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# Orthorhombic distortion-induced anatase-like optoelectronic properties of rutile TiO<sub>2</sub>

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## ABSTRACT

Titanium dioxide (TiO<sub>2</sub>) is an excellent photocatalyst and transparent conducting oxide. It has two major crystal structures: rutile and anatase. Anatase TiO<sub>2</sub> is valuable from an industrial point of view because it typically displays better photocatalytic and electronic transport properties than rutile TiO<sub>2</sub>. To further extract the functional properties of TiO<sub>2</sub>, understanding the correlation between the electronic structure and the crystal structure is essential. Because the electronic structure strongly depends on the crystal structure, introducing lattice distortion to rutile TiO<sub>2</sub> should effectively modulate its electronic structure. Here, we show that Nb-doped rutile TiO<sub>2</sub> epitaxial films on (1100)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates exhibit anatase-like optoelectronic properties due to orthorhombic lattice distortions and experimentally observe the change in the electronic structure. Reducing the film thickness increases the orthorhombic distortion ratio ( $b/a$ ) up to 3.4%. As  $b/a$  increases, the carrier effective mass decreases from 35 to 3  $m_0$  ( $m_0$ : electron mass) and the optical bandgap significantly increases. The present observations provide insight into regulating the TiO<sub>2</sub> physical properties and should be beneficial for designing TiO<sub>2</sub>-based photocatalysts and transparent conducting electrodes.

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## I. INTRODUCTION

Titanium dioxide (TiO<sub>2</sub>) is an active material for photocatalytic water splitting. The optical bandgap ( $E_g$ ) of TiO<sub>2</sub> is 3.1–3.3 eV, which is close to the maximum energy of visible light ( $\sim 3.1$  eV).<sup>1–3</sup> Fundamentally, the  $E_g$  of TiO<sub>2</sub> is composed of a Ti 3d-based conduction band minimum (CBM) and an O 2p-based valence band maximum (VBM). When TiO<sub>2</sub> absorbs light (photon energy  $> E_g$ ), the valence electron is excited to the conduction band, generating a positive hole in the valence band. The conduction electron reduces water while the hole oxidizes it.<sup>4–7</sup> In addition, the photocatalytic activity strongly depends on the crystal structure of TiO<sub>2</sub> because the electronic structure is affected by the crystal structure.<sup>8–12</sup>

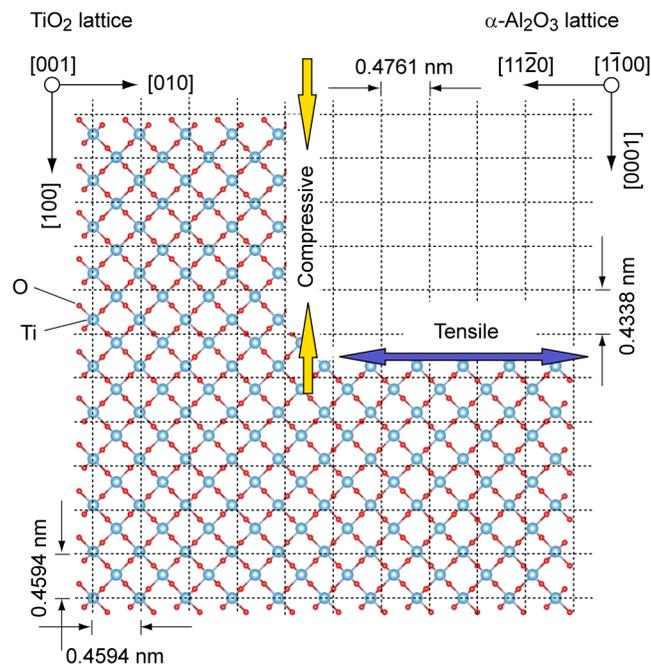
Thus, understanding the correlation between the electronic and crystal structures is essential to extract the functional properties of TiO<sub>2</sub>.

TiO<sub>2</sub> has a series of stable polymorphs in nature, e.g., rutile, anatase, brookite, etc. Among them, rutile and anatase are the most thermodynamically stable and representative. Rutile is the most stable phase at high temperatures. Anatase is stable at low temperatures but changes into the rutile phase when heated up above 600 °C.<sup>13,14</sup> The photocatalytic activity of the anatase phase is an order of magnitude higher than that of the rutile phase,<sup>11,15</sup> possibly due to higher mobility and the nature of indirect bandgap. Still due to the conduction electrons of the anatase phase having a higher mobility than those of the rutile phase,<sup>16,17</sup> it is more

suitable as transparent conducting oxide (TCO) when donor dopants are doped. Therefore, anatase  $\text{TiO}_2$  is more valuable than rutile  $\text{TiO}_2$  from an industrial point of view.

To clarify the difference, high-quality epitaxial films of  $\text{TiO}_2$  are useful. Although high-quality anatase  $\text{TiO}_2$  can be heteroepitaxially grown on several perovskite oxide substrates ( $\text{SrTiO}_3$  and  $\text{LaAlO}_3$ ) at high temperatures ( $T_g \sim 700^\circ\text{C}$ ),<sup>18–21</sup> fabricating large-area films is difficult due to the size limitation of the substrates. This study focuses on the anisotropic crystal structure of  $\alpha\text{-Al}_2\text{O}_3$  substrates. Figure 1 depicts the lattices of (001) rutile  $\text{TiO}_2$  and (1100)  $\alpha\text{-Al}_2\text{O}_3$  crystals. The epitaxial relationship is (001) [100]  $\text{TiO}_2 \parallel (1100)$  [0001]  $\alpha\text{-Al}_2\text{O}_3$ .<sup>22–24</sup> Due to the anisotropic lattice parameter of (1100)  $\alpha\text{-Al}_2\text{O}_3$  in the in-plane directions, the rutile  $\text{TiO}_2$  lattice sustains compressive strain along [100] (lattice mismatch: +5.9%), whereas tensile strain occurs along [010] (lattice mismatch: –3.5%). Because the electronic structure strongly depends on the crystal structure, introducing lattice distortion to rutile  $\text{TiO}_2$  should effectively modulate its electronic structure.

Here, we show that electron-doped rutile  $\text{TiO}_2$  epitaxial films on (1100)  $\alpha\text{-Al}_2\text{O}_3$  substrates exhibit anatase-like optoelectronic properties, presumably due to orthorhombic lattice distortions.



