad B_2 = X_2 - (A_{12} + A_{22} + S_2 + W_2) = 7.5$$

$$(19) \quad B_4 = X_4 - (C_4 + A_4 + S_4 + W_4) = -16.7$$

$$(20) \quad B_5 = X_5 - (C_5 + A_5 + W_5) = -0.7$$

Herein we find that the system cannot independently decide **B** (payment of "household" sector into "government" sector, i. e., income tax, public charges, insurance, savings, purchase of government bonds and so on). **B** must be decided in accordance with statistical data based on reality. Given **B** as 25.2 in the table, it follows that:

$$(21) \quad X_6 = 231.8, \quad F = B = 124.0, \quad F_6 = 34.3 \quad \text{and} \quad X = 1186.6$$

In connection with this, we should take note of the fact that $X : x = 1186.6 : 1062.8 = 1.12$ means, in a sense, a deflator of the national economy (or a kind of index of inflation) and it depends upon the size of **B**, which shows the volume necessary for absorbing the purchasing power of people into the "government" sector.

Of course it is simple to prove the following equation:

$$\sum_{i=1}^6 B_i = C_7 + A_7 + S_7 + W_7 + \sum_{i=1}^6 F_i \quad (B_3 = F_3 = 0)$$

Next, let us determine the **B** and **F** series in section VI and VII. According to the entering rule of this table, **B** should have the following relation:

$$(22) \quad B_{13} = (d_1 + p_1 + m_1) - (s_1 + k_{11} + k_{21} + i_{11}) = 108.7$$

where $B_{13} = B_1$

Because of:

$$\begin{aligned} B_1 &= X_1 - (A_{11} + A_{21} + S_1 + W_1) \\ &= a_{11} + d_1 + w_1 + p_1 + m_1 - [(a_{11} + k_{11} + i_{11}) + k_{21} + s_1 + w_1] \\ &= (d_1 + p_1 + m_1) - (s_1 + k_{11} + k_{21} + i_{11}) = 108.7 \end{aligned}$$

$$(23) \quad B_{14} = (d_1 + p_1) - (s_2 + k_{12} + k_{22} + i_{12}) = 7.5$$

similarly $B_{14} = B_2$

$$(24) \quad B_{16} = (d_4 + p_4) - (s_4 + k_{14} + k_{24} + i_{14}) = -16.7$$

similarly $B_{16} = B_4$

$$(25) \quad B_{17} = (d_4 + p_4) - (s_5 + k_{15} + k_{25}) = -0.7$$

similarly $B_{17} = B_5$

Now, if we assume that $B_{18} = B_6 = 25.2$, then we get $F'_6 = 34.3$. Because $cs + s_6 + c_6 + k_{16} + k_{26} + B_{18} = W + F'_6 \rightarrow F'_6 = 34.3$.

At this point we will prove the balance relation $F'_6 = F_6$ under the relation of $B_{18} = B_6$

$$\begin{aligned} F_6 &= X_6 - \sum_i W_i \\ F'_6 &= (cs + s_6 + c_6 + k_{15} + k_{25} + B_{18}) - W \\ &\text{where } X_6 = cs + s_6 + c_6 + k_{15} + k_{25} + B_{18} \quad (\text{see "18; 9~27"}) \\ &\text{therefore } F_6 = F'_6 \end{aligned}$$

As for the "government" sector, we assume a balance relation as follows:

$$(26) \quad F_7 = (S_7 + F_8 + k_{17} + k_{27}) - (d_7 + p_7) = 56.0$$

Up to this point, we have decided all variables upon the relation that the revenue of each sector is equal to the each expenditure. According to the entering rule of the table, we enter the following figures; 2.9 in F'_4 , -1.9 in F'_5 , 15.1 in F_{17} and 17.6 in

F_{18} .

Using these conditions, we attempt to prove the following:

$$(27) \quad \sum F_j = \sum B_i \quad (j=4, 5, 6, 7, 17, 18, i=13, 14, 16, 17, 18)$$

$$(28) \quad CS + S + C_6 + F_8 + K + I + B = D + P + W + m + F'_6 + F_7$$

$$\text{(where } B = B_{13} + B_{14} + B_{16} + B_{17} + B_{18}\text{)}$$

Since section V = section VII (in table 5)

(29) We get

$$D + P + W + m = F'_4 + F'_5 + F_{17} + F_{18} + S + SC + C_6 (=x_6) + F_8 + K + I$$

$$(28) + (29) \quad B = F'_6 + F_7 + F'_4 + F'_5 + F_{17} + F_{18}$$

II. An analysis of the effect of final demand⁵⁾

In this section we attempt to characterize the production structure of the Soviet Union by the use of the I-O table.

Table 6 shows the original input data of the I-O tables in 1959, 1966 and 1972 prepared by Sverdlik. Using these data, we get the "input coefficients" of each table (see *table 7*; Divided matrix-I), the structure of industry based on total supply and the structure dynamics (see *table 8*). As you see in *table 8*, the industry structure has undergone a minor transformation in the 1960's, except for heavy, light and food industries. Among these sectors, heavy industry (including mining) is the only section which raised its own ratio to the total output. Average rate of growth a year of this sector for 13 years was 9.8% and while total output average rate of growth was 7.7%. Let us take note of the ratio $\frac{\sum a_{ij}}{x_j}$ or $\frac{\sum \sum a_{ij}}{\sum x_j}$, which here means effectiveness of production (so-called **Материалоемкость**). We can see that the ratio $\left(\frac{\sum \sum a_{ij}}{\sum x_j}\right)$ was worsening gradually: 50.3% (1959), 51.8% (1966) and 54.2% (1972). This tendency is, as a whole, found in each sector too.

Next, we calculate delivery ratios $\frac{a_{ij}}{x_i}$ ($i=1, \dots, 9; j=1, \dots, 9$), which show the ratio of product used by each sector to total demand for each good. Concerning the "agriculture (private)" sector, we can say that the ratio of product in this sector directly consumed by the "consumption" sector was keeping almost more than half of its production (see "6; 16" of *table 10*), whereas in the socialized "agriculture" sector, more than half of the product was used for the "food industry" sector in 1962 and 1972 (see "5; 3") and the ratio of total interindustry use of its sector's product was approximately 80% or more (see "5; 10").

It can be thought that every industry produces goods to support the final demand such as consumption, capital formation and exports in the end. This means, in a sense, that every product is generated by the final demand. Now we analyze the dynamics of total supply generated by the final demand sectors (R (I)) and their coefficients (R (2)) (see *table 10*). A conventional calculation process is as follows.

$$R (I) = (I - A)^{-1} [C \cdot I \cdot E]$$

5) I am grateful to Mrs. Sachiko Mineno for her assistance. By using of the computer of Hokkaido University, she made a calculation of most of data in this section.