**FIG. 1.** Hypothesis of the orthorhombic lattice distortion of the rutile-structured  $\text{TiO}_2$  epitaxial film on an M-plane sapphire substrate. Schematic of the crystal lattice of rutile  $\text{TiO}_2$  on (1100)  $\alpha\text{-Al}_2\text{O}_3$  (sublattice of oxide ions, dotted lines). Since lattice parameter  $a$  of  $\text{TiO}_2$  is longer than lattice parameter  $c$  of  $\alpha\text{-Al}_2\text{O}_3$  (lattice mismatch: –5.9%), compressive strain is assumed, whereas the tensile strain is assumed because lattice parameter  $a$  of  $\alpha\text{-Al}_2\text{O}_3$  is larger than that of the lattice parameter  $b$  of  $\text{TiO}_2$  (lattice mismatch: +3.5%). Therefore, we hypothesized that orthorhombic distortion is introduced in the  $\text{TiO}_2$  lattice. For convenience, the  $\text{TiO}_2$  lattice is represented by the ball and stick model, while the  $\alpha\text{-Al}_2\text{O}_3$  lattice is simplified to the sublattice of oxide ions, which is shown by the dotted lines.

In addition, we demonstrate that the  $\text{TiO}_2$  film thickness controls the degree of orthorhombic distortion. The present observations provide insight into regulating the physical properties of  $\text{TiO}_2$  and should be beneficial for designing  $\text{TiO}_2$ -based photocatalysts and transparent conducting electrodes.

## II. EXPERIMENTAL SECTION

### A. Sample preparation

The target was a 0.5%-Nb-doped  $\text{TiO}_2$  ceramic disk. Pulsed laser deposition (PLD) with a KrF excimer laser ( $\lambda = 248$  nm, laser fluence  $\sim 1$  J  $\text{cm}^{-2}$  pulse<sup>-1</sup>, and repetition rate = 10 Hz) was used to fabricate 0.5%-Nb-doped  $\text{TiO}_2$  films on (1100)  $\alpha\text{-Al}_2\text{O}_3$  single crystal substrates, where the slight doping is to provide the donor dopant to facilitate further electronic measurements. Such low-level doping does not affect the lattice structure significantly.<sup>25,26</sup> During film growth, the substrate temperature and oxygen pressure were kept constant at  $500^\circ\text{C}$  and  $5 \times 10^{-3}$  Pa, respectively. Adjusting the deposition time controlled the film thickness.

### B. Crystallographic analyses

The film thickness, crystallographic orientations, and lattice parameters were determined using high-resolution x-ray diffraction (XRD, ATX-G, Rigaku) with  $\text{Cu K}\alpha_1$  ( $\lambda = 0.154$  059 nm) radiation. Both out-of-plane and in-plane measurements were performed to extract the lattice parameters. The atomic arrangement of the resultant films was visualized using STEM (ARM200CF, JEOL Co. Ltd) operated at 200 keV. HAADF-STEM images were taken with a detection angle of 68–280 mrad.

All measurements were conducted at room temperature.

### C. Electrical and optical properties' measurements

The electrical resistivity ( $\rho$ ), carrier concentration ( $n$ ), and Hall mobility ( $\mu_{\text{Hall}}$ ) at room temperature were measured by the dc four-probe method with the van der Pauw electrode configuration in air. The temperature-dependent electrical resistivity ( $\rho - T$ ), carrier concentration ( $n - T$ ), and Hall mobility ( $\mu_{\text{Hall}} - T$ ) were performed using the same configuration in a vacuum and a variable temperature of 10–300 K. The thermopower ( $S$ ) of the films in the in-plane direction was measured by the conventional steady-state method. The transmission and reflection spectra in the 200–1600 nm wavelength range were measured by a spectrophotometer (SolidSpec-3700, Shimadzu).

### D. X-ray absorption spectroscopy (XAS) measurements

XAS measurements were performed at the 2A beamline of the Pohang Accelerator Laboratory (PAL) with the grazing incidence ( $22.5^\circ$ ) configuration in the total-electron-yield (TEY) mode. The Ti L-edge spectra were measured at room temperature.

### E. Density functional theory (DFT) calculations

DFT calculations were performed with the projector-augmented wave method implemented in the Vienna *Ab initio* Simulation Package (VASP) program.<sup>27,28</sup> For the exchange-correlation term of the electrons, the generalized gradient approximation (GGA) parameterized by Perdew, Burke, and Ernzerhof was used.<sup>29</sup> The electrons

**TABLE I.** Calculated effective masses for electrons in non-distorted (case 1) or orthogonally distorted (cases 2 and 3) rutile TiO<sub>2</sub>.

	Effective mass $m^*/m_0$			
	$\Gamma \rightarrow X$	$\Gamma \rightarrow Y$	$\Gamma \rightarrow M$	$\Gamma \rightarrow S$
Case 1 ( $a_0, b_0 = a_0, c_0$ )	1.672		0.588	
Case 2 ( $a_0, b_0 = 1.030a_0, c_0$ )	1.777	1.698		0.656
Case 3 ( $0.995a_0, b_0 = 1.030a_0, 0.994c_0$ )	1.759	1.664		0.742

were  $3p^6$ ,  $3d^2$ , and  $4s^2$  for Ti and  $2s^2$  and  $2p^4$  for O. To describe the localized features of the Ti 3d orbitals, the GGA + U method was employed, where the onsite Coulomb repulsion was considered with an effective parameter of  $U = 7.0$  eV for Ti 3d.<sup>30,31</sup> Han *et al.* suggested the optimum choice of the  $U$  parameter for TiO<sub>2</sub>.<sup>31</sup> The electronic wavefunctions were expanded by plane waves up to a cutoff energy of 500 eV. Brillouin zone integration was performed with the Monkhorst-Pack mesh of  $4 \times 4 \times 6$  for the unit cell of rutile TiO<sub>2</sub>. The structure was optimized until the atomic forces converged to less than 0.01 eV/Å. The calculated lattice parameters of  $a = 0.469$  nm and  $c = 0.305$  nm slightly overestimated the experimental data,<sup>32</sup> but the trends were similar to those in previous GGA calculations.<sup>31</sup>

The present GGA + U calculations indicated that rutile TiO<sub>2</sub> had a direct theoretical  $E_g$  of 2.30 eV at the  $\Gamma$  point (Fig. S1 in the supplementary material). To evaluate effective masses ( $m^*$ ) of electrons in rutile TiO<sub>2</sub>, the energy dispersion curves at the CBM were obtained around the  $\Gamma$  point for the rutile TiO<sub>2</sub> unit cell (structure-optimized as above) using a  $k$ -point mesh density toward a particular symmetric point of more than 4.2 nm. Subsequently, parabolic curve fitting for five  $k$ -points centered at  $\Gamma$  was performed, and the  $m^*$  values of electrons were obtained from the second partial derivatives of the parabolic fitting curves.<sup>33</sup>

Although the theoretical  $E_g$  (2.30 eV) of bulk rutile TiO<sub>2</sub> underestimated the experimental value (3.03 eV),<sup>34</sup> which is a standard feature of GGA-related DFT calculations, such a small theoretical  $E_g$  may also affect the theoretical  $m^*$ . To evaluate the effect of the theoretical  $E_g$  on  $m^*$ , hybrid-functional calculations only at the  $\Gamma$  point were also performed using the hybrid density functional proposed by Heyd, Scuseria, and Ernzerhof (HSE06).<sup>35,36</sup> The  $E_g$  of 3.20 eV calculated by HSE06 reproduced the experimental  $E_g$  value better than that by the GGA + U calculations. However, the calculated  $m^*$  of 1.168 for  $\Gamma$  to X and 0.414 for  $\Gamma$  to M were slightly smaller than the corresponding GGA + U values of 1.672 and 0.588, respectively (Table I). However, these differences do not affect the conclusion of this paper. Since hybrid-functional calculations are computationally demanding, the GGA + U calculations were mainly used to investigate  $m^*$  in distorted rutile TiO<sub>2</sub>.

### III. RESULTS AND DISCUSSIONS

#### A. Epitaxial film growth of rutile Nb:TiO<sub>2</sub> with orthorhombic distortion

Figure 2 summarizes the crystallographic characterization of the resultant Nb:TiO<sub>2</sub> films on (1 $\bar{1}$ 00)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates. The out-of-plane XRD patterns exhibit intense 002 diffraction peaks of

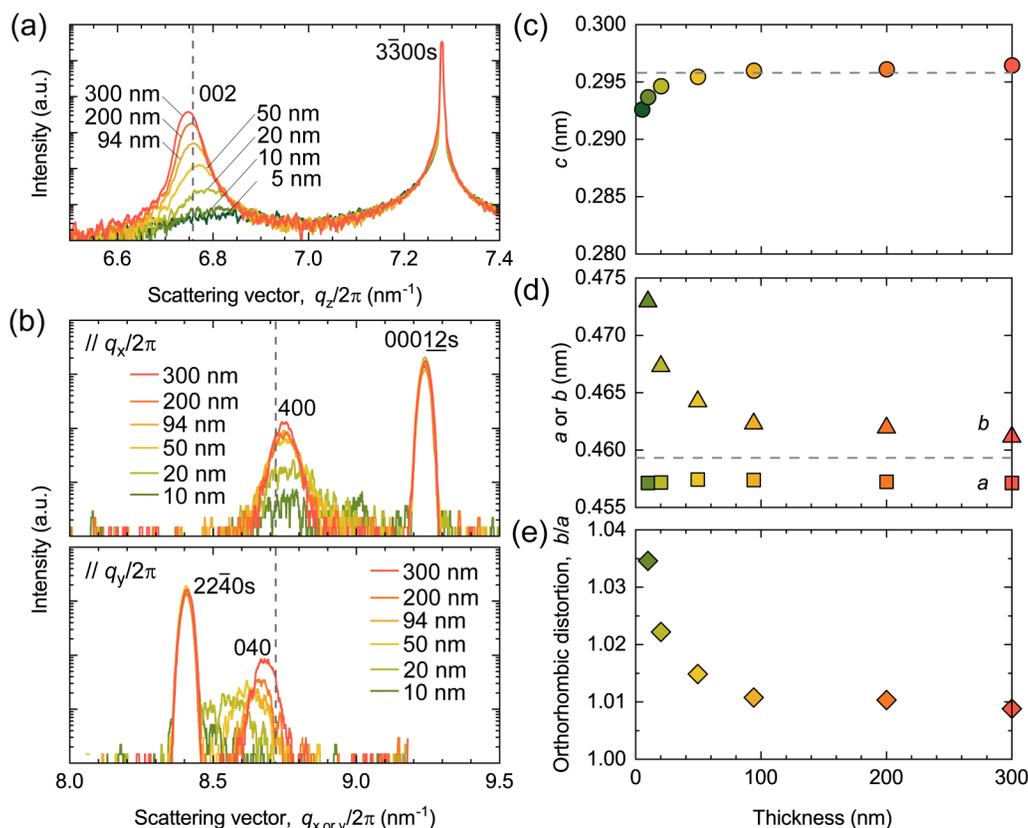
rutile Nb:TiO<sub>2</sub> and those of 3 $\bar{3}$ 00  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrate [Fig. 2(a)], indicating a high  $c$ -axis orientation. As the thickness increases, the 002 peak shifts toward the smaller scattering vector and approaches the bulk position (dashed line), which suggests an increasing trend of the lattice parameter  $c$  [Fig. 2(c)]. The in-plane XRD patterns [Fig. 2(b)] have different peak positions for the 400 (upper) and the 040 (lower). The 400 diffraction peaks of Nb:TiO<sub>2</sub> are seen together with those of 00 01 $\bar{2}$   $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates at  $\sim q_x/2\pi = 8.75$  nm<sup>-1</sup>. This is slightly larger than that of bulk (dashed line), but the 400 peaks are independent of thickness. In contrast, the 040 diffraction peaks of Nb:TiO<sub>2</sub>, which are seen together with 2240  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates, shift toward a larger scattering vector as the thickness increases and approaches  $\sim q_y/2\pi = 8.67$  nm<sup>-1</sup>. This value is slightly smaller than that of the bulk (dashed line).

Figure 2(d) summarizes the in-plane lattice parameters  $a$  and  $b$  as functions of the film thickness. Note that the lattice parameters of the 10-nm-thick and 20-nm-thick samples were extracted from the 200 Nb:TiO<sub>2</sub> and 020 Nb:TiO<sub>2</sub> diffraction peaks due to the weak peak intensities of 400 Nb:TiO<sub>2</sub> and 040 Nb:TiO<sub>2</sub> (Fig. S2 in the supplementary material). Lattice parameter  $a$  is  $\sim 0.457$  nm, which is slightly shorter than that of the bulk (0.4594 nm) due to the compressive strain originating from the lattice mismatch ( $-5.9\%$ ). Lattice parameter  $a$  is independent of the thickness. Unlike lattice parameter  $a$ , lattice parameter  $b$  shows a clear thickness dependence. For a 10-nm-thick film, lattice parameter  $b$  is 0.473 nm, which is  $\sim 3\%$  longer than that of bulk rutile TiO<sub>2</sub>. However, it decreases to 0.461 nm, which is slightly longer than that of the bulk when the thickness is 300 nm. This clearly indicates the presence of a strong tensile strain originating from the lattice mismatch ( $+3.5\%$ ) (Table II).

To visualize the orthorhombic lattice distortion, we defined the ratio of lattice parameters ( $b/a$ ) as the degree of orthorhombic distortion [Fig. 2(e)]. The ratio  $b/a$  gradually decreases as the Nb:TiO<sub>2</sub> thickness increases and ranges from  $\sim 1.035$  to  $\sim 1.01$ . It should be noted that the Nb:TiO<sub>2</sub> films were grown incoherently on (1 $\bar{1}$ 00)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates (Figs. S3–S8 in the supplementary material). These results confirm that orthorhombic strain is successfully introduced to the rutile TiO<sub>2</sub> and that the strain becomes smaller as the thickness increases. Also note that the change tendency of lattice parameter  $b$  slowed down when the films are thicker than 100 nm, indicating such tensile strain has been highly weakened under this condition.