Table 6. Input-Output Table of each year (Original Input Data)

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1959																															
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
1	35.4	1.3	1.6	13.6	3.7	0.0	3.2	1.2	0.4	60.4	8.9	2.0	1.2	1.1	4.3	13.2	8.1	0.0	8.1	0.9	0.2	1.1	3.7	0.0	3.7	0.6	4.7	18.2	3.5	95.3	
2	2.4	15.4	0.2	0.6	0.0	0.0	0.2	0.5	0.0	19.3	19.5	0.0	0.0	0.8	0.8	20.3	0.0	0.0	0.0	0.0	0.0	0.0	1.5	0.0	1.5	0.0	1.2	2.7	0.6	42.8	
3	0.9	0.7	13.3	0.0	1.6	0.0	0.0	0.0	0.0	16.5	37.8	0.0	0.0	1.2	1.2	39.0	0.0	0.0	0.0	0.0	0.0	0.0	1.4	0.0	1.4	0.0	1.4	2.8	0.5	58.8	
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	16.3	0.0	16.3	9.7	3.2	12.9	0.0	0.0	0.0	0.0	0.0	29.2	0.0	29.2	
5	0.3	4.4	14.5	0.0	5.0	3.3	0.0	0.0	0.0	27.5	2.6	0.0	0.0	0.6	0.6	3.2	1.4	0.0	-0.4	0.0	0.0	0.0	2.5	0.0	2.5	0.0	-1.0	2.0	0.7	33.4	
6	0.0	0.1	2.0	0.0	0.0	4.2	0.0	0.0	0.0	6.3	14.5	0.0	0.0	0.0	0.0	14.5	0.0	-0.4	1.4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	20.4	
7	8.6	0.4	1.2	0.1	0.8	0.0	0.0	0.1	0.1	11.3	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	-0.4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	11.3	
8	3.2	1.4	3.7	0.0	2.9	0.0	0.0	0.0	0.0	11.2	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	11.2	
9	0.7	0.1	0.0	0.3	0.0	0.0	0.0	0.0	0.0	1.1	1.9	0.0	0.0	0.2	0.2	2.1	0.0	0.0	0.0	0.0	0.0	0.0	0.1	0.0	0.1	0.0	-0.1	0.0	0.0	3.2	
T	51.5	23.8	36.5	14.0	14.0	7.5	3.4	0.8	0.5																						
D	4.7	0.3	0.5	0.7	1.7	0.4	1.2	0.3	0.0																						
L	19.3	2.8	1.9	11.0	13.5	12.2	4.0	4.2	2.4																						
S	16.9	12.5	18.4	2.0	2.8	0.0	2.5	4.9	0.3																						
T	36.2	15.3	20.3	13.9	16.3	12.2	6.5	9.1	2.7																						
P	92.5	39.3	57.3	29.2	32.0	20.4	11.3	11.2	3.2																						
M	2.8	3.5	1.5	0.0	1.4	0.0	0.0	0.0	0.0																						
TS	95.3	42.8	58.8	29.2	33.4	20.4	11.3	11.2	3.2																						
1966																															
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
1	72.4	2.2	2.4	21.3	5.7	0.0	3.9	1.2	0.6	109.7	14.7	3.1	2.9	1.9	7.9	22.6	17.7	0.0	17.7	2.2	0.2	2.4	3.4	0.0	3.4	0.4	9.2	33.1	7.3	172.7	
2	1.9	27.0	0.5	0.6	0.3	0.0	0.2	0.3	0.0	38.8	27.5	0.0	0.0	1.3	1.3	28.8	0.0	0.0	0.0	0.0	0.0	0.0	0.2	0.0	0.2	0.0	1.4	1.6	0.9	62.1	
3	0.0	0.7	22.1	0.1	0.9	0.0	0.0	0.3	0.0	25.0	62.0	0.0	0.0	2.3	2.3	64.3	0.0	0.0	0.0	0.0	0.0	0.0	1.7	0.0	1.7	0.0	1.0	2.7	1.0	93.0	
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	24.0	0.0	24.0	16.5	3.0	12.5	0.0	0.0	0.0	0.0	0.0	43.5	0.0	43.5	
5	0.7	5.2	27.9	0.0	6.4	2.9	0.0	0.1	0.0	43.2	3.7	0.0	0.0	0.7	0.7	4.4	0.4	0.0	0.4	0.0	0.0	0.0	6.2	0.0	6.2	0.0	0.8	7.4	0.4	55.4	
6	0.0	0.2	3.3	0.0	0.0	8.3	0.0	0.0	0.0	11.8	17.4	0.0	0.0	0.0	0.0	17.4	0.0	0.4	0.4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.4	0.0	29.6	
7	15.9	0.4	1.5	0.1	0.9	0.0	0.0	0.1	0.1	19.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	19.0	
8	3.9	1.7	7.0	0.0	2.8	0.0	0.0	0.0	0.3	15.7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	15.7	
9	0.7	0.0	0.0	0.5	0.1	0.0	0.0	0.1	0.0	1.4	2.4	0.0	0.0	0.2	0.2	2.6	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	4.0	
T	96.4	37.4	64.7	22.6	17.1	11.2	4.1	2.1	1.0																						
D	9.9	0.5	1.0	1.8	4.0	0.4	2.7	1.2	0.0																						
L	30.4	4.5	3.5	15.9	20.0	18.0	6.5	7.2	2.7																						
S	30.2	14.6	21.4	3.2	12.3	0.0	5.7	5.2	0.3																						
T	60.6	19.1	24.9	19.1	32.3	18.0	12.2	12.4	3.9																						
P	166.9	57.0	90.6	43.5	53.4	29.6	19.0	15.7	4.0																						
M	5.8	5.1	2.4	0.0	2.0	0.0	0.0	0.0	0.0																						
TS	172.7	62.1	93.0	43.5	55.4	29.6	19.0	15.7	4.0																						

1972

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
1	140.2	4.2	4.1	38.1	13.3	0.0	6.4	1.5	0.6	208.4	26.2	5.4	5.4	3.0	13.8	40.0	32.6	0.0	32.6	4.3	0.3	4.6	4.2	0.0	4.2	0.3	17.8	59.5	15.0	322.9	
2	2.8	41.4	0.8	0.6	0.4	0.0	0.2	0.3	0.1	46.6	44.5	0.0	0.0	1.8	1.8	36.3	0.0	0.0	0.0	0.0	0.0	0.0	1.4	0.0	1.4	0.0	-0.3	1.1	1.0	95.0	
3	1.3	0.5	30.0	0.1	4.3	0.0	0.0	0.7	0.0	36.9	88.3	0.0	0.0	3.2	3.2	91.5	0.0	0.0	0.0	0.0	0.0	0.0	-0.2	0.0	-0.2	0.0	-0.3	-0.5	0.9	128.8	
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	44.5	0.0	44.5	29.6	3.3	32.0	0.0	0.0	0.0	0.0	0.0	0.0	77.4	0.0	77.4
5	2.4	8.6	45.7	0.0	13.3	0.0	0.0	0.2	0.0	70.2	8.3	0.0	0.0	0.7	0.7	9.0	0.0	0.0	0.0	0.0	0.0	0.0	2.9	0.0	2.9	0.0	-1.9	1.9	0.7	81.8	
6	0.0	0.3	4.7	0.0	0.0	10.6	0.0	0.0	0.0	15.6	20.1	0.0	0.0	0.0	0.0	20.4	0.0	0.2	0.2	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.2	0.0	35.9
7	24.3	0.9	2.3	0.1	1.4	0.0	0.0	0.2	0.3	29.5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	29.5
8	6.3	2.9	10.9	4.6	0.0	0.0	0.0	0.0	0.5	25.2	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	25.2
9	1.6	0.1	0.1	0.4	0.2	0.0	0.0	0.1	0.1	2.3	2.9	0.0	0.0	0.2	0.2	3.1	0.0	0.0	0.0	0.0	0.0	0.0	0.2	0.0	0.2	0.0	-0.2	0.0	0.0	5.4	
T	178.9	58.9	98.6	39.1	37.4	10.6	6.6	3.0	1.6																						
D	17.7	0.8	1.6	3.6	6.5	0.6	4.4	1.0	0.0																						
L	45.8	6.7	5.3	25.8	25.9	24.7	9.2	10.4	3.4																						
S	65.3	21.1	19.4	8.9	9.9	0.0	9.3	9.9	0.4																						
T	111.1	27.8	24.7	34.7	34.9	24.7	18.5	20.3	3.8																						
P	307.7	87.5	124.9	77.4	78.8	35.9	29.5	25.2	5.4																						
M	15.2	7.5	3.9	0.0	3.0	0.0	0.0	0.0	0.0																						
TS	322.9	95.0	128.8	77.4	81.8	35.9	29.5	25.2	5.4																						

Note: Figures in the input-output table are given in terms of organizational-units-base at current purchasers' price.

- | | |
|---|--|
| 1. Heavy industry. | 19. Total of these. |
| 2. Light industry. | 20. Non-productive social investment. |
| 3. Food industry. | 21. Non-productive private investment. |
| 4. Construction. | 22. Total of these |
| 5. Agriculture (Socialized sector). | [Increase in stocks] |
| 6. Agriculture (private sector). | 23. Productive social increase in stocks. |
| 7. Transportation & communications. | 24. Productive private increase in stocks. |
| 8. Trade and distribution. | 25. Total of these. |
| 9. Other branches. | 26. Non-productive increase in stocks. |
| 10. Total interindustry use. | 27. Others. |
| [Consumption] | 28. Total of "accumulation & others". |
| 11. Household. | 29. Exports. |
| 12. Services. | 30. Total. |
| 13. Science & scientific services. | T: Total. |
| 14. Public administration & other services. | D: Depreciation. |
| 15. Total of service sector. | L: Labor income. |
| 16. Total of consumption. | S: Surplus product. |
| [Accumulation & others] | P: Gross value of output. |
| (Gross fixed capital formation). | M: Imports. |
| 17. Productive social investment. | TS: Total supply. |
| 18. Productive private investment. | |

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Table 7. DIVIDED MATRIX-I: $\frac{a_{ij}}{X_j}$ & $\frac{T}{X_j}$, $\frac{D}{X_j}$, $\frac{L}{X_j}$, $\frac{S}{X_j}$, $\frac{P}{X_j}$, $\frac{M}{X_j}$ ($i, j=1, \dots, 9$)

1959

	1	2	3	4	5	6	7	8	9
1	0.3715	0.0304	0.0272	0.4658	0.1108	0.0	0.2832	0.1071	0.1250
2	0.0252	0.3598	0.0034	0.0205	0.0	0.0	0.0177	0.0446	0.0
3	0.0094	0.0164	0.2262	0.0	0.0479	0.0	0.0	0.0	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0031	0.1028	0.2466	0.0	0.1497	0.1618	0.0	0.0	0.0
6	0.0	0.0023	0.0340	0.0	0.0	0.2059	0.0	0.0	0.0
7	0.0902	0.0093	0.0204	0.0034	0.0240	0.0	0.0	0.0089	0.0313
8	0.0336	0.0327	0.0629	0.0	0.0868	0.0	0.0	0.0	0.0
9	0.0073	0.0023	0.0	0.0103	0.0	0.0	0.0	0.0	0.0
T	0.5404	0.5561	0.6207	0.4795	0.4192	0.3676	0.3009	0.0714	0.1563
D	0.0493	0.0070	0.0085	0.0240	0.0509	0.0196	0.1062	0.0268	0.0
L	0.2025	0.0654	0.0323	0.3767	0.4042	0.5980	0.3540	0.3750	0.7500
S	0.1773	0.2921	0.3129	0.0685	0.0838	0.0	0.2212	0.4375	0.0938
T	0.3799	0.3575	0.3452	0.4760	0.4880	0.5980	0.5752	0.8125	0.8437
P	0.9706	0.9182	0.9745	1.0000	0.9581	1.0000	1.0000	1.0000	1.0000
M	0.0294	0.0818	0.0255	0.0	0.0419	0.0	0.0	0.0	0.0

1966

	1	2	3	4	5	6	7	8	9
1	0.4192	0.0354	0.0258	0.4897	0.1029	0.0	0.2053	0.0764	0.1500
2	0.0110	0.4348	0.0054	0.0138	0.0054	0.0	0.0105	0.0191	0.0
3	0.0	0.0113	0.2376	0.0023	0.0162	0.0	0.0	0.0191	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0041	0.0837	0.3000	0.0	0.1155	0.0980	0.0	0.0064	0.0
6	0.0	0.0032	0.0355	0.0	0.0	0.2804	0.0	0.0	0.0
7	0.0921	0.0064	0.0161	0.0023	0.0162	0.0	0.0	0.0064	0.0250
8	0.0226	0.0274	0.0753	0.0	0.0505	0.0	0.0	0.0	0.0750
9	0.0041	0.0	0.0	0.0115	0.0018	0.0	0.0	0.0064	0.0
T	0.5582	0.6023	0.6957	0.5195	0.3087	0.3784	0.2158	0.1338	0.2500
D	0.0573	0.0081	0.0108	0.0414	0.0722	0.0135	0.1421	0.0764	0.0
L	0.1760	0.0725	0.0376	0.3655	0.3610	0.6081	0.3421	0.4586	0.6750
S	0.1749	0.2351	0.2301	0.0736	0.2220	0.0	0.3000	0.3312	0.0750
T	0.3509	0.3076	0.2677	0.4391	0.5830	0.6031	0.6421	0.7898	0.9750
P	0.9664	0.9179	0.9742	1.0000	0.9639	1.0000	1.0000	1.0000	1.0000
M	0.0336	0.0821	0.0258	0.0	0.0361	0.0	0.0	0.0	0.0