To further clarify the orthorhombic distortion, cross-sectional STEM images were acquired for 6- and 200-nm-thick TiO<sub>2</sub> films prepared under the same growth conditions. Figure 3 shows the high-resolution HAADF-STEM images along the [0001]Al<sub>2</sub>O<sub>3</sub> zone axis and the corresponding inverse fast Fourier transformation (IFFT) images. HAADF-STEM images [Figs. 3(a) and 3(b)] exhibit a clear Z-contrast for the Ti and Al atoms. Consequently, the interface of TiO<sub>2</sub>/M-plane sapphire can be observed, as shown by the dashed line.

Comparing the observed and theoretical structures of TiO<sub>2</sub> demonstrates that both the 6- and 200-nm-thick films show (001) oriented rutile structures, which is consistent with our XRD results. IFFT is an intuitive method for observing dislocations. The lack of dislocations in IFFT of the 6-nm-thick film indicates that the TiO<sub>2</sub>



**FIG. 2.** Crystallographic characterization of the resultant  $\text{TiO}_2$  films on an M-plane sapphire substrate. (a) Out-of-plane and (b) in-plane XRD patterns of 5–300-nm-thick  $\text{TiO}_2$  films grown on a (1100)  $\alpha\text{-Al}_2\text{O}_3$  substrate. For the in-plane pattern, the upper and lower figures correspond to the XRD patterns among azimuth [0001]  $\alpha\text{-Al}_2\text{O}_3$  and azimuth [1120]  $\alpha\text{-Al}_2\text{O}_3$ , respectively. Dotted lines indicate the position of bulk  $\text{TiO}_2$ . Thickness dependence of the (c) out-of-plane lattice parameter  $c$  and (d) in-plane lattice parameters  $a$  and  $b$ , which are extracted from the XRD patterns. Dotted lines indicate the lattice parameters of bulk  $\text{TiO}_2$ . (e) Orthorhombic distortion  $b/a$  of the resultant  $\text{TiO}_2$  films.

lattice is strained [Fig. 3(c)]. In contrast, the edge dislocations at the interface of the 200-nm-thick film [Fig. 3(d)] suggest that the strain is released by forming dislocations. The uneven distribution of dislocations may be due to no post-annealing. Based on the dislocation observations, the orthorhombic distortion originates from the elastic deformation of the lattice and was relieved

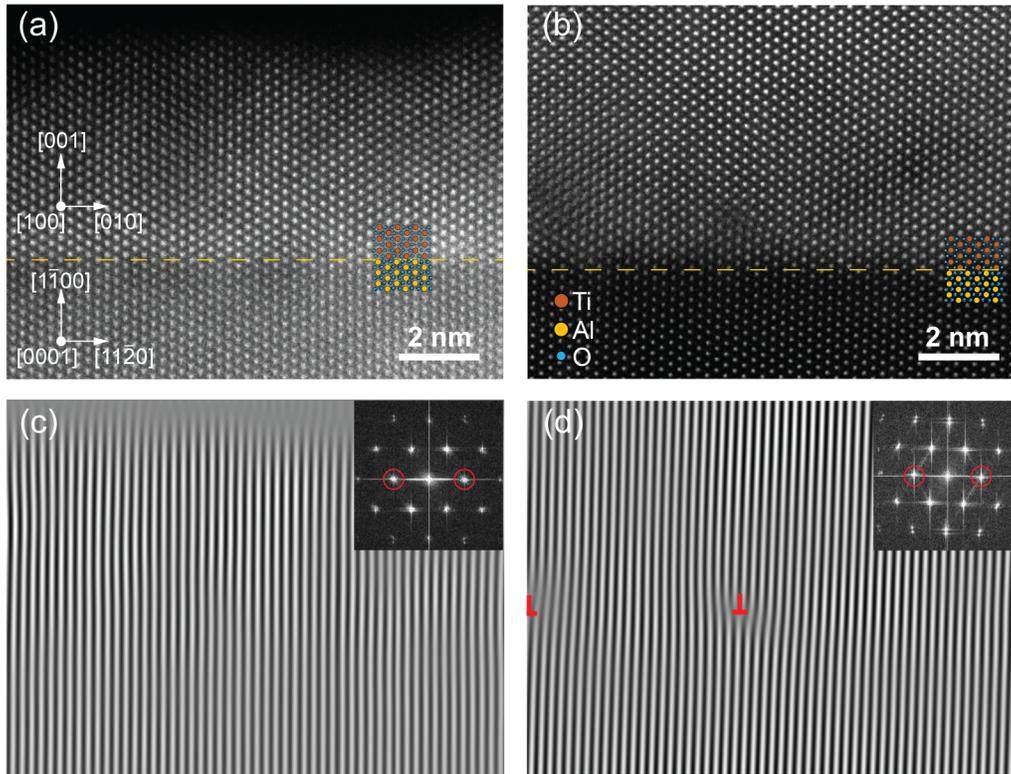
**TABLE II.** The comparison of lattice mismatch and distortion along [0001]  $\text{Al}_2\text{O}_3$  and [1120]  $\text{Al}_2\text{O}_3$  direction.

	0001	1120
Substrate orientation	0001	1120
Film orientation	100	010
Lattice mismatch	+5.9%	−3.5%
Lattice parameter of films	0.457 nm (10 nm)	0.473 nm (10 nm)
	0.457 nm (300 nm)	0.461 nm (300 nm)
Relation between lattice parameter and thickness	Weak	Strong

through dislocation formation. In addition, we also observed the HAADF-STEM images along the [1120]  $\text{Al}_2\text{O}_3$  zone axis of these two films (Fig. S9 in the supplementary material). The existence of edge dislocations in both films along this direction is also well consistent with the smaller change tendency of lattice parameter  $a$  [Fig. 2(d)]. For the 200-nm-thick films, we also observed the lattice parameter difference along the out-of-plane. No clear atom spacing difference was observed, indicating that the strain release only occurs around the dislocation at the interface instead of a gradient release from the interface to the surface. Such phenomenon has been experimentally revealed by other reports,<sup>37,38</sup> and it also confirms the uniformity of the film.