1972

	1	2	3	4	5	6	7	8	9
1	0.4342	0.0442	0.0318	0.4922	0.1626	0.0	0.2169	0.0595	0.1111
2	0.0087	0.4358	0.0062	0.0078	0.0049	0.0	0.0068	0.0119	0.0185
3	0.0040	0.0053	0.2329	0.0013	0.0526	0.0	0.0	0.0278	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0074	0.0905	0.3548	0.0	0.1626	0.0	0.0	0.0079	0.0
6	0.0	0.0032	0.0365	0.0	0.0	0.2953	0.0	0.0	0.0
7	0.0753	0.0095	0.0179	0.0013	0.0171	0.0	0.0	0.0079	0.0556
8	0.0195	0.0305	0.0846	0.0594	0.0	0.0	0.0	0.0	0.0926
9	0.0050	0.0011	0.0008	0.0052	0.0024	0.0	0.0	0.0040	0.0185
T	0.5540	0.6200	0.7655	0.5052	0.4572	0.2953	0.2237	0.1190	0.2963
D	0.0548	0.0084	0.0124	0.0465	0.0795	0.0167	0.1492	0.0397	0.0
L	0.1418	0.0705	0.0411	0.3333	0.3166	0.6880	0.3119	0.4127	0.6296
S	0.2022	0.2221	0.1506	0.1150	0.1210	0.0	0.3153	0.3929	0.0741
T	0.3441	0.2926	0.1918	0.4483	0.4267	0.6880	0.6271	0.8056	0.7037
P	0.9529	0.9211	0.9697	1.0000	0.9633	1.0000	1.0000	1.0000	1.0000
M	0.0471	0.0789	0.0303	0.0	0.0367	0.0	0.0	0.0	0.0

Table 8. The structure of the industry by total supply (nominal)
(billion rubles)

	year	value	the compo- nent ratio (%)	Increase		
				For 5 years (%)	value	Increase contribution ratio (%)
1. Heavy industry	1959	95.3	31.18	—	—	—
	1966	172.7	34.89	81.2	77.4	40.9
	1972	322.9	40.27	87.0	150.2	48.9
2. Light industry	1959	42.8	14.00	—	—	—
	1966	62.1	12.55	45.1	19.3	10.2
	1972	95.0	11.85	53.0	32.9	10.7
3. Food industry	1959	58.8	19.24	—	—	—
	1966	93.0	18.79	58.6	34.2	18.1
	1972	128.8	16.06	38.5	35.8	11.7
4. Construction	1959	29.2	9.55	—	—	—
	1966	43.5	8.79	49.0	14.3	7.6
	1972	77.4	9.65	77.9	33.9	11.0
5. Agriculture (socialized sector)	1959	33.4	10.93	—	—	—
	1966	55.4	11.19	65.9	22.0	11.6
	1972	81.8	10.20	47.7	26.4	8.6
6. Agriculture (private sector)	1959	20.4	6.68	—	—	—
	1966	29.6	5.98	45.1	9.2	4.9
	1972	35.9	4.48	21.3	6.3	2.1
7. Transportation & communications	1959	11.3	3.70	—	—	—
	1966	19.0	3.84	68.1	7.7	4.1
	1972	29.5	3.68	55.3	10.5	1.3
8. Trade & distribution	1959	11.2	3.66	—	—	—
	1966	15.7	3.17	40.2	4.5	2.4
	1972	25.2	3.14	60.5	9.5	3.1
9. Other branches	1959	3.2	1.05	—	—	—
	1966	4.0	0.81	25.0	0.8	0.4
	1972	5.4	0.67	35.0	1.4	0.5
10. Total	1959	305.6	100.0	—	—	—
	1966	495.0	100.0	62.0	189.4	100.0
	1972	801.9	100.0	62.0	306.9	100.0

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Table 9. DIVIDED MATRIX-2: $\frac{a_{ij}}{\bar{x}_i}$ ($i, j=1, \dots, 9$)

1959									
	1	2	3	4	5	6	7	8	9
1	0.3715	0.0136	0.0168	0.1427	0.0388	0.0	0.0336	0.0126	0.0042
2	0.0561	0.3598	0.0047	0.0140	0.0	0.0	0.0047	0.0117	0.0
3	0.0153	0.0119	0.2262	0.0	0.0272	0.0	0.0	0.0	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0090	0.1317	0.4341	0.0	0.1497	0.0988	0.0	0.0	0.0
6	0.0	0.0049	0.0980	0.0	0.0	0.2059	0.0	0.0	0.0
7	0.7611	0.0354	0.1062	0.0088	0.0708	0.0	0.0	0.0088	0.0088
8	0.2857	0.1250	0.3304	0.0	0.2589	0.0	0.0	0.0	0.0
9	0.2187	0.0313	0.0	0.0938	0.0	0.0	0.0	0.0	0.0

	10	11	12	13	14	15	16	17	18	19
1	0.6338	0.0934	0.0210	0.0126	0.0115	0.0451	0.1385	0.0850	0.0	0.0850
2	0.4509	0.4556	0.0	0.0	0.0187	0.0187	0.4743	0.0	0.0	0.0
3	0.2806	0.6429	0.0	0.0	0.0204	0.0204	0.6633	0.0	0.0	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5582	0.0	0.5582
5	0.8234	0.0778	0.0	0.0	0.0180	0.0180	0.0958	0.0419	0.0	0.0419
6	0.3088	0.7108	0.0	0.0	0.0	0.0	0.7108	0.0	-0.0196	-0.0196
7	1.0000	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
8	1.0000	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
9	0.3438	0.5937	0.0	0.0	0.0625	0.0625	0.6563	0.0	0.0	0.0

	20	21	22	23	24	25	26	27	28	29
1	0.0094	0.0021	0.0115	0.0388	0.0	0.0388	0.0063	0.0493	0.1910	0.0367
2	0.0	0.0	0.0	0.0350	0.0	0.0350	0.0	0.0280	0.0631	0.0140
3	0.0	0.0	0.0	0.0238	0.0	0.0238	0.0	0.0238	0.0476	0.0085
4	0.3322	0.1096	0.4418	0.0	0.0	0.0	0.0	0.0	1.0000	0.0
5	0.0	0.0	0.0	0.0749	0.0	0.0749	0.0	-0.0299	0.0599	0.0210
6	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	-0.0196	0.0
7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
9	0.0	0.0	0.0	0.0313	0.0	0.0312	0.0	-0.0313	0.0	0.0

1966									
	1	2	3	4	5	6	7	8	9
1	0.4192	0.0127	0.0139	0.1233	0.0330	0.0	0.0226	0.0069	0.0035
2	0.0306	0.4348	0.0081	0.0097	0.0048	0.0	0.0032	0.0048	0.0
3	0.0	0.0075	0.2376	0.0011	0.0097	0.0	0.0	0.0032	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0126	0.0939	0.5036	0.0	0.1155	0.0523	0.0	0.0018	0.0
6	0.0	0.0068	0.1115	0.0	0.0	0.2804	0.0	0.0	0.0
7	0.8368	0.0211	0.0789	0.0053	0.0474	0.0	0.0	0.0053	0.0053
8	0.2484	0.1083	0.4459	0.0	0.1783	0.0	0.0	0.0	0.0191
9	0.1750	0.0	0.0	0.1250	0.0250	0.0	0.0	0.0250	0.0

	10	11	12	13	14	15	16	17	18	19
1	0.6352	0.0851	0.0180	0.0168	0.0110	0.0457	0.1309	0.1025	0.0	0.1025
2	0.6248	0.4428	0.0	0.0	0.0209	0.0209	0.4638	0.0	0.0	0.0
3	0.2688	0.6667	0.0	0.0	0.0247	0.0247	0.6914	0.0	0.0	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5517	0.0	0.5517
5	0.7798	0.0668	0.0	0.0	0.0126	0.0126	0.0794	0.0072	0.0	0.0072
6	0.3986	0.5878	0.0	0.0	0.0	0.0	0.5878	0.0	0.0135	0.0135
7	1.0000	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
8	1.0000	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
9	0.3500	0.6000	0.0	0.0	0.0500	0.0500	0.6500	0.0	0.0	0.0

	20	21	22	23	24	25	26	27	28	29
1	0.0127	0.0012	0.0139	0.0197	0.0	0.0197	0.0023	0.0533	0.1917	0.0423
2	0.0	0.0	0.0	0.0032	0.0	0.0032	0.0	0.0225	0.0258	0.0145
3	0.0	0.0	0.0	0.0183	0.0	0.0183	0.0	0.0108	0.0290	0.0108
4	0.3793	0.0690	0.4483	0.0	0.0	0.0	0.0	0.0	1.0000	0.0
5	0.0	0.0	0.0	0.1119	0.0	0.1119	0.0	0.0144	0.1336	0.0072
6	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0135	0.0
7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
9	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

1972

	1	2	3	4	5	6	7	8	9
1	0.4342	0.0130	0.0127	0.1180	0.0412	0.0	0.0198	0.0046	0.0019
2	0.0295	0.4358	0.0084	0.0063	0.0042	0.0	0.0021	0.0032	0.0011
3	0.0101	0.0039	0.2329	0.0008	0.0334	0.0	0.0	0.0054	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0293	0.1051	0.5587	0.0	0.1626	0.0	0.0	0.0024	0.0
6	0.0	0.0084	0.1309	0.0	0.0	0.2953	0.0	0.0	0.0
7	0.8237	0.0305	0.0780	0.0034	0.0475	0.0	0.0	0.0068	0.0102
8	0.2500	0.1151	0.4325	0.1825	0.0	0.0	0.0	0.0	0.0198
9	0.2963	0.0185	0.0185	0.0741	0.0370	0.0	0.0	0.0185	0.0185

	10	11	12	13	14	15	16	17	18	19
1	0.6454	0.0811	0.0167	0.0167	0.0093	0.0427	0.1239	0.1010	0.0	0.1010
2	0.49 5	0.4684	0.0	0.0	0.0189	0.0189	0.3821	0.0	0.0	0.0
3	0.2865	0.6856	0.0	0.0	0.0248	0.0248	0.7104	0.0	0.0	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5749	0.0	0.5749
5	0.8582	0.1015	0.0	0.0	0.0086	0.0086	0.1100	0.0	0.0	0.0
6	0.4345	0.5599	0.0	0.0	0.0	0.0	0.5682	0.0	0.0056	0.0056
7	1.0000	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
8	1.0000	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
9	0.4259	0.5370	0.0	0.0	0.0370	0.0370	0.5741	0.0	0.0	0.0

	20	21	22	23	24	25	26	27	28	29
1	0.0133	0.0009	0.0142	0.0130	0.0	0.0130	0.0009	0.0551	0.1843	0.0465
2	0.0	0.0	0.0	0.0147	0.0	0.0147	0.0	-0.0032	0.0116	0.0105
3	0.0	0.0	0.0	-0.0016	0.0	-0.0016	0.0	-0.0023	-0.0039	0.0070
4	0.3824	0.0426	0.4134	0.0	0.0	0.0	0.0	0.0	1.0000	0.0
5	0.0	0.0	0.0	0.0355	0.0	0.0355	0.0	-0.0232	0.0232	0.0086
6	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0056	0.0
7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
9	0.0	0.0	0.0	0.0370	0.0	0.0370	0.0	-0.0370	0.0	0.0

$$R(2)=R(1)[(1...1) (C \cdot I \cdot E)]^{-1}$$

Where R(1)—the total supply generated by the final demand sectors.

R(2)—its coefficients.

R(1) shows how many products of each production sector each final demand (C·I·E) generated.