## B. Electrical and optical properties of the rutile $\text{Nb:TiO}_2$ films

The electron transport properties of the resultant  $\text{Nb:TiO}_2$  films were measured at room temperature. Figure 4 summarizes the electron transport properties as a function of the



**FIG. 3.** Cross-sectional STEM images of the TiO<sub>2</sub> films on an M-plane sapphire substrate. (a) and (b) HAADF-STEM images of (a) 6-nm-thick and (b) 200-nm-thick TiO<sub>2</sub> films grown on (1100)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates along the [0001]Al<sub>2</sub>O<sub>3</sub> zone axis. The dashed line indicates the interface of TiO<sub>2</sub>/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>. (c) and (d) Corresponding IFFT images of (c) 6-nm-thick and (d) 200-nm-thick TiO<sub>2</sub> films. The red marker denotes edge dislocations. Insets are the corresponding FFT patterns.

orthorhombic distortion (i.e.,  $b/a$ ). The electrical conductivity ( $\sigma$ ) is 2–3 S cm<sup>-1</sup> and is independent of  $b/a$  [Fig. 4(a)]. Similar to the Nb concentration (0.5%  $\approx 1.6 \times 10^{20}$  cm<sup>-3</sup>), the carrier concentration ( $n$ ) is in the range of  $10^{19}$ – $10^{20}$  cm<sup>-3</sup> and shows a gradual decreasing tendency as  $b/a$  increases [Fig. 4(b)]. For a semiconductor film depositing on sapphire, the band bending possibly occurs around the interface. Thus, the carriers within a contained thickness would be trapped, resulting in the decreasing of  $n$  when thickness decreased. In contrast,  $\mu_{\text{Hall}}$  shows the opposite trend [Fig. 4(c)]. For a small  $b/a$  ratio ( $\sim 1.01$ ), the  $\mu_{\text{Hall}}$  value is  $\sim 0.3$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup>.  $\mu_{\text{Hall}}$  increases with  $b/a$  and exceeds 1 cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> when  $b/a = 1.034$ . The variety of  $\mu_{\text{Hall}}$  should be related to the change of effective mass, which would be revealed later.

It should be noted that the thermopower ( $-S$ ) gradually decreases with  $b/a$  from  $\sim 600$  to  $\sim 430$   $\mu$ V K<sup>-1</sup> [Fig. 4(d)]. According to Mott’s formula,  $-S$  reflects  $n$  for semiconductors;  $-S$  decreases as  $n$  increases if the Fermi energy increases on the parabolic electronic density of states (DOS) and  $m^*$  is constant. Thus, the observed tendencies of  $-S$  and  $n$  reveal that the  $m^*$  becomes lighter when orthorhombic lattice distortion is introduced.

For visualization,  $m^*$  is estimated from the relation between  $n$  and  $S$  as<sup>39</sup>

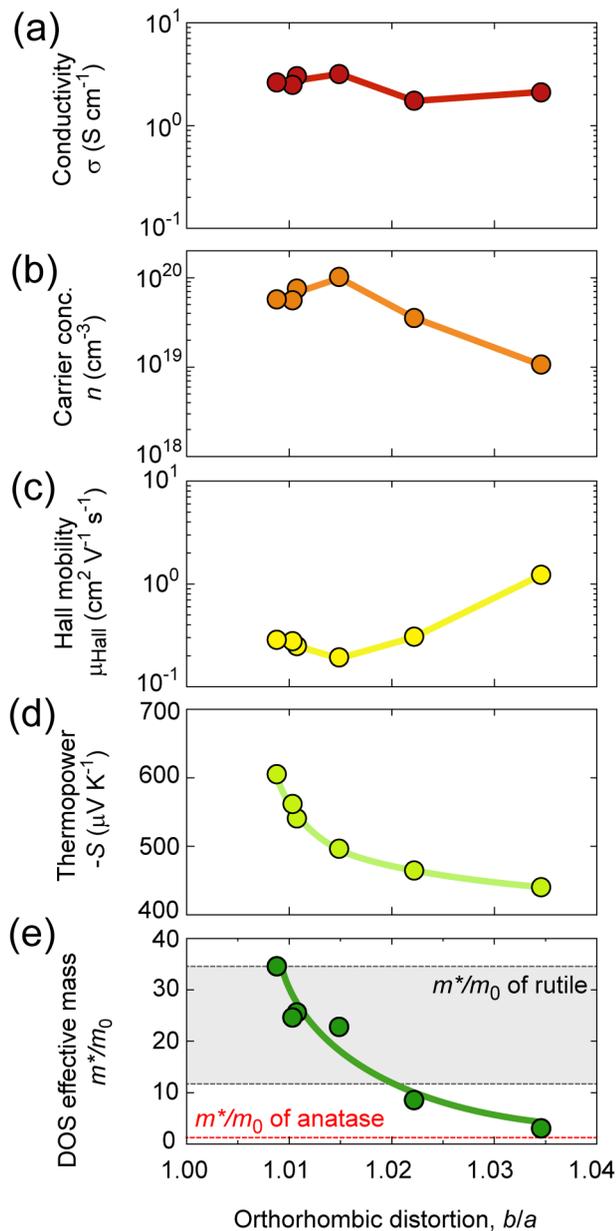
$$S = -\frac{k_B}{e} \left( \frac{(r+2)F_{r+1}(\xi)}{(r+1)F_r(\xi)} - \xi \right),$$

$$n = 4\pi \left( \frac{2m^* k_B T}{h^2} \right)^{3/2} F_{1/2}(\xi),$$

where  $k_B$ ,  $r$ ,  $F_r$ ,  $\xi$ ,  $T$ , and  $h$  are the Boltzmann constant, scattering parameter of the relaxation time, Fermi integral, chemical potential, absolute temperature, and Planck’s constant, respectively.  $F_r$  can be further expressed as

$$F_r(\xi) = \int_0^\infty \frac{x^r}{1 + e^{x-\xi}} dx.$$

Figure 4(e) plots the estimated  $m^*$  as a function of  $b/a$ .  $m^*$  of the almost relaxed rutile TiO<sub>2</sub> film ( $b/a \sim 1.008$ ) is  $\sim 35 m_0$ . This value is consistent with the reported  $m^*$  of bulk rutile TiO<sub>2</sub> (12–35  $m_0$ ).<sup>40–43</sup> It should be noted that the  $m^*$  decreases as  $b/a$