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Table 10. Total supply generated by final demand sectors (R(1)) and its coefficients (R(2))

Table 10—1 (1959)

1.6823	0.1441	0.1738	0.7904	0.2620	0.0534	0.4789	0.1910	0.2253
0.0749	1.5743	0.0240	0.0675	0.0205	0.0042	0.0491	0.0787	0.0109
0.0235	0.0478	1.3195	0.0120	0.0781	0.0159	0.0075	0.0047	0.0032
0.0	0.0	0.0	1.0000	0.0	0.0	0.0	0.0	0.0
0.0223	0.2060	0.3970	0.0147	1.2028	0.2450	0.0100	0.0117	0.0031
0.0012	0.0067	0.0566	0.0007	0.0034	1.2600	0.0005	0.0004	0.0002
0.1545	0.0345	0.0535	0.0768	0.0554	0.0113	1.0444	0.0274	0.0519
0.0624	0.0772	0.1241	0.0308	0.1188	0.0242	0.0190	1.0103	0.0084
0.0125	0.0047	0.0013	0.0162	0.0020	0.0004	0.0036	0.0016	1.0017

1959

13.2000	18.2000	3.5000
20.3000	2.7000	0.6000
39.0000	2.8000	0.5000
0.0	29.2000	0.0
3.2000	2.0000	0.7000
14.5000	-0.4000	0.0
0.0	0.0	0.0
0.0	0.0	0.0
2.1000	0.0	0.0

$$\equiv \begin{bmatrix} C & I & E \end{bmatrix} \equiv Y$$

where: final demand (Y)
Y=C+I+E

1959

33.9932	55.0765	6.2447
34.0318	7.6924	1.2332
53.2284	4.7511	0.8253
0.0	29.2000	0.0
27.3673	4.8111	1.2422
20.6393	-0.2776	0.0390
5.2746	5.4020	0.6268
7.9802	2.8177	0.4098
2.4292	0.7225	0.0487

$$\equiv R(1) \leftarrow (I-A)^{-1} * \begin{bmatrix} C & I & E \end{bmatrix}$$

1959

0.0108	0.0	0.0
0.0	0.0183	0.0
0.0	0.0	0.1887

$$\equiv \begin{bmatrix} \frac{1}{\sum C_i} & 0 & 0 \\ 0 & \frac{1}{\sum I_i} & 0 \\ 0 & 0 & \frac{1}{\sum E_i} \end{bmatrix} \equiv (\hat{Y})$$

where $i=(1, \dots, 1)$ and \hat{Y} diagonal matrix

1959

0.3683	1.0106	1.1782
0.3687	0.1411	0.2327
0.5767	0.0872	0.1557
0.0	0.5358	0.0
0.2965	0.0883	0.2344
0.2236	-0.0051	0.0074
0.0571	0.0991	0.1183
0.0865	0.0517	0.0773
0.0263	0.0133	0.0092

$$\equiv R(2) \leftarrow R(1) (\hat{Y})^{-1}$$

total 2.0037 2.0220 2.0132(1959)

Table 10-2 (1966)

$$\begin{bmatrix} 1.7929 & 0.1614 & 0.1758 & 0.8847 & 0.2287 & 0.0311 & 0.3697 & 0.1491 & 0.2894 \\ 0.0396 & 1.7771 & 0.0256 & 0.0441 & 0.0186 & 0.0025 & 0.0268 & 0.0378 & 0.0094 \\ 0.0019 & 0.0317 & 1.3251 & 0.0045 & 0.0263 & 0.0036 & 0.0007 & 0.0263 & 0.0023 \\ 0.0 & 0.0 & 0.0 & 1.0000 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0130 & 0.1813 & 0.4609 & 0.0100 & 1.1430 & 0.1556 & 0.0046 & 0.0206 & 0.0036 \\ 0.0003 & 0.0095 & 0.0655 & 0.0004 & 0.0014 & 1.3899 & 0.0002 & 0.0015 & 0.0002 \\ 0.1660 & 0.0302 & 0.0461 & 0.0848 & 0.0407 & 0.0055 & 1.0344 & 0.0213 & 0.0524 \\ 0.0429 & 0.0639 & 0.1279 & 0.0232 & 0.0657 & 0.0089 & 0.0095 & 1.0080 & 0.0823 \\ 0.0076 & 0.0014 & 0.0024 & 0.0152 & 0.0034 & 0.0005 & 0.0016 & 0.0071 & 1.0017 \end{bmatrix} = (I-A)^{-1}$$

1966

$$\begin{bmatrix} 22.6000 & 33.1000 & 7.3000 \\ 28.8000 & 1.6000 & 0.9000 \\ 64.3000 & 2.7000 & 1.0000 \\ 0.0 & 43.5000 & 0.0 \\ 4.4000 & 7.4000 & 0.4000 \\ 17.4000 & 0.4000 & 0.0 \\ 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 \\ 2.6000 & 0.0 & 0.0 \end{bmatrix} = C I E = Y$$

1966

$$\begin{bmatrix} 58.7727 & 100.2652 & 13.5005 \\ 53.8743 & 6.2851 & 1.9219 \\ 86.3464 & 4.0808 & 1.3781 \\ 0.0 & 43.5000 & 0.0 \\ 42.8928 & 10.9169 & 1.1758 \\ 28.6792 & 0.7813 & 0.0762 \\ 7.9968 & 9.6570 & 0.5030 \\ 11.6934 & 3.3641 & 0.5249 \\ 2.9901 & 0.9479 & 0.0602 \end{bmatrix} = R(1) \leftarrow (I-A)^{-1} * C I E$$

1966

$$\begin{bmatrix} 0.0071 & 0.0 & 0.0 \\ 0.0 & 0.0123 & 0.0 \\ 0.0 & 0.0 & 0.1042 \end{bmatrix} = \begin{bmatrix} \frac{1}{\sum C_i} & 0 & 0 \\ 0 & \frac{1}{\sum I_i} & 0 \\ 0 & 0 & \frac{1}{\sum E_i} \end{bmatrix} = (\hat{Y})^{-1}$$

1966

$$\begin{bmatrix} 0.4195 & 1.2333 & 1.4063 \\ 0.3845 & 0.0773 & 0.2238 \\ 0.6163 & 0.0502 & 0.1605 \\ 0.0 & 0.5351 & 0.0 \\ 0.3062 & 0.1343 & 0.1369 \\ 0.2047 & 0.0096 & 0.0089 \\ 0.0571 & 0.1188 & 0.0586 \\ 0.0835 & 0.0414 & 0.0611 \\ 0.0213 & 0.0117 & 0.0070 \end{bmatrix} = R(2) \leftarrow (R(1)) (\hat{Y})$$

total 2.0931 2.2117 2.0631(1966)

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Table 10-3

$$\begin{bmatrix}
 1.8376 & 0.2223 & 0.2795 & 0.9160 & 0.3845 & 0.0 & 0.4002 & 0.1270 & 0.2469 \\
 0.0314 & 1.7798 & 0.0275 & 0.0310 & 0.0187 & 0.0 & 0.0189 & 0.0243 & 0.0405 \\
 0.0130 & 0.0298 & 1.3495 & 0.0108 & 0.0875 & 0.0 & 0.0030 & 0.0394 & 0.0059 \\
 0.0 & 0.0 & 0.0 & 1.0000 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\
 0.0256 & 0.2076 & 0.5783 & 0.0168 & 1.2368 & 0.0 & 0.0070 & 0.0300 & 0.0100 \\
 0.0008 & 0.0095 & 0.0700 & 0.0007 & 0.0046 & 1.4190 & 0.0002 & 0.0021 & 0.0005 \\
 0.1401 & 0.0384 & 0.0565 & 0.0722 & 0.0523 & 0.0 & 1.0307 & 0.0193 & 0.0767 \\
 0.0388 & 0.0615 & 0.1209 & 0.0801 & 0.0160 & 0.0 & 0.0088 & 1.0070 & 0.1011 \\
 0.0095 & 0.0038 & 0.0044 & 0.0103 & 0.0052 & 0.0 & 0.0021 & 0.0048 & 1.0206
 \end{bmatrix} = (I-A)^{-1}$$