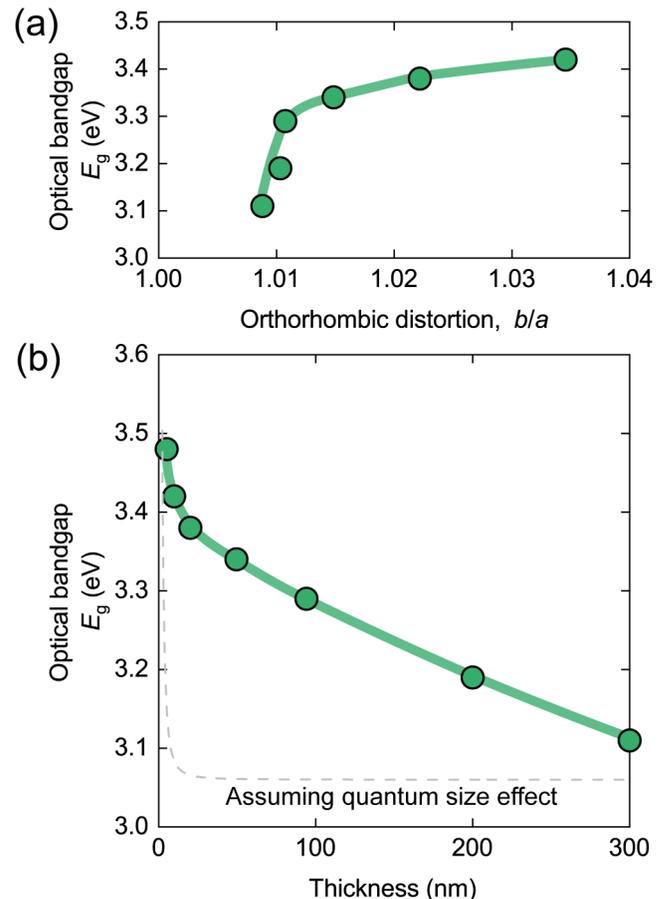


**FIG. 4.** Room temperature electron transport properties of the  $\text{TiO}_2$  films as the function of orthorhombic distortion. (a) Electrical conductivity ( $\sigma$ ), (b) carrier concentration ( $n$ ), (c) Hall mobility ( $\mu_{\text{Hall}}$ ), (d) Thermopower ( $S$ ), and (e) DOS effective mass ( $m^*/m_0$ ). The gray region and red dotted line in (e) indicate the reported effective masses of rutile<sup>40–43</sup> and anatase  $\text{TiO}_2$ ,<sup>17,19</sup> respectively. Solid lines are to guide the eye. Note that  $n$  decreases while  $|S|$  increases with  $b/a$ .

increases and reaches  $\sim 3 m_0$  when  $b/a = 1.034$ . This smaller  $m^*$  is closer to that of anatase  $\text{TiO}_2$  ( $\sim 1 m_0$ ).<sup>17,19</sup> So far, we demonstrated the relation between distortion and effective mass. The decreasing tendency is corresponding to the increase of mobility, revealing the major factor in the change of mobility.

In addition to the electron transport properties,  $E_g$  is also a property associated with the electronic structure. There is a consensus that the  $E_g$  of bulk rutile  $\text{TiO}_2$  is  $\sim 3.06$  eV while that of anatase is  $\sim 3.20$  eV.<sup>1,44,45</sup> To clarify the effect of the orthorhombic distortion on  $E_g$ , we measured the optical transmission and reflection spectra of the resultant films (Fig. S10 in the [supplementary material](#)). It should be noted that, although rutile  $\text{TiO}_2$  is a direct bandgap semiconductor, the direct transition is dipole-forbidden and degenerated with the indirect allowed transition.<sup>46–48</sup> Thus, direct  $E_g$  is equivalent to indirect  $E_g$  and was possible to be evaluated by extrapolating the linear region of the Tauc  $[(\alpha h\nu)^{1/2} - h\nu]$  plot (Fig. S11 in the [supplementary material](#)).  $E_g$  gradually increases from  $\sim 3.11$  to  $\sim 3.48$  eV as  $b/a$  increases [Fig. 5(a)]. Even a highly relaxed film (300 nm) shows a small distortion ( $b/a \sim 1.008$ ), which may explain why  $E_g$  is slightly higher than the rutile bulk value ( $\sim 3.06$  eV).<sup>49</sup>

Generally, the  $E_g$  of an extremely thin layer is greater than that of the bulk due to the quantum size effect (QSE). QSE occurs



**FIG. 5.** Denying the quantum size effect of  $\text{TiO}_2$  epitaxial films. Change in  $E_g$  of the  $\text{TiO}_2$  films. (a)  $E_g$  increases with  $b/a$ . (b)  $E_g$  increases as the thickness decreases. This increasing tendency completely differs from the assumption for the quantum size effect.

when the film thickness is thinner than the de Broglie wavelength.  $E_g$  gradually increases as the film thickness decreases [Fig. 5(b)]. To clarify the origin of the increased  $E_g$ , we calculated  $E_g$  assuming that QSE can be expressed as<sup>50,51</sup>

$$E_g = E_{g, Bulk} + \frac{h^2}{2d^2} \left( \frac{1}{m_e^*} + \frac{1}{m_h^*} \right),$$

where  $E_{g, Bulk}$ ,  $h$ , and  $d$  are the bulk bandgap, Planck's constant, and film thickness, respectively.  $m_e^*$  and  $m_h^*$  are the electron and hole effective masses, which are assumed to be  $\sim 20^{41}$  and  $\sim 5 m_0^{52}$  respectively. The calculated  $E_g$  increases dramatically when the film thickness is thinner than  $\sim 10$  nm. This behavior does not fit with the observed  $E_g$ , indicating that the QSE theory cannot explain the observed  $E_g$ . These observations confirm that the electronic structure of a rutile  $\text{TiO}_2$  film is predominantly modulated via orthorhombic distortion.

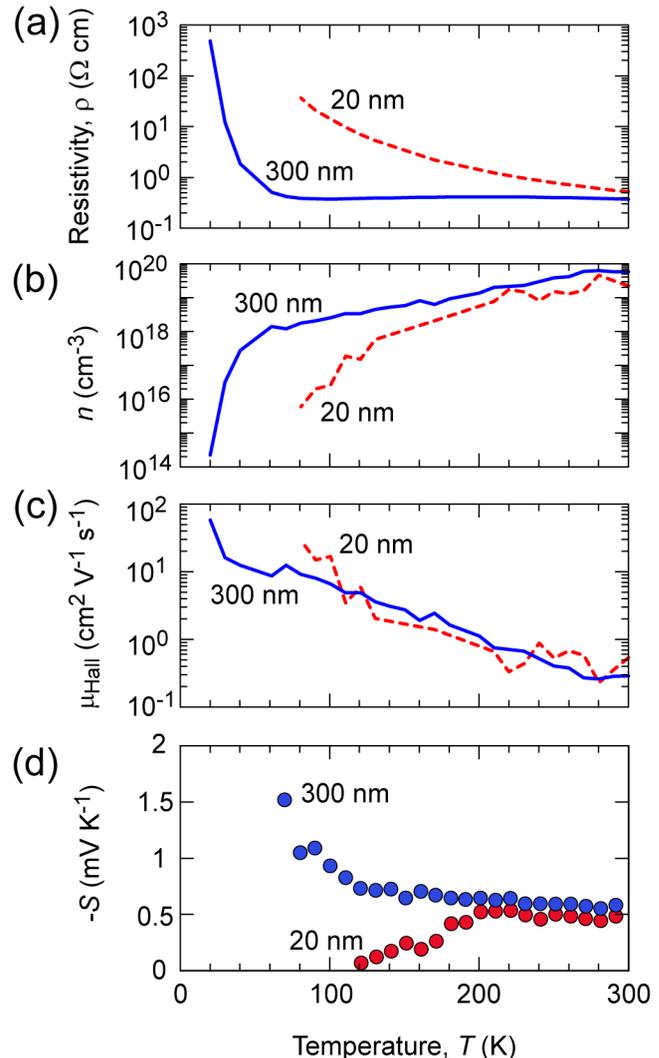
Nb: $\text{TiO}_2$  films grown on (1 $\bar{1}00$ )  $\alpha$ - $\text{Al}_2\text{O}_3$  substrate show differentiated properties from the rutile phase when the thickness is sufficiently thin due to orthorhombic lattice distortion but typical properties of the rutile phase appear as the thickness increases. Since rutile Nb: $\text{TiO}_2$  shows interesting transport properties at low temperatures and the temperature-related behavior may provide information about the transport mechanism, we measured the temperature dependence of the electron transport properties of the 300-nm-thick Nb: $\text{TiO}_2$  film ( $b/a \sim 1.008$ ) and the 20-nm-thick Nb: $\text{TiO}_2$  film ( $b/a = 1.034$ ). Both films show semiconductor-like behaviors of  $\rho$  [Fig. 6(a)]. As the temperature decreases,  $\rho$  gradually increases,  $n$  gradually decreases [Fig. 6(b)], and  $\mu_{\text{Hall}}$  increases [Fig. 6(c)]. These results suggest that phonons dominate carrier scattering.