1972

$$\begin{bmatrix}
 40.0000 & 59.5000 & 15.0000 \\
 36.3000 & 1.1000 & 1.0000 \\
 91.5000 & -0.5000 & 0.9000 \\
 0.0 & 77.4000 & 0.0 \\
 9.0000 & 1.9000 & 0.7000 \\
 20.4000 & 0.2000 & 0.0 \\
 0.0 & 0.0 & 0.0 \\
 0.0 & 0.0 & 0.0 \\
 3.1000 & 0.0 & 0.0
 \end{bmatrix} \equiv C I E \equiv Y$$

1972

$$\begin{bmatrix}
 111.3749 & 181.0687 & 28.3069 \\
 68.6780 & 6.2469 & 2.2890 \\
 125.8712 & 1.1315 & 1.5007 \\
 0.0 & 77.4000 & 0.0 \\
 72.6375 & 5.1118 & 1.9777 \\
 35.7723 & 0.3704 & 0.0880 \\
 12.8744 & 14.0376 & 2.2272 \\
 15.3047 & 8.5467 & 0.7635 \\
 4.1368 & 1.3766 & 0.1546
 \end{bmatrix} \equiv R 1 \Leftrightarrow (I-A)^* C I E$$

1972

$$\begin{bmatrix}
 0.0050 & 0.0 & 0.0 \\
 0.0 & 0.0072 & 0.0 \\
 0.0 & 0.0 & 0.568
 \end{bmatrix} \equiv \begin{bmatrix}
 \frac{1}{\sum C_i} & 0 & 0 \\
 0 & \frac{1}{\sum I_i} & 0 \\
 0 & 0 & \frac{1}{\sum E_i}
 \end{bmatrix} \equiv (\widehat{iY})^{-1}$$

1972

$$\begin{bmatrix}
 0.5560 & 1.2971 & 1.6083 \\
 0.3429 & 0.0447 & 0.1301 \\
 0.6284 & 0.0081 & 0.0853 \\
 0.0 & 0.5544 & 0.0 \\
 0.3626 & 0.0366 & 0.1124 \\
 0.1786 & 0.0027 & 0.0050 \\
 0.0643 & 0.1006 & 0.1265 \\
 0.0764 & 0.0612 & 0.0434 \\
 0.0207 & 0.0099 & 0.0088
 \end{bmatrix} \equiv R(2) \Leftrightarrow (R(1)) (\widehat{iY})^{-1}$$

total 2.2299 2.1153 2.1198 (1972)

Table 11. Crude value added generated by final demand sectors (R(3))

Table 11—1 (1959)

$$\begin{bmatrix} 0.4292^* & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.3645^* & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.3537 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.4692 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.5389 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.6176 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.6814 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.8393 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.8437 \end{bmatrix} * \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} \quad (1959)$$

* $0.4292 = \frac{D_1 + L_1 + P_1}{X_1 + X_1 + X_1}$
 $0.3645 = \frac{D_2 + L_2 + P_2}{X_2 + X_2 + X_2}$ and so on

$$\begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix} \begin{bmatrix} 14.5889 & 23.6372 & 2.6800 \\ 12.4041 & 2.8038 & 0.4495 \\ 18.8291 & 1.6806 & 0.2920 \\ 0.0 & 13.7000 & 0.0 \\ 14.7488 & 2.5928 & 0.6695 \\ 12.7478 & -0.1714 & 0.0241 \\ 3.5942 & 3.6810 & 0.4271 \\ 6.6977 & 2.3648 & 0.3440 \\ 2.0496 & 0.6096 & 0.0411 \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} \quad (1959) \quad \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix} \begin{bmatrix} 0.1581 & 0.4337 & 0.5057 \\ 0.1344 & 0.0514 & 0.0848 \\ 0.2040 & 0.0308 & 0.0551 \\ 0.0 & 0.2514 & 0.0 \\ 0.1598 & 0.0476 & 0.1263 \\ 0.1381 & -0.0031 & 0.0045 \\ 0.0389 & 0.0675 & 0.0806 \\ 0.0726 & 0.0434 & 0.0649 \\ 0.0222 & 0.0112 & 0.0078 \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} \quad (1959) \quad \text{total } 0.9281 \quad 0.9339 \quad 0.9297 \quad (1959)$$

Table 11—2 (1966)

$$\begin{bmatrix} 0.4082 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.3156 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.2785 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.4805 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.6552 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.6216 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.7842 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.8662 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.7500 \end{bmatrix} * \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} \quad (1966)$$

$$\begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix} \begin{bmatrix} 23.9923 & 40.9282 & 5.5109 \\ 17.0038 & 1.9836 & 0.6066 \\ 24.0470 & 1.1365 & 0.3838 \\ 0.0 & 20.9000 & 0.0 \\ 28.1048 & 7.1528 & 0.3120 \\ 17.8276 & 0.4857 & 0.0474 \\ 6.2712 & 7.5730 & 0.3945 \\ 10.1293 & 2.9140 & 0.4547 \\ 2.2426 & 0.7109 & 0.0452 \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} \quad (1966) \quad \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix} \begin{bmatrix} 0.1713 & 0.5034 & 0.5741 \\ 0.1214 & 0.0244 & 0.0632 \\ 0.1716 & 0.0140 & 0.0400 \\ 0.0 & 0.2571 & 0.0 \\ 0.2006 & 0.0880 & 0.0325 \\ 0.1272 & 0.0060 & 0.0049 \\ 0.0448 & 0.0931 & 0.0411 \\ 0.0723 & 0.0358 & 0.0474 \\ 0.0160 & 0.0087 & 0.0047 \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} \quad (1966) \quad \text{total } 0.9252 \quad 1.0305 \quad 0.8079 \quad (1966)$$