The films display different temperature dependences of  $-S$  [Fig. 6(d)]. At room temperature, the  $-S$  values of the 300- and the 20-nm-film are  $\sim 0.6$  and  $0.45 \text{ mV K}^{-1}$ , respectively. As the temperature decreases, the former increases dramatically and exceeds  $1.5 \text{ mV K}^{-1}$ . In contrast, the latter decreases gradually and approaches zero. It has been observed that rutile  $\text{TiO}_2$  shows a colossal  $-S$  at low temperature due to the phonon drag effect.<sup>40,53</sup> This behavior is usually observed in materials with a large  $m^*$ .<sup>54–57</sup> As above described,  $m^*$  of the 300-nm-film is  $35 m_0$  while that of the 20-nm-film is  $\sim 3 m_0$ . Similarly, the presence or absence of a colossal  $-S$  reflects the distortion-induced  $m^*$  modulation at room temperature.

These observations reveal that introducing orthorhombic lattice distortion using (1 $\bar{1}00$ )  $\alpha$ - $\text{Al}_2\text{O}_3$  substrates significantly modulates the electronic structure of rutile  $\text{TiO}_2$ . Orthorhombic distortion realizes changes in  $E_g$ ,  $m^*$ , and  $-S$ , indicating that the electronic structure of rutile  $\text{TiO}_2$  shifts toward that of anatase  $\text{TiO}_2$ .

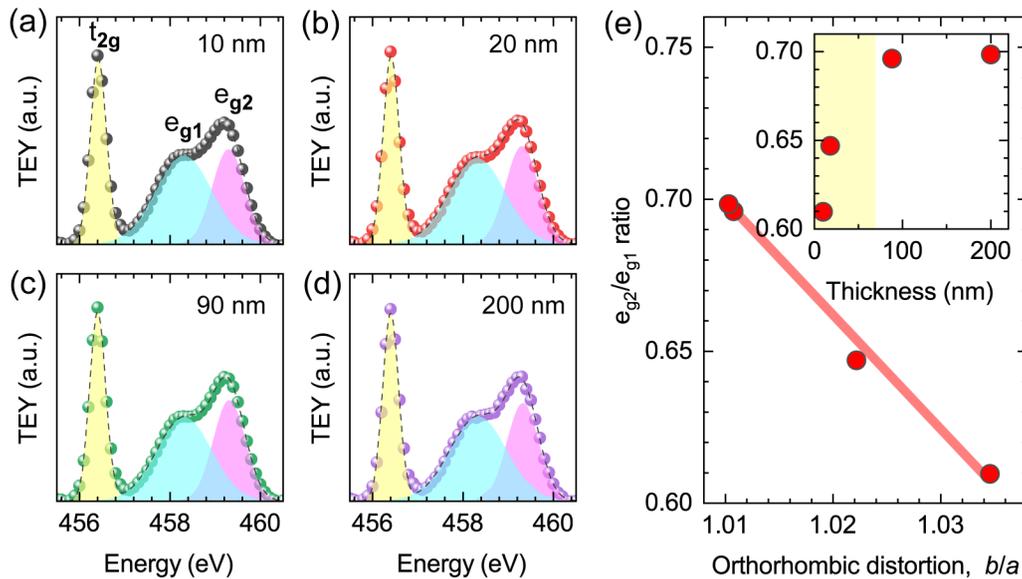
### C. Changes in the electronic structure of rutile $\text{TiO}_2$ due to orthorhombic distortion

The XAS spectra of the  $\text{TiO}_2$  films were measured to directly clarify the change in the electronic structure of rutile  $\text{TiO}_2$  upon orthorhombic distortion. Figure 7 shows the XAS spectra of the 10–200-nm-thick rutile  $\text{TiO}_2$  films at the Ti  $L_3$ -edge. The single peak around  $\sim 456 \text{ eV}$  corresponds to the threefold degenerate  $t_{2g}$  state, and the double peak around  $\sim 459 \text{ eV}$  corresponds to the



**FIG. 6.** Low-temperature electron transport properties of the  $\text{TiO}_2$  films. (a) Resistivity, (b) carrier concentration ( $n$ ), (c) Hall mobility ( $\mu_{\text{Hall}}$ ), and (d) thermopower ( $S$ ) of 20- and 300-nm-thick rutile  $\text{TiO}_2$  films grown on (1 $\bar{1}00$ )  $\alpha$ - $\text{Al}_2\text{O}_3$  substrates. Note that the  $|S|$ - $T$  curve of the 300-nm-thick  $\text{TiO}_2$  is similar to that of the reduced rutile  $\text{TiO}_2$  single crystal, whereas that of the 20-nm-thick  $\text{TiO}_2$  is similar to that of the anatase  $\text{TiO}_2$  epitaxial film.

twofold degenerate  $e_g$  state. The  $e_g$  peak is further split into two peaks ( $e_{g1}$  and  $e_{g2}$ ) due to the octahedral distortion of  $\text{TiO}_6$  octahedra. The octahedral distortion differs between rutile and anatase. Rutile is  $D_{2h}$  symmetry, while anatase is  $D_{2d}$ . This difference is reflected in the XAS spectra as the inversion of the relative intensities of the  $e_{g1}$  and  $e_{g2}$  peaks. Hence, their intensities can be used as a fingerprint for different  $\text{TiO}_2$  polymorphs (Fig. S12 in the supplementary material).<sup>58</sup> The observed XAS spectra indicate that the  $\text{TiO}_2$  films maintain the electronic structure of the rutile phase. Although the anatase phase does not appear even with a



**FIG. 7.** Ti  $L_3$  XAS spectra of the 10–200-nm-thick rutile  $\text{TiO}_2$  films. (a) 10-nm-thick  $\text{TiO}_2$ , (b) 20-nm-thick  $\text{TiO}_2$ , (c) 90-nm-thick  $\text{TiO}_2$ , and (d) 200-nm-thick  $\text{TiO}_2$  grown on (1100)  $\alpha\text{-Al}_2\text{O}_3$  substrates. Peak fitting is processed by the Gaussian distribution. (e) Relative peak area ratio of  $e_{g2}/e_{g1}$  as a function of orthorhombic distortion. The inset plots the  $e_{g2}/e_{g1}$  ratio as a function of the film thickness.

large orthorhombic distortion, we consider that changes in the lattice parameters result in changes in the degree of octahedral distortion. This small perturbation has a non-negligible effect on the physical properties.<sup>9,59,60</sup> From this viewpoint, we fitted the XAS data into a Gaussian distribution (the fitting parameters were available in Table S1 in the [supplementary material](#)) and calculated the relative peak area ratio of  $e_{g2}/e_{g1}$  [Figs. 7(a)–7(d)]. As the thickness increases,  $e_{g2}/e_{g1}$  shows an increasing tendency [Fig. 7(e), inset]. However,  $e_{g2}/e_{g1}$  linearly decreases as  $b/a$  increases [Fig. 7(e)], clearly indicating that there is a strong correlation between the electronic structure of rutile  $\text{TiO}_2$  and the orthorhombic lattice distortion.

#### D. DFT calculation of $\text{TiO}_2$ with orthorhombic lattice distortion

Finally, DFT calculations of rutile  $\text{TiO}_2$  with orthorhombic lattice distortion were performed to investigate the influence of lattice distortion of  $\text{TiO}_2$  thin films on electron  $m^*$ . Three  $\text{TiO}_2$  unit cells were considered: (1) a rutile unit cell with fully optimized  $a$ - and  $c$ -axis lengths ( $a_0, b_0 = a_0, c_0$ ), (2) a rutile unit cell with the  $b$ -axis length extended 3% from the fully optimized value ( $a_0, 1.030b_0, c_0$ ), and (3) a rutile unit cell with the  $a$ -axis length compressed 0.5% and the  $b$ -axis length extended 3% ( $0.995a_0, 1.03b_0, 0.994c_0$ ). These extensions and compressions of  $a_0$  and  $b_0$  are based on the experimental data shown in Fig. 2. It should be noted that the  $c$ -axis length in case 3 was optimized by the DFT calculations, and the optimized  $c$ -axis length of  $0.994c_0$  agrees well with that for the thin-film value (about  $0.9925c_0$ ) shown in Fig. 2(c). Moreover, the theoretical  $E_g$  value for the

distorted unit cell (case 3) is 2.37 eV, which is larger than the fully optimized unit cell value of 2.30 eV. The increased  $E_g$  trend for the distorted rutile unit cell agrees well with the experimental  $E_g$  variation against orthogonal distortion shown in Fig. 5(a).

Table I lists the calculated  $m^*$  values at the  $\Gamma$  point toward the X (or Y) point and the M (or S) point (these directions correspond to the in-plane ones to the thin-film surface). The DFT results show that the  $m^*$ s of the fully optimized rutile  $\text{TiO}_2$  are around 1.7 and  $0.6 m_0$ , which are much smaller than the experimentally observed value ( $\sim 35 m_0$ ). Previous GGA calculations provided similar theoretical results.<sup>47,61,62</sup> It is thought that electronic conduction in rutile  $\text{TiO}_2$  is not simply described by the  $m^*$ -like states, but is strongly affected by the formation of polarons, namely, electron coupling with lattice vibrations (phonons). As the orthogonal distortions increase (cases 2 and 3), the calculated  $m^*$  values tend to increase. However, the  $m^*$  values are still smaller than the experimentally observed one ( $3 m_0$ ) for the distorted thin films [Fig. 4(e)]. Hence, it is most likely that the original orthogonal distortions of the rutile  $\text{TiO}_2$  thin films due to the substrate considerably change the lattice vibrational states in the thin films.

#### IV. CONCLUSION

Nb-doped rutile  $\text{TiO}_2$  epitaxial films on (1100)  $\alpha\text{-Al}_2\text{O}_3$  substrate exhibit anatase-like optoelectronic properties due to orthorhombic lattice distortions. As the film thickness decreases,  $b/a$  increases up to 3.4%. As  $b/a$  increases, the carrier  $m^*$  decreases from 35 to  $3 m_0$  ( $m_0$ : electron mass) but  $E_g$  increases. The electronic structure change was observed experimentally. The present observations provide insight into regulating the physical properties

of TiO<sub>2</sub> and should aid in the design of TiO<sub>2</sub>-based photocatalysts and transparent conducting electrodes.

### SUPPLEMENTARY MATERIAL

See the [supplementary material](#) for x-ray reciprocal space mappings (RSMs) around (left) (3306)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> and (right) (4220)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> diffraction spots of the TiO<sub>2</sub> film (300, 200, 100, 50, 20, and 10 nm) grown on (1100)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates. Optical transmission and reflection spectra of the 5–300-nm-thick TiO<sub>2</sub> films grown on (1010)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates and Tauc plots ( $(\alpha h\nu)^{1/2} - h\nu$ ) of the 5–300-nm-thick rutile TiO<sub>2</sub> films grown on (1100)  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> substrates.

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### AUTHOR DECLARATIONS

#### Conflict of Interest

The authors have no conflicts to disclose.

#### Author Contributions

B.C. prepared the samples and conducted the measurements. K.K. and H.J. performed the XAS measurements and analyses. Y.Z. analyzed the effective mass. J.L., B.F., and Y.I. performed the STEM observations and analyses. S.H. and K.M. performed DFT calculations. B.C. and H.O. planned and supervised the project. All authors discussed the results and commented on the manuscript.

**Binjie Chen:** Conceptualization (equal); Data curation (equal); Formal analysis (equal); Investigation (equal); Validation (equal); Writing – original draft (equal); Writing – review & editing (equal). **Kungwan Kang:** Investigation (equal); Writing – review & editing (equal). **Hyoungjeen Jeon:** Investigation (equal); Writing – review & editing (equal). **Yuqiao Zhang:** Investigation (equal); Validation (equal); Writing – review & editing (equal). **Jinghuang Lin:** Investigation (equal); Writing – review & editing (equal). **Bin Feng:** Investigation (equal); Writing – review & editing (equal). **Yuichi Ikuhara:** Investigation (equal); Writing – review & editing

(equal). **Sena Hoshino:** Investigation (equal); Writing – review & editing (equal). **Katsuyuki Matsunaga:** Investigation (equal); Writing – review & editing (equal). **Hirokichi Ohta:** Conceptualization (equal); Data curation (equal); Funding acquisition (equal); Project administration (equal); Supervision (equal); Writing – original draft (equal); Writing – review & editing (equal).

### DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author on reasonable request.

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