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Table 11-3 (1972)

$$\begin{bmatrix} 0.3989 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.3011 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.2042 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.4948 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.5171 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.7047 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.7763 & 0.0 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.8452 & 0.0 \\ 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.7037 \end{bmatrix} * \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} \quad (1972)$$

$$\begin{array}{l} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{array} \begin{bmatrix} 44.4258 & 72.2256 & 11.2912 \\ 20.6757 & 1.8806 & 0.6891 \\ 25.7020 & 0.2311 & 0.3064 \\ 0.0 & 38.3000 & 0.0 \\ 37.5619 & 2.6434 & 1.0227 \\ 25.2100 & 0.2610 & 0.0620 \\ 9.9940 & 10.8970 & 1.7289 \\ 12.9361 & 7.2240 & 0.6453 \\ 2.9111 & 0.9687 & 0.1088 \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} = R(3) \quad (1972)$$

$$\begin{array}{l} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{array} \begin{bmatrix} 0.2218 & 0.5174 & 0.6415 \\ 0.1032 & 0.0135 & 0.0392 \\ 0.1283 & 0.0017 & 0.0174 \\ 0.0 & 0.2744 & 0.0 \\ 0.1875 & 0.0189 & 0.0581 \\ 0.1259 & 0.0019 & 0.0035 \\ 0.0499 & 0.0781 & 0.0982 \\ 0.0646 & 0.0517 & 0.0367 \\ 0.0145 & 0.0069 & 0.0062 \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{bmatrix} = R(4) \quad (1972)$$

total 0.7674 0.9645 0.9008

The total supplies of goods generated by the final demand sectors are shown as follows in % of total supply.

product value generated (% of total)			
	1959	1966	1972
C	60.5%	59.6%	57.4%
I	36.0%	36.4%	37.8%
E	3.5%	4.0%	4.8%

The ratios of the total supply generated by the items of final demand to the original final sectors in 1959, 1966 and 1972 are shown as follows.

	1959	1966	1972
C	2.0037	2.0931	2.2299
I	2.0220	2.2117	2.1153
E	2.0132	2.0631	2.1198

As you see, generally speaking, each unit of final demand (C•I•E) generated twice as much as the value of the final demand in each year and this tendency was observed during this period.

In case of Japan, these coefficients in 1970 were as follows; gross fixed capital formation—2.16, exports—2.13, increase in stocks—2.10, private consumption—1.76, consumption of government—1.49.

As for the crude value added generated by final demand sectors, it is shown in *table 11*. The value added is produced through the industrial production activities, which are generated by the final demand. Total crude value added produced by all industrial production activities (in case of this, in productive sectors) (R(3)) was 142.3 billion rubles (1959), 223.1 (1966) and 337.6 (1972).

Coefficients of the crude value added generated by the final demand sectors (R(4)) means how many crude value added of each production sector a unit of each final demand (C I E) generated. These were, as a whole, as follows.

	1959	1966	1972
C	0.9281	0.9252	0.7674
I	0.9339	1.0305	0.9645
E	0.9297	0.8079	0.9008

References

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Notes:

X_{ij} : Intermediate products;
 D : Provisions for the consumption of fixed capital;
 W : Compensation of employees;
 P : Profit of enterprises;
 T : Indirect taxes;
 S : Social insurance;
 Sb : Current subsidies;
 SjA : Income from private subsidiary agriculture;
 M : Import;
 X : Total supply and demand;
 $C_2G + C_2S$: Government and institution's consumption expenditure of goods;
 $C_2H + C_2H$: Private consumption expenditure of goods;
 IP : Net productive domestic fixed capital formation;
 IN : Net non-productive domestic fixed capital formation;
 RP : Replacement;
 V : Increase in stocks of incompletd fixed capital formation;
 SK : Increase in stock in industry;
 R : National reserve;
 LS : Loss;
 E : Exports;
 $SH + CH$: Private consumption expenditure;
 CG : General government consumption expenditures of goods and services;
 SII : General enterprise consumption expenditure;
 CG : General government consumption expenditure;
 KH : Investment in houses (private investment);
 KII : Enterprise investment and Kolkhoz investment;
 KG : Government bond issue;
 TH : Direct taxes and charges on inhabitants;
 BH : Government bond issue;
 $Z1$: Social insurance and social security contributions of enterprises;
 $Z2$: Pioneer-camp- Sanatorium- and Hot-spring-rest- expenditure of enterprises and others;
 ΔW : Adjustment item deducted from profit=the bonus included in wages;
 αP : Deduction from enterprises' profit;
 TII : Income taxes on Kolkhoz and Cooperatives;
 ΔAH_0 : Saving of persons;
 ΔAII_0 : Saving of enterprises;
 $Z3$: Social insurance and Social security contributions of government;
 $Z4$: Subsidies to households;
 $Z5$: Scholarship given by government;
 $Z6$: Social security (of Kolkhoz) contributions of government;
 $Z7$: Adjustment item in financial revenue;
 ΔAG : Saving of government;
 CrH : Credit loan to consumers;
 CrL : Long-term credit to industry;
 CrS : Short-term credit to industry;
 CrK : Long-term credit to Kolkhoz;
 rE, rM : External transaction in foreign currency, r : Exchange rate;

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(Stock Account)

$AI, AII, AA, AG, AS, AH, AII, AG, AB$: Balance of saving of each subject at the beginning or the end of period;

$FI, FII, FA, FG, FS, FB, FF$: Foreign currency deposit account;

$\Phi I, \Phi II, \Phi A, \Phi G, \Phi S, \Phi H, \Phi II$: Fixed assets account;

RI, RII, RA, RG, RS, SK : Goods-in-stock account;

LI, LII, LA, LG, LS, LII : Employment of each item;

(Balance of stock account)

1, Saving in households— $AH_{-1} = \Delta AH_0 + AH_0$

2, Saving in enterprises— $(AI)_{-1} + (AII)_{-1} + (AA)_{-1} \equiv AII_{-1}; AII_{-1} + \Delta AII_0 = AII_0$

3, Saving in government— $AG_{-1} + \Delta AG_0 = AG_0$

4, Cash balance in bank— $AB_{-1} + \Delta AH_0 + \Delta AG_0 + \Delta AII_0 = AB_0$

Foreign currency balance in bank— $\gamma E + \gamma(SF + CF) + FB_{-1} = \gamma M + FB_0, \gamma$: Exchange rate

5, Balance of ruble account in external transaction— $SF + CF + F_{-1} = CF + SF + F_0$

Balance of foreign currency in external transaction— $\gamma M + FF_{-1} = \gamma E + \gamma(SF + CF) + FF_0$

6, Balance of saving account— $AH_{-1} + AII_{-1} + AG_{-1} + AB_{-1} + 2(\Delta AH_0 + \Delta AII_0 + \Delta AG_0) = AG_0 + AH_0 + AII_0 + AB_0$